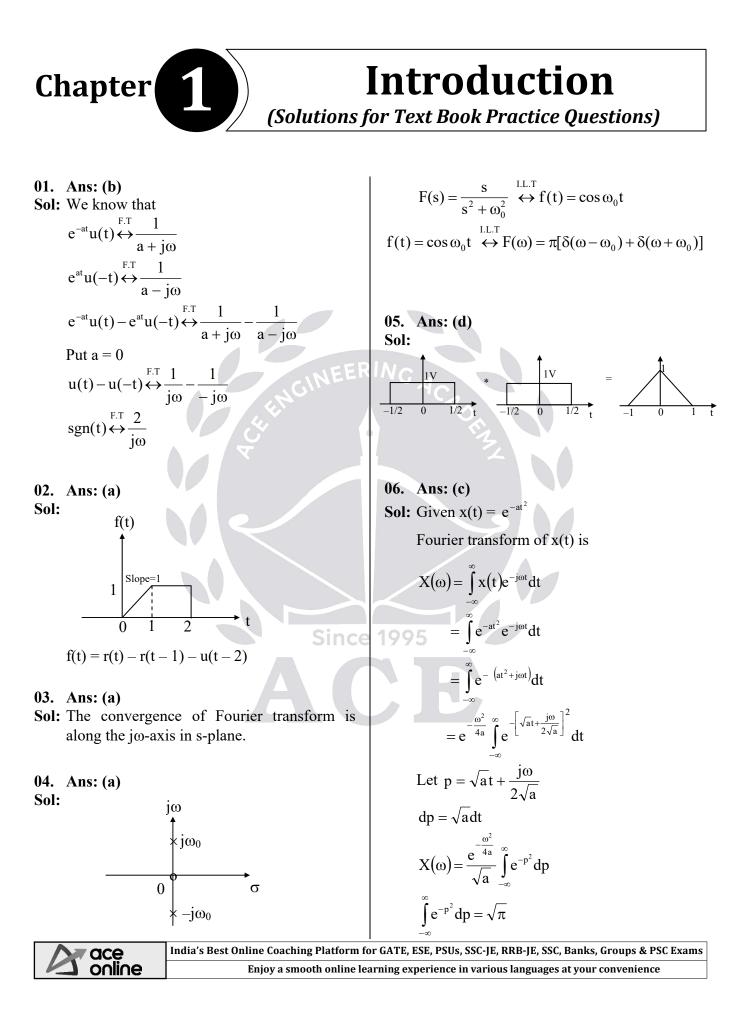




## Electronics & Communication Engineering

# COMMUNICATIONS

**Text Book:** Theory with worked out Examples and Practice Questions



$$X(\omega) = \frac{e^{-\frac{\omega^2}{4a}}}{\sqrt{a}}\sqrt{\pi}$$
$$X(\omega) = \sqrt{\frac{\pi}{a}}e^{-\frac{\omega^2}{4a}}$$

#### 07. Ans: (d)

**Sol:** The EFS expression of a periodic signal x(t)

is 
$$x(t) = \sum_{n=-\infty}^{\infty} c_n e^{jn\omega_0 t}$$

where,  $c_n$  is EFS coefficient.

$$X(\omega) = \sum_{n=-\infty}^{\infty} c_n FT \left[ e^{jn\omega_0 t} \right]$$
$$\underset{e^{jn\omega_0 t}}{\overset{1}{\leftrightarrow}} \frac{2\pi\delta(\omega)}{2\pi\delta(\omega - n\omega_0)}$$

$$X(\omega) = 2\pi \sum_{n=-\infty}^{\infty} c_n \delta(\omega - n\omega_0)$$

So, it is a train of impulse.

#### 08. Ans: (a)

**Sol:**  $V(j\omega) = e^{-j2\omega}; \ |\omega| \le 1$ 

Energy = 
$$\frac{1}{2\pi} \int_{-\infty}^{\infty} |V(j\omega)|^2 d\omega$$
  
=  $\frac{1}{2\pi} \int_{-1}^{1} |e^{-j2\omega}|^2 d\omega$   
=  $\frac{1}{2\pi} \int_{-1}^{1} 1d\omega$   
=  $\frac{2}{2\pi}$   
=  $\frac{1}{\pi}$ 

#### 09. Ans: (b)

**Sol:** Parseval's theorem is used to find the energy of the signal in frequency domain.

$$\therefore \int_{-\infty}^{\infty} |f(t)|^2 dt = \frac{1}{2\pi} \int_{-\infty}^{\infty} |F(j\omega)|^2 d\omega$$

10. Ans: (a)

**Sol:**  $f(t) = A.e^{-a|t|} \stackrel{F.T}{\longleftrightarrow} F(j\omega) = \frac{2Aa}{a^2 + \omega^2}$ 

11. Ans: (d) Sol:  $m(t) = f(t) \cos 2t$ Apply Fourier transform

$$M(\omega) = \frac{1}{2} [F(\omega - 2) + F(\omega + 2)]$$

$$M(\omega)$$

$$\frac{1}{2} \bigwedge^{1} \qquad \uparrow \qquad \frac{1}{2}$$

12. Ans: (b) Sol: For band limited signals,  $S(f) \neq 0; |f| < W$ S(f) = 0; |f| > W

#### 13. Ans: (a)

**Sol:** In a communication system, antenna is used to convert voltage variations to field variation and vice-versa.

14. Ans: (d)Sol: Hilbert transform of f(t) is

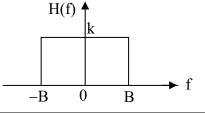
$$H.T{f(t)} = f(t)*\frac{1}{\pi t}$$

It is in the terms of 't'.

15. Ans: (a) Sol: For an ideal LPF

$$H(f) = k e^{-j\omega t_0} \quad \text{for } -B < f < B$$

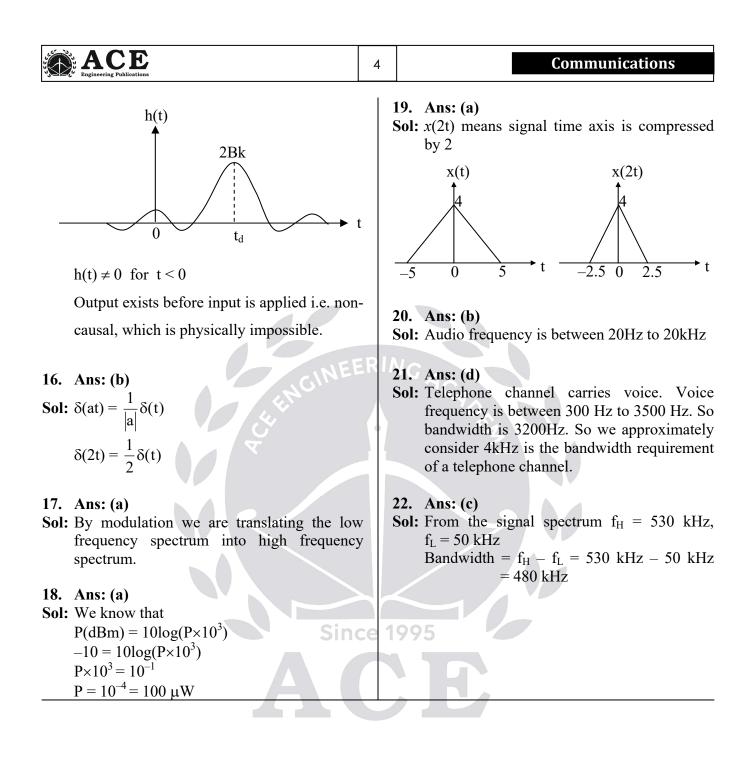
$$h(t) = F^{-1}[H(f)] = 2Bk \text{ sinc } 2B(t-t_d)$$



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Chapter 2 Amplitude Modulation

01. Ans: (a) Sol:  $V(t) = A_c . \cos \omega_c t + 2 \cos \omega_m t . \cos \omega_c t$ . Comparing this with the AM-DSB-SC signal A  $\cos \omega_c t + m(t) . \cos \omega_c t$ , it implies that  $m(t) = 2\cos \omega_m t \Longrightarrow E_m = 2$ To implement Envelope detection,  $A_c \ge E_m$  $\therefore (A_c)_{min} = 2$ 

#### 02. Ans: (d)

**Sol:**  $m(t) = (A_c + A_m \cos \omega_m t) \cos \omega_c t$ .

$$= A_{c}(1 + \frac{A_{m}}{A_{c}}\cos\omega_{m}t)\cos\omega_{c}t.$$

Given

 $A_c = 2A_m$ 

$$= \mathbf{A}_{c}(1 + \frac{1}{2}\cos\omega_{m}t)\cos\omega_{c}t.$$

$$P_{T} = \frac{A_{c}^{2}}{2} \left[ 1 + \frac{\mu^{2}}{2} \right], P_{s} = \frac{A_{c}^{2}}{2} \left[ \frac{\mu^{2}}{4} \right]$$
$$\frac{P_{T}}{P_{s}} = \frac{1 + \frac{\mu^{2}}{2}}{\frac{\mu^{2}}{4}} = \frac{1 + \frac{1}{8}}{\frac{1}{16}} = \frac{9}{8} \times 16$$

$$P_{\rm T} = 18 P_{\rm s}$$

03. Ans: (a) Sol:  $m(t) = 2\cos 2\pi f_1 t + \cos 2\pi f_2 t$  $C(t) = A_c \cos 2\pi f_c t$  $S(t) = [A_c + m(t)] \cos 2\pi f_c t$ 

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$$\begin{split} S(t) &= A_{c} [1 + \frac{1}{A_{C}} m(t)] cos 2\pi f_{c} t \\ K_{a} &= \frac{1}{A_{c}} \\ A_{m1} &= 2, A_{m2} = 1 \\ \mu_{1} &= K_{a} A_{m1} = \frac{2}{A_{C}}, \ \mu_{2} &= K_{a} A_{m2} = \frac{1}{A_{C}} \\ \mu &= \sqrt{\mu_{1}^{2} + \mu_{2}^{2}} \\ &\Rightarrow 0.5 &= \sqrt{\frac{4}{A_{c}^{2}} + \frac{1}{A_{c}^{2}}} \\ &\Rightarrow A_{C} &= \sqrt{20} \end{split}$$

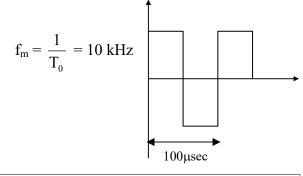
04. Ans: (c)

Sol: 
$$m(t) = -0.2 + 0.6 \sin \omega_1 t$$
,  $k_a = 1$ ,  $A_c = 100$   
 $S(t) = A_c [1 - 0.2 + 0.6 \sin \omega_1 t] \cos \omega_c t$   
 $= 100[0.8 + 0.6 \sin \omega_1 t] \cos \omega_c t$   
 $V_{max} = A_c [1 + \mu] = 100[0.8 + 0.6] = 140 V$   
 $V_{min} = A_c [1 - \mu] = 100[0.8 - 0.6] = 20 V$   
 $= 20V$  to 140 V

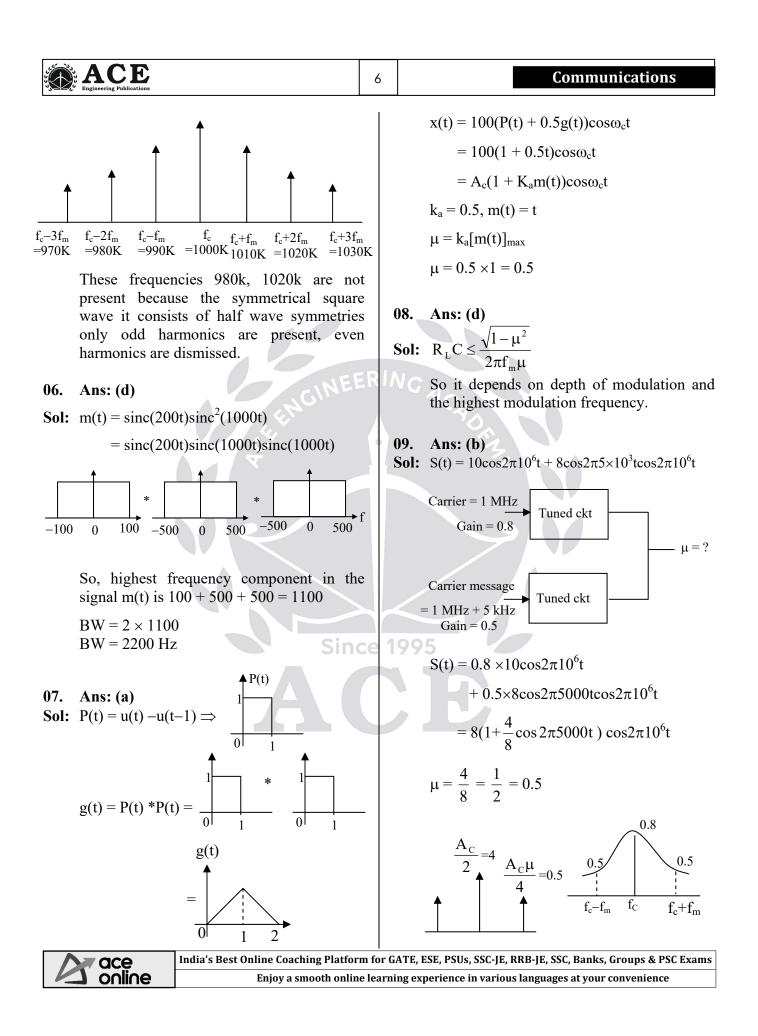
05. Ans: (c)

**Sol:**  $f_C = 1 \text{ MHz} = 1000 \text{ kHz}$ 

The given m(t) is symmetrical square wave of period T =  $100 \ \mu sec$ 



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	Ans: (d) $A_{max} = 10V$ $A_{min} = 5V$ $\mu = 0.1$ $\mu = \frac{A_{max} - A_{min}}{A_{max} + A_{min}} = \frac{1}{3} = 0.33$ $A_{C} = \frac{A_{max} + A_{min}}{2} = \frac{10 + 5}{2} = 7.5 V$ $A_{C}(1+\mu) = A_{C} + A_{c}\mu$ $\Rightarrow 10V = 7.5 + 2.5$	1 S
	$\mathbf{m}(\mathbf{t}) = 0 - \mathbf{A}$	
	$A_{\rm C}(1-\mu) = A_{\rm C} - A_{\rm C}\mu$ 5V = 7.5 - 2.5	
	Amplitude deviation $A_{C}\mu = 7.5 \times \frac{1}{3} = 2.5 \text{ V}$	
	$\mu_2 = 0.1 \Rightarrow A_{c2}\mu_2 = 2.5$ A <sub>c2</sub> = 25 V Which must be added to attain = 17.5	
11. Sol:	Ans: (d) Modulation index $\mu = k_a  m(t) _{max}$ $k_a = \frac{2b}{a} = \frac{2(\text{square term coefficient})}{\text{linear term coefficient}}$ $ m(t) _{max} = 1$ $\mu = 2\left(\frac{b}{a}\right)$	1 S
	$\mu = 2\left(\frac{1}{a}\right)$ $P_{SB} = \frac{1}{2}P_{C} \Longrightarrow P_{C}\frac{\mu^{2}}{2} = \frac{1}{2}P_{C}$	
	$\mu^2 = 1 \Longrightarrow \left(2\frac{b}{a}\right)^2 = 1$	
	$\Rightarrow 2\frac{b}{a} = 1 \Rightarrow \frac{a}{b} = 2$	
12. Sol:	Ans: 0.125 $s(t) = \cos (2000\pi t) + 4\cos (2400\pi t)$ $+ \cos (2000\pi t)$ Here $4\cos(2400\pi t)$ is the carrier signal.	
	$\cos (2000\pi t)$ and $\cos (2000\pi t)$ are the sideband message signals.	

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$$P_{c} = \frac{4^{2}}{2} = 8 W$$

$$P_{m} = \frac{1}{2} + \frac{1}{2} = 1 W$$

$$\frac{P_{m}}{P_{c}} = \frac{1}{8} = 0.125$$

7

13. Ans: (a, c & d) Sol:  $S_{AM}(t)=10\cos(2\pi\times5000t) + 25\cos(2\pi\times5200t) + 25\cos(2\pi\times4800t)$ 

$$\therefore \text{ USB Frequency} = 5200 \text{ Hz}$$
  
LSB Frequency = 4800 Hz  

$$\frac{A_{c}\mu}{2} = 25$$
  

$$\frac{10 \times \mu}{2} = 25$$
  

$$\therefore \mu = 5$$
  
a, c & d are correct.  
**NOTE:** options are changed for  
(a)  $\mu = 5$  (b)  $\mu = 2.5$ 

14. Ans: (a & c) Sol:  $S_{AM}(t) = K_1 \cos(2\pi \times 5000t) + K_2 \cos(2\pi \times 5200t) + K_3 \cos(2\pi \times 4800t)$ 

 $c(t) = 10 \cos(2\pi \times 5000t)$ 

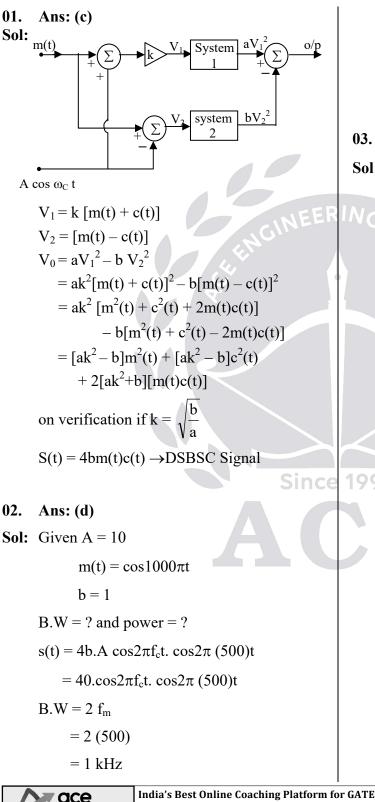
$$\begin{split} & K_1 = 10 = A_C & f_c + f_m = 5200 \text{ Hz} \\ & \mu = 0.5 & f_c - f_m = 4800 \text{ Hz} \\ & \therefore \frac{A_c \mu}{2} = K_2 = K_3 & \therefore 2 f_m = 400 \text{ Hz} \\ & \frac{10 \times 0.5}{2} = K_2 = K_3 & f_m = 200 \text{ Hz} \\ & \therefore K_2 = K_3 = 2.5 \\ & a \& c \ are \ correct. \end{split}$$

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Chapter

### **Sideband Modulation Techniques**



Power =  $\frac{A_c^2 A_m^2}{4}$  $= \frac{1600 \times 1}{4}$ = 400W

### 03. Ans: (c)

**Sol:** Carrier =  $\cos 2\pi (100 \times 10^6)$ t Modulating signal =  $\cos(2\pi \times 10^6)$ t Output of Balanced modulator  $= 0.5 [\cos 2\pi (101 \times 10^6)t + \cos 2\pi (99 \times 10^6)t]$ The Output of HPF is  $0.5 \cos 2\pi (101 \times 10^6)$ t Output of the adder is  $= 0.5 \cos 2\pi (101 \times 10^6) t + \sin 2\pi (100 \times 10^6) t$  $= 0.5 \cos 2\pi [(100+1)10^{6}t] + \sin 2\pi (100\times10^{6})t$  $= 0.5 [\cos 2\pi (100 \times 10^6) t. \cos 2\pi (10^6) t]$  $-\sin 2\pi (100 \times 10^6)$ t.  $\sin 2\pi (10^6)$ t]  $+\sin 2\pi (100 \times 10^6)t$ = 0.5 cos  $2\pi$  (100 ×10<sup>6</sup>)t. cos  $2\pi$  (10<sup>6</sup>)t + sin  $2\pi(100 \times 10^6)$ t [1-0.5 sin $2\pi$  (10<sup>6</sup>)t] Let  $0.5 \cos 2\pi (10^6)t = r(t) \cos \theta(t)$  $1 - 0.5 \sin 2\pi (10^6)t = r(t).\sin \theta(t)$ The envelope is  $\mathbf{r}(t) = [0.25 \cos^2 2\pi \ (10^6)t]$ + {1-0.5 sin  $2\pi$  (10<sup>6</sup>)t}<sup>2</sup>]<sup>1/2</sup>  $= [1.25 - \sin 2\pi (10^6)t]^{1/2}$ 

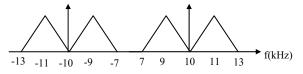
$$= \left[\frac{5}{4} - \sin 2\pi \, (10^6) t\right]^{1/2}$$



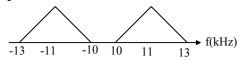
<b>A</b>	A	C	E	

04. Ans: (b)

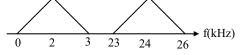
**Sol:** Output of 1<sup>st</sup> balanced modulator is



Output of HPF is



The Output of 2<sup>nd</sup> balanced modulator is consisting of the following +ve frequencies.



Thus, the spectral peaks occur at 2 kHz and 24 kHz.

Ans: (c) 05.

Sol: Given

$$f_{m_{1}} = 100 \text{Hz}, \ f_{m_{2}} = 200 \text{Hz}, \ f_{m_{3}} = 400 \text{Hz}, f_{c} = 100 \text{KHz}, \ f_{c_{L0}} = 100.02 \text{KHz} S(t) / T_{X} = \frac{A_{c}A_{m}}{2} [\cos(f_{c} + f_{m_{1}})t + \cos(f_{c} + f_{m_{3}})t] S(t) / R_{x} = [S(t) / T_{x}]A_{c} \cos 2\pi f_{c_{L0}}t 
$$\Rightarrow \frac{A_{c}^{2}A_{m}}{4} [\cos(f_{c} + f_{c_{L0}} + f_{m_{1}}) + \cos(f_{m_{1}} - 20) + \cos(f_{c} + f_{c_{L0}} + f_{m_{2}}) + \cos(f_{m_{2}} - 20) + \cos(f_{c} + f_{c_{L0}} + f_{m_{3}}) + \cos(f_{m_{3}} - 20)] Detector output frequencies: 80 \text{Hz}, 180 \text{Hz}, 380 \text{Hz}$$
  
**06.** Ans: (b)  
Sol: Given$$

SSB AM is used, LSB is transmitted

 $f_{10} = (f_c + 10)$ 

06.

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 $S(t)/T_{x} = \frac{A_{c}A_{m}}{2}\cos 2\pi [f_{c} - f_{m}]t$  $S(t) / R_{X} = \left[ \frac{A_{c}A_{m}}{2} \cos 2\pi (f_{c} - f_{m})t \right] \cos 2\pi (f_{c} + 10)t$  $\Rightarrow \frac{A_c A_m}{4} [\cos 2\pi (2f_c + 10 - f_m)t + \cos 2\pi (10 + f_m)t]$ 

i.e., from 310 Hz to 1010 Hz

07. Ans: (b)

**Sol:** BW of Basic group =  $12 \times 4 = 48$  kHz BW of super group =  $5 \times 48 = 240$  kHz

08. Ans: (d)

Sol: Given 11 voice signals B.W. of each signals = 3 kHzGuard Band Width = 1 kHzLowest  $f_c = 300 \text{ kHz}$ Highest f<sub>e</sub> =  $\Rightarrow f_{c_{H}} + f_{m_{lost}} = 300 \text{kHz} + 11(3 \text{kHz}) + 10(1 \text{kHz})$ = 343 kHz $f_{c_{H}} = 343 \, \text{kHz} - 3 \, \text{kHz}$  $= 340 \, \text{kHz}$ 

**09.** Ans: (b) **Sol:**  $f_{m1} = 5 \text{ kHz} \rightarrow AM$  $f_{m2} = 10 \text{ kHz} \rightarrow \text{DSB}$  $f_{m3} = 10 \text{kHz} \rightarrow \text{SSB}$  $f_{m4} = 2kHz \rightarrow SSB$  $f_{m5} = 5 k H z \rightarrow A M$  $f_g = 1 kHz$  $BW = (2fm_1 + 2f_{m_2} + f_{m_3} + f_{m_4} + 2f_{m_5} + 4f_s)$  $= 2 \times 5 + 2 \times 10 + 10 + 2 + 2 \times 5 + 4 \times 1$ = 10 + 20 + 10 + 10 + 6= 56 kHz $\therefore$  BW = 56 kHz

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	11. Ans: (a, c & d) Sol: For DSB-SC $\eta = 100\%$ $BW = 2f_{max} = 2 \times 3 \times 10^4 = 60 (kHz)$ S(t) = m(t) c(t) $= 50 cos(2\pi \times 10^7 t) cos(2\pi \times 10^4 t)$ $+ 50 cos(2\pi \times 10^7 t) 4 cos(6\pi \times 10^4 t)$ $P_t = 26.25 (kW)$ (a, c & d are correct)



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## **Angle Modulation**

- 01. Ans: (a) Sol:  $s(t) = 10 \cos(20\pi t + \pi t^2)$  $f_i = \frac{1}{2\pi} \frac{d\theta_i(t)}{dt}$  $f_i = \frac{1}{2\pi} [20\pi + 2\pi t]$  $\frac{df_i}{dt} = \frac{1}{2\pi} \times 2\pi \times 1 = 1 \text{Hz/sec}$
- 02. Ans: (d) Sol:  $P_{fc} = \frac{A_c^2 J_0^2(\beta)}{2}$

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So,  $J_0^2(\beta)$  is decreasing first, becoming zero and then increasing so power is also behave like  $J_0^2(\beta)$ .

#### 03. Ans: (a)

Sol: In an FM signal, adjacent spectral components will get separated by  $f_m = 5 \text{ kHz}$ 

Since BW = 
$$2(\Delta f + f_m) = 1$$
MHz  
= $1000 \times 10^3$   
 $\Delta f + f_m = 500$  kHz

 $\Delta f = 495 \text{ kHz}$ 

The  $n^{th}$  order non-linearity makes the carrier frequency and frequency deviation increased by n-fold, with the base-band signal frequency (f<sub>m</sub>) left unchanged since n = 3,

:. 
$$(\Delta f)_{New} = 1485 \text{ kHz} \&$$
  
 $(f_c)_{New} = 300 \text{ MHz}$   
New BW = 2(1485 + 5) ×10<sup>3</sup>  
= 2.98 MHz  
= 3 MHz

≥β

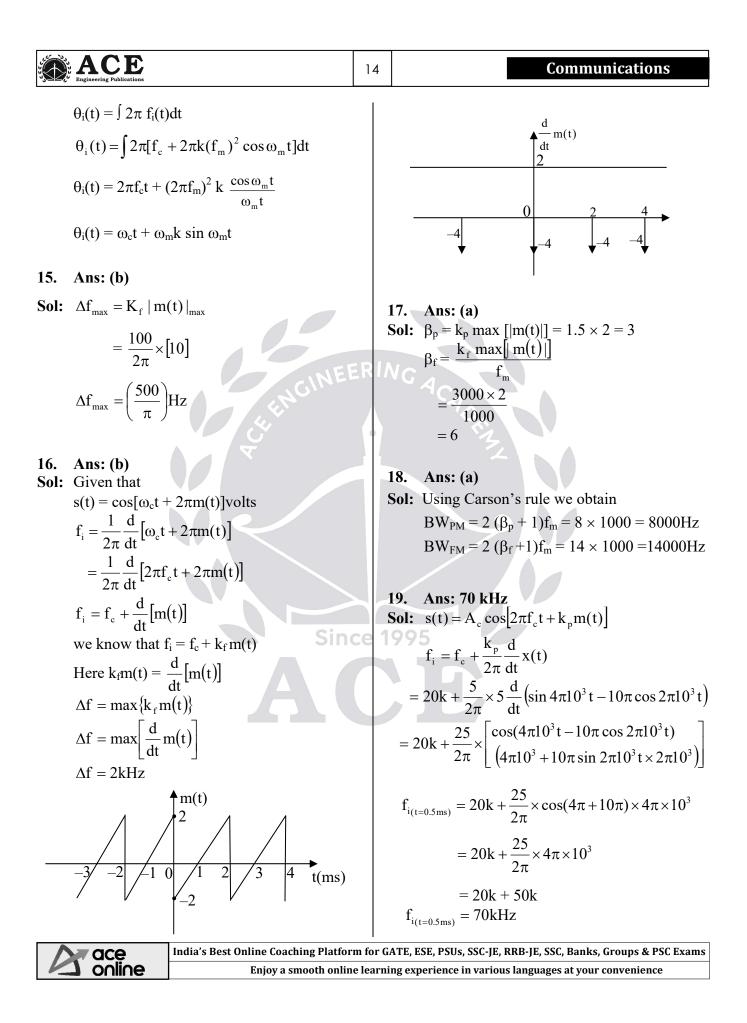
Fol: 
$$S(t) = A_c \sum_{n=-\infty}^{\infty} J_n(\beta) \cos 2\pi (f_c + nf_m) t$$
  
 $\Delta f = 3(2f_m) = 12 \text{ kHz}$   
 $\beta = \frac{\Delta f}{f_m} = 6$   
 $\therefore S(t) = \sum_{n=-\infty}^{\infty} 5.J_n(6) \cos 2\pi (f_c + nf_m) t$   
 $f_c = 1000 \text{ kHz}, f_m = 2 \text{ kHz}$   
 $= \cos 2\pi (1008 \times 10^3) t$   
 $= \cos 2\pi (1000 + 4 \times 2) \times 10^3 t$   
i.e.,  $n = 4$   
The required coefficient is  $5.J_4(6)$ 

05. Ans: (c)  
Sol: 
$$2\pi f_m = 4\pi \ 10^3$$
  
 $\Rightarrow f_m = 2k$   
 $J_0(\beta) = 0 \text{ at } \beta = 2.4$   
 $\beta = \frac{k_f A_m}{f_m} \Rightarrow 2.4 = \frac{k_f \times 2}{2k}$   
 $k_f = 2.4 \text{ KHz /V}$   
 $at \beta = 5.5$ 

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$5.5 = \frac{2.4 \mathrm{k} \times 2}{\mathrm{f_m}}$	From $f_c$ to $f_c + 4f_m$ pass through ideal BPF
III	Powers in these frequency components
$\Rightarrow$ f <sub>m</sub> = 872.72 Hz	$P = \frac{A_C^2}{2R} J_0^2(\beta) + 2 \frac{A_C^2}{2R} J_1^2(\beta) + 2 \frac{A_C^2}{2R} J_2^2(\beta)$
06. Ans: (c)	2R $2R$ $2R$ $2R$ $2R$
Sol: $\beta = 6$ $J_0(6) = 0.1506$ ; $J_3(6) = 0.1148$	$+2\frac{A_{\rm C}^2}{2R}J_3^2\beta+2\frac{A_{\rm C}^2}{1R}J_4^2(\beta)$
$J_1(6) = 0.2767 \; ; \; \; J_4(6) = 0.3576$	$\Lambda^{2} \left[ (-0.178)^{2} + 2(-0.328)^{2} + 2(0.049)^{2} \right]$
$J_2(6) = 0.2429$ ;	$= \frac{A_{\rm C}^2}{2R} \left[ \frac{(-0.178)^2 + 2(-0.328)^2 + 2(0.049)^2}{+ 2(0.365)^2 + 2(0.391)^2} \right]$
$\frac{P_{f_c \pm 4f_m}}{P_T} = ? \qquad P_T = \frac{A_c^2}{2R}$	= 41.17 Watts
GINE	08. Ans: (d)
$P_{f_{c}\pm 4f_{m}} = \frac{A_{C}^{2}}{R} \left  \frac{J_{0}^{2}(\beta)}{2} + J_{1}^{2}(\beta) + J_{2}^{2}(\beta) + J_{3}^{2}(\beta) + J_{4}^{2}(\beta) \right $	<b>Sol:</b> $P_t = \frac{A_c^2}{2R}$ (R =1 $\Omega$ )
$P_{f_{c \pm 4f_{m}}} = \frac{A_{c}^{2}}{R} \left[ \frac{J_{0}^{2}(\beta)}{2} + J_{1}^{2}(\beta) + J_{2}^{2}(\beta) + J_{4}^{2}(\beta) \right]$	$=\frac{100}{2}=50$ W
$\frac{P_{f_c \pm 4f_m}}{P_T} = \frac{0.2879}{\frac{1}{2}} = 0.5759 = 57.6 \%$	% Power = $\frac{Power in components}{total power} \times 100$
07. Ans: (c)	$=\frac{41.17}{50}\times 100$
<b>Sol:</b> $m(t) = 10\cos 20\pi t$	= 82.35%
$f_m = 10 Hz$ Sin	nce 1995 09. Ans: (d)
inserting correct signal and frequency	09. Ans: (d) Sol: In frequency modulation the spectrum
$\beta = \frac{k_f A_m}{5 \times 10} = 5$	contains $f_c \pm nf_1 \pm mf_2$ , where n & m =
$\beta = \frac{k_f A_m}{f_m} = \frac{5 \times 10}{10} = 5$	0, 1, 2, 3
$\frac{A_{C}J_{0}(\beta)}{2}$	10. Ans: (c)
$A_{C}J_{1}(\beta) \stackrel{2}{\uparrow} \underline{A_{C}J_{1}(\beta)}$	<b>Sol:</b> Given $f_c = 1MHz$
$\frac{2}{2}$ $A_{C}J_{2}(\beta)$	$f_{max} = f_c + k_f A_m$
$\frac{A_{C}J_{2}(\beta)}{2}$	$k_p = 2\pi \ k_f$
$ \xrightarrow{A_{C}J_{0}(\beta)}{2} \xrightarrow{A_{C}J_{1}(\beta)}{2} \xrightarrow{2} \xrightarrow{A_{C}J_{1}(\beta)}{2} \xrightarrow{2} \xrightarrow{A_{C}J_{2}(\beta)}{2} \xrightarrow{2} \xrightarrow{A_{C}J_{2}(\beta)}{2} \xrightarrow{2} \xrightarrow{A_{C}J_{2}(\beta)}{2} \xrightarrow{2} \xrightarrow{2} \xrightarrow{A_{C}J_{2}(\beta)}{2} \xrightarrow{2} \xrightarrow{2} \xrightarrow{2} \xrightarrow{2} \xrightarrow{2} \xrightarrow{2} \xrightarrow{2} $	$k_{\rm f} = \frac{k_{\rm p}}{2\pi} = \frac{\pi}{2\pi}$
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\frac{1}{f_m} = \frac{1}{2}$
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$= (10^{6} + 5 \times 10^{4})$ $= (10^{3} + 50)10^{3}$ $= (10^{3} + 50) k$ $= 1050 kHz.$ $f_{min} = f_{c} - k_{f} A_{m}$ $= (10^{6} - \frac{1}{2} \times 10)$ $= (10^{6} - 0.5 \times 10^{4})$	$\begin{pmatrix} 5 \\ 5 \end{pmatrix} = (10^{6} + 0.5 \times 10^{5})$ $\begin{pmatrix} 5 \\ 5 \end{pmatrix}$ $\begin{pmatrix} 5 \\ 0 \end{pmatrix}$	13.	$f_{i} = f_{c} \pm \Delta f$ $= f_{c} \pm k_{f} A_{m}$ $= 100 \times 10^{3} \pm 10 \times 10^{3} (m(t))$ $= 110 \text{ kHz } \& 90 \text{ kHz}$ Ans: (c) $S(t) = A_{c} \cos (2\pi f_{c}t + k_{p}m(t))$ $f_{i} = \frac{1}{2\pi} \frac{d}{dt} \theta_{i}(t) \xrightarrow{\theta_{i}(t)} \theta_{i}(t)$ $= \frac{1}{2\pi} \frac{d}{dt} (2\pi f_{c}t + k_{p}m(t))$ $= f_{c} + \frac{1}{2\pi} k_{p} \frac{d}{dt} m(t)$
$= (10^{3} - 50)10^{3}$ $= (10^{3} - 50) k$ $= 950 \text{ kHz}$			$f_{max} = f_c + \frac{k_p}{2\pi} \frac{1}{\left(\frac{10^{-3}}{4}\right)} = f_c + \frac{k_p}{2\pi} \times 4 \times 10^3$
11. Ans: (d) Sol: $\beta = \frac{\Delta f}{f_m}$		b	$= 100 \text{ kHz} + \frac{\pi}{2\pi} \times 4 \times 10^3$ $= 102 \text{ kHz}$
$\Delta \phi = \frac{\Delta f}{f_m}$ $\Delta f = \Delta \phi f_m$ $= k_p A_m f_m$			$f_{min} = f_{c} - k_{p} \frac{1}{\left(\frac{10^{-3}}{4}\right)}$ $= f_{c} - 2 \text{ kHz}$ $f_{min} = 98 \text{ kHz}$
12. Ans: (c)		14.	Ans: (c)
Sol: Given $+1$ -1 T/4	$=10^{-3} \text{sec}$	Sol:	Given, $S(t) = A_c \cos (\theta_i(t))$ $= A_c \cos (\omega_c t + \phi(t))$ $m(t) = \cos (\omega_m t)$ $f_i(t) = f_c + 2\pi k (f_m)^2 \cos \omega_m t$ $f_i = \frac{1}{2\pi} \frac{d\theta_i(t)}{dt}$
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20. Ans: (a, b & c) Sol: s(t) = 100cos[2π × 10 <sup>7</sup> t + 10sin(8π × 10 <sup>3</sup> t)] $\Delta f_i(t) = \frac{1}{2\pi} \frac{d}{dt} [10 sin(8π × 10^3 t)]$ $\Delta f_i(t) = 40 × 10^3 cos[8π × 10^3 t]$ $\Delta f_{max} = 40(kHz)$ $\beta = \frac{\Delta f_{max}}{f_{max}} = \frac{40 × 10^3}{4 × 10^3} = 10$ BW = 2[β+1] f <sub>max</sub> = 2 [10 + 1] 4×10 <sup>3</sup> = 88(kHz) $P_T = P_C = \left[\frac{100}{\sqrt{2}}\right]^2 = 5(kW)$ $\therefore$ a, b & c are correct		21. Ans: (a, c & d)







## **Radio Receivers**

#### 01. Ans: (d)

Sol: The image channel selectivity of super heterodyne receiver depends upon Pre selector and RF amplifier only.

#### 02. Ans: (b)

Sol: The image (second) channel selectivity of a super heterodyne communication receiver is determined by the pre selector and RF amplifier.

#### 03. Ans: (d)

**Sol:** Given  $f_s = 4$  to 10 MHz

IF = 1.8 MHz $f_{si} = ?$  $f_{si} = f_s + 2 \times IF$ = 7.6 MHz to 13.6 MHz

#### 04. Ans: (a)

**Sol:** Image frequency  $f_{si} = f_s + 2 \times IF$  $= 700 \times 10^{3} + 2(450 \times 10^{3})$ = 1600 kHzLocal oscillator frequency,  $f_l = f_s + IF$  $(f_l)_{max} = (f_s)_{max} + IF = 1650 + 450$ = 2100 kHz $(f_l)_{\min} = (f_s)_{\min} + IF = 550 + 450$ = 1000 kHz $R = \frac{C_{\text{max}}}{C_{\text{min}}} = \left(\frac{f_{l \text{max}}}{f_{l \text{min}}}\right)^2 = \left(\frac{2100}{1000}\right)^2 = 4.41$ 

05. Ans: (a) **Sol:**  $f_s(range) = 88 - 108MHz$ Given condition  $f_{IF} < f_{LO}$ ,  $f_{si} > 108$  MHz  $f_{si} = f_s + 2 \times IF$  $f_{si} > 108 \text{ MHz}$  $f_{s} + 2IF > 108 \text{ MHz}$ 

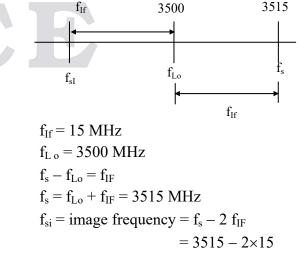
 $88MHz + 2 \times IF > 108 MHz$ IF > 10MHzAmong the given options IF = 10.7 MHz

#### **06.** Ans: (a)

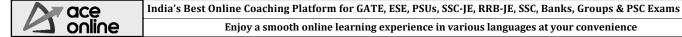
- Sol: Range of variation in local oscillator frequency is  $f_{Lmin} = f_{smin} + IF$ = 88 + 10.7 $f_{Lmin} = 98.7 \text{ MHz}$  $f_{Lmax} = f_{smax} + IF$ =108 + 10.7
  - $f_{Lmax} = 118.7 \text{ MHz}$
- 07. Ans: 5

**Sol:**  $f_s = 58 \text{ MHz} - 68 \text{ MHz}$ When  $f_s = 58 \text{ MHz}$  $f_{si} = f_s + 2IF > 68 \text{ MHz}$ 2IF > 10 MHz $IF \ge 5 MHz$ 





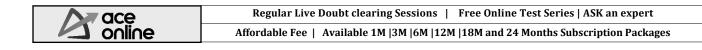
= 3485 MHz



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Engineering Publications	17	Postal Coaching Solutions
<b>09.</b> Ans: (a, b & c) <b>Sol:</b> → $f_{IM} = f_S + 2f_{IF} = 555 \times 10^3 + 2(455 \times 10^3)$ = 1465  kHz $\rightarrow f_{IF} = f_{Io} - f_S = 1010 \times 10^3 - 555 \times 10^3$ $= 455 \times 10^3 \text{ Hz}$ $\rightarrow IRR = \sqrt{1 + Q^2 \rho^2} = 113$ Q = 50 $\rho = \frac{f_{IM}}{f_S} - \frac{f_S}{f_{IM}} = \frac{1465}{555} - \frac{555}{1465}$ $\therefore$ a, b & c are correct.		10. Ans: (b & c) Sol: → $f_{Io} - f_s = f_{IF}$ $f_{Io} = f_{IF} + f_s$ $= 555 \times 10^3 + 1500 \times 10^3$ = 2055  kHz → $f_{IM} = f_s + 2f_{IF}$ $= 1500 \times 10^3 + 2(555 \times 10^3)$ = 2610  kHz $\therefore$ b & c are correct





Chapter

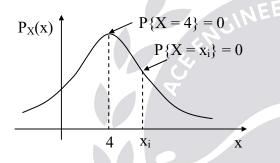
## **Random Variables & Noise**

#### 01. Ans: (c)

Sol: A continuous Random variable X takes every value in a certain range, the probability that X = x, is zero for every x in that range.

Given 
$$P_X(x) = \frac{1}{3\sqrt{2\pi}}e^{-\frac{(x-4)^2}{18}}$$
 is a

continuous Random variable therefore probability of the event  $\{X = 4\}$  is zero.



#### 02. Ans: (b)

Sol: Given,

X & Y are two Random Variables

 $Y = cos\pi x$ 

$$f(x) = 1$$
  $\frac{-1}{2} < x < \frac{1}{2}$ 

= 0 else where f(y) = 2

$$f(y) = f(x) \left| \frac{dx}{dy} \right|$$

$$x = \frac{1}{\pi} \cos^{-1}(y)$$

$$dx = \frac{1}{\pi} \times \frac{-1}{\sqrt{1 - y^2}} dy$$

$$\Rightarrow \frac{\mathrm{dx}}{\mathrm{dy}} = \frac{-1}{\pi\sqrt{1-y^2}}$$

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$$f(y) = \frac{1}{\pi \sqrt{1 - y^2}}$$
  
$$\sigma_y^2 = E[y^2] - [E[y]]^2$$

#### 03. Ans: (d)

**Sol:** The probability density function of the envelope of a sinusoidal plus narrrow band noise is Rician.

$$f_{\rm R}(\mathbf{r}) = \frac{\mathbf{r}}{\sigma^2} \exp(-\frac{\mathbf{r}^2 + \mathbf{A}^2}{2\sigma^2}) I_0(\frac{\mathbf{A}\mathbf{r}}{\sigma^2})$$

04. Ans: (a)

Sol: Given,

Differential equation of a system is

$$\frac{dy(t)}{dt} + y(t) = \frac{dx(t)}{dt} - x(t)$$

Applying Fourier transform,  

$$\Rightarrow Y(f)(1+jf) = X(f)(jf-1)$$

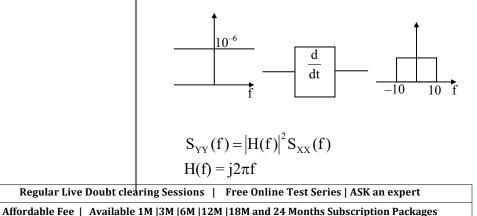
$$\frac{Y(f)}{X(f)} = \frac{-1 + jf}{1 + jf}$$

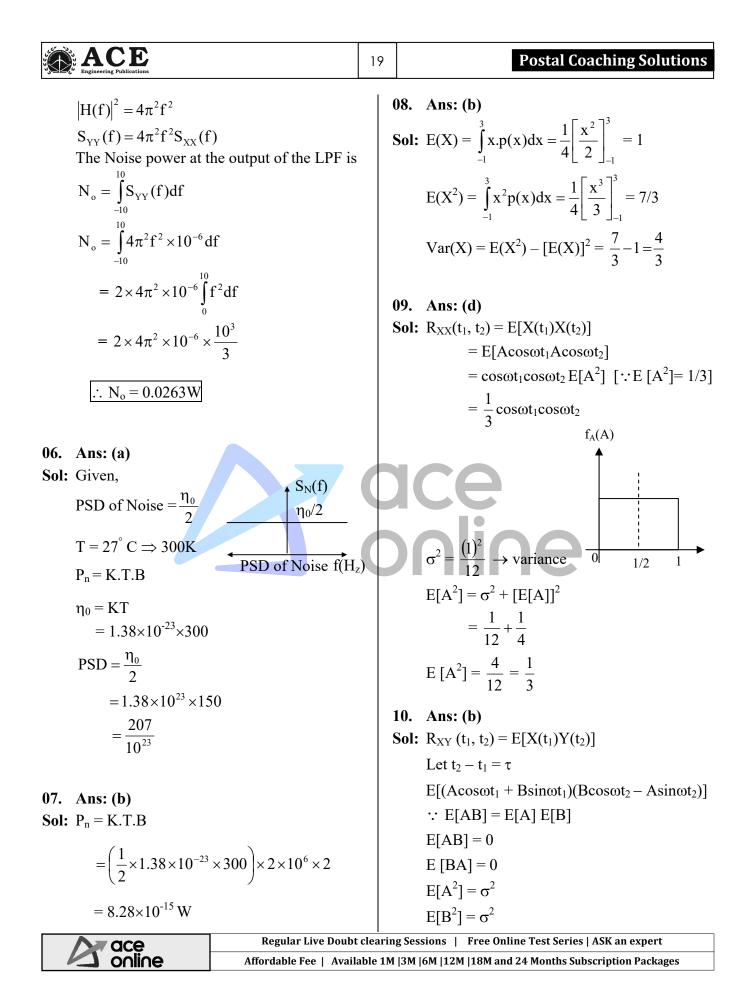
The transform function of system is a All pass filter

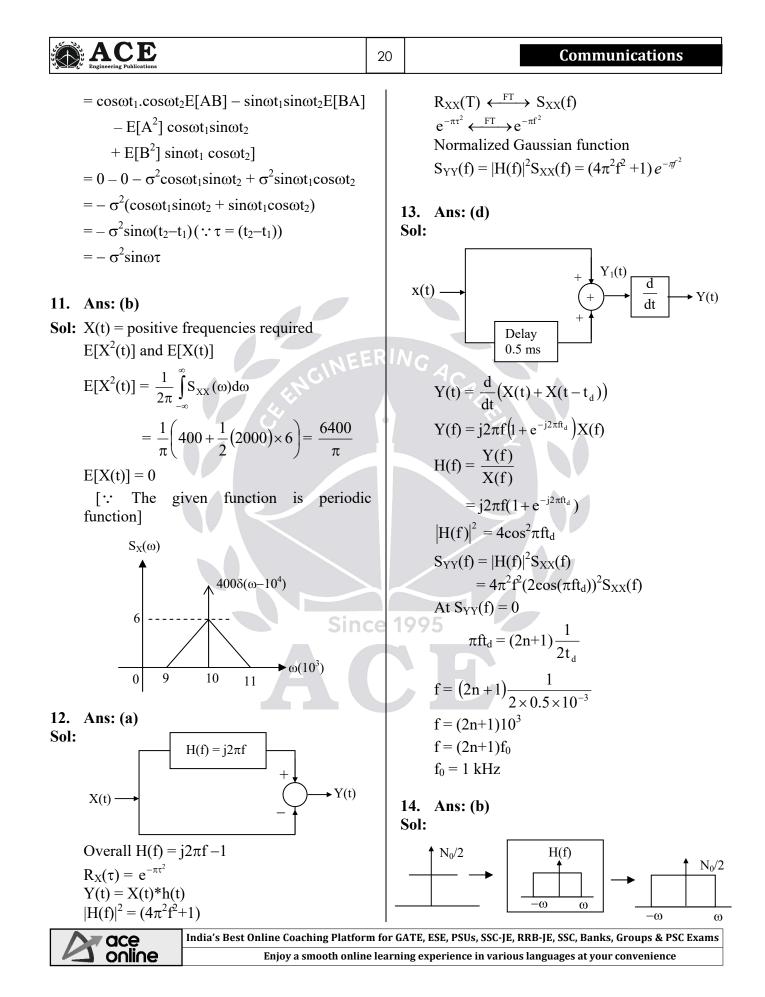
$$\therefore$$
 S<sub>y</sub>(f) = S<sub>x</sub>(f)

05. Ans: (a) Sol:

Since







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Uncorrelated  $\Rightarrow \operatorname{cov}(\tau) \Rightarrow R_{XX}(\tau) - \mu^2 \times (\tau)$   $\operatorname{cov}(\tau) = R_{XX}(\tau) \Rightarrow R_{n_0}(\tau) = 0$   $\Rightarrow N\omega_0 \sin(2\omega\tau) = 0, \sin Cx = 0; x \text{ is an}$ integer  $2\omega\tau = m$  $\tau = \frac{m}{2\omega}$ , integer m = 1, 2, 3 .....

#### 15. Ans: (b)

Sol: We know that,

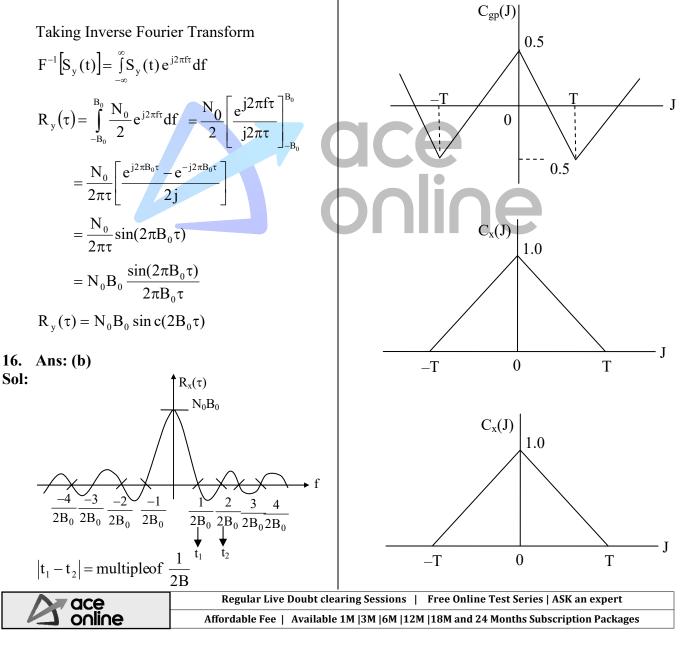
$$ACF \xleftarrow{F.T} S_x(f)$$

### 17.

Sol: Since

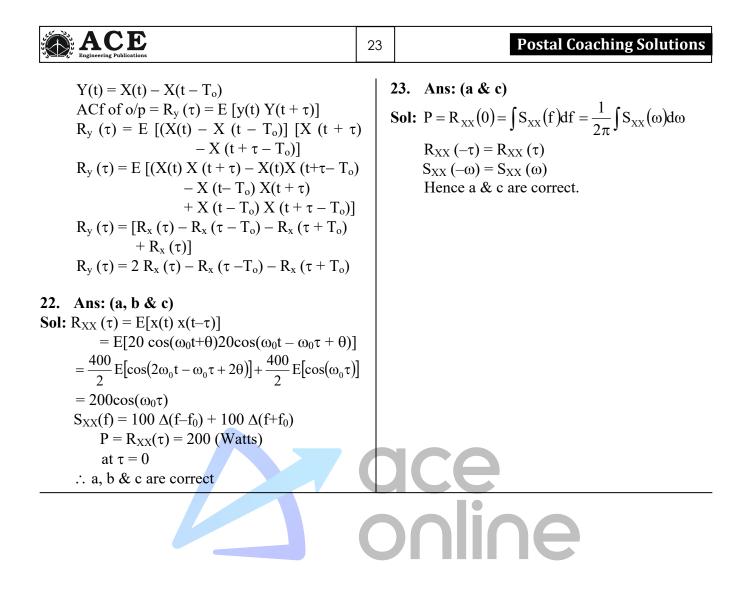
$$\begin{split} y(t) &= g_p\left(t\right) + X(t) + \sqrt{3/2} \\ \text{and } g_p\left(t\right) \text{ and } X\left(t\right) \text{ are uncorrelated, then } \\ C_Y(\tau) &= C_{g_p}(\tau) + C_X(\tau) \,. \end{split}$$

Where  $C_{gp}(\tau)$  is the auto covariance of the periodic component and  $C_x(\tau)$  is the auto covariance of the random component  $C_Y(\tau)$  is the plot figure shifted down by 3/2, removing the DC component  $C_{gp}(\tau)$  and  $C_x(\tau)$  are plotted below

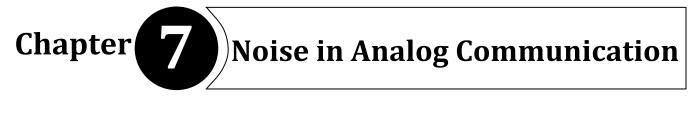


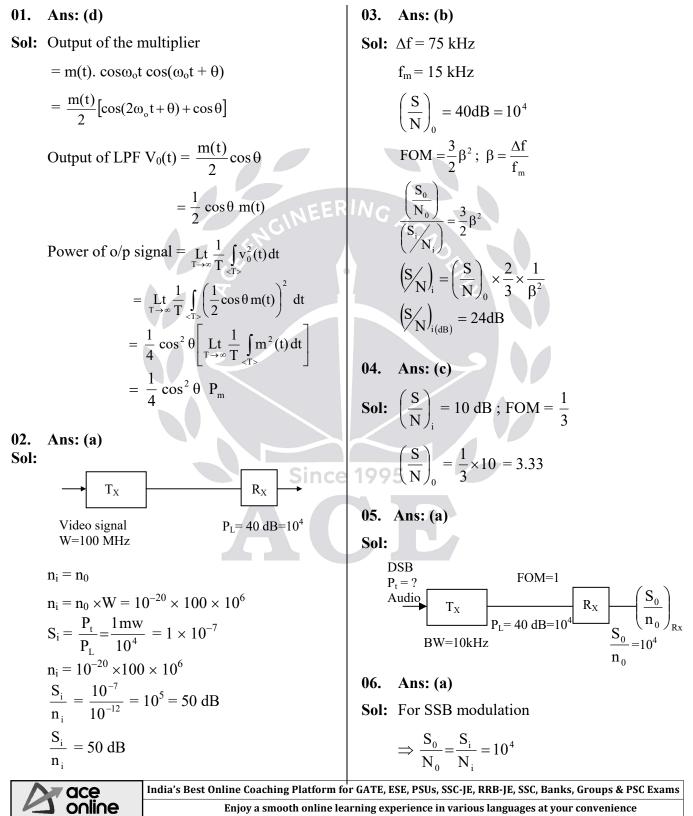
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Both $g_p(t)$ and $X(t)$ have zero mean Average (a) The power of the periodic component $g_p(t)$ is therefore, $\frac{1}{T_0} \int_{-T_0/2}^{T_0/2} g_p^2(t) dt = C_{g_p}(0) = \frac{1}{2}$ (b) The average power of the random component $x(t)$ is $E[X^2(t)] = C_x(0) = 1$	<ul> <li>therefore equal to f<sub>0</sub>.</li> <li>(d) If the sampling rate is f<sub>0</sub>/n, where n is an integer, the samples are uncorrelated. They are not, however, statistically independent. They would be statistically</li> </ul>
<ul> <li>18.</li> <li>Sol: <ul> <li>(a) The power spectral density consists of two components:</li> <li>(b) to b be for all the formula (b) to b be formula (b) to be formula (b) to b be formula (b) to b be formula (b) to b be</li></ul></li></ul>	$\frac{\text{Pre amp}}{\text{NF} = 2\text{dB}}$
<ol> <li>A delta function δ(t) and the origin whose inverse Fourier transform i one.</li> <li>A triangular component of uni amplitude and width 2f<sub>0</sub>, centered a the origin; the inverse Fourie</li> </ol>	s t t t t t t t t t t t t t
transform of this component is $f_{sinc}^2(f_0\tau)$ Therefore, the autocorrelation function of $X(t)$ is $R_X(\tau) = 1+f_0 sinc^2 (f_0\tau)$	= 169.36  K
Which is sketched below: $R_X(\tau)$ $1+f_0$ Sine	<b>20.</b> Ans: 100 W Sol: $E[x^2(t)] = E[(3V(t) - 8)^2]$ $= E[(9V(t)^2 + 64 - 2 \times 3V(t) \times 8]$
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$= E[(9V^{2}(t) + 64 - 48V(t)] \\= 9E[V^{2}(t)] + E[64] - 48E[V(t)] \\[EV(t)]=0, E[V^{2}(t)]=MS=R(0)=4e^{-5(0)}=4, \\E[constant] = constant] \\E[x^{2}(t)] = 9\times4 + 64 = 36 + 64 \\= 100$
(b) Since $R_X(\tau)$ contains a constant component of amplitude 1. It follows that the dc power contained in $X(t)$ is 1.	Sol
(c) The mean-square value of X(t) is given by $E[X^{2}(t)] = R_{X}(0)$ $= 1+f_{0}$	$X$ $X(t)$ $Delay T_0$ $Y(t)$
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(Only SSB modulation in one sided $n/2$ ) $P_t = ?$ $n/2$	$SNR_{o/p,dB} = SNR_{I/P,dB} - Nf_{dB} = 37 - 3$ $= 34 \text{ dB}$
$\frac{\mathbf{S}_{i}}{\mathbf{n}_{i}} = \frac{\mathbf{S}_{0}}{\mathbf{n}_{0}} = 10^{4} \qquad \qquad$	<b>09.</b> Ans: (a, c & d)
$\begin{split} \mathbf{S}_i &= 10^4 \times 10 \times 10^3 \times 2 \times 10^{-9} \text{ w/Hz} \\ \mathbf{S}_i &= 20 \times 10^{-2} \end{split}$	<b>Sol:</b> FOM Sinusoidal = $\frac{\mu^2}{2 + \mu^2} = \frac{\frac{1}{4}}{2 + \frac{1}{4}} = \frac{1}{9} = 0.111$
$(S_i)_{dB} = (P_t)_{dB} - (P_t)_{dB}$	FOM Triangular 1
$(P_t)_{dB} = (S_i)_{dB} + (P_L)_{dB}$ $P_t = S_i P_L = 20 \times 10^{-2} \times 10^4$	$=\frac{\mu^2 p_{mn}}{1+\mu^2 p_{mn}}=\frac{\overline{12}}{1+\frac{1}{12}}=\frac{1}{13}=0.0769$
$P_L = 2 \text{ kW}$	Here $P_{mn} = \frac{1}{3}$
07. Ans: (c) Sol: For AM	FOM Square wave $\frac{1}{1}$ 1
FOM = $\frac{1}{3}$ (if $\mu = 1$ ) $\frac{S_0}{N_0} = \left(\frac{1}{3}\right) \frac{S_i}{N_i} \implies S_i = 3 \left(\frac{S_0}{N_0}\right) \times N_i$	$= \frac{\mu^2 p_{mn}}{1 + \mu^2 p_{mn}} = \frac{\frac{1}{4}}{1 + \frac{1}{4}} = \frac{1}{5} = 0.2$ Here $P_{mn} = 1$
$= 3 \times 10^4 \times 2 \times 10^{-9} \times 10 \text{ kHz} = 0.6$ $\therefore P_t = S_i \times P_L = 0.6 \times 10^4 = 6 \text{ kW}$	FOM Square wave (at $\mu=1$ ) = $\frac{1}{1+1} = \frac{1}{2} = 0.5$ a, c & d are correct.
08. Ans: (b)	10. Ans: (b & c)
<b>Sol:</b> Noise figure = $\frac{(SNR)_{I/P}}{(SNR)_{O/P}}$	
$Nf_{,dB} = SNR_{i,dB} - SNR_{o/p,dB}$	



Chapter

### **Baseband Data Transmission**

- 01. Ans: (d) Sol:  $\Delta = \frac{V_{max} - V_{min}}{2^{n}}$  $\Delta \alpha \frac{1}{2^{n}}$ ;  $\frac{\Delta_{1}}{\Delta_{2}} = \frac{2^{n_{2}}}{2^{n_{1}}}$  $\frac{0.1}{\Delta_{2}} = \frac{2^{n+3}}{2^{n}}$  $\Delta_{2} = 0.1 \times \frac{1}{8}$ = 0.0125
- 02. Ans: (3)
- **Sol:** (BW)<sub>PCM</sub> =  $\frac{n f_s}{2}$

Where 'n' is the number of bits to encode the signal and  $L = 2^n$ , where 'L' is the number of quantization levels.

$$\begin{split} L_1 &= 4 \Longrightarrow n_1 = 2 \\ L_2 &= 64 \Longrightarrow n_2 = 6 \\ \frac{(BW)_2}{(BW)_1} &= \frac{n_2}{n_1} = \frac{6}{2} = 3 \\ (BW)_2 &= 3 \ (BW)_1 \end{split}$$

#### 03. Ans: (c)

Sol: Given, Two signals sampled are with  $f_s = 44100 \text{ s/sec}$ sample and each contains '16' bits Due to additional bits there is a 100%overhead. Out put bit rate =?  $R_{h} = n^{\dagger}f_{s}^{\dagger}$  $f_{s}^{\mid} = 2f_{s\mid} = 2 \text{ [44100]}$ (: two signals sampled simultaneously)

 $n^{|}=2n$ 

(:: due to overhead by additional bits)

 $R_b = 4 (nf_s) = 2.822 Mbps$ 

04. Ans (c)

Sol: Number of bits recorded over an hour =  $R_b \times 3600 = 10.16$  G.bits

05. Ans: (c)

Sol: 
$$p(t) = \frac{\sin(4\pi W t)}{4\pi W t (1-16 W^2 t^2)}$$

At 
$$t = \frac{1}{4W}$$
;  $P\left(\frac{1}{4W}\right) = \frac{0}{0}$ 

Use L-Hospital Rule

$$Lt_{t \to \frac{1}{4W}} p(t) = Lt_{t \to \frac{1}{4W}} \frac{4\pi W \cos(4\pi W t)}{4\pi W - 64\pi W^3 (3t^2)}$$
$$= \frac{4\pi W (-1)}{4\pi W - 64\pi W^3 3 \left(\frac{1}{16W^2}\right)}$$
$$= \frac{-4\pi W}{-8\pi W} = 0.5$$

06. Ans: 35

Since

Sol: Given bit rate  $R_b = 56$  kbps, Roll of factor  $\alpha = 0.25$ 

BW required for base band binary PAM system

BW = 
$$\frac{R_b}{2}[1 + \alpha] = \frac{56}{2}[1 + 0.25]kHz = 35kHz$$

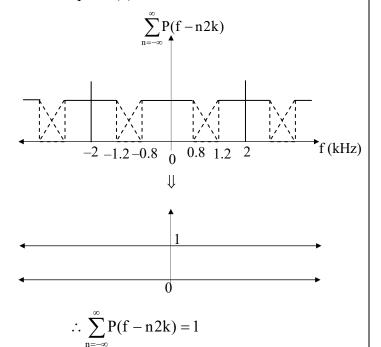
e 07. Ans: 16  
Sol: 
$$R_b = nf_s = 8bit/sample \times 8kHz = 64 kbps$$
  
 $(B_T)_{min} = \frac{R_b}{2 \log_2 M}$   
 $= \frac{R_b}{2 \log_2 4} = \frac{R_b}{2 \times 2}$   
 $= \frac{R_b}{4} = \frac{64}{4}$   
 $= 16kHz$ 



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### 08. Ans: (b) Sol: Given $f_s = 1/T_s = 2k$ symbols/sec If P(f) $\stackrel{F.T}{\leftrightarrow} p(t)$ , Condition for zero ISI is given by $\frac{1}{T_s} \sum_{n=-\infty}^{\infty} P(f - n / T_s) = p(0)$ $\Rightarrow \sum_{n=-\infty}^{\infty} P(f - n / T_s) = p(0)T_s$ p(0) = area under P(f) p(f) 1 -1.2 - 0.8 - 0 0.8 - 1.2 - 0.8k = 2k $p(0) T_s = 2k \times \frac{1}{2k} = 1$ $\Rightarrow \sum_{n=-\infty}^{\infty} P(f - n / T_s) = 1$

The above condition is satisfied by only option (b)



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#### 09. Ans: 200

Sol:  $m(t) = \sin 100\pi t + \cos 100\pi t$   $= \sqrt{2} \cos [100\pi t + \phi]$   $\Delta = 0.75 = \frac{V_{max} - V_{min}}{L} = \frac{\sqrt{2} - (-\sqrt{2})}{L} = \frac{2\sqrt{2}}{L}$   $L = \frac{2\sqrt{2}}{0.75} \approx 4 = 2^{n}$ So n = 2 f = 50 Hz so Nyquist rate = 100 So, the bit rate =  $100 \times 2 = 200$  bps

0. Ans: (b)  
ol: Given  

$$f_{m_1} = 3.6 \text{kHz} \Rightarrow f_{s_1} = 7.2 \text{kHz}$$
  
 $f_{m_2} = f_{m_3} = 1.2 \text{kHz} \Rightarrow f_{s_2} = f_{s_3} = 2.4 \text{kHz}$   
 $f_s = f_{s_1} + f_{s_2} + f_3$   
 $= 12 \text{kHz}$   
No. of Levels used = 1024  
 $\Rightarrow n = 10 \text{bits}$   
 $\therefore$  Bit rate = nf\_s  
 $= 10 \times 12 \text{ kHz}$   
 $= 120 \text{ kbps}$ 

11. Ans: (a) Sol:  $(f_s)_{min} = (f_{s_1})_{min} + (f_{s_2})_{min} + (f_{s_3})_{min} + (f_{s_4})_{min} = 200 + 200 + 400 + 800 = 1600 \text{ Hz}$ 

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12. Ans: (c) $2^n = 500$ Sol: $r = 9$ $C_1   C_2 \dots C_N $ $R_b = n(f_S)_{TDM} + 9$ $M_i = 12 C_1   C_2 \dots C_N $ $r = 9$ $M_i = 12 C_1   C_2 \dots C_N $ $r = 12 C_1   C_2 \dots C_N $ $M_i = 12 C_1   C_2 \dots C_N $ $r = 12 C_1   C_2 \dots C_N $ $M_i = 12 C_1   C_2 \dots C_N $ $r = 12 C_1   C_2 \dots C_N $ $M_i = 12 C_2 \dots C_N $ $r = 12 C_1   C_2 \dots C_N $ $M_i = 12 C_1   C_2 \dots C_N $ $r = 12 C_1   C_2 \dots C_N $ $M_i = 12 C_1   C_2 \dots C_N $ $r = 12 C_1   C_2 \dots C_N $ $M_i = 12 C_1   C_2 \dots C_N $ $r = 12 C_1   C_2 \dots C_N $ $M_i = 12 C_1   C_2 \dots C_N $ $r = 12 C_1   C_2 \dots C_N $ $M_i = 12 C_1   C_1   C_2 \dots C_N $ $r = 12 C_1   C_2   C_1   C_2   C_1   C_1   C_2   C_2   C_1   C_1   C_2   C_2   C_1   C_2   C_2   C_1   C_2   C_2   C_2   C_1   C_2   C_2   C_2   C_1   C_2   C_2$	
ECG signal B.W = 100Hz $(Q_e)_{max} \le (0.25) \% V_{max}$ $\frac{2V_{max}}{2 \times 2^n} \le \frac{0.25}{100} V_{max}$ $2^n \ge 400$ $n \ge 8.64$ $n = 9$ 15. Ans: (b)Sol: To avoid slope over loading the o/p of the Integrator are the Base band signal should $\therefore \Delta f_s =$ slope of base band $\Delta \times 32 \times 10^3 = 125$ $\Delta = 2^{-8}$ Volts.	and rate of rise of d be the same.
14. Ans: (a) Since 1995 16. Ans: (b)	
Sol: Peak amplitude $\rightarrow A_m$ Peak to peak amplitude $A_m$ $\frac{-\Delta}{2} \le Q_e \le \frac{\Delta}{2}$ A sol: $x(t) = E_m \sin 2\pi f_m(t)$ $\frac{\Delta}{T_s} < \left \frac{dm(t)}{dt}\right  \rightarrow slope on takes place$	verload distortion
PCM maximum tolerable $\frac{\Delta}{2} = 0.2\% A_{\rm m}$ $\Delta = \frac{\text{Peak to peak}}{L} \Rightarrow \frac{2A/m}{2L} = \frac{0.2}{100} A_{\rm m}$ $\Rightarrow \frac{\Delta f_{\rm s}}{2\pi} < E_{\rm m} f_{\rm m} \qquad (\because$	$\Delta = 0.628)$
$(:: \Delta = \frac{2A_{m}}{L})$ $\Rightarrow L = 500$ $\Rightarrow 2L = 100$ $\Rightarrow \frac{2\pi}{2\pi}$ $\Rightarrow \frac{0.628 \times 40K}{2\pi} < E_{m}f_{m}$ $f_{s} = 40 \text{ kHz} \Rightarrow 4 \text{ kHz} < E_{n}$	
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17. Sol:	Check for options (a) $E_m \times f_m = 0.3 \times 8 \text{ K} = 2.4 \text{ kHz}$ $(4K \leq 2.4 \text{ K})$ (b) $E_m \times f_m = 1.5 \times 4K = 6 \text{ kHz}$ (4K < 6  K)  correct (c) $E_m \times f_m = 1.5 \times 2 \text{ K} = 3 \text{ kHz}$ $(4K \leq 3K)$ (d) $E_m \times f_m = 30 \times 1 \text{ K} = 3 \text{ kHz}$ $(4K \leq 3K)$ Ans: (a) Given		20. 20. Sol	m(t) = Sinc (400t) × Sinc(600t) is sampled then which of the following option is/are correct. <b>NOTE:</b> options are changed (a) Nyquist rate = 2 kHz (b) Nyquist rate = 1 kHz (c) Nyquist interval = 0.5 ms (d) Nyquist interval = 1 ms <b>Ans:</b> (b & d) Sinc(400t) $\underbrace{CTFT}_{-200}$ $\underbrace{0}_{200}$
18.	$m(t) = 6 \sin (2\pi \times 10^{3} t) + 4 \sin (4\pi \times 10^{3} t)$ $\Delta = 0.314 V$ Maximum slope of $m(t) = \frac{d}{dt} (m(t))/t = \frac{\pi}{2}$ $= 2\pi \times 10^{3} (6) + 4\pi \times 10^{3} [4] = 28\pi \times 10^{3}$ Ans: (c) Pulse rate which avoid distortion $\Delta f_{s} = \frac{d}{dt} m(t)$			$\rightarrow f$ Sinc(600t) $\xrightarrow{\text{CTFT}}$ $\xrightarrow{-300} \xrightarrow{0} \xrightarrow{300}$ $\rightarrow f$ M(f) frequency will range from -500 to 500 Hz $\therefore f_q = 2f_{max} = 1 \text{ kHz}$ $T_s = \frac{1}{f_q} = 1 \text{ ms}$ b & d are correct
	$f_{s} = \frac{28\pi \times 10^{5}}{0.314}$ $f_{s} = 280 \times 10^{3} \text{ pulses/sec}$ Ans: (a, b & c) a. $r_{b} = (Nn + EB)f_{s}$ $r_{b} = (80 + 5) 5000 = 425(kbps)$ b. $r_{b} = Nnf_{s}$ $r_{b} = 10(8+1) 5000 = 450(kbps)$ c. $r_{b} = (Nn + EB)f_{s}$ $r_{b} = (80 + 10) 5000 = 450(kbps)$ d. $r_{b} = Nnf_{s}$ $r_{b} = 10(8+0.8) 5000 = 440(kbps)$ $\therefore$ a, b & c are correct			

Chapter

### **Bandpass Data Transmission**

01. Ans: (c) 04. Ans: (a) **Sol:**  $(BW)_{BPSK} = 2f_b = 20 \text{ kHz}$ Sol: Non coherent detection of PSK is not possible. So to overcome that, DPSK is  $(BW)_{OPSK} = f_b = 10 \text{ kHz}$ implemented. A coherent carrier is not required to be generated at the receiver. 02. Ans: (b) **Sol:**  $f_H = 25 \text{ kHz}$ ;  $f_L = 10 \text{ kHz}$ 05. Ans: (c) .: Center frequency **Sol:** In QPSK baud rate =  $\frac{\text{bit rate}}{2} = \frac{34}{2}$  $=\left(\frac{25+10}{2}\right)$  kHz = 17 Mbps= 17.5 kHz06. Ans: (d) .:. Frequency offset, Sol:  $\Omega = 2\pi \ (25 - 17.5) \times 10^3$ b(t) $o/p b^{1}(t)$  $=2\pi$  (7.5) × 10<sup>3</sup>  $= 15 \times 10^3 \pi \text{ rad/sec}$ Delay The two possible **FSK** signals are orthogonal, if  $2\Omega T = n\pi$ 0 0 b(t)0 0 0  $b^{1}(t)_{(Ref.bit)}$ 0 1 0  $\Rightarrow 2(15\pi) \times 10^3 \times T = n\pi$ Phase 0 π π π π  $\Rightarrow 30 \times 10^3 \times T = n$  (integer) This is satisfied for,  $T = 200 \mu sec.$ 07. Ans: (b) Sol: Given Bit stream 110 111001 Since 03. Ans: (a) Reference bit = 1**Sol:**  $r_b = 8$  kbps Coherent detection b(t) $\Delta f = \frac{nr_b}{2}$ Q(t)Best possible n = 1 $\Delta f = \frac{8K}{2} = 4K$  $b^{l}(t) = b(t) \odot Q(t)$  $1 \ 1 \ 0 \ 1 \ 1 \ 1 \ 0 \ 0 \ 1$ To verify the options  $\Delta f = 4k$ i.e.  $f_{C2} - f_{C1} = 4K$ (a) 20 K - 16 K = 4 K1 1 0 0 0 0 1 0 0 (b) 32 K - 20 K = 12 K(c) 40 K - 20 K = 20 KΟΟππππΟππ (d) 40 K - 32 K = 8 KIndia's Best Online Coaching Platform for GATE, ESE, PSUs, SSC-JE, RRB-JE, SSC, Banks, Groups & PSC Exams ace online Enjoy a smooth online learning experience in various languages at your convenience

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### 08. Ans: (d) Sol: $r_b = 1.544 \times 10^6$ $\alpha = 0.2$ $BW = \frac{r_b}{\log_2^M} (1 + \alpha)$ $= \frac{1.544 \times 10^6}{2} (1 + 0.2)$ ( $\therefore M = 4$ ) $BW = 926.4 \times 10^3$ Hz

09. Ans: 0.25 Sol: BW = 1500 Hz BW required for M-ary PSK is  $\frac{R_b[1+\alpha]}{\log_2 16} = 1500 Hz$  $\Rightarrow R_b [1+\alpha] = 1500 \times 4 = 6000$  $\Rightarrow (1+\alpha) = \frac{6000}{4800}$ Roll off factor  $\Rightarrow \alpha = \frac{6000}{4800} - 1 = 0.25$ 

10. Ans: (b) Sol:

> Here only phase is changing. From options (b) is the optimum answer.

#### 11. Ans: (b)

- **Sol:** Here 16-points are available in constellation which are varying in both amplitude and phase. So, it 16QAM.
- 12. Ans: (d)

Sol: BW = 
$$\frac{r_b}{\log_2 M} (1 + \alpha)$$
  
 $36 \times 10^6 = \frac{r_b}{2} (1 + 0.2) (:: M = 4, QPSK)$   
 $r_b = 60 \times 10^6 \text{ bps}$ 

#### NOTE: new question 13<sup>th</sup> is added in text book

13. Which among the following modulation, schemes consume less bandwidth(a) B-PSK(b) Q-PSK

(c) 64-PSK (d) 64-QAM

13. Ans: (c & d)

**Sol:** Bandwidth of 64-PSK  $=\frac{2r_b}{6}=\frac{r_b}{3}$ 

14. Ans: (a, b & d)Sol: M-ary ASK constellation plot will always come on a single line (either x-axis or y-axis).

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#### Communications

**Noise in Digital Communication** 

#### **Noise Ratio**

01. Ans: (b)

Chapter

**Sol:** Signal to quantization noise ratio only depends on no. of quantization levels (L) and no. of bits per sample(n)

For sinusoidal input SQNR = 1.76+6n dB=  $1.76+6\times12$ = 73.76 dB

For uniform distributed signal = 6ndB=  $6 \times 12$ = 72 dB

02. Ans: (a) Sol: For Bipolar pulses,

$$PSD = \frac{|P(\omega)|^2}{T_b} \cdot \sin^2\left(\frac{\omega T_b}{2}\right)$$

The zero magnitude occurs for  $f = n/T_b$ .  $\therefore$  The width of the major lobe =  $1/T_b$   $= f_b$   $\therefore$  (B.W)<sub>min</sub> =  $f_b$ Here, Data rate =  $nf_s$  = 8(8 kHz) = 64 kbps $\therefore$  (B.W)<sub>min</sub> = 64 kHz

03. Ans: (c)Sol: Since the signal is uniformly distributed,

$$f(x) = \frac{1}{10} \quad \text{for } -5 \le x \le 5$$
$$= 0 \quad : \text{ else where.}$$

Signal Power =  $\int_{-5}^{5} x^2 f(x) dx = \frac{25}{3} \text{ volts}^2$ Step size =  $\frac{V_{p-p}}{L} = \frac{10}{2^8} = 0.039 \text{ V}$  $N_q = \frac{\Delta^2}{12} = 0.126 \text{ mW}$ 

Signal to noise ratio, SNR in dB is

SNR = 
$$10 \log \left( \frac{\text{signal power}}{\text{Noise power}} \right)$$
  
=  $10 \log \left( \frac{25/3}{0.126 \times 10^{-3}} \right)$   
= 48 dB

04. Ans: (b)
Sol: For every one bit increase in data word length, quantization Noise Power becomes <sup>1</sup>/<sub>4</sub> th of the original. Hence, Data word length for n = 9 bits is, ∴ L = 2<sup>n</sup> = 2<sup>9</sup> = 512

**05.** Ans: (c) Sol:  $V_{P-P} = -5V$  to 5V  $20\log L = 43.5$  $L = 10^{2.175}$ = 149.6 $\Rightarrow \Delta = \frac{V_H - V_L}{L}$  $= \frac{5 - (-5)}{10^{2.175}}$  $\Delta = 0.06683$ 



Since

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06. Ans: (c) Sol: $f_{x}(x)$ 0.1V	$= \frac{5}{3} (125 \times 10^{-6} + 125 \times 10^{-6}) + \frac{10}{3} [(0.025)^3 + (0.025)^3]$ $= \frac{5}{3} (125 \times 10^{-6} + 125 \times 10^{-6}) + \frac{10}{3} (3.125 \times 10^{-5})$ $= \frac{1250}{3} \times 10^{-6} + \frac{312.5}{3} \times 10^{-6}$ $= 520.83333 \times 10^{-6}$ $(SNR)_{dB} = 10 \log \left(\frac{25}{3 \times 5.2 \times 10^{-4}}\right)$ $= 42.04  dB$ $\approx 42  dB$ $R_x(x)$
$= \frac{1}{10} \left( \frac{x^3}{3} \right)_{-5}^5 = \frac{1}{30} (250) = \frac{25}{3} \text{ W}$ Quantization Noise power $= \text{E}[[X - Q(X)]^2]$ $= \int_{-5}^5 [x - Q(x)]^2 f_x(x) dx$	<b>0</b> <b>0</b> $\frac{\Delta}{20}$ <b>1</b> $3\frac{\Delta}{2}$ <b>07.</b> Ans: (b) <b>Sol:</b> E[X - Q(x)] <sup>2</sup> $= \int_{0.3}^{0.3} (X - 0)^{2} (1) dx \int_{0.2}^{1} (X - (0.7))^{2} (1) dx$
$= \int_{-5}^{-4.9} [x - (-4.95)]^2 \frac{1}{10} dx$ + $\int_{-4.9}^{-4.8} [x - (-4.85)^2] \frac{1}{10} dx + \dots (50 \text{ times})$ + $\int_{0}^{0.05} (x - 0.025)^2 \frac{1}{10} dx$	$= \left[\frac{x^3}{3}\right]_0^{0.3} + \left[\frac{(x-0.7)^3}{3}\right]_{0.3}^1$ $= \frac{(0.3)^3}{3} + \frac{(0.3)^3}{3} + \frac{(0.4)^3}{3}$ $= 0.198$
$+ \int_{0.05}^{0.1} [(x - 0.075)^2] \frac{1}{10} dx + \dots (100 \text{ times})$ = 50 $\int_{-5}^{-4.9} (x + 4.95)^2 \frac{1}{10} dx + 100 \int_{0}^{0.05} (x - 0.025)^2 \frac{1}{10} dx$ = 5 $\left[ \frac{(x + 4.95)^3}{3} \right]_{-5}^{-4.9} + 10 \left[ \frac{(x - 0.025)^3}{3} \right]_{0}^{0.05}$ = $\frac{5}{3} [(0.05)^3 + (0.05)^3] + \frac{10}{3} [(0.025)^3 + (0.025)^3]$	<b>08.</b> Ans: (b) . Sol: Since, all the quantization levels are equiprobable, $\int_{-a}^{a} \frac{1}{4} dx = \frac{1}{3} \implies a = \frac{2}{3}$ <b>09.</b> Ans: (a) Sol: $\int_{2/3}^{2/3} x^{2} f(x) dx = \frac{1}{4} \int_{2/3}^{2/3} x^{2} dx = \frac{4}{81}$
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#### Communications

#### **Matched Filter**

#### 01. Ans: (d)

**Sol:** The time domain representation of the o/p of a Matched filter is proportional to Auto correlation function of the i/p signal, except for a time delay

$$R_{ss}(\tau) = \int_{0}^{10^{-4}} S(t) \cdot S(t+\tau) dt$$
  
=  $\int_{0}^{10^{-4}} 10 \sin(2\pi \times 10^{6} t) \cdot 10 \sin(2\pi \times 10^{6} (t+\tau)] dt$   
=  $50 \int_{0}^{10^{-4}} [\cos(2\pi \times 10^{6} \tau) - \cos(4\pi \times 10^{6} t + 2\pi \times 10^{6} \tau)] dt$   
=  $50 \times 10^{-4} \cos(2\pi \times 10^{6}) \tau$ 

 $\therefore$  The Peak is 5mV

#### 02. Ans: (b)

Sol: The matched filter has maximum value of output at t = T is energy of the signal

 $\Rightarrow \mathbf{E}_{s} = \int_{0}^{1} \mathbf{A}^{2} dt + \int_{2}^{3} \mathbf{A}^{2} (1) dt$  $= \mathbf{A}^{2} + \mathbf{A}^{2} = 2\mathbf{A}^{2}$ 

Sol: 
$$(SNR)_0 = \frac{E_s}{N_0} = \frac{\frac{B}{2} \cdot T}{N}$$
$$= \frac{B^2 T}{2N}$$

04. Ans: (b)

Sol: Given,

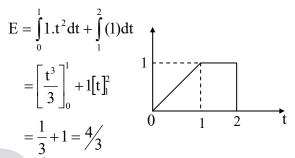
$$\frac{S_{02}(t)}{N} = \frac{S_{01}(t)}{N} \Longrightarrow \frac{2E_{s_1}}{N} = \frac{2E_2}{N}$$
$$A^2T = \frac{B^2}{N}T \implies A = \frac{B}{N}$$

 $\sqrt{2}$ 

2

#### 05. Ans: (d)

**Sol:** Output of the matched filter is maximum which is equal to the energy in the signal



The time instant which occurs the maximum value is its time period T = 2

#### 06. Ans: (c)

Sol: Given,

$$H(f) = \frac{1 - e^{-j\omega t}}{j\omega}$$

$$H(f) = \frac{1}{j\omega} - \frac{e^{-j\omega t}}{j\omega}$$
Applying I.F.T
$$h(t) = 0.5(sgn(t) - sgn(t - T_0))$$

$$\left(\because F(sgn(t)) = \frac{2}{j\omega}\right)$$

$$= 0.5[2 u(t) - 1 - [2u(t - T_0) - 1]]$$

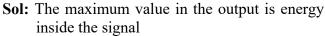
$$= [u(t) - u(t - T_0)]$$
We know that
$$h(t) = s^*(t - T)$$

$$h(t) = s^{*}(t - T)$$

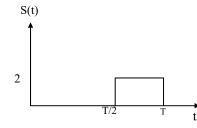
$$\therefore S_{i}(t) \qquad 0 \qquad T$$

07. Ans: (d)

Since 19



→ t



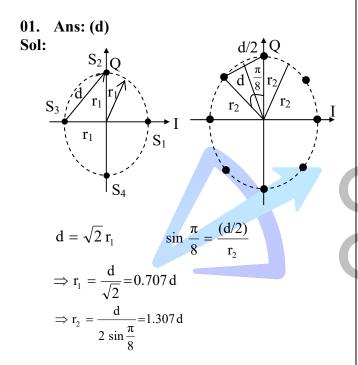
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$$\Rightarrow S_0(t)\Big|_{max} = \int_{\frac{T}{2}}^{T} 2^2 dt$$
$$= 4 \int_{\frac{T}{2}}^{T} 1 dt$$
$$= 4 [T - \frac{T}{2}]$$
$$= 2T$$

### **Probability of Error**

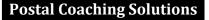


#### 02. Ans: (d)

Sol: 4-PSK, 8-PSK both have same error probability when both signals have same minimum distance between pairs of signal points.

$$P_{e} = Q\left(\frac{\sqrt{d_{min}^{2}}}{2N_{0}}\right)$$
$$P_{e} = 2Q\left(\sqrt{\frac{2E_{s}}{N_{0}}}\sin^{2}\left(\frac{\pi}{N_{0}}\right)\right)$$

Where  $E_s$  is the average symbol energy



Given both constellation  $d_{min}$ is same i.e., 'd'

$$(\mathbf{E}_{s})_{4\text{PSK}} = \frac{\mathbf{E}_{s_{1}} + \mathbf{E}_{s_{2}} + \mathbf{E}_{s_{3}} + \mathbf{E}_{s_{4}}}{4}$$

Where  $E_{s_k}$  is the symbol 'S<sub>k</sub>' Energy

= (distance from the origin to the symbol  $(S_{k})^{2}$ 

$$(E_s)_{4PSK} = \frac{r_1^2 + r_1^2 + r_1^2 + r_1^2}{4} = r_1^2$$

Similarly, For 8 PSK

$$(E_s)_{8PSK} = r_2^2$$

$$\frac{(E_{s})_{8PSK}}{(E_{s})_{4PSK}} = \left(\frac{r_{2}}{r_{1}}\right)^{2} = \left(\frac{1.307d}{0.707d}\right)^{2}$$
  
In dB

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$$(E_{s})_{8PSK(dB)} - (E_{s})_{4PSK(dB)} = 10 \log \left(\frac{1.307}{0.707}\right)^{2}$$
  
= 5.33 dB  
$$(E_{s})_{8PSK} = (E_{s})_{4PSK} + 5.33 \text{ dB}$$
  
8 PSK required additional 5.33 dB

Sol: Constellation 1:

$$s_{1}(t) = 0;$$
  

$$s_{2}(t) = -\sqrt{2} a \phi_{1} + \sqrt{2} a \phi_{2}$$
  

$$s_{3}(t) = -2\sqrt{2} a \phi_{1};$$
  

$$s_{4}(t) = -\sqrt{2} a \phi_{1} - \sqrt{2} a \phi_{2}$$

Energy of  $S_1(t) = E_{S1} = 0$ ;  $E_{S2} = 4a^2$ ;  $E_{S3} = 8a^2$ ;  $E_{S4} = 4a^2$ 

Average Energy of constellation 1  $a^2$ 

$$=\frac{E_{S1}+E_{S2}+E_{S3}+E_{S4}}{4}=4a$$

**Constellation 2:** 

$$\begin{aligned} s_1(t) &= a \phi_1 \quad \Rightarrow \ E_{S1} &= a^2 \\ s_2(t) &= a . \phi_2 \quad \Rightarrow \ E_{S2} &= a^2 \end{aligned}$$

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$$\begin{split} s_3(t) &= -a.\varphi_1 \implies E_{S3} = a^2\\ s_4(t) &= -a.\varphi_2 \implies E_{S4} = a^2\\ \text{Average Energy of constellation 2}\\ &= \frac{E_{S1} + E_{S2} + E_{S3} + E_{S4}}{4} = a^2 \end{split}$$

The required Ratio is 4

#### 04. Ans: (a)

Sol: The distance between the two closest points in constellation 1 is  $d_1 = 2a$ .

The same in constellation 2,

$$\mathbf{d}_2 = \sqrt{2} \mathbf{a}$$

Since  $d_1 > d_2$ , Probability of symbol error for constellation 1 is lower

05. Ans: (a)  
Sol: 
$$S(t) = \sqrt{\frac{2E}{T_b}} \left[ \cos(\omega_c t + \frac{2\pi}{m}(i-1)) \right]$$
  
 $= \sqrt{\frac{2E}{T_b}} \left[ \cos\omega_c t..\cos\left(\frac{2T}{m}(i-1)\right) - \sin\omega_c t.\sin\frac{2\pi}{m}(i-1) \right]$   
 $= \sqrt{\frac{2}{T_b}} \cos\omega_c \sqrt{E} \cos\left(\frac{2\pi}{m}(i-1)\right) - \sqrt{\frac{2}{T_b}} \sin\omega_c \sqrt{E} \sin\frac{2\pi}{m}(i-1)$   
Given binary digital communication m = 2  
 $\sqrt{\frac{2}{T_b}} \cos\omega_c t \sqrt{E} \cos\pi$   
 $\therefore$  basic function = 2 cos  $\omega_c t$ 

$$\Rightarrow T_b = \frac{1}{2}$$

$$2\cos\omega_{c}t\left(\sqrt{E}\cos\pi(f-1)\right) - [2\sin\omega_{c}t]\sqrt{E}\sin\pi(i-1)$$

$$\begin{array}{c|c} -\mathbf{x} & \mathbf{x} \\ (-\sqrt{E},0) & (\sqrt{E},0) \end{array}$$

Distance between two points is:

$$\sqrt{(\sqrt{E} + \sqrt{E})^2} + 0$$
$$\sqrt{4E} = 2\sqrt{E}$$



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Energy of the signal:  

$$\int_{0}^{T_{b}} (A \cos \omega_{c} t)^{2} = \frac{A^{2}T}{2}$$

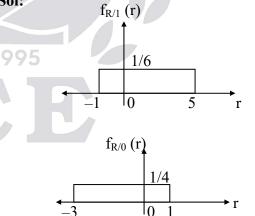
$$\Rightarrow d = 2\sqrt{\frac{A^{2}T_{b}}{2}} = 2\sqrt{\frac{A^{2} \times T_{b}}{2}} = A$$

$$\left(:: T_{b} = \frac{1}{2}\right) \qquad \therefore \quad d = A$$

06. Ans: (c)

Sol: 
$$P_e = Q\left[\sqrt{\frac{E_b}{N_o}}\right]$$
  
 $E_b = \frac{\alpha^2 T_b}{2} = \frac{\alpha^2}{2R_b}$   
 $\alpha = 4mV, R_b = 500 \text{ kbps},$   
 $N_o = 10^{-12} \text{W/Hz}.$   
 $\frac{E_b}{N_o} = \frac{16 \times 10^{-6}}{2 \times 500 \times 10^3 \times 10^{-12}} = 16$   
 $P_e = Q\left[\sqrt{16}\right] = Q[4]$ 

07. Ans: (d) Sol:



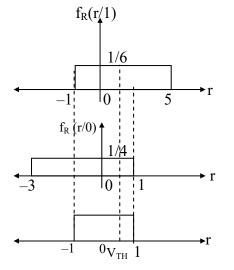
P(0) = 1/3; P(1) = 2/3

The probability of error of the symbols 0 & 1 are not the same.

 $\therefore$  The intersection point of the two pdf's is

not the threshold of detection.

Assume the threshold value to be  $V_{\text{TH}}$ 



For minimum error the  $V_{TH}$  should lie in the area of intersection of the 2 pdf's.

$$P_{e_{1}} = \int_{-1}^{V_{TH}} \left(\frac{1}{6}\right) dr = \frac{1}{6} \left(V_{TH} + 1\right)$$
$$P_{e_{0}} = \int_{V_{TH}}^{1} \left(\frac{1}{4}\right) dr = \frac{1}{4} \left(1 - V_{TH}\right)$$

Decision error probability

$$= P_{e_0} P(0) + P_{e_1} P(1)$$
  
=  $\frac{1}{4} (1 - V_{TH}) \left(\frac{1}{3}\right) + \frac{1}{6} (1 + V_{TH}) \left(\frac{2}{3}\right)$   
 $P_e = \frac{1 - V_{TH}}{12} + \frac{2(1 + V_{TH})}{18}$   
For minimum decision error proba

For minimum decision error probability,  $-1 \le V_{TH} \le 1$ For  $V_{TH} = -1$ 1 - (-1) 1

BER = 
$$\frac{1-(-1)}{12} = \frac{1}{6}$$
 (min value)

 $\therefore$  Decision error probability = 1/6

#### 08. Ans: (c)

**Sol:** The optimum threshold value is

$${}^{\Lambda}_{X} = \frac{\sigma^{2}}{x_{1} - x_{2}} \left[ \ell n \frac{P(x_{2})}{P(x_{1})} + \frac{x_{1}^{2} - x_{2}^{2}}{2\sigma^{2}} \right]$$

$$x_1 = 1, x_2 = -1$$

 $P(x_1) = 0.75, \quad P(x_2) = 0.25$  $x = \frac{\sigma^2}{2} \left[ \ell n \frac{0.25}{0.75} \right] = -\frac{\sigma^2}{2}$ 

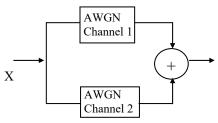
So  $\stackrel{\Lambda}{x}$  should be strictly negative.

#### 09. Ans: (c)

Sol: Y = X + ZZ is Gaussian RV with mean  $\beta x$  $x \in \{-a, +a\}$ when  $\beta = 0$  E[y] = E[x] + E[z]E[y] = E[x] = +a= a  $BER = Q(a) = 1 \times 10^{-8}$  $Q(v) = \frac{1}{\sqrt{2\pi}} \int_{v}^{\infty} e^{\frac{-v^2}{2}} du \cong e^{\frac{-v^2}{2}}$  $Q(a) = 1 \times 10^{-8} \approx e^{-\frac{a^2}{2}}$ a = 6 when  $\beta = -0.3$  mean =  $6 \times -0.3 = -1.8$ so E (y) = E(x)+E(z) = 6 - 1.8 = 4.2so BER = Q (4.2)  $\cong e^{\frac{-(4.2)^2}{2}}$ ≅ 0.0001 ≅ 10<sup>-4</sup>

#### **10.** Ans: 1.414 Sol: When the signal

Sol: When the signal is transmitted through a channel BER =  $Q[\sqrt{r}]$ .





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At the input of the receiver signal amplitude  $E_{d,d} = 4 \int (t)^2 dt = \frac{4}{3}$ is doubled. But when two independent Gaussian Random Variables are added, the  $P_e$  is minimum when  $E_d$  is maximum resultant random variables is also a Gaussian random. The pdf is the  $E_d$  of signal (a) is more when compared to convolution of individual pdf's.  $E_d$  of other signals. The variance indicates the noise power .: Probability of error is minimum for But the variance is doubled. signal (a). Signal power increased by a factor of 12. Ans: (b) 4(mean is doubled). **Sol:** o/p Noise Power = o/p PSD × B.W But the noise increases by a factor of 2  $=10^{-20} \times 2 \times 10^{6}$ So the signal to noise increases by a factor of 2  $= 2 \times 10^{-14} \text{ W}$ So  $b = \sqrt{2} = 1.414$ Since mean square value = Power BER =  $Q[\sqrt{2r}] = Q[\sqrt{2}\sqrt{r}] = Q[1.414\sqrt{r}]$  $\frac{2}{\alpha^2} = 2 \times 10^{-14} \Longrightarrow \alpha = 10^7$ So b = 1.41413. Ans: (d) 11. Ans: (a) Sol: When a 1 is transmitted:  $Y_k = a + N_k$ Sol: Probability of error for an AWGN channel for binary transmission is given as Threshold  $Z = \frac{a}{2} = 10^{-6}$  $P_e = Q\left(\sqrt{\frac{E_d}{2N_e}}\right)$  $\Rightarrow a = 2 \times 10^{-6}$ For error to occur,  $Y_k < 10^{-6}$  $2 \times 10^{-6} + N_k < 10^{-6}$ Where  $E_{d} = \int_{0}^{T} [s_{1}(t) - s_{2}(t)]^{2} dt$  $N_k < -10^{-6}$  $\therefore P(0/1) = \int^{-10^{-6}} P(n) dn$ : Given  $s_1(t) = g(t)$ Since  $s_{2}(t) = -g(t)$  $= \int_{0}^{10^{\circ}} (0.5) \alpha e^{-\alpha n} dn, \text{ with } \alpha = 10^{7}$  $E_{d} = \int_{0}^{T} [g(t) - (-g(t))]^{2} dt$  $= 0.5 \times e^{-10}$  $=4\int_{0}^{T}g^{2}(t)dt$ When a '0' is Transmitted:  $E_{d,a} = 4 \int_{}^{1} (1)^2 dt = 4$  $Y_k = N_k$ For error to occur,  $Y_k > 10^{-6}$  $E_{d,b} = 4 \left| \int_{0}^{1/2} (2t)^2 dt + \int_{0}^{1} (-2t+2)^2 \right| dt$ :  $P(1/0) = \int_{0}^{\infty} P(n) dn = 0.5 \times e^{-10}$ Since, both bits are equiprobable, the  $=\frac{4}{6}+\frac{4}{6}=\frac{4}{3}$ Probability of bit error  $=\frac{1}{2} \left[ P(0/1) + P(1/0) \right]$  $E_{d,c} = 4 \int_{0}^{1} (1-t)^2 dt = \frac{4}{3}$  $= 0.5 \times e^{-10}$ India's Best Online Coaching Platform for GATE, ESE, PSUs, SSC-JE, RRB-JE, SSC, Banks, Groups & PSC Exams ace online Enjoy a smooth online learning experience in various languages at your convenience

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- 14. Ans: (a) **Sol:** P(0/1) = P(1/0) = p $\Rightarrow P(1/1) = P(0/0) = 1 - p.$ Reception with error means getting at most one 1.  $\therefore$  P(reception with error) = P(X = 0) + P(X = 1) $= 3_{C_0} (1-p)^0 p^3 + 3_{C_1} (1-p)^1 p^2$  $= p^{3} + 3p^{2}(1-p)$ 15. Ans: (d) **Sol:**  $p = probability of a bit being in error = 10^{-3}$ q = probability of the bit not being in error  $= 1 - p = 1 - 10^{-3}$ = 0.999(1) Total number of bits = 10;  $P_e =$  probability of error = 1 - P(X = 0)P(X = 0) = Probability of no error $\therefore P_{e} = 1 - [{}^{10}C_{0}(10^{-3})^{0}(1 - 10^{-3})^{10}] = 0.00995$ (2) Total number of bits = 100 $P_e = 1 - [{}^{100}C_0(10^{-3})^0(1 - 10^{-3})^{100}]$ = 0.0952
- (3) Total number of bits = 1000  $P_e = 1 - [^{1000}C_0(10^{-3})^0(0.999^{1000})]$  $P_e = 0.632$
- (4) If total number of bits = 10, 000 =  $1 - [(^{10,000}C_0)(1 - 10^{-3})^0 (0.999)^{10,000}]$ = 0.9999

Conclusion: As the number of bits increases, the probability of error increases and it approaches unity.

#### 16. Ans: (a)

- **Sol:** Higher modulation techniques requires more power i.e., to achieve same probability of error, bit energy has to be increased. So, power also increased.
- 17. Ans: (a)
- **Sol:** Higher modulation techniques requires more power i.e., to achieve same probability of error, bit energy has to be increased. So, power also increased.

18. Ans: 0.125 Sol:  $f_N(n)$ 0.5 1/4 1/4 P(N<−1) P(N>1)  $P(E) = P(x = -1)P\left(\frac{R}{x = -1} > 0\right) + P(x = 1)P\left(\frac{R}{x = +1} < 0\right)$ = 0.5P(x+N>0) + 0.5 P(x+N<0)= 0.5 P(-1+N>0) + 0.5P(1+N<0)= 0.5 P(N>1) + 0.5P(N<-1) $=0.5\left|\frac{1}{2}\frac{1}{4}(1)\right|+0.5\left|\frac{1}{2}\frac{1}{4}\right|$  $=\frac{1}{-}=0.125$ 19. Ans:  $x = \{-0.5, 0.5\}$ Sol: -0.5 = <sup>1</sup>/<sub>4</sub>, P (x = 0.5) = 3/4  $\rightarrow \underbrace{-0.5}_{-1.5} \qquad \alpha$ 

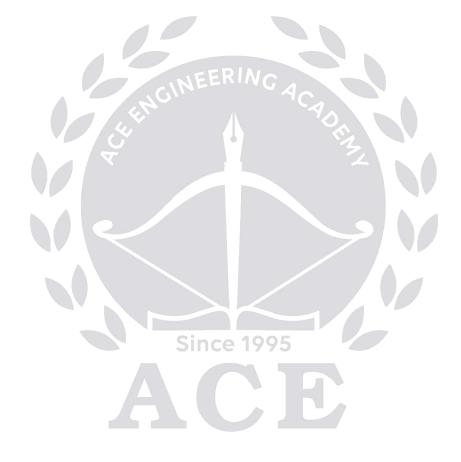
$$P_e$$
 in the overlap region –  $0.5 < \alpha < 0.5$ 

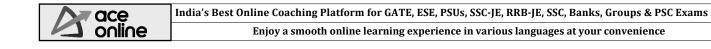
$$P_{e} = \frac{1}{4} \frac{1}{2} (0.5 - \alpha) + \frac{3}{4} \left(\frac{1}{2}\right) (\alpha + 0.5)$$
$$= \frac{0.5}{8} + \frac{1.5}{8} + \left(\frac{3}{8} - \frac{1}{8}\right) \alpha$$
$$= \frac{2}{8} + \frac{2}{8} \alpha$$

$$\therefore$$
 P<sub>e</sub> is minimum for  $\alpha = -0.5$ 



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20. Ans: (a & c) Sol: $f_m = 15 \text{ kHz}$ $f_s = 2f_m = 30 \text{ kHz}$ L = 128 n = 7  (Bits/sample) $R_b = nf_s = 7 \times 30 \times 10^3 = 210 \text{ (Kbps)}$ ∴ a & c are correct.		21. Ans: (a & d) Sol: $s(t)$ occurs at $t = T_b = T(sec)$ $s(t)_{MAX} = E\{s(t)\} = \int_{0}^{\frac{T}{2}} \frac{A^2}{4} dt + \int_{\frac{T}{2}}^{T} \frac{A^2}{4} dt = \frac{A^2}{4}T$ $\therefore$ a & d are correct





Chapter III) Information Theory & Coding

#### 01. Ans: (b)

Sol: Huffman encoder is the most efficient source encoder

$$\begin{array}{c|c}
0.5 & 1 & 0.5 & 0 \\
0.25 & 00 & 0.5 & 1 \\
0.25 & 01 & 0.5 & 1 \\
\overline{L} = 1 \times 0.5 + 2 \times 0.25 + 2 \times 0.25$$

= 1.5 bits/symbol

Average bit rate  $= 3000 \times 1.5$ 

= 4500 bps

- 02. Ans: (c)
- Sol: Assuming all the 64 levels are equiprobable,  $H = \log_2 64 = 6$  bits/pixel Total No. of pixels =  $625 \times 400 \times 400$ = 100 M pixels /sec
  - Data rate = 6 bits/pixel×100×10<sup>6</sup> pixel/sec = 600 Mbps
- 03. Ans: (b)
- Sol: C = B log  $(1 + \frac{S}{N})$ Since  $\frac{S}{N} >> 1$ .  $1 + \frac{S}{N} \cong \frac{S}{N}$   $\therefore$  C<sub>1</sub> = B log  $\frac{S}{N}$ C<sub>2</sub> = B log  $(2, \frac{S}{N})$ = B log2 + B log  $(\frac{S}{N}) = C_1 + B$

04. Ans: (b) Sol: Given B. W = 3 kHzSNR = 10dB $\Rightarrow 10 \log_{10} (SNR) = 10$  $SNR = 10^{|} = 10$ Number of characters = 128Channel capacity = B log<sub>2</sub>  $\left(1 + \frac{S}{N}\right)$  $= 3 \times 10^3 \log_2(1+10)$ = 10378bps 05. Ans: (b) Sol: Number of characteristics can be sent without any error  $=\frac{c}{\log_2 M}=\frac{c}{7}=1482.cps$ 06. Ans: (c) Sol: n/2

$$C = Blog_{2}(1 + \frac{S}{N})$$
$$\lim_{B \to \infty} C = \lim_{B \to \infty} \frac{S}{n} \times \frac{n}{S} Blog_{2}\left(1 + \frac{S}{nB}\right)$$
$$\lim_{B \to \infty} C = \frac{S}{n} \log_{2} e$$

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$(:: \lim_{n \to \infty} x \log \left( 1 + \frac{1}{Q} \right) = \log e)$ $\lim_{B \to \infty} C = 1.44 \frac{S}{n}$	$=\frac{0.8\times\frac{1}{7}}{0.8\times\frac{1}{7}+0.2\times\frac{6}{7}}=0.4$	
07. Ans: (b)	10. Ans: (a & d)	
Sol: Max. entropy = $512 \times 512 \times \log_2 8$ = 786432 bits	11. Ans: (b & c) Sol: $P(x_1) = \frac{1}{3}$	
08. Ans: (d) Sol: Maximum entropy of a binary source: $H(x)/_{max} = \log_{2} M$ $H(x)/_{max} = \log_{2} 2 = 1 \text{ bit/symbol}$ 09. Ans: 0.4 Sol: $P\left(\frac{x=1}{y=0}\right) = \frac{P(x=1,y=0)}{P(y=0)}$ $= \frac{P(x=1)P\left(\frac{y=0}{x=1}\right)}{P(x=1)P\left(\frac{y=0}{x=1}\right) + P(x=0)P\left(\frac{y=0}{x=0}\right)}$	$P(x_{2}) = 1 - \frac{1}{3} = \frac{2}{3}$ $P(y_{1}) = P(x_{1})P\left(\frac{y_{1}}{x_{1}}\right) + P(x_{2})P\left(\frac{y_{1}}{x_{2}}\right)$ $P(y_{1}) = \frac{1}{3}(0.9) + \frac{2}{3}(0.2)$ $P(y_{1}) = \frac{1.3}{3} = 0.433$ $P(y_{2}) = P(x_{1})P\left(\frac{y_{2}}{x_{1}}\right) + P(x_{2})P\left(\frac{y_{2}}{x_{2}}\right)$ $P(y_{2}) = \frac{1}{3}[0.1] + \frac{2}{3}[0.8] = \frac{1.7}{3} = 0.5666$ $\therefore$ b & c are correct	
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01. Ans: (a & d)

**02.** Ans: (a, b & c) Sol:  $G = \begin{bmatrix} 1 & 0 & 0 & 1 & 1 & 0 \\ 0 & 1 & 0 & 0 & 1 & 1 \\ 0 & 0 & 1 & 1 & 0 & 1 \end{bmatrix}$   $H = \begin{bmatrix} 1 & 0 & 1 & 1 & 0 & 0 \\ 1 & 1 & 0 & 0 & 1 & 0 \\ 0 & 1 & 1 & 0 & 0 & 1 \end{bmatrix}$   $H = \begin{bmatrix} 1 & 0 & 1 & 1 & 0 & 0 \\ 1 & 1 & 0 & 0 & 1 & 0 \\ 0 & 1 & 1 & 0 & 0 & 1 \end{bmatrix}$ 

Option (a) is correct

[C] = [D] [G]  $\therefore [C] = [0 \ 1 \ 1 \ 1 \ 0]$ Option (b) is correct  $[S] = [r] [H^{T}] = 0$   $\therefore [r] = [C] = [100110]$ Option (c) is correct  $\therefore a, b and c are correct$ 

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For (d), syndrome is not equal to zero. Hence  $[r] \neq [c]$ 

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Chapter 13 Optical Fiber Communication