## General Aptitude (GA)

## Q. 1 - Q. 5 Carry ONE mark Each

\(\left.$$
\begin{array}{|l|l|}\hline \text { Q.1 } & \begin{array}{l}\text { If ' } \rightarrow \text { ' denotes increasing order of intensity, then the meaning of the words } \\
\text { [drizzle } \rightarrow \text { rain } \rightarrow \text { downpour] is analogous to }[\ldots \\
\text { Which one of the given options is appropriate to fill the blank? }\end{array}
$$ <br>

\hline (A) \& bicker \rightarrow feud] .\end{array}\right]\)| (B) |
| :--- |
| bog |
| (D) |
| dither |


| Q.2 | Statements: <br> 1. All heroes are winners. <br> 2. All winners are lucky people. <br> Inferences: <br> I. All lucky people are heroes. |
| :--- | :--- |
| (A). Some lucky people are heroes. |  |
| (AII. Some winners are heroes. |  |
| Which of the above inferences can be logically deduced from statements 1 and $2 ?$ |  |
| (B) | Only I and II |
| (C) | Only II and III |
| Only III |  |
|  |  |


| Q.3 | A student was supposed to multiply a positive real number $p$ with another positive <br> real number $q$. Instead, the student divided $p$ by $q$. If the percentage error in the <br> student's answer is $80 \%$, the value of $q$ is |
| :--- | :--- |
|  |  |
| (A) | 5 |
| (B) | $\sqrt{2}$ |
| (C) | 2 |
| (D) | $\sqrt{5}$ |
| Q.4 | If the sum of the first 20 consecutive positive odd numbers is divided by $20^{2}$, the <br> result is <br> (B) <br> (C) |
| (D) | $1 / 2$ |


| Q.5 | The ratio of the number of girls to boys in class VIII is the same as the ratio of the <br> number of boys to girls in class IX. The total number of students (boys and girls) in <br> classes VIII and IX is 450 and 360, respectively. If the number of girls in classes <br> VIII and IX is the same, then the number of girls in each class is |
| :--- | :--- |
|  |  |
| (A) | 150 |
| (B) | 200 |
| (C) | 250 |
| (D) | 175 |
|  |  |

## Q. 6 - Q. 10 Carry TWO marks Each

| Q. 6 | In the given text, the blanks are numbered (i)-(iv). Select the best match for all the blanks. <br> Yoko Roi stands $\qquad$ (i) as an author for standing $\qquad$ (ii) as an honorary fellow, after she stood (iii) $\qquad$ her writings that stand $\qquad$ (iv) the freedom of speech. |
| :---: | :---: |
|  |  |
| (A) | $\begin{array}{llll}\text { (i) out } & \text { (ii) down } & \text { (iii) in } & \text { (iv) for }\end{array}$ |
| (B) | $\begin{array}{lll}\text { (i) down } & \text { (ii) out } & \text { (iii) by }\end{array}$ |
| (C) | $\begin{array}{llll}\text { (i) down } & \text { (ii) out } & \text { (iii) for } & \text { (iv) in }\end{array}$ |
| (D) | $\begin{array}{llll}\text { (i) out } & \text { (ii) down } & \text { (iii) by } & \text { (iv) for }\end{array}$ |
|  |  |


| Q.7 | Seven identical cylindrical chalk-sticks are fitted tightly in a cylindrical container. <br> The figure below shows the arrangement of the chalk-sticks inside the cylinder. |
| :--- | :--- |
| The length of the container is equal to the length of the chalk-sticks. The ratio of |  |
| the occupied space to the empty space of the container is |  |
| (A) | $5 / 2$ |
| (B) | $7 / 2$ |
| (C) | $9 / 2$ |
| (D) | 3 |


| Q. 8 | The plot below shows the relationship between the mortality risk of cardiovascular <br> disease and the number of steps a person walks per day. Based on the data, which <br> one of the following options is true? |
| :--- | :--- |
| (A) | The risk reduction on increasing the steps/day from 0 to 10000 is less than the risk <br> reduction on increasing the steps/day from 10000 to 20000 . |
| (B) | The risk reduction on increasing the steps/day from 0 to 5000 is less than the risk <br> reduction on increasing the steps/day from 15000 to 20000 . |
| (C) | For any <br> 0 <br> 0 |


| Q.9 | Five cubes of identical size and another smaller cube are assembled as shown in <br> Figure A. If viewed from direction X, the planar image of the assembly appears as <br> Figure B. |
| :--- | :--- |
| (A) | If viewed from direction Y, the planar image of the assembly (Figure A) will |
| (B) |  |
| (C) |  |


|  |  |
| :--- | :--- |
| Q.10 | Visualize a cube that is held with one of the four body diagonals aligned to the <br> vertical axis. Rotate the cube about this axis such that its view remains unchanged. <br> The magnitude of the minimum angle of rotation is |
| (A) | $120^{\circ}$ |
| (B) | $60^{\circ}$ |
| (C) | $90^{\circ}$ |
| (D) | $180^{\circ}$ |
|  |  |

## Q. 11 - Q. 35 Carry ONE mark Each

| Q.11 | Let $\mathbf{z}=x+i y$ be a complex variable and $\overline{\mathbf{z}}$ be its complex conjugate. The equation <br> $\overline{\mathbf{z}}^{2}+\mathbf{z}^{2}=2$ represents a |
| :--- | :--- |
| (A) | parabola |
| (B) | hyperbola |
| (C) | ellipse |
| (D) | circle |
| Q.12 | The pressure drop across a control valve is constant. The control valve with inherent <br> characteristic has decreasing sensitivity. If $x$ represents the fraction of maximum <br> stem position of the control valve, then the function $f(x)$ representing the fraction <br> of maximum flow is |
| (D) | $x$ <br> (A) <br> $x^{x}$ <br> (D) where $\alpha$ is constant |


| Q.13 | A discrete-time sequence is given by $x[n]=[1,2,3,4]$ for $0 \leq n \leq 3$. The zero <br> lag auto-correlation value of $x[n]$ is |
| :--- | :--- |
|  |  |
| (A) | 1 |
| (B) | 10 |
| (C) | 20 |
| (D) | 30 |
|  |  |


| Q. 14 | Match the following measuring devices with their principle of measurement. |  |
| :---: | :---: | :---: |
|  | Measuring Device | Principle of Measurement |
|  | (P) Optical pyrometer | (I) Variation in mutual inductance |
|  | (Q) Thermocouple | (II) Change in resistance |
|  | (R) Strain gauge | (III) Wavelength of radiated energy |
|  | (S) Linear variable differential transformer | (IV) Electromotive force generated by two dissimilar metals |
| (A) | (P) - (III), (Q) - (IV), (R) - (II), (S) - (I) |  |
| (B) | (P) - (IV), (Q) - (III), (R) - (II), (S) - (I) |  |
| (C) | (P) - (III), (Q) - (I), (R) - (IV), (S) - (II) |  |
| (D) | (P) - (II), (Q) - (IV), (R) - (I), (S) - (III) |  |
|  | $\square$ - |  |


| Q. 15 | The capacitor shown in the figure has parallel plates, with each plate having an area $A$. The thickness of the dielectric materials are $\mathrm{d}_{1}$ and $\mathrm{d}_{2}$ and their relative permittivities are $\varepsilon_{1}$ and $\varepsilon_{2}$, respectively. Assume that the fringing field effects are negligible and $\varepsilon_{0}$ is the permittivity of free space. <br> If $\mathrm{d}_{1}$ is decreased by $\delta \mathrm{d}_{1}$, the resultant capacitance becomes |
| :---: | :---: |
|  |  |
| (A) | $\frac{\varepsilon_{0} \mathrm{~A}}{\mathrm{~d}_{1}-\delta \mathrm{d}_{1}+\frac{\mathrm{d}_{2}}{\varepsilon_{2}}}$ |
| (B) | $\frac{\varepsilon_{0} \mathrm{~A}}{\mathrm{~d}_{2}+\frac{\mathrm{d}_{1}}{\varepsilon_{2}}}$ |
| (C) | $\frac{\varepsilon_{0} \mathrm{~A}}{\mathrm{~d}_{2}-\delta \mathrm{d}_{2}+\frac{\mathrm{d}_{1}}{\varepsilon_{2}}}$ |
| (D) | $\frac{\varepsilon_{0} \mathrm{~A}}{\mathrm{~d}_{1}+\delta \mathrm{d}_{1}+\frac{\mathrm{d}_{2}}{\varepsilon_{2}}}$ |
|  |  |


| Q. 16 | Among the given options, the simplified form of the Boolean function $F=(A+\bar{A} \cdot B)+\bar{A} \cdot(A+\bar{B}) \cdot C$ is |
| :---: | :---: |
|  |  |
| (A) | $A+B+C$ |
| (B) | A.B.C |
| (C) | $B+\bar{A} . C$ |
| (D) | $\bar{A}+B . C$ |
| Q. 17 | Consider the state-space representation of a system $\dot{x}=A x+B u$ <br> where $x$ is the state vector, $u$ is the input, $A$ is the system matrix and $B$ is the input matrix. Choose the matrix $A$ from the following options such that the system has a pole at the origin. |
| (A) | $\left[\begin{array}{rr} 0 & 1 \\ -2 & -3 \end{array}\right]$ |
| (B) | $\left[\begin{array}{rc} 1 & -1.5 \\ -2 & 3 \end{array}\right]$ |
| (C) | $\left[\begin{array}{cc}1 & 1.5 \\ 2 & -3\end{array}\right]$ |
| (D) | $\left[\begin{array}{rr} 0 & 1 \\ -2 & 3 \end{array}\right]$ |
|  |  |


| Q.18 | The sinusoidal transfer function corresponding to the polar plot shown in the figure, <br> for $T>0$, is |
| :--- | :--- | :--- |
|  |  |
| (A) | $1-j \omega T$ |
| (B) | $\frac{1-j \omega T}{1+j \omega T}$ |
| (C) | $1+j \omega T$ |


| Q. 19 | A matrix $M$ is constructed by stacking three column vectors $v_{1}, v_{2}, v_{3}$ as $M=\left[\begin{array}{lll} v_{1} & v_{2} & v_{3} \end{array}\right] .$ <br> Choose the set of vectors from the following options such that $\operatorname{rank}(M)=3$. |
| :---: | :---: |
|  |  |
| (A) | $v_{1}=\left[\begin{array}{l}1 \\ 0 \\ 1\end{array}\right], \quad v_{2}=\left[\begin{array}{r}0 \\ -1 \\ 0\end{array}\right], \quad v_{3}=\left[\begin{array}{r}1 \\ -1 \\ 1\end{array}\right]$ |
| (B) | $v_{1}=\left[\begin{array}{l}1 \\ 1 \\ 1\end{array}\right], v_{2}=\left[\begin{array}{r}1 \\ 0 \\ 1\end{array}\right], v_{3}=\left[\begin{array}{l}0 \\ 0 \\ 0\end{array}\right]$ |
| (C) | $v_{1}=\left[\begin{array}{l}1 \\ 0 \\ 1\end{array}\right], \quad v_{2}=\left[\begin{array}{r}-1 \\ 0 \\ 1\end{array}\right], v_{3}=\left[\begin{array}{r}1 \\ -1 \\ 1\end{array}\right]$ |
| (D) | $v_{1}=\left[\begin{array}{l}1 \\ 1 \\ 1\end{array}\right], \quad v_{2}=\left[\begin{array}{r}-1 \\ 1 \\ -1\end{array}\right], \quad v_{3}=\left[\begin{array}{r}0 \\ -1 \\ 0\end{array}\right]$ |
|  |  |


| Q.20 | The capacitance formed between two concentric spherical metal shells having radii <br> $x$ and $y$ with $y>x$ is <br> Note: $\epsilon$ is the permittivity of the medium between the shells. |
| :--- | :--- |
| (A) | $4 \pi \epsilon\left(\frac{x y}{y-x}\right)$ |
| (B) | $4 \pi \epsilon\left(\frac{x^{2}}{y-x}\right)$ |
| (C) | $4 \pi \epsilon\left(\frac{y^{2}}{y-x}\right)$ |
| (D) $2 \pi \epsilon\left(\frac{y^{2}-x y}{x}\right)$ |  |
|  | A linear transducer is calibrated for the ranges shown in the figure. The gain of the <br> transducer is |
|  |  |


| Q. 22 | Consider a filter defined by the difference equation $y[n]-0.5 y[n-2]=a x[n-4]$ <br> where $x[n]$ and $y[n]$ represent the input and output, respectively. If the magnitude response of the filter at $\omega=\frac{\pi}{2}$ is $\left\|H\left(\frac{\pi}{2}\right)\right\|=0.5$, the value of $a$ is $\qquad$ (rounded off to two decimal places). |
| :---: | :---: |
|  |  |
| Q. 23 | Consider the circuit shown in the figure. <br> The CMOS digital logic circuit has infinite input impedance. Assume the opamp is ideal. A 1.8 V Zener diode with a minimum Zener current of 2 mA is used. The corresponding maximum value of resistance $\mathrm{R}_{\mathrm{z}}$ is $\qquad$ $\mathrm{k} \Omega$. (rounded off to one decimal place). |
|  |  |


| Q. 24 | Figure shows an amplifier using an NMOS transistor. Assume that the transistor is in saturation with device parameters, $\mu_{\mathrm{n}} \mathrm{C}_{\mathrm{ox}}=250 \mu \mathrm{~A} / \mathrm{V}^{2}$, threshold voltage $\mathrm{V}_{\mathrm{T}}=0.65 \mathrm{~V}$ and $\mathrm{W} / \mathrm{L}=4$. Ignore the channel length modulation effect. The drain current of the transistor at the operating point is $\qquad$ $\mu \mathrm{A}$ (rounded off to nearest integer). |
| :---: | :---: |
|  |  |
|  |  |
| Q. 25 | The number of complex multiplications required for computing a 16 -point DFT using the decimation-in-time radix-2 FFT is $\qquad$ (in integer). |
|  |  |
| Q. 26 | A $3 \times 3$ matrix $P$ with all real elements has eigenvalues $\frac{1}{4}, 1$, and -2 . The value of $\left\|P^{-1}\right\|$ is $\qquad$ (rounded off to nearest integer). |
|  |  |
| Q. 27 | The Nyquist sampling frequency for $x(t)=10 \sin ^{2}(200 \pi t)$ is $\qquad$ Hz (rounded off to nearest integer). |
|  |  |


| Q. 28 | The resistance of a $20 \mathrm{k} \Omega$ resistor is measured six consecutive times using an LCR meter. The first five readings are $19 \mathrm{k} \Omega, 18 \mathrm{k} \Omega, 23 \mathrm{k} \Omega, 21 \mathrm{k} \Omega$ and $17 \mathrm{k} \Omega$. If the mean of the measurements and the true value are equal, the last reading is $\qquad$ $\mathrm{k} \Omega$ (rounded off to nearest integer). |
| :---: | :---: |
|  |  |
| Q. 29 | Consider the readout circuit of a piezoelectric sensor shown in the figure. <br> When the piezoelectric sensor generates a charge $q_{p}$, the resulting change in voltage $\mathrm{V}_{\mathrm{x}}$ is -2 V . Then the corresponding change in the voltage $\mathrm{V}_{\text {out }}$ is $\qquad$ V (rounded off to nearest integer). <br> Note: Assume all components are ideal. |
|  |  |
| Q. 30 | The voltage applied and the current drawn by a circuit are $\begin{aligned} v(t) & =95+200 \cos (120 \pi t)+90 \cos \left(360 \pi t-60^{\circ}\right) \mathrm{V} \\ i(t) & =4 \cos \left(120 \pi t-60^{\circ}\right)+1.5 \cos \left(240 \pi t-75^{\circ}\right) \mathrm{A} \end{aligned}$ <br> The average power absorbed by the circuit is $\qquad$ W (rounded off to nearest integer). |
|  |  |


| Q. 31 | The current $i(t)$ drawn by a circuit is given as $i(t)=4+30 \cos (t)-20 \sin (t)+15 \cos (3 t)-10 \sin (3 t) \mathrm{A}$ <br> The root-mean-square value of $i(t)$ is $\qquad$ A (rounded off to one decimal place). |
| :---: | :---: |
|  |  |
| Q. 32 | A linear potentiometer $(0-10 \mathrm{k} \Omega)$ is used to measure the water level as shown in the figure. The resistance between A and C varies linearly from 0 to $10 \mathrm{k} \Omega$ for a change in water level from 0 to 20 cm . The sensor is excited using a DC voltage source, $\mathrm{V}_{\mathrm{S}}=10 \mathrm{~V}$ with an internal resistance, $\mathrm{R}_{\mathrm{S}}=200 \Omega$. If $\mathrm{V}_{\text {out }}=5 \mathrm{~V}$, the water level is $\qquad$ cm (rounded off to one decimal place). |
|  |  |
|  |  |


| Q. 33 | The switch in the following figure has been closed for a long time $(t<0)$. It is opened at $t=0$ seconds. The value of $d v_{c} d t$ at $t=0^{+}$is $\qquad$ V/s (rounded off to nearest integer). |
| :---: | :---: |
|  |  |
| Q. 34 | Consider a system given by the following first order differential equation: $\frac{d y}{d t}=y+2 t-t^{2}$ <br> where, $y(0)=1$ and $0 \leq t<\infty$. Using a step size $h=0.1$ for the improved Euler method, the value of $y(t)$ at $t=0.1$ is $\qquad$ (rounded off to two decimal places). |
| Q. 35 | Indian Premier League has divided the sixteen cricket teams into two equal pools: Pool-A and Pool-B. Four teams of Pool-A have blue logo jerseys while the rest four have red logo jerseys. Five teams of Pool-B have blue logo jerseys while the rest three have red logo jerseys. <br> If one team from each pool reaches the final, the probability that one team has a blue logo jersey and another has a red logo jersey is $\qquad$ (rounded off to one decimal place). |
|  |  |

## Q. 36 - Q. 65 Carry TWO marks Each

| Q.36 | A wire of circular cross section with radius $a$ is shown in the figure. The current <br> density is given by $\mathbf{J}=k s^{2}$, where $k$ is a constant, $s$ is the radial distance from the <br> axis and $0 \leq s \leq a$. The total current $I$ in the wire is |
| :--- | :--- |
| (A) | $\frac{\pi k a^{4}}{2}$ |
| (B) | $\frac{2 \pi k a^{3}}{3}$ |
| (C) | $\frac{\pi k a^{3}}{2}$ |
| (D) | $\frac{\pi k a^{4}}{4}$ |


| Q. 37 | The measured values from a flow instrument, whose range is between 0 and 2 flow units, are shown in the histogram. The systematic error (bias) and the maximum error (in flow units), respectively are |
| :---: | :---: |
|  |  |
| (A) | 0.12 and 0.14 |
| (B) | 0.01 and 0.10 |
| (C) | 0.10 and 0.14 |
| (D) | 0.04 and 0.12 |
|  |  |


| Q. 38 | Consider a discrete-time sequence $x[n]= \begin{cases}(0.2)^{n}, & 0 \leq n \leq 7 \\ 0, & \text { otherwise }\end{cases}$ <br> The region of convergence of $X(z)$, the $z$-transform of $x[n]$, consists of |
| :---: | :---: |
|  |  |
| (A) | all values of $z$ except $z=0.2$ |
| (B) | all values of $z$ |
| (C) | all values of $z$ except $z=0$ |
| (D) | all values of $z$ except $z=\infty$ |
|  |  |


| Q. 39 | In the bridge circuit shown in the figure, under balanced condition, the values of R <br> and C respectively, are |
| :--- | :--- |
| (A) | $1.010 \Omega$ and $19.802 \mu \mathrm{~F}$ |
| (B) | $9.901 \Omega$ and $0.505 \mu \mathrm{~F}$ |
| (C) | $19.802 \Omega$ and $1.01 \mu \mathrm{~F}$ |
| (D) | $39.604 \Omega$ and $2.02 \mu \mathrm{~F}$ |


| Q. 40 | Laplace transform of a signal $x(t)$ is <br>  <br>  <br>  <br>  <br>  <br> Let $u(t)$ be the unit step function. Choose the signal $x(t)$ from the following options <br> if the region of convergence is $-7<\operatorname{Re}\{s\}<-6$. <br> (A) <br> (B) <br> $-e^{-6 t} u(t)-e^{-7 t} u(-t)$ <br> (C) <br> $e^{-6 t} u(t)-e^{-7 t} u(-t)-e^{-7 t} u(t)$ <br> (D) <br> $-e^{-6 t} u(-t)-e^{-7 t} u(-t)$ |
| :--- | :--- |


| Q.41 | In the figure shown, both the opamps $\mathrm{A}_{1}$ and $\mathrm{A}_{2}$ are ideal, except that the opamp $\mathrm{A}_{1}$ <br> has an offset voltage ( V os of 1 mV . For $\mathrm{V}_{\text {in }}=0 \mathrm{~V}$, the values of the output voltages <br> $\mathrm{V}_{\text {out }}$ and $\mathrm{V}_{\text {out } 2}$, respectively, are |
| :--- | :--- |
| (A) | 3 mV and -1 mV |
| (B) | 1 mV and 0 mV |
| (C) | 1 mV and -1 mV |
| (D) | 2 mV and 0 mV |


| Q. 42 | In the figure shown, the positive edge triggered D flip-flops are initially reset <br> to $\mathrm{Q}=0$. The logic gates and the multiplexers have no propagation delay. After <br> reset, a train of clock pulses (CLK) are applied. The logic-states of the inputs DIN, <br> S and the clock pulses are also shown in the figure. Assuming no timing violations, <br> the sequence of output Y from the $3^{\text {rd }}$ clock to the $5^{\text {th }}$ clock, $\mathrm{Y}_{3} \mathrm{Y}_{4} \mathrm{Y}_{5}$ is |
| :--- | :--- |
| (A) | 001 |
| (B) | 010 |
| (C) | 000 |
| (D) | 011 |


| Q. 43 | In the figure shown, $\mathrm{R}=1 \mathrm{k} \Omega$ and $\mathrm{C}=0.1 \mu \mathrm{~F}$. For a dc gain of -10 , the 3 dB <br> cut-off frequency (rounded off to one decimal place) is <br> Assume the opamp is ideal. <br> (A) <br> (B) <br> 159.1 Hz <br> (C) <br> 1750.7 Hz <br> (D) <br> 175.0 Hz |
| :--- | :--- |


| Q.44 | Consider the feedback control system shown in the figure. The steady-state error <br> $e_{s s}=\lim _{t \rightarrow \infty}(r(t)-y(t))$ due to unit step reference $r(t)$ is |  |
| :--- | :--- | :--- |
|  |  | $\frac{K-1}{K}$ |
| (A) | $\frac{1}{2}$ |  |
| (C) | 0 |  |
| (D) | $\frac{1-K}{K}$ |  |


| Q.45 | The transfer function of a system is |
| :--- | :--- |
|  | Choose the range of $\xi$ and $\omega_{n}($ in $\mathrm{rad} / \mathrm{s}$ ) from the following options such that the <br> poles lie on the shaded region of the $s$-plane as shown in the figure. |
|  |  |
| (A) | $\xi \geq \frac{1}{2}$ and $\omega_{n} \geq 2$ |
| (B) | $\xi \geq \frac{1}{4}$ and $\omega_{n} \geq 2$ |
| (C) | $\xi \geq \frac{1}{2}$ and $\omega_{n} \geq \sqrt{3}$ |
|  |  |


| Q.46 | Let $C$ be the closed curve in the $x y$-plane, traversed in the counterclockwise <br> direction along the boundary of the rectangle with vertices at <br> $(0,0),(2,0),(2,1),(0,1)$. The value of the line integral <br> is |
| :--- | :--- |
| (A) | $e_{C}\left(-e^{y} d x+e^{x} d y\right)$ |
| (B) | $e^{2}-2 e-3$ |
| (C) | $e^{2}+e-1$ |
| (D) | $e^{2}+e+1$ |
|  |  |


| Q. 47 | In the figure shown, assume <br> - $\alpha$ is the phase angle between the load current and the load voltage <br> - $\quad \beta$ is the phase angle by which pressure coil current lags the pressure coil voltage of the wattmeter <br> - $\gamma$ is the phase angle between currents in the pressure coil and the current coil of the wattmeter <br> - $\delta$ is the phase angle of the voltage transformer <br> - $\theta$ is the phase angle of the current transformer <br> When the load has a lagging phase angle of $\alpha$, which one of the following options is correct? |
| :---: | :---: |
|  |  |
| (A) | $\alpha=-\gamma \pm \delta \pm \theta-\beta$ |
| (B) | $\alpha=-\gamma \pm \delta \pm \theta+\beta$ |
| (C) | $\alpha=\gamma \pm \delta \pm \theta+\beta$ |
| (D) | $\alpha=\gamma \pm \delta \pm \theta-\beta$ |
|  |  |


| Q. 48 | Consider an ultrasonic measurement system shown in the figure. The ultrasonic transmitter (T) sends a continuous wave signal $x(t)=\cos \left(2 \pi f_{1} t\right)$ volts towards an object whose vibration is modeled as $\mathrm{m}(\mathrm{t})=0.5 \sin \left(2 \pi \mathrm{f}_{2} \mathrm{t}\right)$ volts. Neglecting the phase shift due to any other effect, the received signal at the receiver ( R ) is $y(t)=\cos \left(2 \pi f_{1} t+\beta \cos \left(2 \pi f_{2} t\right)\right)$ volts. <br> Assuming the frequency sensitivity factor as $500 \mathrm{~Hz} / \mathrm{volt}, \mathrm{f}_{1}=40 \mathrm{kHz}, \mathrm{f}_{2}=1 \mathrm{kHz}$, the modulation index $(\beta)$ and the frequency deviation in $y(t)$, respectively, are |
| :---: | :---: |
|  |  |
| (A) | 0.25 and $\pm 250 \mathrm{~Hz}$ |
| (B) | 0.5 and $\pm 500 \mathrm{~Hz}$ |
| (C) | 1 and $\pm 1000 \mathrm{~Hz}$ |
| (D) | 0.75 and $\pm 1000 \mathrm{~Hz}$ |
|  |  |


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| Q. 51 | In the figure shown, $\mathrm{R}=4.5 \mathrm{k} \Omega, \Delta \mathrm{R}=1.5 \mathrm{k} \Omega$, and INA is assumed to be ideal. <br> The equivalent resistance between A and B is <br> integer). |
| :--- | :--- |
| Q. 52 |  |


| Q. 53 | The 4-point DFTs of two sequences $x[n]$ and $y[n]$ are $X[k]=[1,-j, 1, j]$ and <br> $Y[k]=[1,3 j, 1,-3 j]$, respectively. Assuming $z[n]$ represents the 4-point circular <br> convolution of $x[n]$ and $y[n]$, the value of $z[0]$ is <br> nearest integer). <br> Note: The DFT of a $N$-point sequence $x[n]$ is defined as off to |
| :--- | :--- |
| Q.54 | Consider the figure shown. For zero deflection in the galvanometer, the required <br> value of resistor $\mathrm{R}_{\mathrm{x}}$ is |
| (rounded off to nearest integer). |  |


| Q. 55 | Consider a unity negative feedback system with its open-loop pole-zero map as shown in the figure. If the point $s=j \alpha, \alpha>0$, lies on the root locus, the value of $\alpha$ is $\qquad$ (rounded off to nearest integer). <br> Note: The poles are marked with $\times$ in the figure. |
| :---: | :---: |
|  |  |
| Q. 56 | A shielded cable with $\mathrm{C}_{\text {stray }}=20 \mathrm{pF}$ and $\mathrm{R}_{\text {wire }}=10 \Omega$ is used to connect the inductive sensors as shown in the figure. The RMS value of $\mathrm{V}_{\text {out }}$ is $\qquad$ $V$ (rounded off to two decimal places). <br> Note: Assume all components are ideal, and sensors are not magnetically coupled. |
|  |  |


| Q. 57 | In the figure shown, the diode current is given by $I_{D}=I_{S} e^{\frac{\alpha V_{D}}{T}} . V_{D}$ is the diode <br> voltage in volts, $T$ is the absolute temperature in Kelvin, $\alpha=1.16 \times 10^{4} \mathrm{~K} / \mathrm{V}$, and <br> $I_{S}=10^{-15} \mathrm{~A}$ is the saturation current. The dc current source, opamp and the <br> resistors are ideal, and are assumed to be temperature independent. The change in <br> the output voltage (Vout) per Kelvin change in temperature is <br> (rounded off to one decimal place). |
| :--- | :--- |
| Q. 58 | An ADC has a full scale voltage of 1.4 V , resolution of 200 mV , and produces <br> binary output data. The input signal of the ADC has a bandwidth of 500 MHz and <br> it samples the data at the Nyquist rate. The parallel data output is converted to a <br> serial bit stream using a parallel-to-serial converter. The data rate at the output of <br> the paraller-to-serial converter is |



| Q. 61 | A 50 kVA transformer has an efficiency of $95 \%$ at full load and unity power factor. Assume the core losses are negligible. The efficiency of the transformer at $75 \%$ of the full load and 0.8 power factor is $\qquad$ \% (rounded off to one decimal place). |
| :---: | :---: |
|  |  |
| Q. 62 | A three-phase squirrel-cage induction motor has a starting torque of $100 \%$ of the full load torque and a maximum torque of $300 \%$ of the full load torque. Neglecting the stator impedance, the slip at the maximum torque is $\qquad$ \% (rounded off to two decimal places). |
| Q. 63 | Two magnetically coupled coils, when connected in series-aiding configuration, have a total inductance of 500 mH . When connected in series-opposing configuration, the coils have a total inductance of 300 mH . If the self-inductance of both the coils are equal, then the coupling coefficient is $\qquad$ (rounded off to two decimal places). |
| Q. 64 | The solution of an ordinary differential equation $y^{\prime \prime \prime}+3 y^{\prime \prime}+3 y^{\prime}+y=30 e^{-t}$ is $y(t)=\left(c_{0}+c_{1} t-c_{2} t^{2}+c_{3} t^{3}\right) e^{-t}$ <br> Given $y(0)=3, y^{\prime}(0)=-3$ and $y^{\prime \prime}(0)=-47$, the value of $\left(c_{0}+c_{1}+c_{2}+c_{3}\right)$ is $\qquad$ (rounded off to nearest integer). <br> Note: $y^{\prime \prime \prime}=d^{3} y / d t^{3}, y^{\prime \prime}=d^{2} y / d t^{2}, y^{\prime}=d y / d t$ and $c_{0}, c_{1}, c_{2}, c_{3}$ are constants. |
|  |  |


| Q. 65 | A random variable $X$ has a probability density function |
| :--- | :--- |
| $\qquad f_{X}(x)=\left\{\begin{array}{cc\|}e^{-x}, & x \geq 0 \\ 0, & \text { otherwise }\end{array}\right.$ |  |
|  | The probability of $X>2$ is $\quad$ (rounded off to three decimal places). |
|  |  |


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| :---: | :---: | :---: | :---: | :---: | :---: |
| Instrumentation Engineering (IN) Final Answer Key |  |  |  |  |  |
|  |  |  |  |  |  |
| Q. No. | Session | Question Type | Section | Key/Range | Mark |
| 1 | 4 | MCQ | GA | A | 1 |
| 2 | 4 | MCQ | GA | B | 1 |
| 3 | 4 | MCQ | GA | D | 1 |
| 4 | 4 | MCQ | GA | A | 1 |
| 5 | 4 | MCQ | GA | B | 1 |
| 6 | 4 | MCQ | GA | D | 2 |
| 7 | 4 | MCQ | GA | B | 2 |
| 8 | 4 | MCQ | GA | C | 2 |
| 9 | 4 | MCQ | GA | A | 2 |
| 10 | 4 | MCQ | GA | A | 2 |
| 11 | 4 | MCQ | IN | B | 1 |
| 12 | 4 | MCQ | IN | B | 1 |
| 13 | 4 | MCQ | IN | D | 1 |
| 14 | 4 | MCQ | IN | A | 1 |
| 15 | 4 | MCQ | IN | A | 1 |
| 16 | 4 | MCQ | IN | A | 1 |
| 17 | 4 | MCQ | IN | B | 1 |
| 18 | 4 | MCQ | IN | A | 1 |
| 19 | 4 | MCQ | IN | C | 1 |
| 20 | 4 | MCQ | IN | A | 1 |
| 21 | 4 | NAT | IN | 0.15 to 0.17 | 1 |
| 22 | 4 | NAT | IN | 0.70 to 0.80 | 1 |
| 23 | 4 | NAT | IN | 1.6 to 1.6 | 1 |
| 24 | 4 | NAT | IN | 498 to 502 | 1 |
| 25 | 4 | NAT | IN | 32 to 32 | 1 |
| 26 | 4 | NAT | IN | -2 to -2 | 1 |
| 27 | 4 | NAT | IN | 400 to 400 | 1 |
| 28 | 4 | NAT | IN | 22 to 22 | 1 |
| 29 | 4 | NAT | IN | -3 to -3 | 1 |
| 30 | 4 | NAT | IN | 200 to 200 | 1 |


| 31 | 4 | NAT | IN | 27.0 to 30.0 | 1 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 32 | 4 | NAT | IN | 10.1 to 10.3 | 1 |
| 33 | 4 | NAT | IN | 15 to 15 | 1 |
| 34 | 4 | NAT | IN | 1.10 to 1.12 | 1 |
| 35 | 4 | NAT | IN | 0.5 to 0.5 | 1 |
| 36 | 4 | MCQ | IN | A | 2 |
| 37 | 4 | MCQ | IN | A | 2 |
| 38 | 4 | MCQ | IN | C | 2 |
| 39 | 4 | MCQ | IN | C | 2 |
| 40 | 4 | MCQ | IN | B | 2 |
| 41 | 4 | MCQ | IN | A | 2 |
| 42 | 4 | MCQ | IN | A | 2 |
| 43 | 4 | MCQ | IN | A | 2 |
| 44 | 4 | MCQ | IN | A | 2 |
| 45 | 4 | MCQ | IN | A | 2 |
| 46 | 4 | MCQ | IN | A | 2 |
| 47 | 4 | MCQ | IN | C | 2 |
| 48 | 4 | MCQ | IN | A | 2 |
| 49 | 4 | MSQ | IN | A; C | 2 |
| 50 | 4 | NAT | IN | 0.450 to 0.550 | 2 |
| 51 | 4 | NAT | IN | 4 to 4 | 2 |
| 52 | 4 | NAT | IN | 6.00 to 6.30 | 2 |
| 53 | 4 | NAT | IN | 2 to 2 | 2 |
| 54 | 4 | NAT | IN | 58 to 62 | 2 |
| 55 | 4 | NAT | IN | 2 to 2 | 2 |
| 56 | 4 | NAT | IN | 2.81 to 2.85 | 2 |
| 57 | 4 | NAT | IN | 9.5 to 10.5 | 2 |
| 58 | 4 | NAT | IN | 3 to 3 | 2 |
| 59 | 4 | NAT | IN | -2.6 to -2.4 | 2 |
| 60 | 4 | NAT | IN | 0 to 0 | 2 |
| 61 | 4 | NAT | IN | 95.2 to 95.4 | 2 |
| 62 | 4 | NAT | IN | 17.00 to 17.30 | 2 |
| 63 | 4 | NAT | IN | 0.25 to 0.25 | 2 |
| 64 | 4 | NAT | IN | 33 to 33 | 2 |
| 65 | 4 | NAT | IN | 0.130 to 0.140 | 2 |

