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Mechanical Engineering

STRENGTH OF MATERIALS

Text Book : Theory with worked out Examples and Practice Questions

Strength of Materials

(Solutions for Text Book Practice Questions)

Simple Stresses and Strains

Fundamental, Mechanical Properties of Materials, Stress Strain Diagram

01. Ans: (b)

Sol:

• **Ductility:** The property of materials to allow large deformations or large extensions without failure (large plastic zone) is termed as ductility.

Chapter

1

- **Brittleness:** A brittle material is one which exhibits a relatively small extensions or deformations prior to fracture. Failure without warning (No plastic zone) i.e. no plastic deformation.
- **Tenacity**: High tensile strength.
- **Creep:** Creep is the gradual increase of plastic strain in a material with time at constant load.
- **Plasticity:** The property by which material undergoes permanent deformation even after removal of load.
- Endurance limit: The stress level below which a specimen can withstand cyclic stress indefinitely without failure.
- **Fatigue:** Decreased Resistance of material to repeated reversal of stresses.

02. Ans: (a)

Sol:

- When the material is subjected to stresses, it undergoes to strains. After removal of stress, if the strain is not restored/recovered, then it is called inelastic material.
- For rigid plastic material:

- Any material that can be subjected to large strains before it fractures is called a ductile material. Thus, it has large plastic zone.
- Materials that exhibit little or no yielding before failure are referred as brittle materials. Thus, they have no plastic zone.

03. Ans: (a)

Sol: *Refer to the solution of Q. No. (01).*

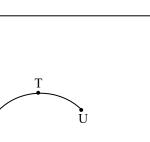
04. Ans: (b)

Sol: The stress-strain diagram for ductile material is shown below.



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- Q Elastic limit
- R Upper yield point
- S Lower yield point
- T Ultimate tensile strength
- U-Failure

From above,

- $OP \rightarrow Stage I$
- $PS \rightarrow Stage II$
- $ST \rightarrow Stage III$
- $TU \rightarrow Stage IV$

05. Ans: (b)

Sol:

• If the response of the material is independent of the orientation of the load axis of the sample, then we say that the material is **isotropic** or in other words we can say the isotropy of a material is its characteristics, which gives us the information that the properties are same in the three orthogonal directions x, y and z. • A material is **homogeneous** if it has the same composition throughout the body. Hence, the elastic properties are the same at every point in the body in a given direction. However, the properties need not to be the same in all the directions for the material. Thus, both A and B are false.

06. Ans: (a)

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- **Sol: Strain hardening** increase in strength after plastic zone by rearrangement of molecules in material.
 - Visco-elastic material exhibits a mixture of creep as well as elastic after effects at room temperature. Thus their behavior is time dependent

07. Ans: (a) Sol: Refer to the solution of Q. No. (01).

08. Ans: (a)

Sol: Modulus of elasticity (Young's modulus) of some common materials are as follow:

Material	Young's Modulus (E)
Steel	200 GPa
Cast iron	100 GPa
Aluminum	60 to 70 GPa
Timber	10 GPa
Rubber	0.01 to 0.1 GPa

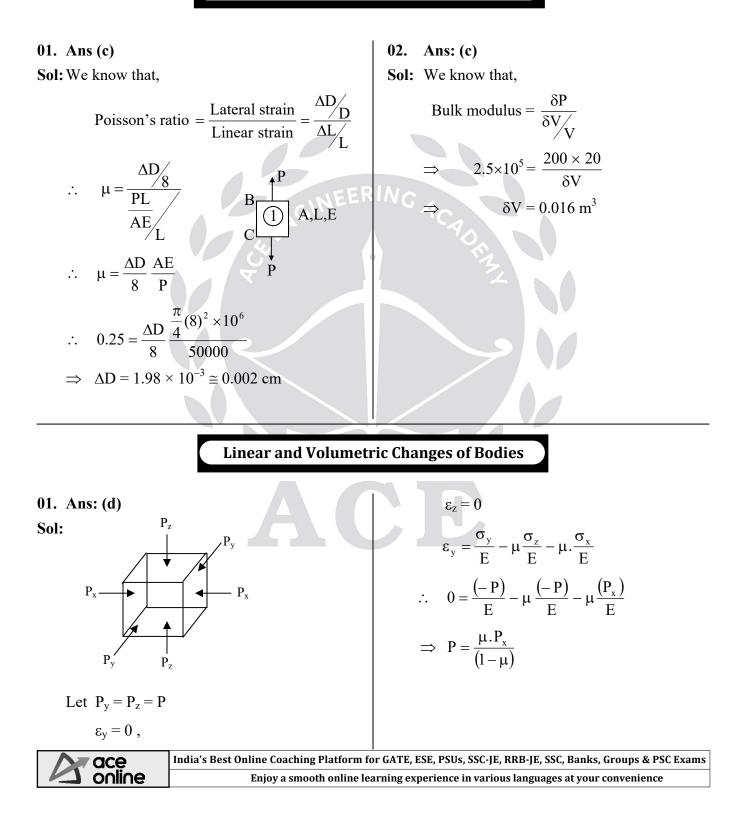
09. Ans: (a)

Sol: Addition of carbon will increase strength, thereby ductility will decrease.

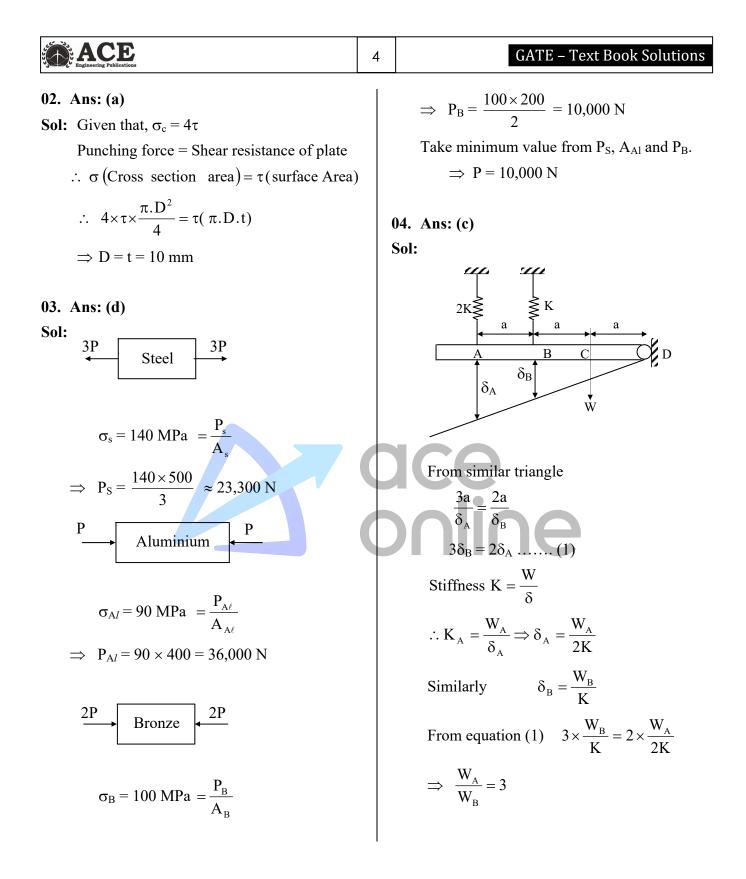
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Strength of Materials

Elastic Constants and Their Relationships



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Thermal/Temperature Stresses

- 01. Ans: (b)
- **Sol:** Free expansion = Expansion prevented

$$\left[\ell \alpha t\right]_{s} + \left[\ell \alpha t\right]_{A1} = \left\lfloor \frac{P\ell}{AE} \right\rfloor_{s} + \left\lfloor \frac{P\ell}{AE} \right\rfloor_{AL}$$

$$11 \times 10^{-6} \times 20 + 24 \times 10^{-6} \times 20$$

$$= \frac{P}{100 \times 10^{3} \times 200} + \frac{P}{200 \times 10^{3} \times 70}$$

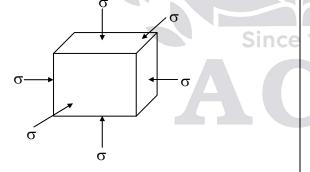
$$\Rightarrow P = 5.76 \text{ kN}$$

$$\sigma_{s} = \frac{P}{A_{s}} = \frac{5.76 \times 10^{3}}{100} = 57.65 \text{ MPa}$$

 $\sigma_{Al} = \frac{P}{A_{al}} = \frac{5.76 \times 10^{3}}{200} = 28.82 \text{ MPa}$

02. Ans: (a)

Sol:



Strain in X-direction due to temperature,

$$\varepsilon_{t} = \alpha (\Delta T)$$

Strain in X-direction due to volumetric stress,

$$\varepsilon_{x} = \frac{\sigma_{x}}{E} - \mu \frac{\sigma_{y}}{E} - \mu \frac{\sigma_{z}}{E}$$

$$\therefore \quad \varepsilon_{x} = \frac{-\sigma}{E} (1 - 2\mu)$$
$$\therefore \quad -\sigma = \frac{(\varepsilon_{x})(E)}{1 - 2\mu}$$
$$\therefore \quad -\sigma = \frac{\alpha(\Delta T)E}{(1 - 2\mu)}$$
$$\Rightarrow \quad \sigma = \frac{-\alpha(\Delta T)E}{1 - 2\mu}$$

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- Free expansion in x direction is aαt.
- Free expansion in y direction is $a\alpha t$.
- Since there is restriction in y direction expansion doesn't take place. So in lateral direction, increase in expansion due to restriction is $\mu a \alpha t$.

Thus, total expansion in x direction is,

 $= a \alpha t + \mu a \alpha t$ $= a \alpha t (1 + \mu)$

04. Ans: (a, b, d)

Sol:

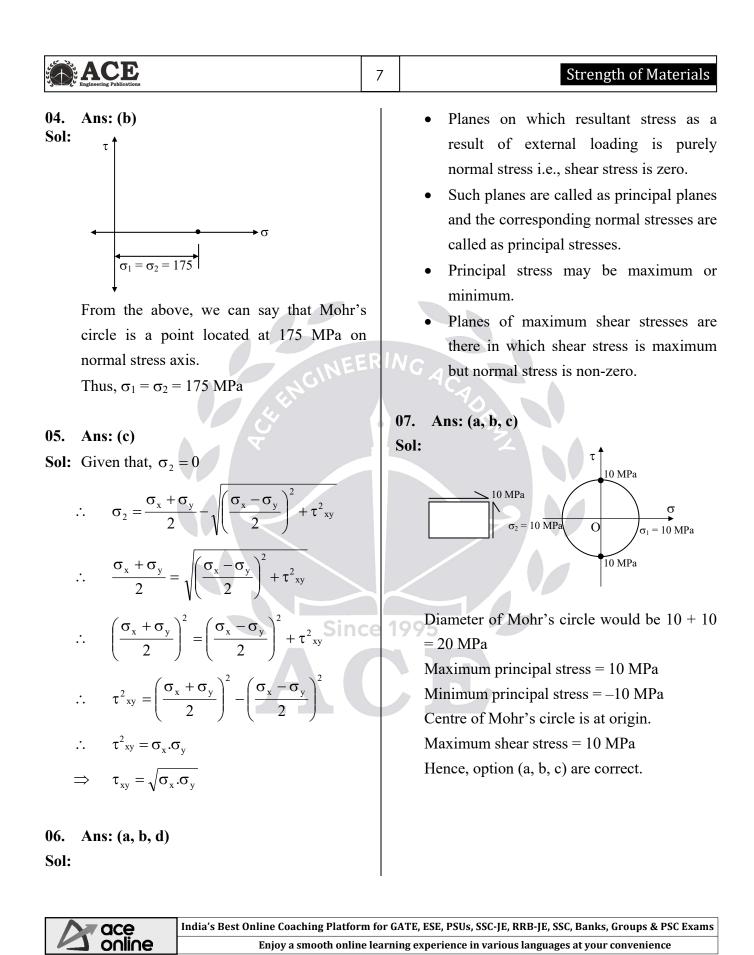
- Brass and copper bars are in parallel arrangement in composite bar.
- In parallel arrangement load is divided and elongation will be same for both the bars.

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$P = P_b + P_c$ $P = A_b \sigma_b + A_c \sigma_c$ $\delta_b = \delta_c$	2 Complex Stresses and Strains
$\Rightarrow \frac{P\ell}{AE}\Big _{b} = \frac{P\ell}{AE}\Big _{cu}$ $\therefore \ \ell_{b} = \ell_{c}$ $\therefore \ \frac{\sigma_{b}}{\sigma_{c}} = \frac{E_{b}}{E_{c}}$ Hence, a, b, d are correct.	01. Ans: (b) Sol: Maximum principal stress $\sigma_1 = 18$ Minimum principal stress $\sigma_2 = -8$ Maximum shear stress $=\frac{\sigma_1 - \sigma_2}{2} = 13$
05. Ans: (b, d) Sol: Elongation produced in prismatic bar due to self weight. $\delta \ell = \frac{\gamma \ell^2}{2E}$	Normal stress on Maximum shear stress plane $\sigma_1 + \sigma_2 = 18 + (-8)$
$\delta \ell = \frac{1}{2E}$ $\gamma = \text{weight density}$ Now, $\ell \to 2\ell$ $\delta \ell' = \frac{\gamma \times (2\ell)^2}{2E} = 4\delta\ell$	Sol: Radius of Mohr's circle, $\tau_{max} = \frac{\sigma_1 - \sigma_2}{2}$ $20 = \frac{\sigma_1 - 10}{2}$ $\Rightarrow \sigma_1 = 50 \text{ N/mm}^2$
Elongation produced will be 4 times original elongation. Stress = E × strain $\sigma = E \times \frac{\delta \ell}{\ell} = E \times \frac{\gamma \ell}{2E}$ $\sigma' = E \times \frac{\gamma 2 \ell}{2E}$ $\sigma' = 2\sigma$ Stress produced will be 2 times maximum	03. Ans: (b) Sol: Given data, $\sigma_x = 150 \text{ MPa}, \ \sigma_y = -300 \text{ MPa}, \ \mu = 0.3$ Long dam \rightarrow plane strain member $\varepsilon_z = 0 = \frac{\sigma_z}{E} - \frac{\mu \sigma_x}{E} - \frac{\mu \sigma_y}{E}$ $\therefore 0 = \sigma_z - 0.3 \times 150 \pm 0.3 \times 300$
Stress produced will be 2 times maximum stress.	$\Rightarrow \sigma_z = 45 \text{ MPa}$



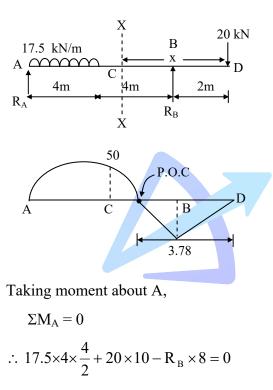


ChapterShear Force3and Bending Moment

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01. Ans: (b)

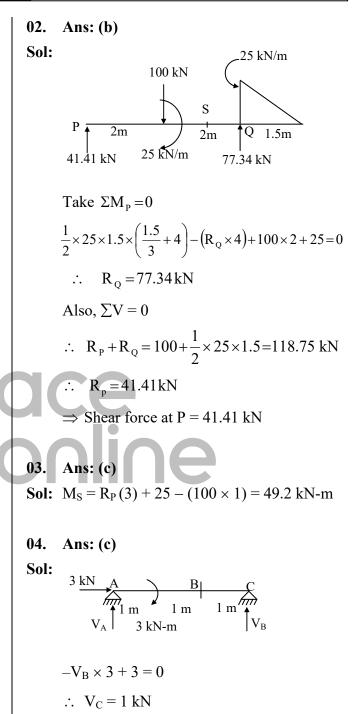
Sol: Contra flexure is the point where BM is becoming zero.



 \therefore R_B = 42.5 kN

Now, $M_x = -20x + R_B(x - 2)$ For bending moment be zero $M_x = 0$, -20x + 42.5(x - 2) = 0

 \Rightarrow x = 3.78 m from right i.e. from D.

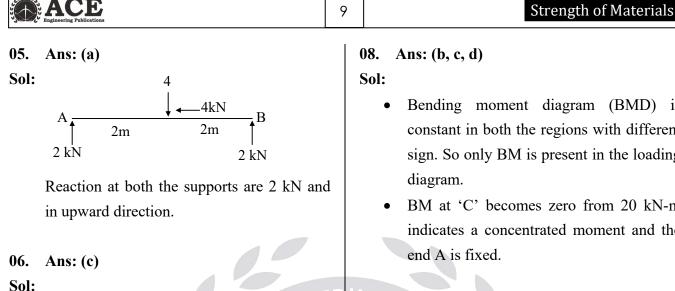


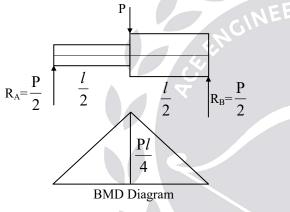
: Bending moment at B,

$$\Rightarrow$$
 M_B = V_C × 1 = 1 kN-m



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Bending moment at $\frac{l}{2}$ from left is $\frac{Pl}{4}$.

The given beam is statically determinate structure. Therefore equilibrium equations are sufficient to analyze the problem. In statically determinate structure the BMD, SFD and Axial force are not affected by section (I), material (E), thermal changes.

07. Ans: (a)

Sol: As the given support is hinge, for different set of loads in different direction beam will experience only axial load.

- Bending moment diagram (BMD) is constant in both the regions with different sign. So only BM is present in the loading
- BM at 'C' becomes zero from 20 kN-m indicates a concentrated moment and the

09. Ans: (b, c)

Sol:

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- For point load shear force will always be • constant.
- There is no change in the shear force diagram due to presence of bending moment at any point.

Hence, option (a & d) are wrong statements.



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$$M.I about CG = I_{CG} = \frac{2b(3d)^3}{12} = \frac{9}{2}bd^3$$

$$M.I about X - X|_{at \frac{6}{4}distance} = I_G + Ay^2$$

$$= \frac{9}{2}bd^3 + 6bd(\frac{5}{4})^2 d^2$$

$$= \frac{111}{8}bd^3 = 13.875bd^3$$

$$Sol: \quad \overline{y} = \frac{A_{1}E_{1}Y_{1} + A_{2}E_{2}Y_{2}}{B_{1} + B_{2}} \quad (::E_{1} = 2E_{2})$$

$$\Rightarrow \overline{y} = 1.167h \text{ from base}$$

$$04. \text{ Ans: } 6.885 \times 10^{6} \text{ mm}^{4}$$

$$Sol: \quad I_{X} = \frac{BD^3}{12} - 2\left(\frac{bd^3}{12} + Ah^2\right)$$

$$= \frac{1.5a \times 3a^2 \times E_{1} + 1.5a \times 6a^2 \times 2E_{1}}{3a^2E_{1} + 6a^2(2E_{1})}$$

$$= \frac{22.5a^3E_{1}}{15a^2E_{1}} = 1.5a$$

$$03. \text{ Ans: } 13.875bd^3$$

$$Sol: \quad \underline{2b}$$

 $y=\frac{5}{4}d$

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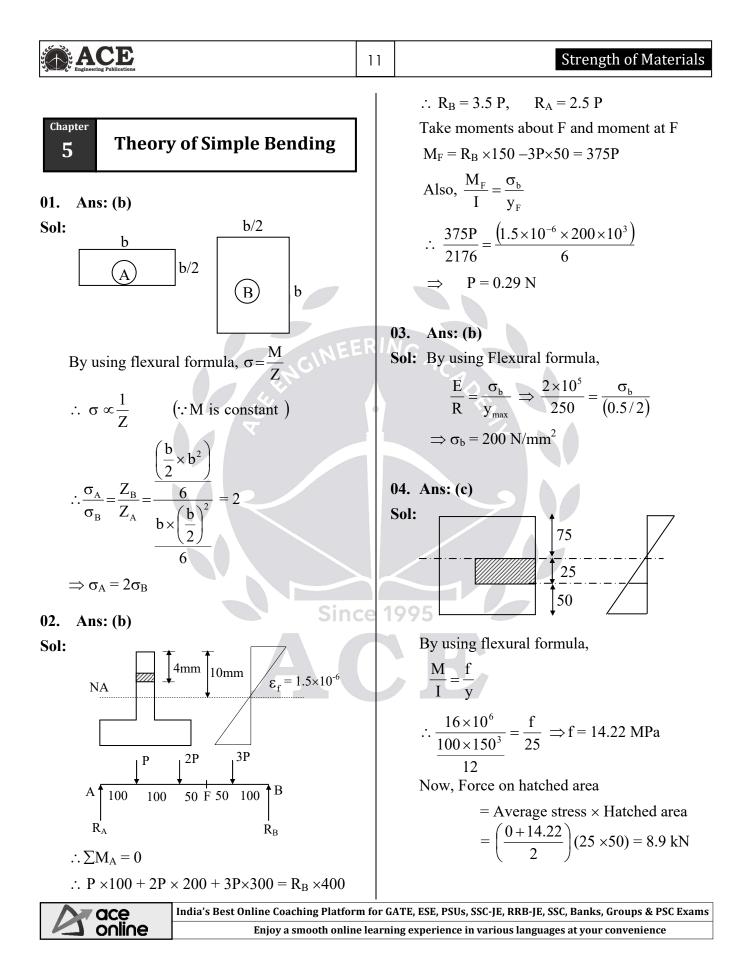
CG X ---

 $= 45801.34 \text{ mm}^4$

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 $=\frac{9}{2}bd^{3}+6bd\left(\frac{5}{4}\right)^{2}d^{2}$

 $=\frac{111}{8}bd^3=13.875bd^3$



05. Ans: (b)

Sol: By using flexural formula, $\frac{f_{\text{Tensile}}}{y_{\text{top}}} = \frac{M}{I}$

$$\Rightarrow f_{\text{Tensile}} = \frac{0.3 \times 3 \times 10^6}{3 \times 10^6} \times 70$$

(maximum bending stress will be at top fibre so $y_1 = 70 \text{ mm}$) $\Rightarrow f_{\text{Tensile}} = 21 \text{ N/mm}^2 = 21 \text{ MN/m}^2$

06. Ans: (c)

Sol: Given data:

P = 200 N,
$$M = 200 \text{ N.m}$$

A = 0.1 m², $I = 1.33 \times 10^{-3} \text{ m}^{2}$

y = 20 mm

Due to direct tensile force P,

$$\sigma_{\rm d} = \frac{\rm P}{\rm A} = \frac{200}{0.1}$$

$$= 2000 \text{ N/m}^2$$
 (Tensile)

Due to the moment M,

$$\sigma_{b} = \frac{M}{I} \times y$$
$$= \frac{200}{1.33 \times 10^{-3}} \times 20 \times 10^{-3}$$
$$= 3007.52 \text{ N/m}^{2} \text{ (Compressive)}$$

 $\sigma_{\text{net}} = \sigma_d - \sigma_b$ $-2000 \quad 3007 52$

$$= 2000 - 3007.32$$

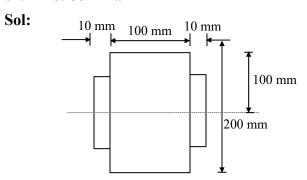
= -1007.52 N/m²

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Negative sign indicates compressive stress.

$$\sigma_{\text{net}} = 1007.52 \text{ N/m}^2$$

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Maximum stress in timber = 8 MPa Modular ratio, m = 20 Stress in timber in steel level.

$$100 \rightarrow 8$$

$$50 \rightarrow f_w$$

$$\Rightarrow$$
 f_w = 4 MPa

Maximum stress developed in steel is = $m \cdot f_w$

 $= 20 \times 4 = 80$ MPa

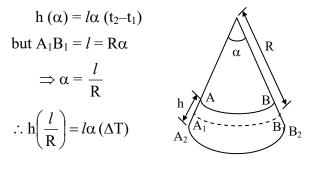
Convert whole structure as a steel structure by using modular ratio.

08. Ans: 2.43 mm

Sol: From figure, $A_1B_1 = l = 3 m$ (given)

$$AB = \left(R - \frac{h}{2}\right)\alpha = l - l\alpha t_1 \dots (1)$$
$$A_2B_2 = \left(R + \frac{h}{2}\right)\alpha = l + l\alpha t_2 \dots (2)$$

Subtracting above two equations (2) - (1)



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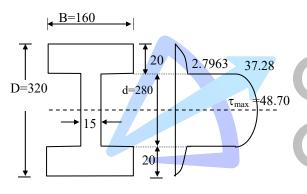
$$R = \frac{h}{\alpha(\Delta T)}$$

$$= \frac{250}{(1.5 \times 10^{-2})(72 - 36)}$$
R = 462.9 m
From geometry of circles
 $(2R - \delta)\delta = \frac{L}{2} \cdot \frac{L}{2}$ {rcf. figure in Q.No.02}
 $2R \cdot \delta - \delta^2 = \frac{L^2}{4}$ (neglect δ^2)
 $\delta = \frac{L^2}{8R} = \frac{3^2}{8 \times 462.9} = 2.43$ mm
Shortcut:
Deflection is due to differential temperature
of bottom and top ($\Delta T = 72^\circ - 36^\circ = 36^\circ$).
Bottom temperature being more, the beam
deflects down.
 $\delta = \frac{\alpha(\Delta T)\ell^2}{8h}$
 $= \frac{1.5 \times 10^{-5} \times 36 \times 3000^\circ}{8 \times 250}$
 $= 2.43$ mm (downward)
09. Ans: (a, c)
Sol:
 $A = \frac{\alpha}{B} \frac{W}{W} = \frac{M}{W}$
 $BM_R = M + Wa$
 $BM_R =$

ChapterShear Stress Distribution6in Beams

- 01. Ans: (a)
- Sol: $\tau_{max} = \frac{3}{2} \times \tau_{avg} = \frac{3}{2} \times \frac{f}{b.d}$ $3 = \frac{3}{2} \times \frac{50 \times 10^3}{100 \times d}$ $\therefore d = 250 \text{ mm} = 25 \text{ cm}$
- 02. Ans: 37.3



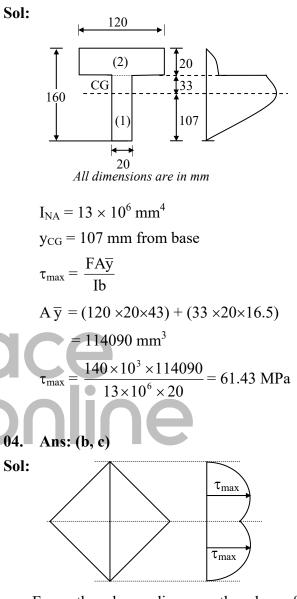


All dimensions are in mm

Bending moment (M) = 100 kN-m, Shear Force (SF) = f = 200 kN $I = \frac{160 \times 320^{3}}{12} - \frac{145 \times 280^{3}}{12}$ = 171.65 × 10⁶ mm⁴ $\tau_{at interface of flange & web = \frac{FA\overline{y}}{Ib}$ $= \frac{200 \times 10^{3}}{171.65 \times 10^{6} \times 15} \times (160 \times 20 \times 150)$ = 37.28 MPa

03. Ans: 61.43 MPa

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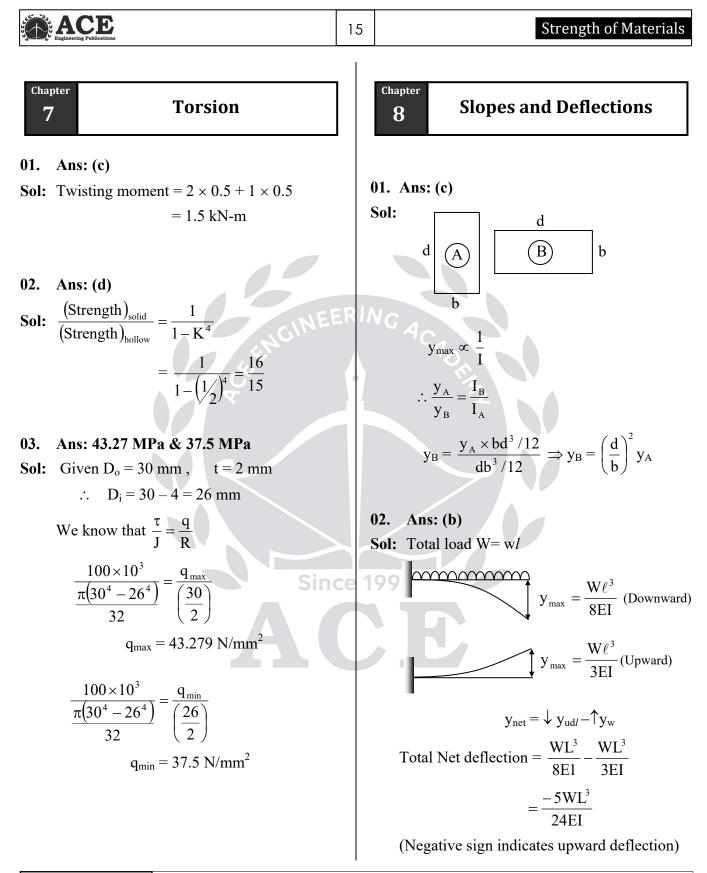


From the above diagram, the shear force distribution across the section of beam will be zero at top and bottom.

Maximum shear stress does not occur at the neutral axis.

Hence, options (b, c) are correct.





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04. Ans: (a)

Sol:

W

Conditions given

$$\downarrow y = \frac{wl^3}{48EI}$$
$$\theta = \frac{wl^2}{16EI}$$
tor 0 = y

$$\tan\theta = \frac{1}{\left(L - \ell\right)/2}$$

 θ is small \Rightarrow tan $\theta = \theta$

$$\therefore \theta = \frac{y}{\left(L - \ell\right)/2}$$

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$$\therefore y = \theta\left(\frac{L-\ell}{2}\right)$$

$$\uparrow y = \theta\left(\frac{L-\ell}{2}\right)$$
Thus $y \downarrow = y \uparrow$

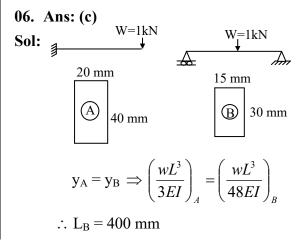
$$\therefore \frac{w\ell^3}{48EI} = \frac{w\ell^2}{16EI} \times \left(\frac{L-\ell}{2}\right)$$

$$\Rightarrow \quad \frac{L}{\ell} = \frac{5}{3}$$

05. Ans: (c)

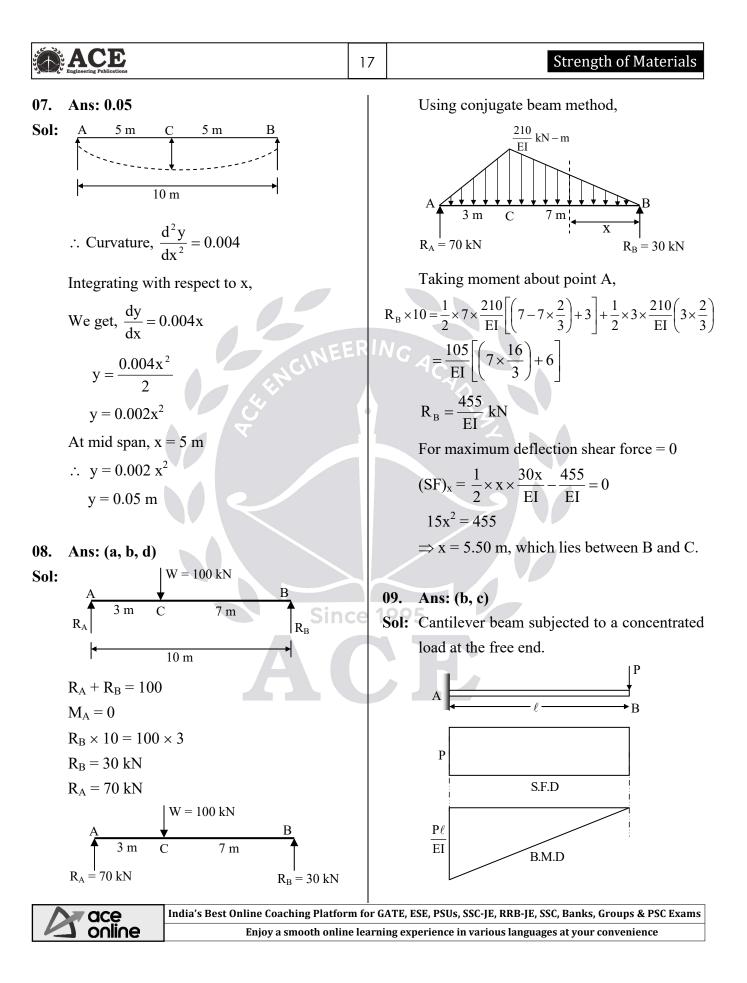
Sol: By using Maxwell's law of reciprocals theorem W

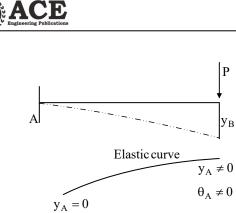
$$C = \delta_{B/C}$$



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 $\theta_{\rm A}=0$

From the above diagram bending moment or stress is maximum at fixed end.

From SFD, shear stress is constant along the length of the beam.

Slope of elastic curve is zero at fixed end and maximum at free end.

Hence, option (b, c) are correct.

Sol:
$$\tau_{\text{max}} = \sigma_1 = \frac{\sigma_h - 0}{2} = \frac{PD}{4t}$$

$$\therefore \tau_{\text{max}} = \frac{1.6 \times 900}{4 \times 12} = 30 \text{ MPa}$$

02. Ans: 2.5 MPa & 2.5 MPa

Sol: Given data:

R = 0.5 m, D = 1m, t = 1mm, $H = 1 \text{ m}, \gamma = 10 \text{ kN/m}^3, h = 0.5 \text{ m}$ At mid-depth of cylindrical wall (h = 0.5m):Circumferential (hoop) stress,

$$\sigma_{c} = \frac{P_{at h=0.5m} \times D}{4t} = \frac{\gamma h \times D}{4t}$$
$$= \frac{10 \times 10^{3} \times (2 \times 0.5)}{4 \times 1 \times 10^{-3}}$$

$$= 2.5 \times 10^6 \text{ N/m}^2 = 2.5 \text{ MPa}$$

Longitudinal stress at mid-height,

 $\sigma_{\ell} = \frac{\text{Net weight of the water}}{\text{Cross-section area}}$

$$= \frac{\gamma \times \text{Volume}}{\pi D \times t}$$

$$= \frac{\gamma \times \frac{\pi}{4} D^2 L}{\pi D \times t} = \frac{\gamma \times DL}{4t}$$
$$= \frac{10 \times 10^3 \times 1 \times 1}{4 \times 10^{-3}}$$
$$= 2.5 \times 10^6 \text{ N/m}^2 = 2.5 \text{ MPa}$$

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04. Ans: (c)		
Sol: Euler's theory is applicable for a loaded columns.	xially	Chapter11Strain Energy
Force in member AB, $P_{AB} = \frac{F}{\cos 45^{\circ}} =$	$\sqrt{2}F$	01. Ans: (d)
$P_{AB} = \frac{\pi^2 EI}{L_e^2}$		Sol:Slope of the stress-strain curve in the elastic
$\therefore \sqrt{2} \mathbf{F} = \frac{\pi^2 \mathbf{EI}}{\mathbf{L_e}^2}$		region is called modulus of elasticity. For the given curves,
\Rightarrow F = $\frac{\pi^2 \text{EI}}{\sqrt{2} \text{L}^2}$		(Modulus of elasticity) _A > (Modulus of elasticity) _E
		$\therefore \mathbf{E}_{\mathbf{A}} > \mathbf{E}_{\mathbf{B}}$
05. Ans: (a)		• The material for which plastic region is
Sol: Given data:		more is stress-strain curve is possesed high
$L_e = L = 3 m$,		ductility. Thus, $\mathbf{D}_{\mathbf{B}} > \mathbf{D}_{\mathbf{A}}$.
$\alpha = 12 \times 10^{-6} / {^{\circ}C},$ d = 50 mm = 0.05 m Buckling load, P _e = $\frac{\pi^2 \text{EI}}{L_c^2}$	C	02. Ans: (b) Sol: $\sigma \uparrow$
$\therefore \frac{P_e L}{AE} = L\alpha \Delta T$		30° B
$\therefore \qquad \frac{\pi^2 \mathrm{EI} \times \mathrm{L}}{\mathrm{L}^2 \times \mathrm{AE}} = \mathrm{L} \alpha \Delta \mathrm{T}$		
$\therefore \qquad \frac{\pi^2 \times E \times \frac{\pi}{64} \times d^4 \times L}{L^2 \times \frac{\pi}{4} d^2 \times E} = L\alpha\Delta T$		$\frac{(SE)_{A}}{(SE)_{B}} = \frac{Area \text{ under curve } A}{Area \text{ under curve } B}$ $= \frac{\frac{1}{2} \times x \times x \tan 60^{\circ}}{\frac{1}{2} \times x \times x \tan 30^{\circ}} = \frac{3}{1}$
$\therefore \qquad \Delta T = \frac{\pi^2 \times d^2}{16 \times L^2 \times \alpha} = \frac{\pi^2 \times (0.05)^2}{16 \times 3^2 \times 12 \times 10^2}$	0^{-6}	$\frac{1}{2} \times x \times x \tan 30^{\circ}$ 1
$\Rightarrow \Delta T = 14.3^{\circ}C$		
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03.	Ans: (a))5.	Ans: (d)
Sol:	$\frac{2 \text{ cm}}{10 \text{ cm}}$ $\frac{10 \text{ cm}}{10 \text{ cm}}$ $\frac{10 \text{ cm}}{10 \text{ cm}}$ $\frac{10 \text{ cm}}{20 \text{ cm}}$ $\frac{2 \text{ cm}}{20 \text{ cm}}$	$\frac{2 \text{ cm}}{20 \text{ cm}}$ $\frac{10 \text{ cm}}{20 \text{ cm}}$ $\frac{2 \text{ cm}}{20 \text{ cm}}$	\$	Sol:	Strain energy, $U = \frac{P^2}{2A^2E}$.V $\therefore U \propto P^2$ Due to the application of P ₁ and P ₂ one after the other $(U_1 + U_2) \propto P_1^2 + P_2^2$ (1) Due to the application of P ₁ and P ₂ together at the same time. $U \approx (P_1 + P_2)^2$ (2)
	$\therefore \frac{U_{B}}{U_{A}} = \frac{\left[\frac{\sigma_{1}^{2}}{2E}\right]}{\left[\frac{\sigma_{1}^{2}}{2E}\right]}$	$\frac{\times V_{1} + \frac{\sigma_{2}^{2}}{2E} \times V_{2}}{\times V_{1} + \frac{\sigma_{2}^{2}}{2E} \times V_{2}} \right]_{A}$		VG)6.	$U \propto (P_{1} + P_{2})^{2} \qquad(2)$ It is obvious that, $(P_{1}^{2} + P_{2}^{2}) < (P_{1} + P_{2})^{2}$ $\Rightarrow (U_{1} + U_{2}) < U$ Ans: 1.5
	L.	$\frac{A_1 \times L_1 + \frac{P^2 \times A_2 \times L_2}{A_2^2}}{\frac{A_1 \times L_1}{A_1^2} + \frac{P^2 \times A_2 \times L_2}{A_2^2}} \right]_A}$ $\frac{\frac{L_2}{A_2}}{\frac{L_2}{A_2}} = \frac{7.165}{4.77} = \frac{3}{2}$	\$	Sol:	Given data: L = 100 mm, G = 80×10 ³ N/mm ² J ₁ = $\frac{\pi}{32}(50)^4$; J ₂ = $\frac{\pi}{32}(26)^4$ U = U ₁ + U ₂ = $\frac{T^2L}{2GJ_1} + \frac{T^2L}{2GJ_2}$
04. Sol:	Ans: (c) $A_1 = Modulus$			07.	$\Rightarrow U = 1.5 \text{ N-mm}$ Ans: (a, b)
		$\times 70 \times 10^6 = 14 \times 10^4$			Strain energy stored in AB = $\frac{1}{2} \times P \times \delta$
	2	$\times 50 \times 10^{6} + (0.008 \times 70 \times 10^{6})$			$= \frac{1}{2} \times P \times \frac{P\ell}{AE}$
	$= 76 \times 10^4$ A ₁ + A ₂ = (14 -	$+76) \times 10^4 = 90 \times 10^4$			$=\frac{P^{2}L}{2AE}$
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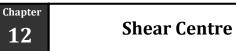
Axial deformation of AB = $\frac{PL}{AE}$

Strain energy stored in BC,

$$U = \int_0^\ell \frac{M^2 dx}{2EI} \quad (M = Px)$$
$$= \int_0^\ell \frac{(Px)^2 dx}{2EI}$$
$$= \frac{P^2 \ell^3}{6EI}$$

The displacement at point B is not equal to $\frac{P\ell^3}{3EI}$, since there is a hinge point C not

fixed.



01. Ans: (a)

Sol:

- Shear centre is related to torsion
- On principal plane shear stress is zero
- At fixed end slope is zero.
- Middle third rule is to avoid tension in columns.

02. Ans: (b)

Sol: In case of a thin channel section, if the resultant shear stress does not pass through the shear center, then the bending will occur with torsion.

If the resultant shear stress pass through the shear center, then the bending will occur without torsion.

03. Ans: (a, b, c, d)

Sol: All diagrams are correct representation of shear centre and centre of gravity of various sections.

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