

ESE | GATE | PSUs

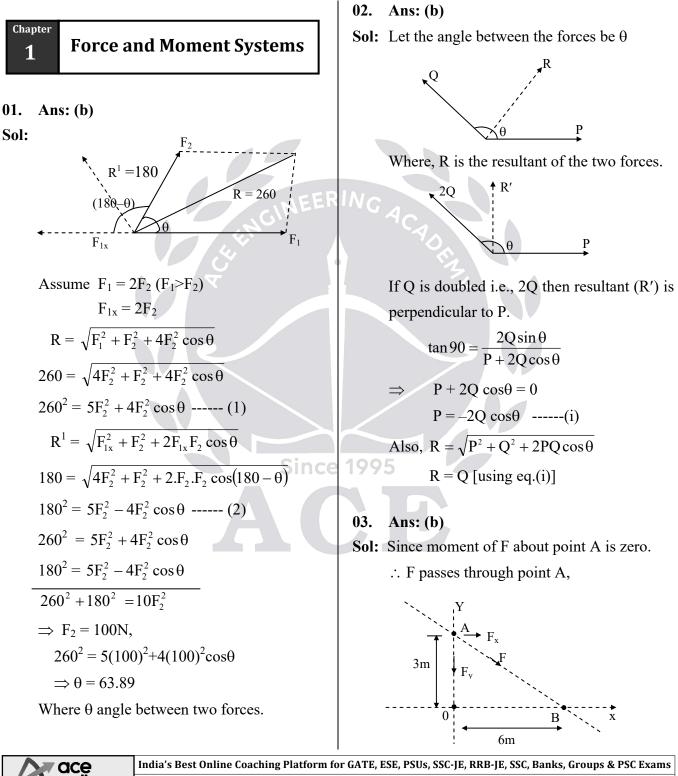
Mechanical Engineering

ENGINEERING MECHANICS

Textbook & Workbook: Theory with worked out Examples and Practice Questions

Engineering Mechanics

(Solutions for Text Book Practice Questions)



A ace online s Best Online Coaching Platform for GATE, ESE, PSUs, SSC-JE, RRB-JE, SSC, Banks, Groups & PSC Exams Enjoy a smooth online learning experience in various languages at your convenience

ACE

$$\begin{split} M_0^F &= 180N - m \\ M_B^F &= 90 N - m \\ M_A^F &= 0 \\ M_0^F &= 180 = F_x \times 3 + F_y \times 0 \\ F_x &= 60N \dots (1) \\ M_B^F &= F_x \times 3 - F_y \times 6 = -90 \\ 60 \times 3 - 6F_y &= -90 \\ \Rightarrow F_y &= \frac{270}{6} \\ F_y &= 45N \\ \therefore F &= \sqrt{F_x^2 + F_y^2} = \sqrt{60^2 + 45^2} = 75 \end{split}$$

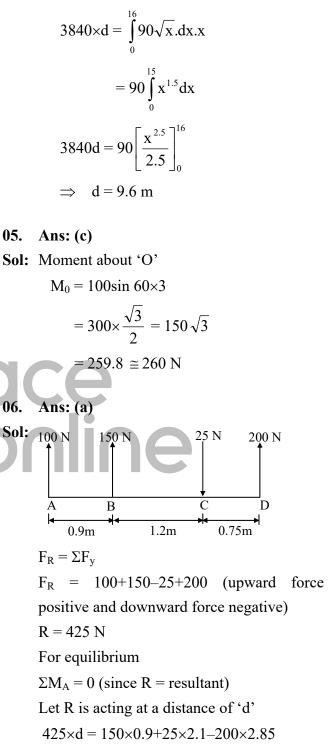
2

04. Ans: (a)

Sol: 360 N/m $\int_{0}^{w} dw = \int_{0}^{16} w dx$ $w = \int_{0}^{16} 90\sqrt{x} dx = 90 \left[\frac{x^{\frac{1}{2}+1}}{\frac{1}{2}+1} \right]_{0}^{16}$ $= 90 \times \frac{2}{3} \left[x^{3/2} \right]_{0}^{16} = 60 (16)^{3/2}$ w = 3840 N

The moment due to average force should be equal to the variable force

 $\mathbf{R} \times \mathbf{d} = \Sigma \mathbf{d} \mathbf{w} \times \mathbf{x}$



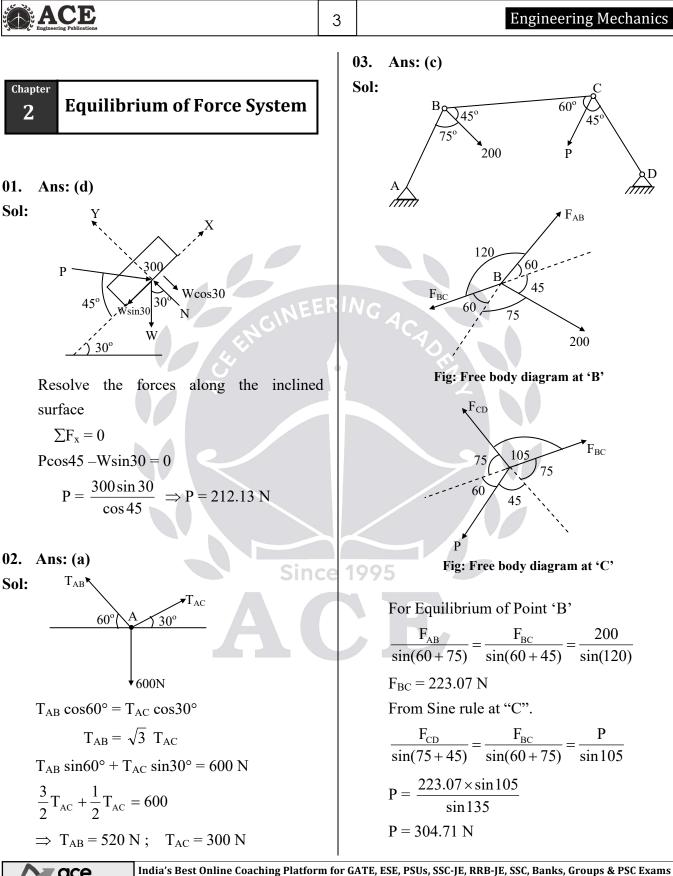
GATE – Text Book Solutions

 \Rightarrow d = 1.535m (from A)

A ace online

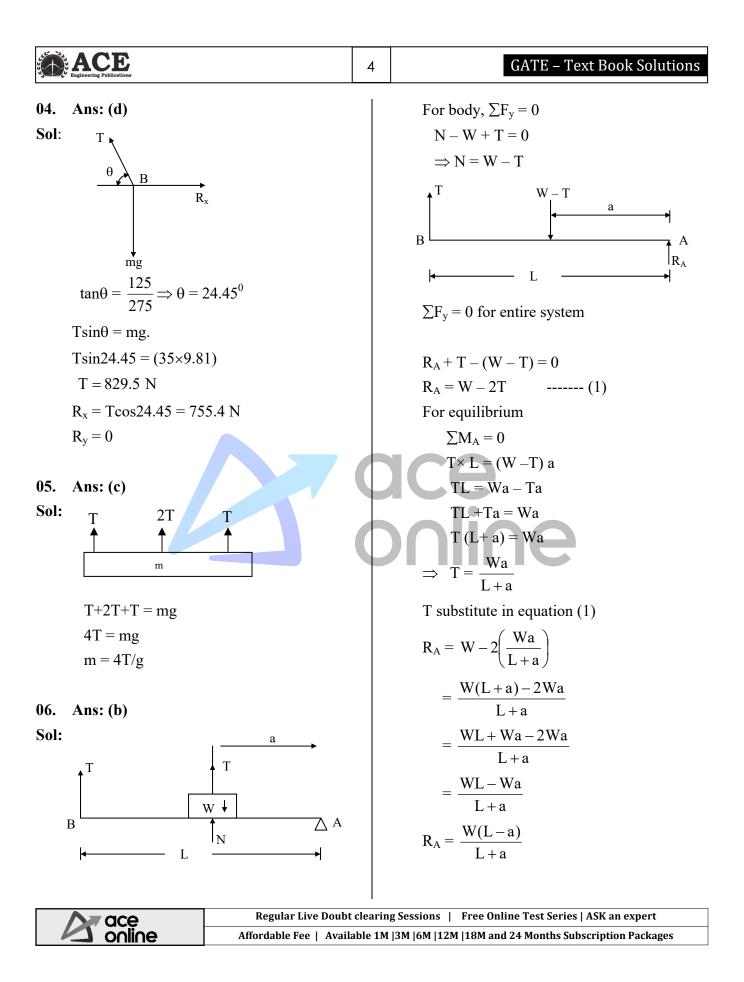
 Regular Live Doubt clearing Sessions
 |
 Free Online Test Series | ASK an expert

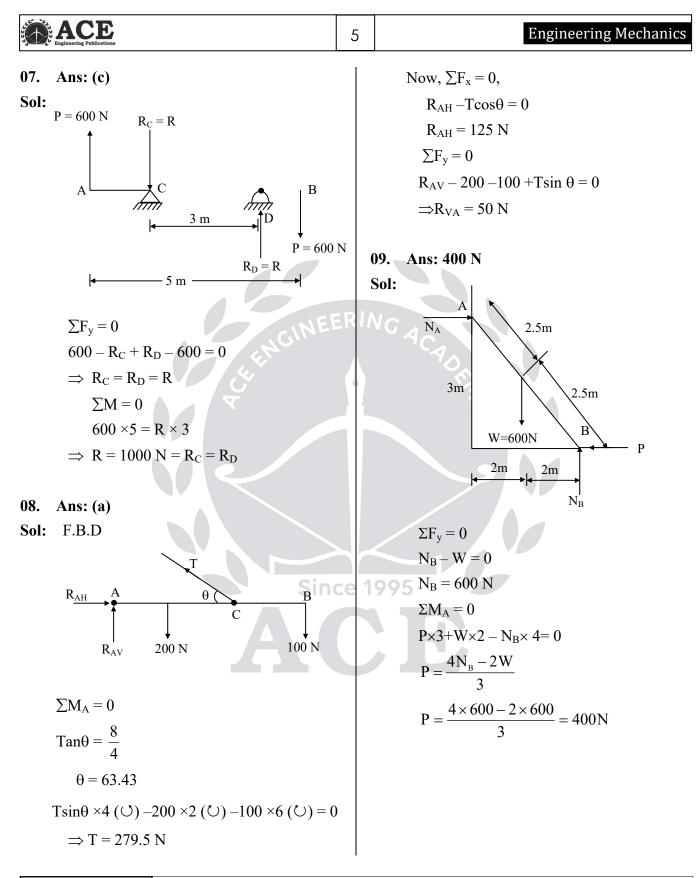
 Affordable Fee
 |
 Available 1M |3M |6M |12M |18M and 24 Months Subscription Packages





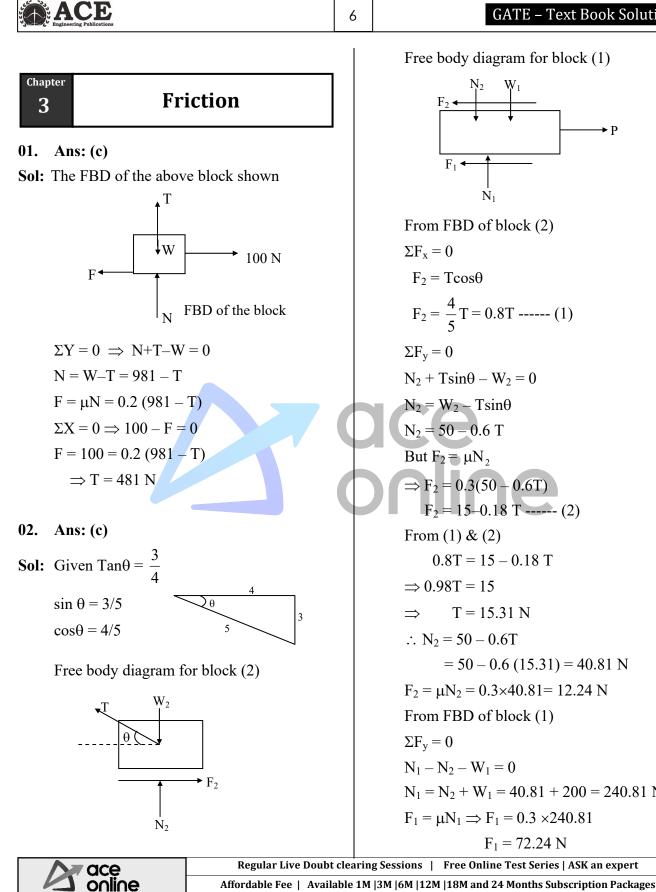
Enjoy a smooth online learning experience in various languages at your convenience

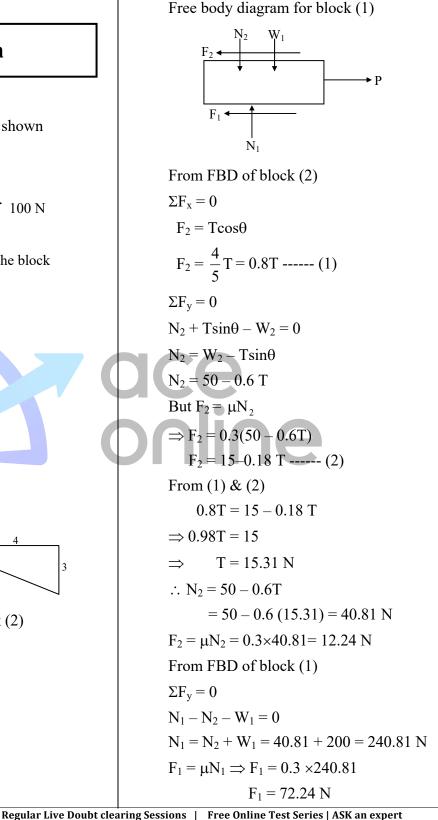




India's Best Online Coaching Platform for GATE, ESE, PSUs, SSC-JE, RRB-JE, SSC, Banks, Groups & PSC Exams Enjoy a smooth online learning experience in various languages at your convenience

ace online





ACE 7 $\Sigma F_x = 0$ 04. Ans: (d) $P - F_1 - F_2 = 0$ $P = F_1 + F_2 = 72.24 + 12.24$ N_2 P = 84.48 N03. Ans: (b) ↓ m₂ g Sol: Free Body Diagram N_2 20 cm 10 cm NB Nı $m_1 g$ where, f is the friction between the two 10 cm 35 cm NA books. W = 100 N f_1 is the friction between the lower book and ground. $F_A = \mu N_A = \frac{1}{3} N_A$ Now, maximum possible acceleration of $F_B = \mu N_B = \frac{1}{3} N_B$ upper book. $a_{\max} = \frac{f_{\max}}{m_2} = \frac{\mu m_2 g}{m_2} = \mu \times g$ $\Sigma M_{\rm B} = 0$ $= 0.3 \times 9.81 = 2.943 \text{ m/s}^2$ $-100 \times 30(\bigcirc) + (N_A \times 20)(\bigcirc) + (F_a \times 12)(\bigcirc) = 0$ For slip to occur, acceleration (a_1) of lower $-3000 + N_A \times 20 + \frac{1}{3}N_A \times 12 = 0$ Since book. i.e, $a_1 \ge a_{max}$ \Rightarrow N_A = 125 N $\frac{F-f-f_1}{m_1} \ge 2.943$ $\Sigma F_{\rm v} = 0$ $N_A - N_B - 100 = 0$ $F - 2.943 - 0.3 \times 2 \times 9.81 \ge 2.943$ \Rightarrow N_B = 25 N $f: f = f_{max} = 2.943$ and $\Sigma F_x = 0$ $f_1 = \mu \times (m_1 + m_2) g = 0.3 \times 2 \times 9.81$ $\mathbf{P} = \mathbf{F}_{\mathrm{A}} + \mathbf{F}_{\mathrm{B}} = \frac{1}{3} \left(\mathbf{N}_{\mathrm{A}} + \mathbf{N}_{\mathrm{B}} \right)$ $F \ge 11.77 \text{ N}$ $F_{min} = 11.77 \text{ N}$ $=\frac{1}{3}(125+25)=50$ N

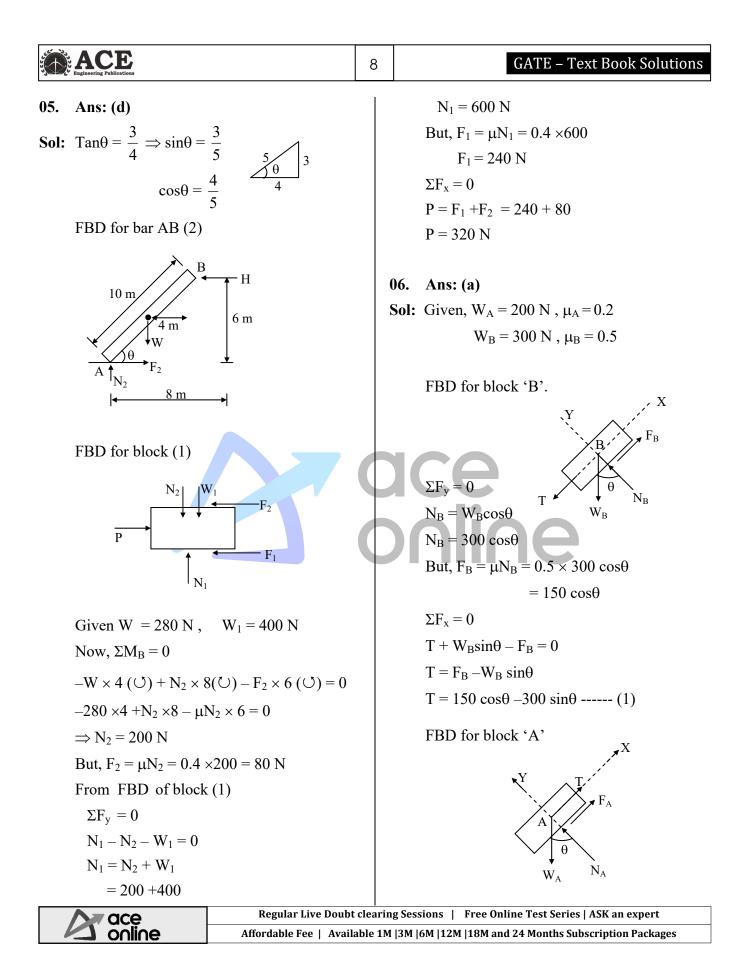
Engineering Mechanics

f

F

Sol: F.B.D of both the books are shown below.

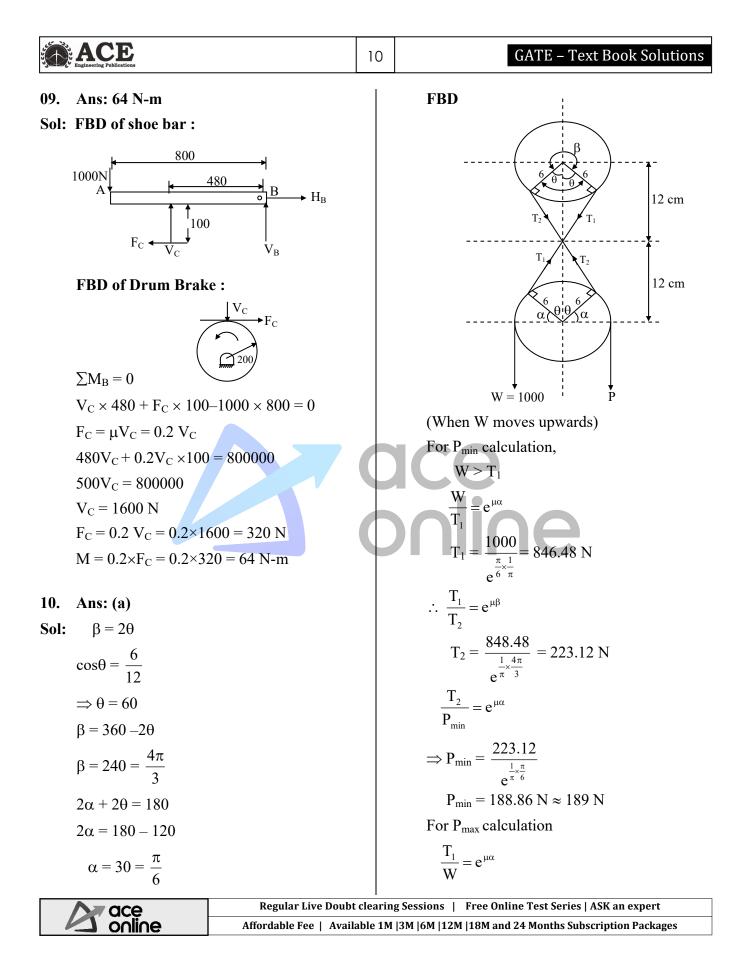
ace online India's Best Online Coaching Platform for GATE, ESE, PSUs, SSC-JE, RRB-JE, SSC, Banks, Groups & PSC Exams Enjoy a smooth online learning experience in various languages at your convenience



ACE Engineering Publications	9	Engineering Mechanics
$\Sigma F_{y} = 0$ $N_{A} - W_{A} \cos \theta = 0$ $N_{A} = 200 \cos \theta$ $F_{A} = \mu N_{A} = 0.2 \times 200 \cos \theta$ But, $F_{A} = 40 \cos \theta$ $\Sigma F_{x} = 0$ $T + F_{A} - W_{A} \sin \theta = 0$ $T = W_{A} \sin \theta - F_{A}$ $T = 200 \sin \theta - 40 \cos \theta$ But from equation (1) $T = 150 \cos \theta - 300 \sin \theta$ $\therefore 150 \cos \theta - 300 \sin \theta = 200 \sin \theta - 40 \cos \theta$ $190 \cos \theta = 500 \sin \theta$ $\tan \theta = \frac{190}{500}$ $\Rightarrow \theta = 20.8^{\circ}$ 07. Ans: (d) Sol: FBD for the block V $V = 500$ $\Sigma F_{y} = 0$ $N - W \sin 45 - P \sin 45 = 0$ $N = \frac{500}{\sqrt{2}} + \frac{P}{\sqrt{2}}$	R /	But, $F = \mu N = 0.25 \left(\frac{500}{\sqrt{2}} + \frac{P}{\sqrt{2}} \right)$ $\Sigma F_x = 0$ $P \cos 45 + F - W \sin 45 = 0$ $P \cos 45 + 0.25 \left(\frac{500}{\sqrt{2}} + \frac{P}{\sqrt{2}} \right) - 500 \times \frac{1}{\sqrt{2}} = 0$ $\Rightarrow P = 300 N$ 08. Ans: (a) Sol: FBD of block $F_1 = \mu N_1$ $F_2 = \mu N_2$ $\Sigma F_x = 0$ $N_2 - F_1 = 0$ $\Rightarrow N_2 = F_1 (\because F_1 = \mu N_1)$ $N_2 = \mu N_1$ $\Sigma F_y = 0$ $N_1 + \mu N_2 - W = 0$ $N_1 + \mu N_2 - W = 0$ $N_1 + \mu^2 N_1 - W = 0$ $(\because N_2 = \mu N_1)$ $N_1 (1 + \mu^2) = W$ $N_1 = \frac{W}{1 + \mu^2}$ $N_2 = \frac{\mu W}{1 + \mu^2}$ $Couple = (F_1 + F_2) \times r$ $= \mu r (N_1 + N_2)$ $= \frac{\mu r \times W(1 + \mu)}{1 + \mu^2}$ $(\because \mu = f)$
	I	

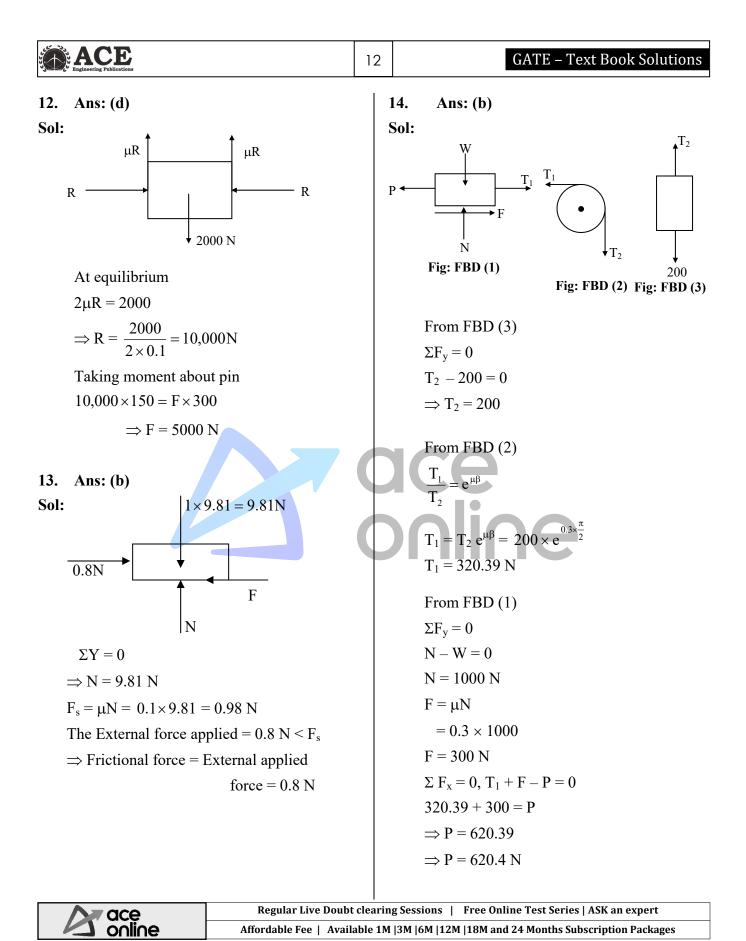
 India's Best Online Coaching Platform for GATE, ESE, PSUs, SSC-JE, RRB-JE, SSC, Banks, Groups & PSC Exams

 Enjoy a smooth online learning experience in various languages at your convenience



ACE	11	Engineering Mechanics
Engineering Publications		
$T_1 = 1000 \times e^{\frac{1}{\pi} \times \frac{\pi}{6}}$		From FBD (1)
		$\Sigma F_y = 0$
$T_1 = 1181.36 \text{ N}$		$N_2 - W_2 \cos\theta = 0$
$\frac{T_2}{T_1} = e^{\mu\beta}$		$N_2 = W_2 \cos\theta = W \times 0.8$
1		$N_2 = 0.8 W$
$T_2 = 1181.36 \times e^{\frac{1}{\pi} \times \frac{4\pi}{3}} = 4481.65 \text{ N}$		$\therefore F_2 = \mu N_2 = 0.2 \times 0.8 \text{ W}$
		$F_2 = 0.16 W$
$\frac{P_{max}}{T_2} = e^{\mu\alpha}$		$\Sigma F_{\rm x} = 0$
$\frac{1}{-\kappa}\pi$		$T_1 - W_2 \sin\theta - F_2 = 0$
$P_{\text{max}} = 4481.68 \times e^{\frac{1}{\pi} \times \frac{\pi}{6}}$	- DI	$T_1 = F_2 + W_2 \sin\theta = 0.16 \text{ W} + 0.6 \text{W}$
$P_{max} = 5300 \text{ N}$	ERI/	$T_1 = 0.76 W$
11. Ans: (b)		
Ga		From FBD (2)
Sol: Given $\mu = 0.2$, $\tan \theta = \frac{3}{4}$		$\Sigma F_y = 0$
$\Rightarrow \cos \theta = \frac{4}{5}$		$N_2 + W_1 \cos\theta = N_1$
5		$N_1 = N_2 + W_1 \cos \theta$
$\sin\theta = \frac{3}{5}$		$N_1 = 0.8W + 1000 \times \frac{4}{5}$
		5
y Ti		$N_1 = 0.8 W + 800$
		$F_1 = \mu N_1 = 0.2 (0.8 \text{ W} + 800)$
Sin	ce 1	995 = $0.16 \text{ W} + 160$
		$\frac{T_2}{T_2} = e^{\mu\beta}$
$W_2 \sin \theta$ F_2 $W_2 \cos \theta$ V_2	x	
$W_2 = W$		$T_2 = T_1 e^{\mu\beta} = 0.76 W e^{0.2 \times \pi}$
Fig: FBD (1) \bigvee_{N_1} F_2		$T_2 = 1.42 W$
		$\Sigma F_x = 0$
		$T_2 + F_1 + F_2 = W_1 \sin \theta$
θ N_1		$1.42W+0.16W+160+0.16W = 1000 \times \frac{3}{5}$
$W_{1}\sin\theta \qquad \qquad$		5
Fig: FBD (2)		$1.74 \text{ W} = 440$ $\implies \text{W} = 252.87 \text{ N}$
rig. rbb (2)		\Rightarrow W = 252.87 N
India's Best Online Coaching Platfor	rm for G	ATE, ESE, PSUs, SSC-JE, RRB-JE, SSC, Banks, Groups & PSC Exams
Enjoy a smooth online learning experience in various languages at your convenience		

A dce online Best Online Coaching Platform for GATE, ESE, PSUs, SSC-JE, RRB-JE, SSC, Banks, Groups & PSC Exams Enjoy a smooth online learning experience in various languages at your convenience



ACE Engineering Publications	13	Engineering Mechanics
		$\Rightarrow C_1 = 0$
Chapter Kinematics of Particle Rectilinear	1	$2\sqrt{V} = 6t$
4 and Curvilinear Motion]	$V = 9t^2$
		But V = $\frac{ds}{dt} = 9t^2$
01. Ans: (d) Sol: $x = 2t^3 + t^2 + 2t$		$\int ds = \int 9t^2 dt$
		$S = 3t^3 + C_2$
$V = \frac{dx}{dt} = 6t^2 + 2t + 2$		At, $t = 2 \sec, S = 30 m$
$a = \frac{dv}{dt} = 12t + 2$	- 01/	$\Rightarrow 30 = 3(2)^3 + C_2$ $\Rightarrow C_2 = 6$
dt At t = 0 \Rightarrow V = 2 and a = 2	EKU	$\therefore S = 3t^3 + 6$
At $t = 0 \implies v = 2$ and $a = 2$		At t = 3 sec
02. Ans: (a)		$S = 3(3)^3 + 6$
Sol: $V = kx^3 - 4x^2 + 6x$		S = 87 m
$V_{\text{at } x = 2 \text{ if } k = 1} = 2^3 - 4(2)^2 + 6(2) = 4$		
$a = \frac{dV}{dt} = k.3x^2 \frac{dx}{dt} - 8x \frac{dx}{dt} + 6 \frac{dx}{dt}$		04. Ans: (a) Sol: Given, $a = -8S^{-2}$
$a = 3x^{2}(V) - 8x(V) + 6(V)$		$\Rightarrow \frac{dV}{dt} = \frac{d^2s}{dt^2} = -8s^{-2} = a$
$= 3(2)^2 \times 4 - (8 \times 2 \times 4) + 6(4)$		ut ut
$= 8 \text{ m/s}^2$	ce 1	We know that, $\int V dv = \int a ds$
03. Ans: (d)		$\frac{V^2}{2} = \int -8s^{-2} ds$ $\frac{V^2}{2} = \frac{8}{2} + C_1$
Sol: Given, $a = 6\sqrt{V}$		V^2 8
$\frac{\mathrm{dV}}{\mathrm{dt}} = 6\sqrt{\mathrm{V}}$		$\frac{V^2}{2} = \frac{8}{S} + C_1$
		Given, at $S = 4 \text{ m}$, $V = 2 \text{ m/sec}$
$\int \frac{\mathrm{dV}}{\sqrt{\mathrm{V}}} = \int 6 \mathrm{dt}$		$\Rightarrow \frac{2^2}{2} = \frac{8}{4} + C_1$
$2\sqrt{V} = 6t + C_1$		$\Rightarrow C_1 = 0$
Given, at $t = 2 \sec$, $V = 36$		$\therefore \frac{V^2}{2} = \frac{8}{8}$
$\Rightarrow 2\sqrt{36} = 6(2) + C_1$		$\frac{1}{2} = \frac{1}{8}$
India's Best Online Coaching Platfor	m for G	ATE, ESE, PSUs, SSC-JE, RRB-JE, SSC, Banks, Groups & PSC Exams
Enjoy a smooth online learning experience in various languages at your convenience		

Engineering Publications	14	GATE – Text Book Solutions	
$V = \frac{4}{\sqrt{s}}$		$\int d\mathbf{x} = \int \left(\frac{4t^3}{3} - 2t + C_1\right) dt$	
$\Rightarrow \frac{\mathrm{ds}}{\mathrm{dt}} = \frac{4}{\sqrt{\mathrm{s}}}$		$\mathbf{x} = \frac{4t^4}{3 \times 4} - 2 \cdot \frac{t^2}{2} + C_1 t + C_2$	
$\Rightarrow \int \sqrt{s} ds = \int 4 dt$		$x = \frac{t^4}{3} - t^2 + C_1 t + C_2$	
$\frac{2}{3}s^{3/2} = 4t + C_2$		3 Given condition,	
At $t = 1$, $S = 4$		At $t = 0$, $x = -2 m$	
$\Rightarrow \frac{2}{2}(4)^{3/2} = 4(1) + C_2$		$\Rightarrow -2 = C_2$	
$\Rightarrow \frac{1}{3}(4) = 4(1) + C_2$		At $t=2, x=-20 m$	
$\Rightarrow C_2 = \frac{16}{3} - 4 = \frac{4}{3}$		$\Rightarrow -20 = \frac{2^4}{3} - 2^2 + 4(2) + (-2)$	
$\therefore \frac{2}{3}s^{3/2} = 4t + C_2$		$\Rightarrow C_1 = \frac{-29}{3}$	
$\Rightarrow \frac{2}{3}s^{3/2} = 4t + \frac{4}{3}$	C	$\therefore x = \frac{t^4}{3} - t^2 - \frac{29}{3}t - 2$	
At t = 2 sec $\frac{2}{3}s^{3/2} = 4(2) + \frac{4}{3}$	C	: at t = 4 sec $x = \frac{4^4}{2} - 4^2 - \frac{29}{2}(4) - 2$	
\Rightarrow s = 5.808 m		= 28.67 m	
$a = \frac{-8}{s^2} = \frac{-8}{5.808^2} = -0.237 \text{ m/sec}^2$		- 28.07 m	
		06. Ans: (b)	
05. Ans: (c)		Sol:	
Sol: Given, $a = 4t^2 - 2$		$u_A = 20 \text{ m/sec}$ $a_A = 5 \text{ m/sec}^2$ $u_B = 60 \text{ m/sec}$ $a_B = -3 \text{ m/sec}^2$	
$\frac{\mathrm{d}v}{\mathrm{d}t} = 4t^2 - 2$		0 0 0	
ut		Pt "A" Pt "B" A & B	
$dv = (4t^2 - 2) dt$		$ \xrightarrow{S_B} S_A $	
$v = \frac{4t^3}{3} - 2t + C_1$			
$\frac{dx}{dt} = \frac{4t^3}{3} - 2t + C_1$		Let S_A be the distance traveled by "A" Let S_B be the distance traveled by "B"	
Regular Live Double	l t clearin	ng Sessions Free Online Test Series ASK an expert	
	Affordable Fee Available 1M 3M 6M 12M 18M and 24 Months Subscription Packages		

SACE
 15
 Engineering Mechanics

$$S_A = S_B + 384$$
 $u_A t + \frac{1}{2} a_A t^2 = u_B t + \frac{1}{2} a_B t^2 + 384$
 08. Ans: (c)

 $u_A t + \frac{1}{2} a_A t^2 = u_B t + \frac{1}{2} a_B t^2 + 384$
 $u_A t + \frac{1}{2} a_A t^2 = u_B t + \frac{1}{2} a_B t^2 + 384$
 $u_A t + \frac{1}{2} a_A t^2 = u_B t + \frac{1}{2} a_B t^2 + 384$
 $4t^2 - 40t - 384 - 0$
 $t = 16 \sec (or) - t = -6 \sec (x + 16 \sin (x +$

A ace online India's Best Online Coaching Platform for GATE, ESE, PSUs, SSC-JE, RRB-JE, SSC, Banks, Groups & PSC Exams Enjoy a smooth online learning experience in various languages at your convenience

CE GATE - Text Book Solutions 16 Ans: (b) u = 0g $t = 5 \sec \theta$ V = u + atV = 0 + 9.81(5)V = u + at

V = velocity with which stone strike the glass

Velocity loss = 20% of V

V = 49.05 m/sec

$$=\frac{49.05\times20}{100}=9.81 \text{ m/sec}$$

... Initial velocity for further movement in

glass = 49.05 - 9.81 = 39.24 m/secDistance traveled for 1 sec of time is given by

$$S = ut + \frac{1}{2}at^{2}$$

$$S = 39.24(1) + \frac{1}{2}(9.81)(1)$$

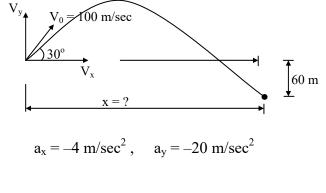
$$S = 44.145 \text{ m}$$

10. Ans: (a)

Sol:

09.

Sol:



$$V_{x} = V_{0} \cos 30 = 100 \times \frac{\sqrt{3}}{2} = 86.6 \text{ m/sec}$$

$$V_{y} = V_{0} \sin 30 = 100 \times \frac{1}{2} = 50 \text{ m/sec}$$

$$y = V_{0y}t + \frac{1}{2}a_{y}t^{2}$$

$$-60 = 50t + \frac{1}{2}(-20)t^{2}$$

$$10t^{2} - 50t - 60 = 0$$

$$t = 6 \text{ (or)} -1 \text{ sec}$$

$$\therefore t = 6 \text{ sec}$$

$$x = V_{0}t + \frac{1}{2}a_{x}t^{2}$$

$$x = (86.6 \times 6) + \frac{1}{2}(-4)6^{2}$$

$$x = 447.6 \text{ m} \approx 448 \text{ m}$$
11. Ans: (a)
Sol: Given, V = 20 m/sec

$$x = 20 \text{ m}, y = 8.0 \text{ m}$$

$$y = V_{0}t + \frac{1}{2}y = 0 \text{ m}$$

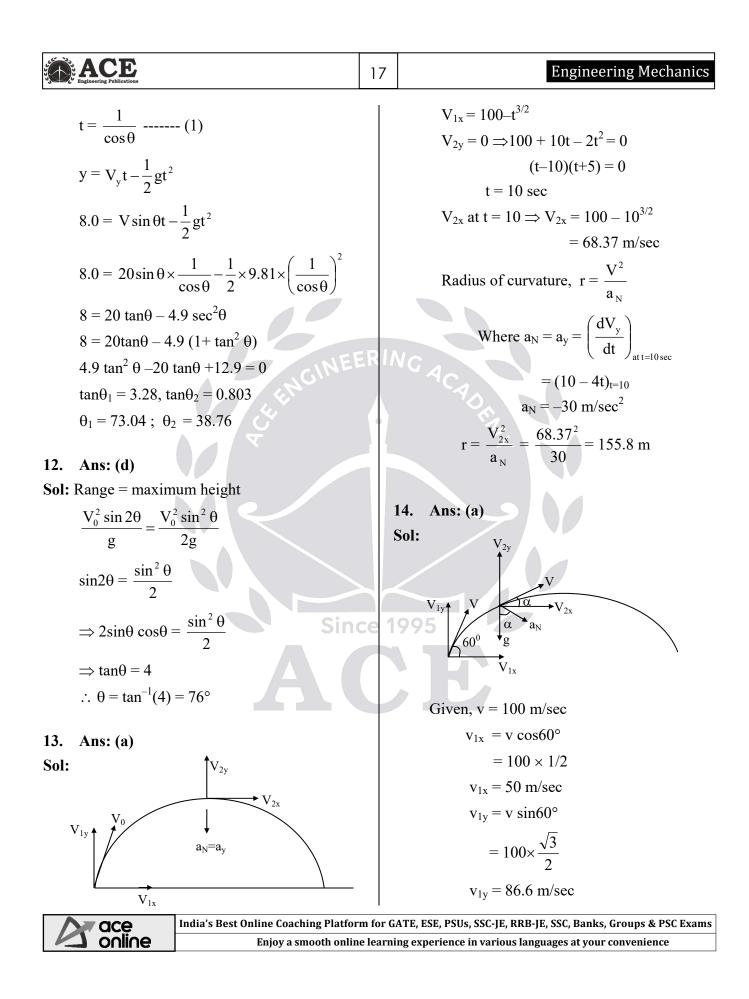
 $V_x = V \cos\theta$, $V_y = V \sin\theta$ $x = V_x t + \frac{1}{2}at^2$ (:: a = 0, along x direction)

► x

 $x = V \cos\theta t$ $20 = 20 \cos\theta t$

Regular Live Doubt clearing Sessions | Free Online Test Series | ASK an expert

ace online Affordable Fee | Available 1M |3M |6M |12M |18M and 24 Months Subscription Packages



ACE Engineering Publications

$$v_{2y} - v_{1y} \text{ gt} (use V - u + at) = 86.6 - 9.8(1)$$

$$v_{2y} = 76.8 \text{ m/sec}$$

$$v_{2x} = v_{1x} = 50 \text{ m/sec}$$

$$v_{2x} = v_{1x} = 50 \text{ m/sec}$$

$$v_{at+1} = \sqrt{v_{1x}^{2} + v_{2y}^{2}}$$

$$= \sqrt{50^{2} + 76.8^{2}}$$

$$= 91.6 \text{ m/sec}$$

$$\alpha = \tan^{1}\left(\frac{v_{y}}{v_{x}}\right) = \tan^{1}\left(\frac{76.8}{50}\right)$$

$$\alpha = 56.9 \text{ rad/sec}$$

$$a_{N} = g\cos\alpha = 9.81 \times \cos56.9^{\circ}$$

$$= 5.35 \text{ m/sec}^{2}$$

$$r = \frac{V^{2}}{a_{N}} = \frac{91.6^{2}}{5.35} - 1568.62 \text{ m}$$
15. Ans: (d)
Sol:

$$v_{1y} \int \frac{1}{30^{d}}$$

$$v_{1x} = v \cos 30 - 43.3 \text{ m/sec}$$

$$a_{N} = g = a$$

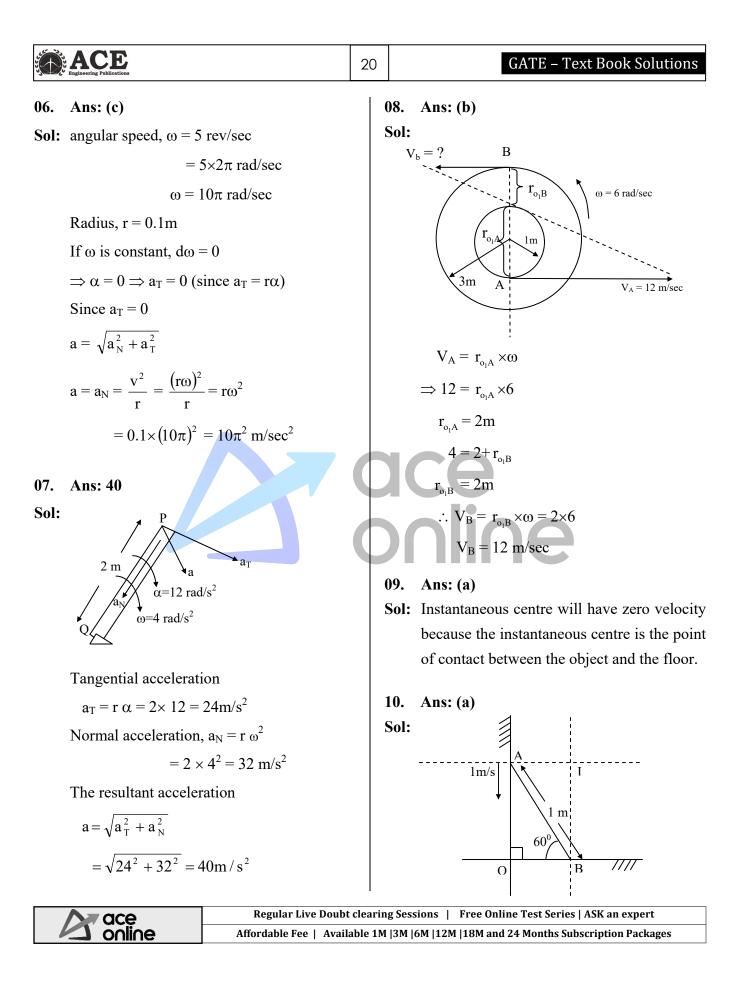
$$r = \frac{V_{1x}^{2}}{a_{N}} = \frac{43.3^{2}}{9.81} = 191.13 \text{ m}$$

$$\alpha = \frac{a_{T}}{r} = \frac{5.83}{10} = 0.583 \text{ rad/sec}^{2}$$

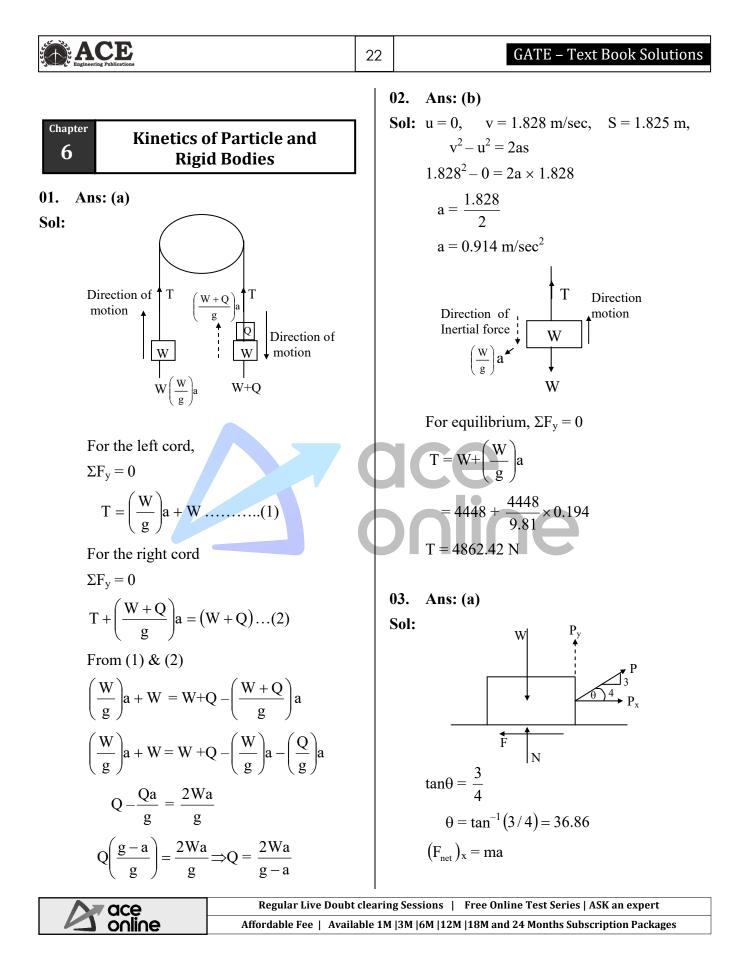
 Regular Live Doubt clearing Sessions
 Free Online Test Series | ASK an expert

 Affordable Fee | Available 1M |3M |6M |12M |18M and 24 Months Subscription Packages

	ACE Engineering Publications	19	,	Engineering Mechanics
02.	Ans: (c)	I	04.	Ans: (d)
Sol:	Given $\omega = 4\sqrt{t}$		Sol:	Given angular acceleration, $\alpha = \pi \operatorname{rad/sec}^2$
	$\theta = 2$ radians at t = 1 sec			Angular displacement in time t_1 and t_2
	$\theta = ? \alpha = ?$ at t = 3sec			$=\pi$ rad $=\theta_2-\theta_1$
	$\omega = \frac{\mathrm{d}\theta}{\mathrm{d}t} \Longrightarrow \int \mathrm{d}\theta = \int \omega \mathrm{d}t$			$\omega_{t2} = 2\pi \text{ rad/sec}$
	ut t			$\omega_{t1} = ?$
	$\theta = \int 4 \sqrt{t} dt$			$\omega_{t1}^2 - \omega_0^2 = 2\alpha\theta_1$
	$\theta = \frac{8}{3}t^{3/2} + c(1)$			$\omega_{t2}^2 - \omega_0^2 = 2\alpha\theta_2$
	From given condition, at $t = 1$, $\theta = 2rad$	Ð	No	$\omega_{t2}^2 - \omega_{t1}^2 = 2\alpha(\theta_2 - \theta_1)$
	$(1) \Longrightarrow 2 = \frac{8}{3} (1)^{3/2} + \mathbf{c}_1 \Longrightarrow \mathbf{c}_1 = \frac{-2}{3} \mathbf{C}$	= 1		$4\pi^2 - \omega_{t1}^2 = 2\pi^2$
	$-8_{+3/2}$ 2			$\omega_{t1}^2 = 2\pi^2$
	$\therefore \theta = \frac{8}{3}t^{3/2} - \frac{2}{3}$			$\omega_{t1} = \pi \sqrt{2} \text{ rad/s}$
	At t = 3 sec, $\theta = \frac{8}{3}(3)^{3/2} - \frac{2}{3}$		05.	Ans: (c)
	$\theta_{t=3} = 13.18$ rad			Given retardation
				$\alpha = -3t^2$
	$\alpha = \frac{d\omega}{dt} = \frac{d(4\sqrt{t})}{dt} = \frac{2}{\sqrt{t}}$			$d\omega 2t^2$
	$a = \frac{2}{115} = 1.15 \text{ rad} (a a a^2)$		<	$\frac{\mathrm{d}\omega}{\mathrm{d}t} = -3t^2$
	$\alpha_{t=3} = \frac{2}{\sqrt{3}} = 1.15 \text{rad/sec}^2$	ce	199	$\int d\omega = \int -3t^2 dt$
03.	Ans: (b)			$\omega = -t^3 + c_1$
	$r = 2 \text{ cm}, \omega = 3 \text{ rad/sec}, a = 30 \text{ cm/s}^2$			From given condition at $t = 0$,
	$a_N = r\omega^2 = 2(3)^2 = 18 \text{ cm/sec}^2$			$\omega = 27 \text{ rad/sec}$
	Since total acceleration $a = \sqrt{a_T^2 + a_N^2}$			$27 = -0^3 + c_1$
	$\Rightarrow a^2 = a_T^2 + a_N^2$			\Rightarrow c ₁ = 27
	$30^2 = a_T^2 + 18^2$			$\therefore \omega = -t^3 + 27$
	1			Wheel stops at $\omega = 0$,
	$a_{\rm T} = 24 \text{ cm/sec}^2$ $a_{\rm T} = r\alpha = 24$			$\Rightarrow 0 = -t^3 + 27$
	-			\Rightarrow t = 3sec
	$\alpha = \frac{24}{2} = 12 \text{ rad/sec}^2$			
		m for	GATE, I	ESE, PSUs, SSC-JE, RRB-JE, SSC, Banks, Groups & PSC Exams
	Contine Enjoy a smooth onlin	e lear	ning ex	perience in various languages at your convenience

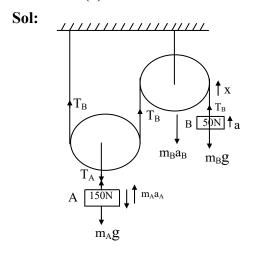


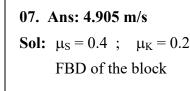
Engineering Publications	21	Engineering Mechanics
$V_a = 1 m/s$		'I' is the instantaneous centre.
$V_a = a long vertical$		From sine rule
$V_b = a \log horizontal$		PQ IQ IP
So instantaneous center of V_a and V_b will b	e	$\frac{PQ}{\sin 45} = \frac{IQ}{\sin 70} = \frac{IP}{\sin 65}$
perpendicular to A and B respectively		$\frac{\mathrm{IP}}{\mathrm{IQ}} = \frac{\sin 65^{\circ}}{\sin 70^{\circ}}$
$IA = OB = l \times \cos \theta = 1 \times \cos 60^{\circ} = \frac{1}{2}m$		$V_Q = IQ \times \omega = 1$
$IB = OA = l \times \sin \theta = 1 \times \sin 60^{\circ} = \frac{\sqrt{3}}{2}m$		$\Rightarrow \omega = \frac{V_{Q}}{IQ}$
$V_a = \omega \times IA$	ERI	$V_{\rm P} = IP \times \omega = \frac{IP}{IQ} \times V_{\rm Q} = \frac{\sin 65^{\circ}}{\sin 70^{\circ}} \times 1$
$\Rightarrow \omega = \frac{V_a}{IA} = 2 \text{ rad/sec}$		= 0.9645 m/s
11. Ans: (d)		
Sol: The velocity directions instantaneous centr	e	
can be located as shown. By knowin	g	
velocity (magnitude) of Q we can get th	e	
angular velocity of the link, from this w	e	
can get the velocity of 'P using sine rule.		
Zin	ce 1	1995
45°		
$V_Q = 1 \text{m/sec}$ $Q = 45^{\circ} 65^{\circ}$ 20° 70°		
V_{P}		
		GATE, ESE, PSUs, SSC-JE, RRB-JE, SSC, Banks, Groups & PSC Exams ing experience in various languages at your convenience

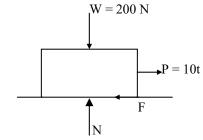


	Engineering Publications	23	Engineering Mechanics
	$P_{x} - F = \left(\frac{W}{g}\right)a$		From static equilibrium condition $\Sigma F_y = 0$
	$\mathbf{P}\mathbf{cos36.86} - \mathbf{F} = \left(\frac{\mathbf{W}}{\mathbf{g}}\right)\mathbf{a}$		N - W = 0 N = W = 44.48N
	$0.8\mathrm{P}-\mathrm{F}=\left(\frac{2224}{\mathrm{g}}\right)(0.2\mathrm{g})$		From dynamic equilibrium condition $\Sigma F_x = 0$
	0.8P - F = 444.8		F = ma
	0.8P - F = 444.8 + F		$\mu \mathbf{N} = \frac{\mathbf{W}}{\mathbf{g}} \mathbf{a}$
	P = 556 + 1.25F(1)		g
	$\Sigma F_y = 0$	ERI	$VG \mu = \frac{a}{r}$
	$N+P_{y}-W=0$	3	Cg
	$N = W - P_y (since \mu = \frac{F}{N})$		$a = \mu g$ (1) Since $v^2 - u^2 = 2as$
	$F = \mu N$	-	$0 - (9.126)^2 = 2(-a) \times 13.689$
	$\mathbf{F} = \boldsymbol{\mu} \left(\mathbf{W} - \mathbf{P}_{\mathbf{y}} \right)$		$a = 3.042 \text{ m/s}^2$ (2)
	$= 0.2(2224 - P \sin 36.86)$		From (1) & (2)
	$F = 444.8 - 0.12P \dots(2)$		$3.042 = \mu(9.81)$
	From (1) & (2)		$\Rightarrow \mu = 0.31$
	P = 556 + 1.25(444.8 - 0.12P)		
	1.15P = 1112		05. Ans: (a)
	P = 966.95	ce 1	Sol:
04.	P = 967 N Ans: (d)		$rac{P}{F}$
Sol:			$\dot{\mathbf{w}}_{\theta} \mathbf{Q}$
	$\frac{W}{u=9.126 \text{ m/s}}$ $\downarrow \rightarrow V=0$		ma N
	↓ ← ma		
	F s		mg.sin0
	N		$mg\cos\theta$ W θ
	18		X
	India's Best Online Coaching Platfor	m for (GATE, ESE, PSUs, SSC-JE, RRB-JE, SSC, Banks, Groups & PSC Exams
K			ning experience in various languages at your convenience

ACE **GATE – Text Book Solutions** 24 $T_A = 2T_B$ $\Sigma F_{\rm v} = 0$ (static equilibrium)(1) Work done by A & B equal $N - W \cos\theta = 0$ $T_A S_A = T_B S_B$ $N = W\cos\theta = mg\cos\theta$ $2T_BS_A = T_BS_B$ Since $F = \mu N = \mu \operatorname{mgcos} \theta$(1) $2S_A = S_B$ $\Sigma F_x = 0$ (Dynamic equilibrium) $2a_A = a_B$(2) $F+ma - Wsin\theta = 0$ For 'B' body $F = mgsin\theta - ma$(2) $T_B = m_B a_B + m_B g$(3) From (1) & (2) For 'A' body $\mu mg \cos\theta = mg \sin\theta - ma$ $T_A = m_A g - m_A a_A \qquad \dots (4)$ $\Rightarrow a = gsin\theta - \mu gcos\theta$ (2), (3) & (4) sub in (1) \Rightarrow a = gcos θ (tan θ – μ) $m_A g - m_A a_A = 2(m_B(2a_A) + m_B g)$ $m_A g - m_A a_A = 4m_B a_A + 2m_B g$ Given, PO = s $m_A a_A + 4m_B a_A = m_A g - 2m_B g$ $s = ut + \frac{1}{2}at^2$ $a_{\rm A} = \frac{m_{\rm A}g - 2m_{\rm B}g}{m_{\rm A} + 4m_{\rm B}}$ $s = 0(t) + \frac{1}{2}at^2 \implies t = \sqrt{\frac{2s}{a}}$ $\frac{150 - 2(50)}{\frac{150}{10} + 4\left(\frac{50}{10}\right)}$ $=\sqrt{\frac{2s}{g\cos\theta(\tan\theta-\mu)}}$







 $=\frac{50}{15+20}=\frac{50}{35}=1.42$ m/s²

- de	ie line
------	------------

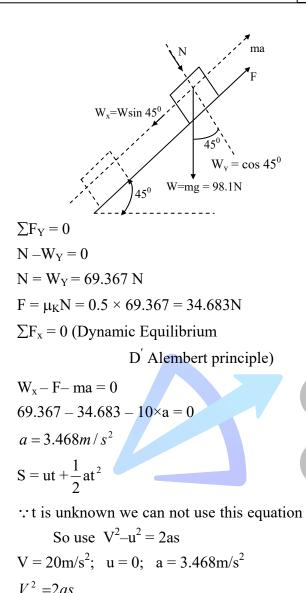
 Regular Live Doubt clearing Sessions
 |
 Free Online Test Series | ASK an expert

 Affordable Fee
 |
 Available 1M |3M |6M |12M |18M and 24 Months Subscription Packages

ace online

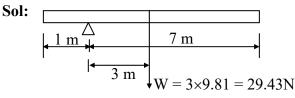
India's Best Online Coaching Platform for GATE, ESE, PSUs, SSC-JE, RRB-JE, SSC, Banks, Groups & PSC Exams Enjoy a smooth online learning experience in various languages at your convenience

ACE Engineering Publications



$$S = \frac{V^2}{2 \times a} = \frac{20^2}{2 \times 3.468} = 57.67 \text{m}$$

10. Ans: 2.053 rad/s²



$$M = I\alpha$$

$$M = 29.43 \times 3 = 88.29N-m$$

$$I = I_0 + Ad^2 = \frac{m\ell^2}{12} + md^2 = \frac{3 \times 8^2}{12} + 3 \times 3^2$$

$$= 16 + 27 = 43kg - m^2$$

$$\alpha = \frac{M}{I} = \frac{88.29}{43} = 2.053 \text{ rad/s}^2$$
11. Ans: (d)
Sol:

Sol:

$$L$$

$$L$$

$$Max = 0$$

$$V_A + ma = W$$

$$V_A = m(g-a)...(1)$$

$$Where, a = \frac{L}{2}\alpha$$
Since, M = I\alpha
$$W \times \frac{L}{2} = \left(\frac{mL^2}{12} + m\left(\frac{L}{2}\right)^2\right)\alpha$$

$$mg \times \frac{L}{2} = \frac{4mL^2}{12} \times \frac{2a}{L}$$

$$a = \frac{3}{4}g...(2)$$
from (1) & (2)

$$V_A = m\left(g - \frac{3}{4}g\right) = \frac{mg}{4}$$

$$V_A = \frac{W}{4}$$

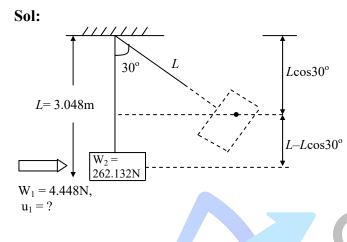
	Regular Live Doubt clearing Sessions Free Online Test Series ASK an expert				
ace online	Affordable Fee Available 1M 3M 6M 12M 18M and 24 Months Subscription Packages				

26

ACE Engineering Publications

ChapterWork-Energy Principle and7Impulse Momentum Equation

01. Ans: (a)



The loss of KE of shell converted to do the work in lifting the sand box and shell to a height of " $L - L\cos 30^{\circ}$ "

i.e.,
$$Wd = \frac{1}{2}mV^2$$

Where $d = L - L\cos 30^\circ$
 $= 3.048 - 3.048 \times \cos 30 = 0.41 \text{ m}$
 $266.58 \times 0.41 = \frac{1}{2} \left(\frac{266.58}{9.81}\right) \times V^2$
 $\Rightarrow V = 2.83 \text{ m/sec}$

Where V is the velocity of block & shell

By momentum equation

ace online

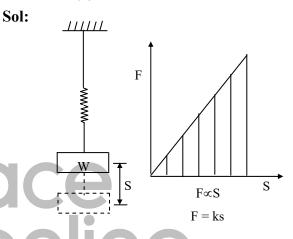
 $m_1u_1 + m_2u_2 = m_1v_1 + m_2v_2$

Where $v_1 = v_2 = V \& u_1 = ?, u_2 = 0$

 $\frac{4.448}{9.81} \times u_1 = \frac{4.448 + 262.132}{9.81} \times 2.83$ $\Rightarrow u_1 = 169.6 \text{ m/sec}$

GATE – Text Book Solutions

- u₁ & u₂ = Initial velocity of shell and block respectively
- $V_1 \& V_2 =$ Final velocity of block & shell



Strain energy in spring = Area under the force displacement curve.

$$= \frac{1}{2} F \times s = \frac{1}{2} (ks) \times s = \frac{1}{2} ks^{2}$$
$$\frac{1}{2} ks^{2} = \text{Gain of KE}$$
$$\frac{1}{2} ks^{2} = \frac{1}{2} mv^{2}$$
$$\Rightarrow v^{2} = \frac{ks^{2}}{m} = \frac{ks^{2}}{w}g$$
$$v = \sqrt{\frac{kg}{w}} \cdot s \qquad \left(\because m = \frac{w}{g}\right)$$

 Regular Live Doubt clearing Sessions
 Free Online Test Series
 ASK an expert

 Affordable Fee
 Available 1M |3M |6M |12M |18M and 24 Months Subscription Packages

28

2 Sol: Given,
$$m = 2 \text{ kg}$$

Position at any time is given as
 $x = t + 5t^2 + 2t^3$
At $t = 0, x = 0,$
At $t = 3 \text{ sco},$
 $x = 3 + 5(3^2) + 2(3^3) = 102 \text{ m}$
Velocity, $V = \frac{dt}{dt} = 1 + 10t + 6t^2$
Initial velocity i.e., $t = 0$, is $v_1 = 1 \text{ m/s}$
Final velocity i.e., $t = 0$, is $v_1 = 1 \text{ m/s}$
Final velocity i.e., $t = 0$, is $v_1 = 1 \text{ m/s}$
Final velocity i.e., $t = 0$, is $v_1 = 1 \text{ m/s}$
 $= \frac{1}{2} \text{ m/s}^2 - \frac{1}{2} \text{ m/s}^2$
 $= \frac{1}{2} \times 2(85^2 - 1^2) = 7224 \text{ J}$
06. Ans: (c)
801: $\int \text{ dw} x \text{ doe } x \text{ doe } x^*$
Work done $= \frac{5}{8} \text{ frak}$
 $= \frac{1}{5} e^{-2x} \text{ dx} = \left[\frac{e^{-2x}}{-2}\right]_{0,2}^{1,2} = 0.31 \text{ J}$
05. Ans: (b)
801: $F = 4x - 3x^2$
Potential Energy at $x = 1.7 = \text{ work required}$
to move object from 0 to 1.7m
 $PE = \int_{0}^{17} \text{ Fdx}$
16. $(1 - b)b = \frac{1}{2} \frac{\text{wLv}^2}{g}$
w $b^2 + \text{w}(L - b)b = \frac{1}{2} \frac{\text{wLv}^2}{g}$
w $b^2 + \frac{1}{2} + \text{w}(L - b)b = \frac{1}{2} \frac{\text{wLv}^2}{g}$
w $b^2 - \frac{1}{2} + \frac{\text{wLv}^2}{g}$
w $b^2 - \frac{1}{2} = \frac{1}{2} \frac{\text{wLv}^2}{g}$

A ace online

 Regular Live Doubt clearing Sessions
 Free Online Test Series | ASK an expert

 Affordable Fee
 Available 1M |3M |6M |12M |18M and 24 Months Subscription Packages

Engineering Publications	31	Engineering Mechanics
$\therefore KE = \frac{1}{2}mV^{2} + \frac{1}{2}\left(\frac{5}{2}mR^{2}\right)\left(\frac{V}{2R}\right)^{2}$ $= \frac{1}{2}mV^{2} + \frac{5}{4}mR^{2} \times \frac{V^{2}}{4R^{2}}$ $= \frac{1}{2}mV^{2} + \frac{5}{16}mV^{2}$ $KE = \frac{13mV^{2}}{16}$ 10. Ans: (a) Sol: $\underbrace{0 \text{ Method I:}}_{1 \text{ kg}}$ By conservation of linear momentum, we get $\Rightarrow 1 \times 10 = (20 + 1) \times V_{em}$ (where, V_{em} = velocity of centre of mass) $\Rightarrow V_{em} = \frac{10}{21}m/s$ Applying angular momentum conservation about an axis passing through the contact point (A) and perpendicular to the plane of paper, we get $1 \times 10 \times 1 = I_{em}\omega + 21 \times \frac{10}{21} \times 1$ [Angular momentum about any axis passing through A can be written as $\vec{L}_{A} = \vec{L}_{em} + m(\vec{r} \times \vec{V}_{em})$] $\Rightarrow \omega = 0 \text{ rad/sec}$	g	<i>Method II</i> : Applying angular momentum conservation about an axis passing through centre of wheel and perpendicular to the plane of paper. $\therefore 0 = I_{cm} \omega$ $\Rightarrow \omega = 0 \text{ rad/sec}$ 11. Ans: (a) Sol: f_d $m_1 = m \rightarrow mass of bullet$ $m_2 = M \rightarrow mass of block$ $u_1 = V \rightarrow bullet initial velocity$ $u_2 = 0 \rightarrow block initial velocity$ $u_2 = 0 \rightarrow block initial velocity$ $v_1 = v_2 = v \rightarrow velocity of bullet and block after impact. F_d = \mu N(M+m)a = \mu(M+m)g\Rightarrow a = \mu gFrom momentum equationm_1u_1 + m_2u_2 = m_1v_1 + m_2v_2mV + m(0) = (m + M)Vv = \frac{mV}{m+M}Now from v^2-u^2 = 2as$
India's Best Online Coaching Platform	m for (GATE, ESE, PSUs, SSC-JE, RRB-JE, SSC, Banks, Groups & PSC Exams

A ace online Best Online Coaching Platform for GATE, ESE, PSUs, SSC-JE, RRB-JE, SSC, Banks, Groups & PSC Exams Enjoy a smooth online learning experience in various languages at your convenience

$$0 - \left(\frac{mV}{m+M}\right)^2 = 2\mu gs$$
$$V = \frac{m+M}{m}\sqrt{2\mu gs}$$

12. Ans: (a)

ACE

Sol:

k = 10.6 kN/mB=133.44 N ~~~~~~ A= 222.4 N 0.3 <u>m</u>

$$u_{A} = 0, \quad u_{B} = 0$$

From momentum equation
$$m_{A}u_{A} + m_{B}u_{B} = m_{A}v_{A} + m_{B}v_{B}$$
$$0 = 222.4V_{A} + 133.44V_{B} \qquad \dots \dots \dots (1)$$
$$\frac{1}{2}ks^{2} = \frac{1}{2}m_{A}v_{A}^{2} + \frac{1}{2}m_{B}v_{B}^{2}$$
$$10.6 \times 10^{3} \times 0.15^{2} = \frac{222.4}{9.81}v_{A}^{2} + \frac{133.44}{9.81}v_{B}^{2}$$
$$\dots \dots \dots (2)$$

From 1 & 2

$$v_A = -1.98 \text{ m/s}$$
,
 $v_B = 3.3 \text{ m/s}$

Chapter **Virtual Work** 8 01. Sol: 25 kN 25 kN A 2 m 2 m 3 m С D Let R_A & R_B be the reactions at support A & B respectively. Let δ_v displacement be given to the beam at 1) B without giving displacement at 'A'

The corresponding displacement at C & D are $\frac{2}{7}\delta_{y}$ and $\frac{4}{7}\delta_{y}$

By virtual work principle,

$$R_{A} \times 0 - 25 \times \frac{2}{7} \delta_{y} - 25 \times \frac{4}{7} \delta_{y} + R_{B} \times \delta_{y} = 0$$

$$\Rightarrow \left(\frac{-150}{7} + R_{B}\right) \delta_{y} = 0$$

Since $\delta_{y} \neq 0, R_{B} - \frac{150}{7} = 0$

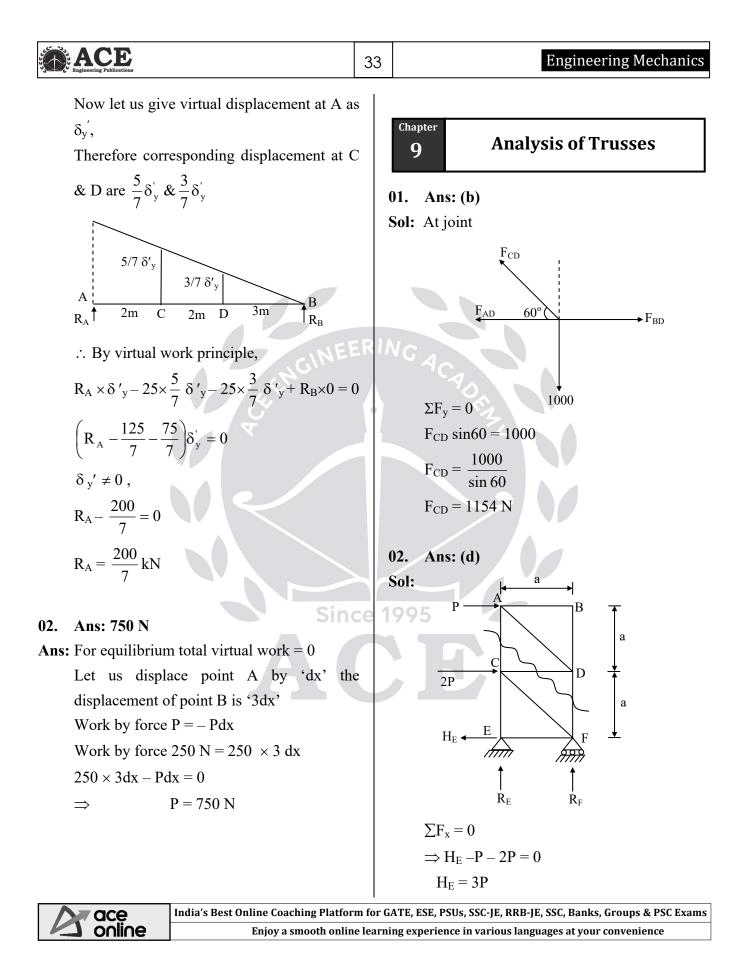
$$R_{\rm B} = \frac{150}{7} kN$$

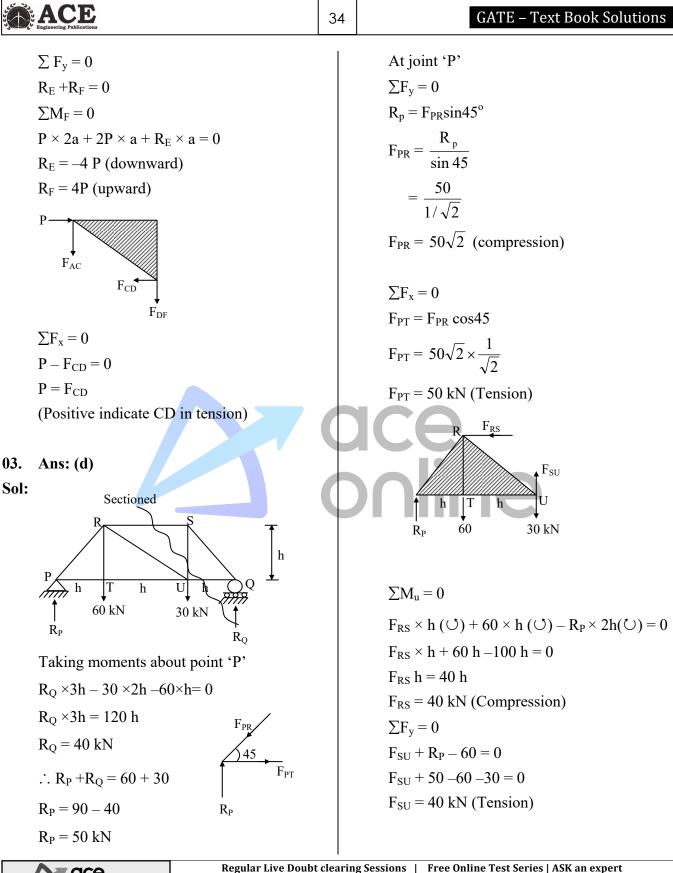
ace online

Regular Live Doubt clearing Sessions | Free Online Test Series | ASK an expert Affordable Fee | Available 1M |3M |6M |12M |18M and 24 Months Subscription Packages

32

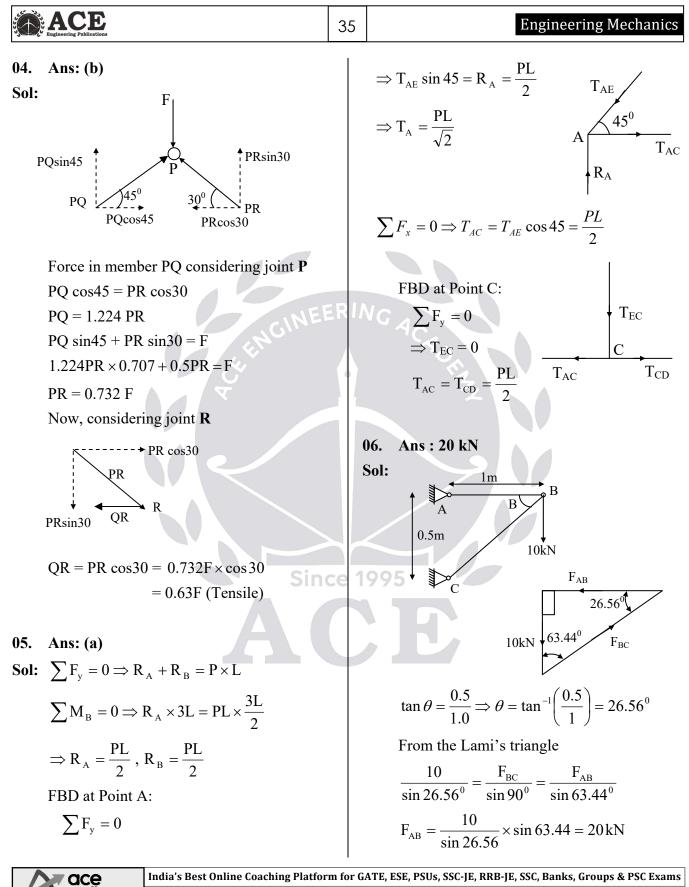
₽





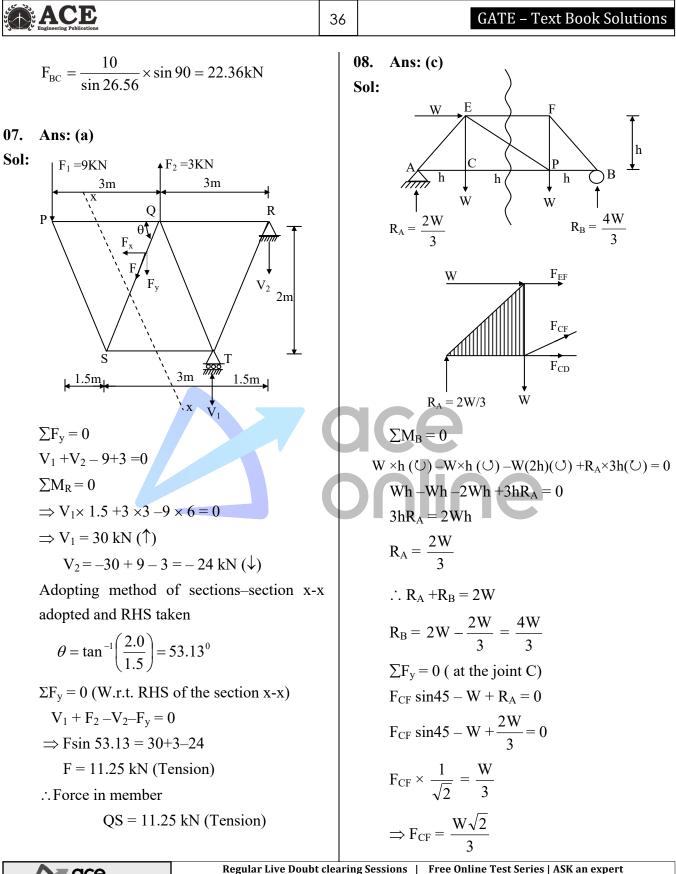


Affordable Fee | Available 1M |3M |6M |12M |18M and 24 Months Subscription Packages



Online Enjoy a

Enjoy a smooth online learning experience in various languages at your convenience



A ace online

Affordable Fee | Available 1M |3M |6M |12M |18M and 24 Months Subscription Packages

	ACE Engineering Publications	37	Engineering Mechanics
09. Sol:	Ans: (c) $R_{HA} \rightarrow A_{VA} \rightarrow $		Chapter 10Power Screw, Belt drive, Lagrange's equationPower Screw
	$\Sigma M_{A} = 0$ $5 \times 3 (\bigcirc) + 5 \times 6 (\bigcirc) - R_{HB} \times 3 = 0$ $15 + 30 = R_{H} \times 3$ $R_{HB} = \frac{45}{3}$	ER I A	 Ans: (b) Sol: The best threads for a power screw are ball bearing threads. Ans: (b) Sol: ACME threads :
	$R_{\rm HB} = 15 \text{ kN}$ $\Sigma F_{\rm X} = 0$		 Acme threads can be used to take a load in both directions. They are strong, smooth have less wear, and easy to manufacture compared to
	$\therefore R_{HA} + R_{HB} = 0$ $R_{HA} = -R_{HB}$ $R_{HA} = -15 \text{ kN}$ (Negative indicate R_{HA} is left side)		 and easy to manufacture compared to square thread. Square thread : In this thread, the flanks are perpendicular to the axis of the thread.
	At joint 'B' R_{HB} F_{AB} F_{BD} $\Sigma F_{x} = 0$	ce 1	• This is used for transmitting motion or power, E.g. Fly presses, Screw jack, vice handles, cross-slide and compound slide, etc.
	$\Sigma F_{\rm BD} = 15 \text{ kN}$ $\Sigma F_{\rm y} = 0$ $F_{\rm AB} = 0$		 The efficiency of a square thread is more than that of trapezoidal threads. It can transmit load and power in both directions but It is difficult to
	India's Best Online Coaching Platfor	rm for G4	 manufacture. There is no radial or side thrust on the nut. The wear on the thread is also a serious problem.



Enjoy a smooth online learning experience in various languages at your convenience

38

03. Ans: (b)

Sol: Screw is subjected to torque, axial compressive load and bending moment also, sometimes.

Screws are generally made of C30 or C40 steel. As the failure of power screws may lead to serious accident, higher factor of safety of 3 to 5 is taken. Threads may fail due to shear, which can be avoided by using nut of sufficient height. Wear is another possible mode of thread failure as the threads of nut and bolt rub against each other. Nuts are made of softer material than screws so that if at all the failure takes place, nut fails and not the screw, which is the costlier member and is also difficult to replace. Plastic, bronze or copper alloys are used for manufacturing nuts. Plastic is used for low load applications and has good friction and wear properties. Bronze and copper alloys are used for high load applications.

Therefore it is essential to design a power screw for maximum shear stress.

04. Ans: (b)

Sol: Under direct compressive stress,

$$d_{c} = \sqrt{\frac{4W}{\pi\sigma_{c}}}$$

Under wear consideration, $d_c = \sqrt{\frac{2W}{P_b \psi \pi}}$

05. Ans: (c)

Sol: Self locking screw:

If friction angle, $\phi \ge$ helix angle, α Screw is self locking.

i.e., torque required to lower the load is positive.

If $\phi < \alpha$, The screw is over hauling

i.e., torque required to lower the load is negative

For self locking screw,

 $tan \phi > tan \alpha$

$$\mu > \frac{L}{\pi d_{m}}$$

06. Ans: (c)

Sol:

A multi-start thread may be used to get larger value of linear displacement per revolution
A differential screw may be used to get a very small value of linear displacement per revolution.

07. Ans: (c)

Sol:

- A multi-start thread may be used to get larger value of linear displacement per revolution with no guarantee of self locking.
- Multi-start threads are used for transmitting power and generating movement. Because each partial or complete revolution equals more linear travel based on the number of threads, multi-threaded components can

 OCE
 Regular Live Doubt clearing Sessions
 Free Online Test Series | ASK an expert

 Affordable Fee | Available 1M |3M |6M |12M |18M and 24 Months Subscription Packages

ACE Engineering Publications

efficiently handle more power. Multi-start threads can also be used for some fastening purposes.

08. Ans: (b)

Sol:

- Multi-start threads are used for transmitting power and generating movement. Because each partial or complete revolution equals more linear travel based on the number of threads, multi-threaded components can efficiently handle more power. Multi-start threads can also be used for some fastening purposes.
- Hence they secure high efficiency.
- 09. Ans: (d)
- Sol: Square thread,

 $\eta = \frac{\text{work output}}{\text{work input}}$

During one revolution of screw

Work input = $P \times \pi d_m$

Work output = WL

$$\eta = \frac{WL}{P\pi d_{m}} = \frac{W \tan \alpha}{P} \quad [\because \tan \alpha = \frac{L}{\pi d_{m}}]$$
$$\eta = \frac{\text{ideal effort (No friction)}}{\Pi = \frac{WL}{R}}$$

$$\eta = \frac{W \tan \alpha}{W \tan(\phi + \alpha)} = \frac{\tan \alpha}{\tan(\phi + \alpha)}$$

Belt Drives & Wedge

01. Ans: (d)
Sol:
$$P = \frac{(T_1 - T_2)V}{1000}$$
 - Flat belt
 $V =$ belt (or) rope drive
 $T_1 \& T_2 =$ Tensions in high and slack side,
 $V = m/sec$, $P = kW$
 $\frac{T_1}{T_2} = e^{\mu\theta}$

02. Ans: (c)

Sol: Condition for maximum power transmitted

(i)
$$T_{c} = \frac{T_{max}}{3}$$

(ii)
$$T_{1} = \frac{2T_{max}}{3}$$

(iii)
$$V = \sqrt{\frac{T_{max}}{3}}$$

03. Ans: (b)

Since

Sol: All the stresses produced in a belt are tensile stresses.

04. Ans: (c)

Sol: Power = $(T_1 - T_2) V$

Due to centrifugal tension,

Total Tension (safe tension):

Total tension on tight side, $T_{t1} = T_1 + T_C$ Total tension on slack side, $T_{t2} = T_2 + T_C$

$$T_{t1} - T_{t2} = T_1 - T$$

Therefore the centrifugal tension has no effect on power transmission.



India's Best Online Coaching Platform for GATE, ESE, PSUs, SSC-JE, RRB-JE, SSC, Banks, Groups & PSC Exams Enjoy a smooth online learning experience in various languages at your convenience

Engineering Mechanics

Ans: (a)

05.

ACE

Sol: A V-belt marked A-914-50 denotes a standard belt of inside length 914 mm and a pitch length 950 mm.

> A belt marked A-914-52 denotes an oversize belt by an amount of (52 - 50) = 2units of grade number.

06. Ans: (a)

Sol:

- Wire ropes make contact at the bottom of the groove of the pulley.
- V-Belt makes contact at the sides of the groove of the pulley.

07. Ans: (c)

Sol: Let, D = diameter of the pitch circle

T = number of teeth on the sprocket

$$p = D \sin\left(\frac{\theta}{2}\right)$$

We know that, $\theta = \frac{360^{\circ}}{T}$

$$p = D \sin\left(\frac{360^{\circ}}{2T}\right) = D \sin\left(\frac{180^{\circ}}{T}\right)$$

or
$$D = p \cos ec\left(\frac{180^{\circ}}{T}\right)$$

08. Ans: (c)

Sol:
$$\frac{T_1}{T_2} = e^{\frac{\mu\theta}{\sin \theta}}$$

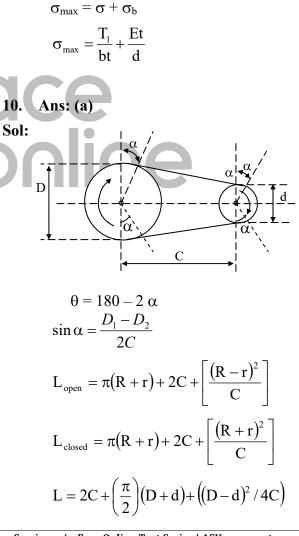
ace online

Regular Live Doubt clearing Sessions | Free Online Test Series | ASK an expert Affordable Fee | Available 1M |3M |6M |12M |18M and 24 Months Subscription Packages

09. Ans: (c)

tension, $\sigma = \frac{T_1}{ht}$

 $\sigma_{\rm b} = \frac{{\rm E} t}{d}$



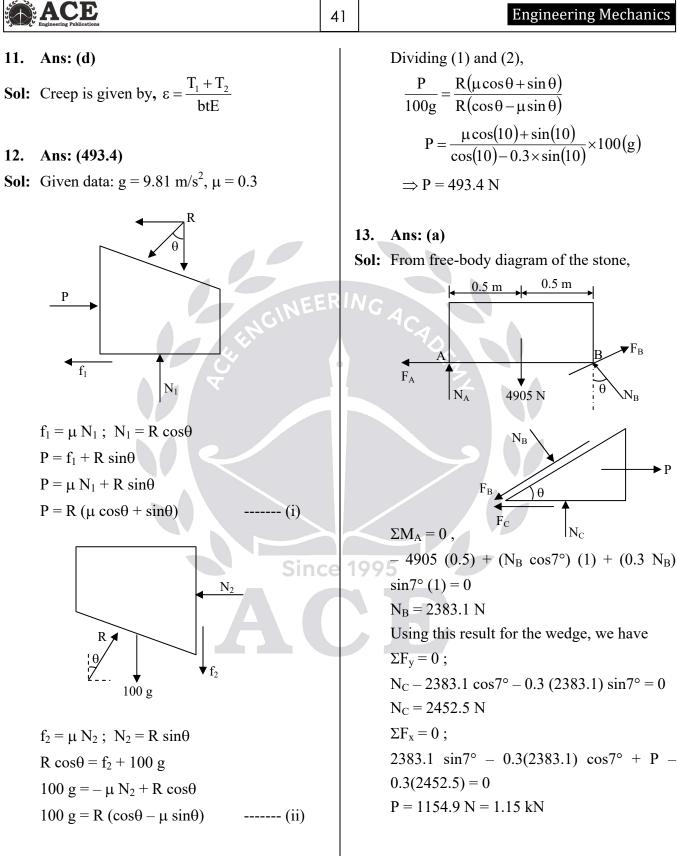
Due to bending maximum tensile stress

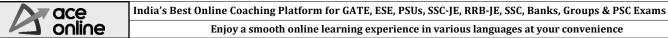
 $\frac{\sigma_{\rm b}}{\rm v} = \frac{\rm E}{\rm r} \qquad \qquad \left| {\rm r} = \frac{\rm d}{\rm 2} \; ; \; {\rm y} = \frac{\rm t}{\rm 2} \right|$

Total maximum stress induced in belt,

occurs on small pulley side 'd'

GATE – Text Book Solutions





Engineering Publications	42	GATE – Text Book Solutions
LAGRANGE'S EQUATION	ı.	$= \frac{m}{2b} \int_{0}^{b} \left\{ \dot{x}^{2} \times b + \dot{\theta}^{2} \times \frac{b^{3}}{3} + \dot{x} \times \dot{\theta} \times \cos \theta \times b^{2} \right\}$
01. Ans: (c)	-	$=\frac{1}{2}m\dot{x}^{2}+\frac{1}{6}m.\dot{\theta}^{2}\times b^{2}+\frac{1}{2}\times m.\dot{x}.\dot{\theta}\times \cos\theta\times b$
Sol: (i) PE of spring $=\frac{1}{2}k.x^2$		P.E of rod = $-\frac{1}{2} \times m \times b \times \cos \theta \times g$ \therefore PE = PE of spring + PE of rod
(ii) K.E of block = $\frac{1}{2} \times M \times x^2$		$PE = \frac{1}{2}k.x^{2} + \left\{-\frac{1}{2} \times m \times g \times b \times \cos\theta\right\}$
(iii) KE of rod:		KE = KE of block + KE of rod
Mass of element, $dm = m \times \frac{dy}{b}$		$KE = \frac{1}{2} \times M \times \dot{x}^{2} + \frac{1}{2}m\dot{x}^{2} + \frac{1}{6}m \times \dot{\theta}^{2} \times b^{2}$
$\mathrm{KE} = \frac{1}{2} \mathrm{dm} \times \mathrm{v}^2 = \frac{1}{2} \times \mathrm{dm} \times \left\{ \mathrm{v}_{\mathrm{x}}^2 + \mathrm{v}_{\mathrm{y}}^2 \right\}$		$+\frac{1}{2} \times \mathbf{m} \times \dot{\mathbf{x}} \times \dot{\mathbf{\theta}} \times \cos \mathbf{\theta} \times \mathbf{b}$
$v_{x} = \dot{x}_{1} = \frac{d}{dt} \{ x_{1} \} = \frac{d}{dt} \{ x + y \sin \theta \}$ $\therefore v_{x} = \dot{x} + y \times \cos \theta \times \dot{\theta}$	C	$\therefore \text{ Lagrange, } L = \text{KE} - \text{PE}$ $= \frac{1}{2} \{m + M\} \times \dot{x}^2 + \frac{1}{6} m \times \dot{\theta}^2 \times b^2 + \frac{1}{2} \times m \times \dot{x}$
$v_y = \frac{d}{dt}(y_1) = \frac{d}{dt}(y\cos\theta) = -y\sin\theta \times \dot{\theta}$	C	$\dot{\theta} \times \cos \theta \times b - \frac{1}{2}k.x^2 + \frac{1}{2} \times m \times b \times \cos \theta \times g$
$\therefore \text{ KE of rod} = \int \frac{1}{2} \cdot d\mathbf{m} \times \mathbf{v}^2$		
$= \int \frac{1}{2} \times \mathbf{m} \times \frac{dy}{b} \times \left\{ \left(\dot{\mathbf{x}} + \mathbf{y} \cos \theta \times \dot{\theta} \right)^2 + \left(-y \sin \theta \times \dot{\theta} \right)^2 \right\}$	}	
$=\frac{m}{2b}\int_{0}^{b}\left\{\dot{x}^{2}+y^{2}\times\dot{\theta}^{2}+2\times\dot{x}\times y\times\dot{\theta}\times\cos\theta\right\}dy$		

	Regular Live Doubt clearing Sessions Free Online Test Series ASK an expert		
	Affordable Fee Available 1M 3M 6M 12M 18M and 24 Months Subscription Packages		