

GATE - 2021

Questions Outions



CIVIL ENGINEERING (Afternoon Session)

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GATE - 2021 CIVIL ENGINEERING

06/02/21 Afternoon Session

Questions with Detailed Solutions

SUBJECTWISE WEIGHTAGE

S. No.	NAME OF THE SUBJECT	Number of Questions			
01	Engineering Mechanics	2			
02	Strength of Material	4			
03	Structural Analysis	3			
04	Construction Materials	2			
05	Construction Planning & Management	3			
06	Reinforced Cement Concrete	1			
07	Design of Steel Structures	-			
08	Geo-technical Engineering	8			
09	Fluid Mechanics & Hydraulic Machines	5			
10	Hydrology	2			
11	Irrigation Engineering	1			
12	Environmental Engineering	7			
13	Transportation Engineering	6			
14	Geomatics Engineering (Surveying)	2			
15	Engineering Mathematics	9			
16	Verbal Ability	2			
17	Numerical Ability	8			
Total No. of Questions 65					

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2

Section : General Aptitude

01. Four persons P, Q, R and S are to be seated in a row. R should not be seated at the second position from the left end of the row. The number of distinct seating arrangements possible is:

(a)	24		(b)	18

(c) 9(d) 6

01. Ans: (b)

Sol: (3!) 3 = 18 chances

(:: 'R' should not be seated at second position from the left end)

 $(, \underline{(R)}, ,)$ ×

- 02. (i) Arun and Aparna are here.
 - (ii) Arun and Aparna is here.
 - (iii) Arun's families is here.
 - (iv) Arun's family is here.

Which of the above sentences are grammatically CORRECT?

(d) (i) and (iv)

- (b) (i) and (ii) (a) (ii) and (iv)
- (c) (iii) and (iv)

02. Ans: (d)

Sol: When two or more singular nouns joined by 'and' the verb should be plural. Singular subject takes singular verb.

03. \oplus and \odot are two operators on numbers p and q such that

 $p \odot q = p - q$, and $p \oplus q = p \times q$ Then, $(9 \odot (6 \oplus 7)) \odot (7 \oplus (6 \odot 5)) =$ (b) -26 (a) 40 (c) - 33(d) - 40

03. Ans: (d)

Sol:
$$p \odot q = p - q$$

 $p \oplus q = p \times q$
Then, $(9 \odot (6 \oplus 7)) \odot (7 \oplus (6 \odot 5))$
 $\Rightarrow (9 - (6 \times 7)) - (7 \times (6 - 5))$
 $= 9 - 42 - 7$
 $= -40$

04.



In the figure shown above, PQRS is a square. The shaded portion is formed by the intersection of sectors of circles with radius equal to the side of the square and centers at S and Q.

The probability that any point picked randomly within the square falls in the shaded area is -----

(a)
$$\frac{\pi}{4}$$
 (b) $\frac{1}{2}$
(c) $4 - \frac{\pi}{2}$ (d) $\frac{\pi}{2} - 1$

Since 199

(a) $\frac{\pi}{4}$

Sol: Area of Shaded region from the figure is $\frac{\pi r^2}{4}$



Area of shaded region from the figure is $r^2 - \frac{\pi r^2}{4}$ Area of shaded part in the question



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* Lectures



$$= r^2 - 2\left(r^2 - \frac{\pi r^2}{4}\right)$$

 $=\frac{\pi r^2}{2}-r^2$

Required probability = $\frac{\frac{\pi r^2}{2} - r^2}{r^2} = \frac{\pi}{2} - 1$

05. On a planar field, you travelled 3 units East from a point O. Next you travelled 4 units South to arrive at point P. Then you travelled from P in the North-East direction such that you arrive at a point that is 6 units East of point O. Next, you travelled in the North-West direction, so that you arrive at point Q that is 8 units North of point P.

The distance of point Q to point O, in the same units, should be _____

(b) 3

(d) 6

(a) 4 (c) 5

05. Ans: (c) Sol:



06. 1. Some football players play cricket.

2. All cricket players play hockey.

Among the options given below, the statement that logically follows from the two statements 1 and 2 above, is:

- (a) No football player plays hockey.
- (b) All hockey players play football.
- (c) All football players play hockey.
- (d) Some football players play hockey.

06. Ans: (d)

Sol: Some foot ball players play cricket All cricket players play hockey



Some football players play hockey is satisfied.

07. The author said. "Musicians rehearse before their concerts. Actors rehearse their roles before the opening of a new play. On the other hand, I find it strange that many public speakers think they can just walk on to the stage and start speaking. In my opinion, it is no less important for public speakers to rehearse their talks."

Based on the above passage, which one of the following is TRUE?

- (a) The author is of the opinion that rehearsal is more important for actors than musicians.
- (b) The author is of the opinion that rehearsing is important for musicians, actors and public speakers.

4

Sol:

Civil Engineering

- (c) The author is of the opinion that rehearsing is less important for public speakers than for musicians and actors.
- (d) The author is of the opinion that rehearsing is more important only for musicians than public speakers.

07. Ans: (b)

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- **Sol:** The author states musicians rehearse, actors rehearse and likewise he states public speakers also should rehearse and this is stated in option (b).
- 08. Two identical cube shaped dice each with faces numbered 1 to 6 are rolled simultaneously. The probability that an even number is rolled out on each dice

(a)
$$\frac{1}{36}$$
 (b) $\frac{1}{8}$ (c) $\frac{1}{4}$ (d) $\frac{1}{12}$

08. Ans: (c)

- **Sol:** The even numbers on the dice are 2, 4, 6
 - The probability of even number on a dice = $\frac{3}{6}$... The probability that an even number is rolled out on each dice is $\frac{3}{6} \times \frac{3}{6} = \frac{1}{4}$



09. In an equilateral triangle PQR, side PQ is divided into four equal parts, side QR is divided into six equal parts and side PR is divided into eight equal parts. The length of each subdivided part in cm is an integer.

The minimum area of the triangle PQR possible, in cm, is

- (b) $48\sqrt{3}$ (a) 24
- (c) $144\sqrt{3}$ (d) 18

The mirror image of the above text about the X-axis is

PHYLAXIS SIXAJYHd GHYLAN ΡΗΥΓΑΧΙΣ





Minimum area of triangle = L.C.M of (4,6,8) = 24







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* All Subjects Launching Soon!

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03.	Ans: 57	
Sol:	$D^o = 2^o$	
	$V_{max} = 100 \text{ kmph}$ $e_d = ?$	
	$V_{equ} = 80 \text{ kmph}$	
	G = 1750 mm	
	$D^{\circ} = \frac{1750}{R} (30.5 \text{ m})$	
	$D^{\circ} = \frac{1750}{R}$	
	$\Rightarrow R = \frac{1750}{2} = 875 \text{ m}$	
	Considering V_{max} , $e_{the} = \frac{GV_{max}^2}{127R}$	
	$=\frac{1.750 \times 100^2}{100} = 157480$ mm	
	Considering V_{equ} 127 × 875 137.100 min	
	$e_{equ} = \frac{GV_{equ}^{2}}{127R} = \frac{1.750 \times 80^{2}}{127 \times 875}$	
	= 100.787 mm	
	$e_{max} = \frac{1}{10}G$	
	10	
	$=\frac{1}{10}(1750 \text{ mm}) = 175.0 \text{ mm}$	
	$\therefore \mathbf{e}_{\text{actual}} = \mathbf{e}_{\text{equ}} = 100.787 \text{ mm}$	
	$e_{tha} = 157.480 \text{ mm}$	
	$e_{am} = 100.787 \text{ mm}$	
	$\therefore e_d$ in field = 157.480 - 100.787 = 56.693 mm	
	Maximum allowable e_{d} for BG = 75 mm	
	$\therefore e_1 = 56.693 \simeq 57 \text{ mm} \text{ is allowable}$ Since	2

04. In an aggregate mix, the proportions of coarse aggregate, fine aggregate and mineral filler are 55%, 40% and 5%, respectively. The values of bulk specific gravity of the coarse aggregate, fine aggregate and mineral filler are 2.55. 2.65 and 2.70, respectively. The bulk specific gravity of the aggregate mix (round off to two decimal places) is

04. Ans: 2.6

Sol: The proportion of mix is Coarse aggregate = 55%Fine aggregate = 40%

Mineral filler = 5%Given Specific gravities are Coarse aggregate, $SG_1 = 2.55$ Fine aggregate, $SG_2 = 2.65$ Mineral filler, $SG_2 = 2.70$ Bulk Specific gravity

$$= \frac{X\% \times SG_1 + Y\% \times SG_2 + Z\% \times SG_3}{100}$$
$$= \frac{55\% \times 2.55 + 40\% \times 2.65 + 5\% \times 2.7}{100}$$
$$= 2.5975$$
$$\cong 2.6$$

05. In a three-phase signal system design for a four-leg intersection, the critical flow ratios for each phase are 0.18, 0.32, and 0.22. The total loss time in each of the phases is 2 s. As per Webster's formula, the optimal cycle length (in s, round off to the nearest integer) is

05. Ans: 50

- Sol: Three phase signal system $y_1 = 0.18$ $y_2 = 0.32$; $y_3 = 0.22$ Lost time per phase = $2 \sec 2$ Lost time per cycle = $2 \times 3 = 6$ sec $y = y_1 + y_2 + y_3 = 0.18 + 0.32 + 0.22 = 0.72$ Cycle time as per Webster is $C_{\circ} = \frac{1.5 \times L + 5}{1 - y} = \frac{1.5 \times 6 + 5}{1 - 0.72} = 50 \text{ sec}$
- 06. The most appropriate triaxial test to assess the longterm stability of an excavated clay slope is (a) unconsolidated undrained test

 - (b) consolidated drained test
 - (c) unconfined compression test
 - (d) consolidated undrained test

06. Ans: (b)

Sol: To assess the long term stability of clayey soil, the results of consolidated drained (CD) test are used.

6

	7	GATE_2021_Questions with Solutions
 07. A rectangular open channel of 6 m width is car a discharge of 20 m³/s. Consider the acceler due to gravity as 9.81 m/s² and assume wat incompressible and inviscid. The depth of in the channel at which the specific energy of flowing water is minimum for the given disclwill then be (a) 3.18 m (b) 0.82 m (c) 1.04 m (d) 2.56 m 	rying 09 ration fer as flow of the harge	 9. A frame EFG is shown in the figure. All members are prismatic and have equal flexural rigidity. The member FG carries a uniformly distributed load w per unit length. Axial deformation of any member is neglected.
07. Ans: (c) Sol: Rectangle, B = 6 m $Q = 20 \text{ m}^3/\text{s}$ $g = 9.81 \text{ m/s}^2$ $\therefore q = \frac{Q}{B} = \frac{20}{6} = 3.33 \text{ m}^2/\text{s}$ Specific energy is minimum at critical flow depth should be critical depth, $y_c = \left(\frac{q^2}{g}\right)^{1/3}$ $y_c = \left(\frac{3.33^2}{9.81}\right)^{1/3} = 1.04 \text{ m}$	EERIM v, so,	2L E Considering the joint F being rigid, the support reaction at G is (a) 0.375 wL (b) 0.453 wL (c) 0.482 wL (d) 0.500 wL
08. A lake has a maximum depth of 60 m. If the atmospheric pressure in the lake region is 91 and the unit weight of the lake water is 979 m ³ , the absolute pressure (in kPa, round off to decimal places) at the maximum depth of the late	mean S I kPa 20 N/ 5 two ake is	ol: x x x x x x x x
08. Ans: 678.4 Sol: \square \square $h = 60 \text{ m}$	C	E Sagging +ve Hogging -ve $M_{x-x} = Rx - \frac{Wx^2}{2}$
$\gamma_{water} = 9790 \text{ N/m}^3$ $P_{atm} = 91 \text{ kPa} \qquad (P_{\Delta})_{abs} = ?$ $P = P_{atm} + \gamma h$ $= 91 \times 10^3 + 9790 \times 60 = 678.4 \text{ kPa}$		$M_{x-x} = RL - \frac{wL^2}{2}$ Compatibility condition $\frac{\partial U}{\partial R} = 0$

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Strain energy (U) =
$$\int_{0}^{t} \frac{M_{x}^{2}}{2EI} dx$$

$$\frac{\partial}{\partial R} \left[\int \frac{M_{x}^{2}}{2EI} dx \right] = 0$$

$$\frac{\partial}{\partial R} \left[\int_{0}^{t} \frac{\left(Rx - \frac{wx^{2}}{2}\right)^{2}}{2EI} dx + \int_{0}^{2L} \frac{\left(RL - \frac{wL^{2}}{2}\right)^{2}}{2EI} dx \right] = 0$$

$$\int_{0}^{L} \frac{2\left(Rx - \frac{wx^{2}}{2}\right)}{2EI} \times x dx + \int_{0}^{2L} \frac{2\left(RL - \frac{wL^{2}}{2}\right)}{2EI} dx = 0$$

$$\int_{0}^{L} \frac{2\left(Rx^{2} - \frac{wx^{3}}{2}\right)}{EI} \times dx + \int_{0}^{2L} \frac{\left(RL^{2} - \frac{wL^{3}}{2}\right)}{EI} = 0$$

$$\frac{RL^{3}}{3} - \frac{W}{2} \times \frac{L^{4}}{4} + RL^{2}(2L) - \frac{wL^{3}}{2}(2L) = 0$$

$$\frac{RL^{3}}{3} - \frac{wL^{4}}{8} + 2RL^{3} - wL^{4} = 0$$

$$\frac{7RL^{3}}{3} = \frac{9}{8}wL^{4}$$

$$R = \frac{27}{56}wL$$

$$R = 0.482 wL$$

10. The smallest eigenvalue and the corresponding eigenvector of the matrix $\begin{bmatrix} 2 & -2 \\ -1 & 6 \end{bmatrix}$, respectively, are are
(a) 2.00 and $\begin{cases} 1.00 \\ 1.00 \end{cases}$ (b) 1.55 and $\begin{cases} 2.00 \\ 0.45 \end{cases}$ (c) 1.55 and $\begin{cases} -2.55 \\ -0.45 \end{cases}$ (d) 1.55 and $\begin{cases} 2.00 \\ -0.45 \end{cases}$

10. Ans: (b)

10. Ans: (b) Sol: Characteristic equation = $\begin{vmatrix} 2-\lambda & -2 \\ -1 & 6-\lambda \end{vmatrix} = 0$

$$(2 - \lambda) (6 - \lambda) - 2 = 0$$

$$\lambda^2 - 8\lambda + 12 - 2 = 0 \Longrightarrow \lambda^2 - 8 \lambda + 10 = 0$$

$$\lambda = \frac{8 \pm \sqrt{64 - 40}}{2} = \frac{8 \pm \sqrt{24}}{2} = 4 \pm \sqrt{6}$$

Smallest eigen value = $4 - \sqrt{6} = 1.5505$ Consider $(A - \lambda I) X = 0$ $\Rightarrow \begin{bmatrix} 2-\lambda & -2\\ -1 & 6-\lambda \end{bmatrix} \begin{bmatrix} \mathbf{x}_1\\ \mathbf{x}_2 \end{bmatrix} = \begin{bmatrix} 0\\ 0 \end{bmatrix}$

$$\Rightarrow \begin{pmatrix} 2 - (4 - \sqrt{6}) & -2 \\ -1 & 6 - (4 - \sqrt{6}) \end{pmatrix} \begin{pmatrix} x_1 \\ x_2 \end{pmatrix} = \begin{pmatrix} 0 \\ 0 \end{pmatrix} \Rightarrow \begin{pmatrix} 2 + \sqrt{6} & -2 \\ -1 & 2 + \sqrt{6} \end{pmatrix} \begin{pmatrix} x_1 \\ x_2 \end{pmatrix} = \begin{pmatrix} 0 \\ 0 \end{pmatrix} \Rightarrow \begin{pmatrix} -(2 - \sqrt{6}) & -2 \\ 0 & 0 \end{pmatrix} \begin{pmatrix} x_1 \\ x_2 \end{pmatrix} = \begin{pmatrix} 0 \\ 0 \end{pmatrix} \Rightarrow -(2 - \sqrt{6}) x_1 + (-2) x_2 = 0 Let x_2 = K Then x_1 = \frac{2K}{-2 + \sqrt{6}} \therefore X_1 = \begin{bmatrix} \frac{2K}{-2 + \sqrt{6}} \\ -2 + \sqrt{6} \\ K \end{bmatrix} = K \begin{bmatrix} \frac{2}{-2 + \sqrt{6}} \\ 1 \end{bmatrix} = \begin{bmatrix} 2 + \sqrt{6} \\ 1 \end{bmatrix}$$
for K = 1
(or)
 X_1 = \begin{bmatrix} 2 \\ -2 + \sqrt{6} \\ 2 \\ -2 + \sqrt{6} \end{bmatrix} = \begin{bmatrix} 2 \\ 0.45 \end{bmatrix} for K = -2 + \sqrt{6}

Verification of options for eigen vectors closest option that matches is (b)

11. For a given traverse, latitudes and departures are calculated and it is found that sum of latitudes is equal to +2.1 m and the sum of departures is equal to -2.8 m.

The length and bearing of the closing error, 199 respectively, are

(a) 2.45 m and 53°7'48" NW

- (b) 3.50 m and 53°7'48" NW
- (c) 3.50 m and 53.13° SE
- (d) 0.35 m and 53.13° SE

11. Ans: (b)

8

Sol:
$$\Sigma L = +2.1 \text{ m}$$

 $\Sigma D = -2.8 \text{ m}$
 $e = \sqrt{\Sigma L^2 + \Sigma D^2}$
 $= \sqrt{(2.1)^2 + (-2.8)^2} = 3.5 \text{ m}$
 $\alpha = \tan^{-1} \left(\frac{\Sigma D}{\Sigma L}\right) = \text{N53.13}^{\circ} \text{W}$

Civil Engineering

UPCOMING BATCHES **a hyderabad**

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Batch Type	Timings	Batch Date	Duration	Venue & Streams	
Butten Type			Duration		
	Daily	2 nd & 17 th April 2021		Abide (CS&IT)	
Regular	4 to 6	1 st & 17 th May 2021	5 to 6 Months	Dilsukhnagar (EC, EE, IN) Kothapet (CE, ME, PI)	
	Hours	1 st & 17 th June 2021	Worlding		
	GAT	E + PSUs - 2022 (FLEXIB	LE BATCHES)		
Flexible	Daily	5 th , 20 th July 2021	3 to 4	Abids (CS&IT)	
Batches	6 to 8 Hours	4 th , 18 th August 2021	Months	Dilsukhnagar (EC, EE, IN) Kothapet (CE, ME, PI)	
	GA	TE + PSUs – 2022 (SPAR	K BATCHES)		
	Daily	17 th May 2021	5 to 6	Abids (CE, ME, CS)	
Spark	5 to 8 Hours	1 st & 17 th June 2021	Months	Kukatpally (EC, EE)	
	ESE + G	ATE + PSUs – 2022 (REG	ULAR BATCH	ES)	
		2 nd & 17 th April 2021			
Regular	Daily 6 to 8	1 st & 17 th May 2021	9 to 10	Kukatpally (EC, EE) Abids (CE, ME)	
	Hours	1 st & 17 th lune 2021	WORTHS		
		,, ,			
	ESE + GATE + PSUs – 2022 (SPARK BATCHES)				
	Daily	17 th May 2021	9 to 10	Kukatpally (EC, EE)	
Spark	6 to 8 Hours	1 st & 17 th June 2021	Months	Abids (CE, ME)	

+L N-W -D

A 12-hour unit hydrograph (of 1 cm excess rainfall) of a catchment is of a triangular shape with a base width of 144 hour and a peak discharge of 23 m³/s. The area of the catchment (in km², round off to the nearest integer) is _____



13. An elevated cylindrical water storage tank is shown in the figure. The tank has inner diameter of 1.5 m. It is supported on a solid steel circular column of diameter 75 mm and total height (L) of 4 m. Take, water density = 1000 kg/m^3 and acceleration due to gravity = 10 m/s^2

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If elastic modulus (E) of steel is 200 GPa, ignoring self-weight of the tank, for the supporting steel column to remain unbuckled, the maximum depth (h) of the water permissible (in m, round off to one decimal place) is _____

109 Ans: 2.7

Sol:

9



ک		10			Civil Engineering
	$P_{\rm cr} = \frac{\pi^2 EI}{\ell_{\rm e}^2} = \text{Buckling load} = \text{weight of water}$	1	5. Ans: (b) Sol: R ₂ (-) R ₄ , R	$_{3} \rightarrow R_{3} + R_{1}$	
$\pi^2 \times$	$\frac{\pi^{2} \text{EI}}{(2\ell)^{2}} = (\rho g h) \times \frac{\pi}{4} d_{i}^{2} = \rho g \times \text{volume of tank}$ $\frac{(200 \times 10^{9} \times \pi (75 \times 10^{-3})^{4})}{(2 \times 4)^{2} 64} = 1000 \times 10 \times h \times \frac{\pi}{4} \times 1.5^{2}$		$\begin{bmatrix} 5 & 0 & -5 & 0 \\ 0 & 1 & 0 & 2 \\ 0 & 0 & 0 & 0 \\ 0 & 2 & 0 & 1 \end{bmatrix}$		
	h = 2.7 m		$R_4 \rightarrow R_4 - 2F$	R ₁	
14.	A prismatic fixed-fixed beam, modelled with a total lumped-mass of 10 kg as a single degree of freedom (SDOF) system is shown in the figure.	1	$\begin{bmatrix} 5 & 0 & -5 & 0 \\ 0 & 1 & 0 & 2 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & -3 \end{bmatrix}$	3]	
	A B C E E E C E E C E E C E E C E E C E E C E E C E E E C E E C E E C E E C E E C E E C E E C E E E C E E E C E E E C E E E C E E E C E E E E C E E E C E E E E C E E E C E E E C E E E C E E E C E E E C E E E C E E E E C E E E E C E E E E C E	RIA	$ \begin{array}{c} R_3(-) R_4 \\ \begin{bmatrix} 5 & 0 & -5 & 0 \\ 0 & 1 & 0 & 2 \\ 0 & 0 & 0 & -3 \\ 0 & 0 & 0 & 0 \end{array} $		
	If the flexural stiffness of the beam is $4\pi^2$ kN/m, its natural frequency of vibration (in Hz, in integer) in the flexural mode will be	5	Rank = 3	l angle θ is n	neasured by four different
14. Sol:	Ans: 10 Civen Data:		surveyors n are given be	nultiple times clow.	s and the values reported
501:	$m = 10 \text{ kg}$ $K = 4\pi^2 \times 10^3$ Since	e 1	Surveyor	Angle θ	Number o Observations
	\rightarrow Natural frequency $f = \frac{1}{\sqrt{k}}$			36°30′	4
	\rightarrow reducing $r_n = 2\pi \cdot V m$		2	36°00′	3
	$=$ $\frac{1}{\sqrt{4\pi^2 \times 10^3}}$		3	35°30′	8

$$= \frac{1}{2\pi} \cdot \sqrt{\frac{4\pi^2 \times 10^3}{10}}$$
$$= \frac{2\pi \times 10}{2\pi} = 10$$

15. The rank of the matrix
$$\begin{bmatrix} 5 & 0 & -5 & 0 \\ 0 & 2 & 0 & 1 \\ -5 & 0 & 5 & 0 \\ 0 & 1 & 0 & 2 \end{bmatrix}$$
 is
(a) 2 (b) 3
(c) 4 (d) 1

The most probable value of the angle θ (in degree, round off to two decimal places) is _____

4

16. Ans: 36

4

Sol: Treating number of observations as weight

36°30'

Most probable value

$$= \frac{4 \times 36^{\circ} 30' + 3 \times 36^{\circ} + 8 \times 35^{\circ} 30' + 4 \times 36^{\circ} 30'}{4 + 3 + 8 + 4}$$

= 36°





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LAST DATE FOR ONLINE REGISTRATION 5th MARCH 2021



Exam Date : **7th March 2021** Timing: **11:00 AM**

No. of Questions: 50 25 Q: 1 Mark | 25 Q: 2 Mark Total : 75 Marks Duration : 90 Mins. Streams: EC | EE | ME | CE | CSIT | IN | PI





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GATE_2021_Questions with Solutions



- 19. The hardness of a water sample is measured directly by titration with 0.01 M solution of ethylenediamine tetraacetic acid (EDTA) using eriochrome black T (EBT) as an indicator. The EBT reacts and forms complexes with divalent metallic cations present in the water. During titration, the EDTA replaces the EBT in the complex. When the replacement of EBT is complete at the end point of the titration, the colour of the solution changes from
 - (a) wine red to blue
 - (b) reddish brown to pinkish yellow
 - (c) blue to colourless
 - (d) blue-green to reddish brown

19. Ans: (a)

Sol: Hardness end point of titration \rightarrow wine red to blue

20. An equipment has been purchased at an initial cost of ₹160000 and has an estimated salvage value of ₹10000. The equipment has an estimated life of 5 years. The difference between the book values (in ₹, in integer) obtained at the end of 4th year using straight line method and sum of years digit method of depreciation is ______

20. Ans: 20,000

Sol: Initial cost (P) = 1,60,000 Salvage value (SV) = 10,000 Useful life (n) = 5 years Straight Line Method: Annual depreciation (D) = $\frac{P-SV}{n}$ = $\frac{1,60,000-10,000}{5}$ = 30000 Book value after 4 years (BV₄) = P -4D = 1,60,000 - 4(30,000) = 40,000 SOY Method (Sum of years Digit)

SOY
$$=\frac{n(n+1)}{2} = \frac{5 \times 6}{2} = 15$$

$$d_{m} = \frac{n - (m - 1)}{SOY}$$

$$D_{m} = (P - SV) \times d_{m}$$

$$BV_{m} = BV_{m-1} - D_{m}$$

$$d_{1} = \frac{5 - (1 - 1)}{15} = \frac{5}{15}; D_{1} = (1,60,000 - 10000) \times \frac{5}{15}$$

$$= 50000$$

$$d_{2} = \frac{4}{15}; D_{2} = 40,000$$

$$d_{3} = \frac{3}{15}; D_{3} = 30,000$$

$$d_{4} = \frac{2}{15}; D_{5} = 10,000$$

$$BV_{0} = 1,60,000$$

$$BV_{1} = 1,60,000 - 50,000 = 1,10,000$$

$$BV_{2} = 1,10,000 - 40,000 = 70,000$$

$$BV_{3} = 70,000 - 30,000 = 40,000$$

$$BV_{4} = 40,000 - 20,000 = 20,000$$

$$BV_{5} = 20,000 - 10,000 = 10,000$$

$$Difference of Book value obtained in two methods = 40,000 - 20,000 = 20,000$$

21. A function is defined in Cartesian coordinate system as f (x, y) = xe^y. The value of the directional derivative of the function (in integer) at the point (2, 0) along the direction of the straight line segment from point (2. 0) to point (¹/₂, 2) is _____

21. Ans: (a)

Since

Sol:
$$\nabla f = \left(\frac{i\partial}{\partial x} + \frac{j\partial}{\partial y}\right) x e^y = e^y i + x e^y j$$

 $\nabla f |_{2,0} = i + 2j$

Vector along the direction of the straight line segment from (2,0) to $(\frac{1}{2},2)$ is given by $\overline{a} = (\frac{1}{2}-2)i + (2-0)j$

 $\overline{a} = \frac{-3}{2}i + 2j$ Unit vector along \overline{a} is $\frac{-3}{2}i + 2j}{\sqrt{\frac{9}{4} + 4}}$

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 $^3 \text{ m/s}$

The value of the directional derivative is

$$\nabla f. \frac{\overline{a}}{|\overline{a}|} = \frac{(i+2j) \cdot \left(-\frac{3}{2}i+2j\right)}{\frac{5}{2}}$$
$$= \frac{-\frac{3}{2}+4}{\frac{5}{2}} = \frac{5/2}{\frac{5}{2}} = 1$$

22. A water filtration unit is made of uniform-size sand particles of 0.4 mm diameter with a shape factor of 0.84 and specific gravity of 2.55. The depth of the filter bed is 0.70 m and the porosity is 0.35. The filter bed is to be expanded to a porosity of 0.65 by hydraulic backwash. If the terminal settling velocity of sand particles during backwash is 4.5 cm/s, the required backwash velocity is

(a)
$$0.75 \text{ cm/s}$$
 (b) 6.35×10^{-3}
(c) $5.79 \times 10^{-3} \text{ m/s}$ (d) 0.69 cm/s

22. Ans: (b)

- Sol: d = 0.4 mm Q = 0.84 s = 2.55 $v_s = 4.5 \text{ cm/sec}$ $ROB v_b = ?$ $v_b = v_s [n_e]^{4.5} = 4.5 \times 10^{-2} \times [0.65]^{4.5}$ = 0.00647 m/sec $= 6.47 \times 10^{-3} \text{ m/sec}$
- 23. The ratio of the momentum correction factor to the energy correction factor for a laminar flow in a pipe is

(a) $\frac{3}{2}$	(b) 1
(c) $\frac{2}{3}$	(d) $\frac{1}{2}$

(c) $\frac{2}{3}$ 23. Ans: (c)

Sol: For Laminar flow,

Kinetic Energy correction factor, $(\alpha) = 2$ Momentum correction factor, $(\beta) = \frac{4}{3}$ $\therefore \frac{\beta}{\alpha} = \frac{4/3}{2} = \frac{2}{3}$ 24. Relationship between traffic speed and density is described using a negatively sloped straight line. If $v_{\rm f}$ is the free-flow speed then the speed at which the maximum flow occurs is

(a)
$$\frac{v_{\rm f}}{4}$$
 (b) 0 (c) $\frac{v_{\rm f}}{2}$ (d) $v_{\rm f}$

24. Ans: (c)

- **Sol:** Given Speed density relation is linear maximum flow occurs at $\frac{v_i}{2}$ as per Greenshield's model.
- 25. As per the Unified Soil Classification System (USCS), the type of soil represented by 'MH' is
 - (a) Inorganic silts of high plasticity with liquid limit more than 50%
 - (b) Inorganic clays of high plasticity with liquid limit less than 50%
 - (c) Inorganic clays of low plasticity with liquid limit more than 50%
 - (d) Inorganic silts of low plasticity with liquid limit less than 50%

25. Ans: (a)

Sol: MH: Inorganic silt of high plasticity with $w_L > 50\%$

26. A perfectly flexible and inextensible cable is shown in the figure (not to scale). The external loads at F and G are acting vertically.



The magnitude of tension in the cable segment FG (in kN, round off to two decimal places) is ——

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26. Ans:8.246



 $\Sigma M_{\rm F} = 0 \quad \downarrow -ve \quad \downarrow +ve$ [Left part]

$$\left(10.667 + \frac{H}{6}\right)2 - H \times 3 =$$

H = 8 kN $V_{\rm E} = 10.667 + \frac{8}{6}$ $V_{E} = 12 \text{ kN}$ $V_{II} = 10 \text{ kN}$ Consider left hand side of section (1) - (1)

 $\Sigma H = 0$

 $T \cos \theta = H$

 $T \cos \theta = 8$ $T \sin \theta = 2$

 $\therefore T^2 \cos^2 \theta + T^2 \sin^2 \alpha = 8^2 + 2^2$

T = 8.246 kN

Tension in segment GF is 8.246 kN

27. The unit normal vector to the surface $X^2 + Y^2 + Z^2$ -48 = 0 at the point (4, 4, 4) is



27. Ans: (a)

Sol: The unit normal vector to the sphere $X^2 + Y^2 + Z^2 =$ r^2 at a point (x_1, y_1, z_1) is given by

$$=\frac{\mathbf{x}_{i}\mathbf{i}+\mathbf{y}_{1}\mathbf{j}+\mathbf{z}_{1}\mathbf{k}}{\sqrt{48}}$$
$$=\frac{4\mathbf{i}+4\mathbf{j}+4\mathbf{k}}{\sqrt{48}}=\frac{\mathbf{i}+\mathbf{j}+\mathbf{k}}{\sqrt{3}}$$

- 28. In case of bids in Two-Envelop system, the correct option is
 - (a) Technical bid is opened first
 - (b) Either of the two (Technical and Financial)
 - bids can be opened first
 - (c) Financial bid is opened first
 - (d) Both (Technical and Financial) bids are opened simultaneously

28. Ans: (a)

Since

Sol: Option 1 technical bid is opened first **Opening of Tender**

> First technical bid is opened and after ensuring that all the technical aspects of a contractor are in order than only financial bid is opened

- Envelope 1 (Technical bid) þ
 - Cover letter
- 2. **Registration Details**
- 3. Pre-qualification documents
- 4. Earnest money deposit
- 5. Assumptions & Deviations in making of tender
- 6. Drawings
- 2. Envelope 2 (Financial Bid)
- Forms of tender 1.
- 29. An activated sludge process (ASP) is designed for secondary treatment of 7500 m³/day of municipal wastewater. After primary clarifier, the ultimate BOD of the influent, which enters into ASP reactor is 200 mg/L. Treated effluent after secondary clarifier is required to have an ultimate BOD of

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	15	GATE_2021_Questions with Solutions
20 mg/L. Mix liquor volatile suspended solids (MLVSS) concentration in the reactor and the underflow is maintained as 3000 mg/L and 12000 mg/L, respectively. The hydraulic retention time and mean cell residence time are 0.2 day and 10 days, respectively. A representative flow diagram of the ASP is shown below. Influent after Improve the shown below. Influent after Improve the shown below. Influent after Improve the shown below. Influent after Improve the shown below. Influent after Improve the shown below. Influent after Improve the shown below. Influent after Improve the shown below. Influent after Improve the shown below. Influent after Improve the shown below. Influent after Improve the shown below. Influent after Improve the shown below. Influent after Improve the shown below. Influent after Improve the shown below. Influent after Improve the shown below. Influent after Improve the shown below. Influent after Improve the shown below. Influent after Improve the shown below. Improve the shown below. Improve the shown below. Improve the shown below. Improve the shown below.	s e) f R //	 proportional to the wind speed. (iii) Value of the wind profile exponent for the 'neutral' atmosphere is smaller than the wind profile exponent for the 'very unstable' atmosphere. (iv) Downwind concentration of air pollutants due to an elevated point source will be directly proportional to the wind speed. Select the correct option. (a) (i) is False and (iii) is True (b) (ii) is False and (iii) is False (c) (i) is True and (iv) is True (d) (iii) is False and (iv) is False 30. Ans: (d) Sol: Concentration α 1/wind speed
29. Ans: 37.5 Sol: $Q = 7500 \text{ m}^3/\text{day}$ $y_i = 200 \text{ mg/l}$ $y_e = 20 \text{ mg/l}$ $X = 3000 \text{ mg/l}$ HDT = 0.2 day $X_U = 12000 \text{ mg/li}$ MCRT $\theta_e = 10 \text{ days}$ $Q_w = ?$ $\theta_e = \frac{VX}{Q_w X_U + (Q - Q_w) X_e}$ $\therefore X_e \text{ is not given}$ $\theta_e = \frac{VX}{Q_w X_U}$ $X_e = 0$ $10 = \frac{(7500 \times 0.2) \times 3000}{Q_w \times 12000}$ $Y = Q \times DT$ $= 7500 \times 0.2$ $= 1500 \text{ m}^3$ $\Rightarrow Q_w = \frac{7500 \times 0.2 \times 3000}{10 \times 12000} = 37.5 \text{ m}^3/\text{day}$		 31. A propped cantilever beam XY, with an internal hinge at the middle, is carrying a uniformly distributed load of 10 kN/m, as shown in the figure. 10 kN/m 10 kN/m<!--</td-->
 30. Read the statements given below. (i) Value of the wind profile exponent for the "very unstable' atmosphere is smaller than the wind profile exponent for the 'neutral' atmosphere. (ii) Downwind concentration of air pollutants due to an elevated point source will be inversely 	d d e y aluru +	$x \downarrow 10 \text{ kN/m} Y$ $x \downarrow 2m z 2m \downarrow R_{Y}$ $\Sigma V = 0$ $R_{x} + R_{y} = 10 \times 4$ Chennai + Vijayawada + Vizag + Tirupati + Kolkata + Ahmedabad

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16

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Bending moment at the internal hinge is zero

$$BM_{z} = 0 \quad \forall -ve \quad + \forall ve [Right side]$$
$$-R_{y} \times 2 + 10 \times 2 \times \frac{2}{2} = 0$$
$$R_{y} = 10 \text{ kN (\uparrow)}$$
$$R_{x} = 40 - 10$$
$$R_{x} = 30 \text{ kN (\uparrow)}$$

32. A rectangular cross-section of a reinforced concrete beam is shown in the figure. The diameter of each reinforcing bar is 16 mm. The values of modulus of elasticity of concrete and steel are 2.0×10^4 MPa and 2.1×10^5 MPa, respectively.



The distance of the centroidal axis from the centerline of the reinforcement (x) for the uncracked section (in mm, round off to one decimal place) is





$$M = \frac{E_s}{E_c} = 10.5$$

Centroid of an equivalent section

$$\overline{\mathbf{y}} = \frac{\mathbf{A}_1 \mathbf{y}_1 + \mathbf{A}_2 \mathbf{y}_2}{\mathbf{A}_1 + \mathbf{A}_2}$$

$$\frac{200 \times 350 \times \frac{350}{2} + (10.5 - 1) \times 3 \times \frac{\pi}{4} \times 16^2 \times 315}{200 \times 350 + (10.5 - 1) \times 3 \times \frac{\pi}{4} \times 16^2}$$

= 185.6 mm
X = d - y = 315 - 185.6 = 129.4 mm

33. If k is a constant, the general solution of $\frac{dy}{dx} - \frac{y}{x} = 1$ will be in the form of

(a) $y = xk \ln (k)$ (b) $y = x \ln (x)$ (c) $y = x \ln (kx)$ (d) $y = k \ln (kx)$

33. Ans: (c) **Sol:** The given D.E is in the form of $\frac{dy}{dx} + py = Q$

> Integrating factor = $e^{\int pdx} = e^{-\int \frac{1}{x}dx}$ = $e^{-\log x} = \frac{1}{x}$ Solution to the D.E is given by $y \cdot \frac{1}{x} = \int \frac{1}{x}dx + e$

 $y.\frac{1}{x} = \log x + \log k \Rightarrow y = x \log kx$

34. The stopping sight distance (SSD) for a level highway is 140 m for the design speed of 90 km/h. The acceleration due to gravity and deceleration rate are 9.81 m/s² and 3.5 m/s², respectively. The perception / reaction time (in s, round off to two decimal places) used in the SSD calculation is

34. Ans: 2.03

Sol: Given: SSD = 140 mLevel highway V = 90 kmph = 25 m/s $g = 9.81 \text{ m/s}^2$ $a = 3.5 \text{ m/s}^2 = \text{f.g}$ t = ?



$$SSD = vt + \frac{v^2}{2gf}$$

$$140 = vt + \frac{v^2}{2g\left(\frac{a}{g}\right)}$$

$$140 = 25 \times t + \frac{25^2}{(2 \times 3.5)}$$

$$140 = 25 \times t + 89.29$$

$$t = 2.028 \simeq 2.03 \text{ sec}$$

35. A reservoir with a live storage of 300 million cubic metre irrigates 40000 hectares (1 hectare = 10^4 m²) of a crop with two fillings of the reservoir. If the base period of the crop is 120 days, the duty for this crop (in hectares per cumec, round off to integer) will then be

35. Ans: 691

Sol: With two fillings of reservoir Volume, $V = 2 \times 300 = 600$ million m³ $= 6 \times 10^8$ m³

> Area irrigated A = 40,000 ha $\Delta = 8.64 \frac{B}{D}$

 $\frac{V}{A} = 8.64 \frac{B}{D}$

 $\frac{6\times10^8}{4\times10^8} = \frac{8.64\times120}{D}$

 \Rightarrow D = 691.2 ha/cumec = 691 ha/cumec

36. A fire hose nozzle directs a steady stream of water of velocity 50 m/s at an angle of 45° above the horizontal. The stream rises initially but then eventually falls to the ground. Assume water as incompressible and inviscid. Consider the density of air and the air friction as negligible, and assume the acceleration due to gravity as 9.81 m/s². The maximum height (in m, round off to two decimal places) reached by the stream above the hose nozzle will then be _____



The water jet performs projectile motion in which horizontal component of velocity remains constant. At point (2) only horizontal component is present which is given by

 $V_{2} = V_{1} \cos\theta = 50 \cos (45) = 35.36 \text{ m/s}^{2}$ Applying Bernoulli's equation between (1) & (2) $\frac{P_{1}}{\rho g} + \frac{V_{1}^{2}}{2g} + Z_{1} = \frac{P_{2}}{\rho g} + \frac{V_{2}^{2}}{2g} + Z_{2} + h_{f}$ $\frac{V_{1}^{2}}{2g} = \frac{V_{2}^{2}}{2g} + h$

$$h = \frac{V_1^2 - V_2^2}{2g} = \frac{50^2 - 35.36^2}{2 \times 9.81} = 63.71 \text{ m}$$

37. A single story building model is shown in the figure. The rigid bar of mass 'm' is supported by three massless elastic columns whose ends are fixed against rotation. For each of the columns, the applied lateral forces (P) and corresponding moment (M) are also shown in the figure. The lateral deflection (δ) of the bar is given by $\delta = \frac{PL^3}{12EI}$, where L is the effective length of the column, E is the Young's modulus of elasticity and I is the area moment of inertia of the column cross-section with respect to its neutral axis.



Since



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١		18	Civil Engineering
	For the lateral deflection profile of the columns as shown in the figure, the natural frequency of the system for horizontal oscillation is $\sqrt{EL} = 2 \sqrt{EL}$	8	Embankment load
37. Sol: 1.	(a) $6\sqrt{\frac{\text{EI}}{\text{mL}^3}} \text{ rad/s}$ (b) $\frac{2}{\text{L}}\sqrt{\frac{\text{EI}}{\text{m}}} \text{ rad/s}$ (c) $\frac{1}{\text{L}}\sqrt{\frac{2\text{EI}}{\text{m}}} \text{ rad/s}$ (d) $2\sqrt{\frac{6\text{EI}}{\text{mL}^3}} \text{ rad/s}$ Ans: (a) $\delta = \frac{\text{PL}^3}{12\text{EI}}$ \therefore Stiffness of bar, $K = \frac{P}{\delta} = \frac{12\text{EI}}{1^3}$		$\gamma = 18.5 \text{ kN/m}^3 \qquad \text{GWT} \qquad 2 \text{ m}$ Clay Specific gravity G = 2.65 Water content w = 45 % Compression index Cc= 0.25
2.	Equivalent stiffness k_e , The bars are in parallel arrangement $\therefore k_e = k + k + k = \frac{36EI}{L^3}$	RI	Impermeable layer The primary consolidation settlement (in m, round off to two decimal places) of the clay layer resulting from this loading will be 38. Ans: 0.33
3.	Natural Frequency ω_n , $\omega_n = \sqrt{\frac{k_e}{m}} \text{ rad/sec}$ $= \sqrt{\frac{36EI}{mL^3}} = 6\sqrt{\frac{EI}{mL^3}} \text{ rad/sec}$		Sol: Embankment load $\downarrow \downarrow $
38.	The soil profile at a road construction site is as shown in figure (not to scale). A large embankmen is to be constructed at the site. The ground wate table (GWT) is located at the surface of the clay layer, and the capillary rise in the sandy soil is negligible. The effective stress at the middle of the clay layer after the application of the embankmen loading is 180 kN/m ² . Take unit weight of water, γ_{e} = 9.81 kN/m ³	s t r y s e t t v	Clay $G_{s} = 2.65$ $W = 45 \%$ $C_{c} = 0.25$ Impermeable layer $\therefore \text{For clay layer } e_{o} S_{r} = WG_{s}$ $e_{o} \times 1 = 0.45 \times 2.65$ $e_{o} = 1.1925$ $\gamma_{sat} = \left(\frac{G_{s} + e}{1 + e}\right) \gamma_{w} = \left(\frac{2.65 + 1.1925}{1 + 1.1925}\right) \times 9.81$ $= 17.193 \text{ kN/m}^{3}$

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	At centre of clay layer:	
	Initial overburden pressure	
	$\sigma_{\rm o}^{\rm l} = \gamma_{\rm sand} \times 2 + \gamma_{\rm clay}^{\rm l} \times 3$	
	$\sigma_{\circ}^{1} = 18.5 \times 2 + (17.193 - 9.81) \times 3 = 59.148 \text{ kN/m}^{2}$	
	After application of embankment loads	,
	$\sigma_{\rm f}^{\rm l}=180~kN/m^2$	
$S_{f} =$	$= \frac{C_{\circ}}{1 + e_{\circ}} \times H \times \log_{10}\left(\frac{\sigma_{f}^{1}}{\sigma_{\circ}^{1}}\right) = \frac{0.25}{1 + 1.1925} \times 6 \times \log_{10}\left(\frac{180}{59.148}\right)$,
	$:: S_{s} = 0.3307 \text{ m}$	
	Say 0.33 m	
39.	Determine the correctness or otherwise of the	9
	following Assertion [a] and the Reason [r]	

following Assertion [a] and the Reason [r]. Assertion [a]: One of the best ways to reduce the amount of solid wastes is to reduce the consumption of raw materials.

Reason [**r**]: Solid wastes are seldom generated when raw materials are converted to goods for consumption.

- (a) Both [a] and [r] are true and [r] is the correct reason for [a]
- (b) [a] is true but [r] is false
- (c) Both [a] and [r] are true [r] is not the correct reason for [a]
- (d) Both [a] and [r] are false

39. Ans: (c)

- **Sol:** Solid waste generated by the use of raw material, processing and finished goods.
- 40. The internal (d_i) and external (d_o) diameters of a Shelby sampler are 48 mm and 52 mm, respectively. The area ratio (A_r) of the sampler (in % round off to two decimal places) is ______

40. Ans: 17.36

Sol: $d_i = 48 \text{ mm}$

$$d_o = 52 \text{ mm}$$

 $A_r = \frac{d_o^2 - d_i^2}{d_i^2} \times 100 = \frac{52^2 - 48^2}{48^2} \times 100 = 17.36\%$

GATE_202	1_Questions	with Solutions

41. If A is a square matrix then orthogonality property mandates

$(a) AA^{T} = A^{-1}$	(b) $AA^T = A^2$
(c) $AA^{T} = 0$	(d) $AA^{T} = I$

41. Ans: (d)

19

Sol: Condition for Orthogonal matrix is $AA^{T} = A^{T}A = I$ (or) $A^{T} = A^{-1}$

42. The activity details for a small project are given in the Table.

	Activity	Duration (days)	Depends on
	A	6	-
6	B	10	А
	C	14	А
	D	8	В
	Е	12	С
	F	8	С
	G	16	D,E
	Н	8	F, G
	K	2	В
	L	5	G, K

The total time (in days, in integer) for project completion is

Since 142.956



The total time required to complete the project = 56 days



Starts from: 1st July 2020 No. of Tests : 44 + Free 30 Practice Tests of ESE - 2020 Online Test Series Total Tests : 74

Note: GATE 2020 & ESE 2020 (Prelims) Online Test Series are available now.

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۲	ACE Engineering Publications	20	Civil Engineering
43.	Numerically integrate, $f(x) = 10x - 20x^2$ from lower limit a = 0 to upper limit b = 0.5. Use Trapezoidal rule with five equal subdivisions. The value (in units, round off to decimal places) obtained is		 (d) Increased levels of carbon monoxide in the indoor environment result in the formation of carboxyhemoglobin and the long term exposure becomes a cause of cardiovascular diseases.
43. Sol:	Ans: 0.4 $f(x) = 10x-20x^2 = y$ Step size $= \frac{b-a}{n} = \frac{0.5}{5} = 0.1$		45. Ans: (a, c and d)Sol: Indoor environment photochemical smog does not form.
	x 0 0.1 0.2 0.3 0.4 0.5 y 0 0.8 1.2 1.2 0.8 0 Required answer = $\frac{h}{2}[(y_0 + y_5) + 2(y_1 + y_2 + y_3 + y_4)]$ = $\frac{0.1}{2}[0 + 2(0.8 + 1.2 + 1.2 + 0.8)]$	R/	 46. The softening point of bitumen has the same unit as that of (a) temperature (b) time (c) viscosity (d) distance 46. Ans: (a)
	= 0.4		Sol: Softening point is the temperature at which bitumen becomes soft and starts flowing.
44.	The value (round off to one decimal place) of $\int_{-1}^{1} x e^{ x } dx$ is	f	47. A clay layer of thickness H has a pre-consolidation pressure p_e and an initial void ratio e_o . The initial effective overburden stress at the mid-height of the layer is P. At the same location, the increment in
44.	Ans: 0		effective stress due to applied external load is Ap
Sol:	$xe^{ x } \text{ is an odd function} \Rightarrow f(-x) = -f(x)$ $\Rightarrow \int_{-1}^{1} xe^{ x } dx = 0$	ce 1	The compression and swelling indices of the clay are C _c and C _s , respectively. If $P_o < P_c < (P_o + \Delta p)$, then the correct expression to estimate the consolidation
45.	 Which of the following statement(s) is/are correct? (a) Volatile organic compounds act as one of the precursors to the formation of photochemical among in the presence of suplight 		settlement (S _c) of the clay layer is (a) S _c = $\frac{H}{1 + e_o} \left[C_s \log \frac{p_o}{p_c} + C_c \log \frac{p_o + \Delta p}{p_c} \right]$
	 (b) Increased levels of volatile organic compounds in the indoor environment will result in the formation of photochemical smog which is a cause of cardiovascular diseases. 	5 2 1	(b) $S_c = \frac{H}{1 + e_o} \left[C_o \log \frac{p_c}{p_o} + C_s \log \frac{p_o + \Delta p}{p_c} \right]$ (c) $S_c = \frac{H}{1 + e_o} \left[C_c \log \frac{p_o}{p_c} + C_s \log \frac{p_o + \Delta p}{p_c} \right]$

(c) Long term exposure to the increased level of photochemical smog becomes a cause of chest constriction and irritation of the mucous membrane.

(d) $S_c = \frac{H}{1 + e_o} \left[C_s \log \frac{p_c}{p_o} + C_c \log \frac{p_o + \Delta p}{p_c} \right]$

47. Ans: (d)



As the soil is initially in over consolidate state ($p_o < p_c$), due to the external applied load (Δp), the soil initially undergoes re-compression upto p_c and then changes to virgin compression from p_c to p_f .

The re-compression index (C_r) is also called Swelling index, (C_s) .

$$S_{\rm c} = \frac{H_{\rm o}}{1 + e_{\rm o}} \left[C_{\rm s} \log \frac{p_{\rm c}}{p_{\rm o}} + C_{\rm c} \log \left(\frac{p_{\rm o} + \Delta p}{p_{\rm c}} \right) \right]$$

48. A prismatic steel beam is shown in the figure



The plastic moment, M_p calculated for the collapse mechanism using static method and kinematic method is

- (a) $M_{p,static} > \frac{2PL}{9} = M_{p,kinematic}$
- (b) $M_{p, static} < \frac{2PL}{9} = M_{p, kinematic}$
- (c) $M_{p, static} = \frac{2PL}{9} = M_{p, kinematic}$
- (d) $M_{p, static} = \frac{2PL}{9} \neq M_{p, kinematic}$



Static Method:

The maximum bending moment of $\frac{Pab}{L}$ evidently occurs under the load, when the load is increased to the collapse load w, the maximum bending moment will be equal to $\frac{P_cab}{L}$. This should evidently be equal to the plastic moment of resistance M_p.

$$\therefore \frac{P_c ab}{L} = M_P$$

$$M_P = P_c \times \frac{L}{3} \times \frac{2L}{3} \times \frac{1}{L}$$

$$M_P = \frac{2P_c L^2}{9L} = \frac{2P_c L}{9}$$

$$A \xrightarrow{L/3} \xrightarrow{P} 2L/3 \xrightarrow{C} B$$

Kinematic Method:

Static indeterminacy $(D_s) = 0$ Number of possible plastic hinges (N) = 1 [at B] No. of plastic hinges required to form a mechanism $(n) = D_s + 1 = 1$



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External work done (W_e) = P_c × δ = P_c × $\frac{L}{3}\theta$

Internal work done $(W_i) = M_p \theta + M_p \alpha$ = $M_P \theta + M_P \left(\frac{\theta}{2}\right)$

$$= 1.5 M_{p} \theta$$

22

 $W_{e} = W_{i}$ $P_{c} \times \frac{L}{3} \theta = 1.5 M_{P} \theta$

- $M_{\rm P} = \frac{P_{\rm c}L}{4.5} = \frac{2P_{\rm c}L}{9}$
- $M_{p,static} = \frac{2P_{\rm c}L}{9} = M_{\rm P,kinematic}$
- 49. Strain hardening of structural steel means
 - (a) decrease in the stress experienced with increasing strain
 - (b) experiencing higher stress than yield stress with increased deformation
 - (c) strengthening steel member externally for reducing strain experienced
 - (d) strain occurring before plastic flow of steel material

49. Ans: (b)

Sol: Strain hardening is experiencing higher stress than yield stress with increased deformation In the figure AB = Strain hardening zone OA = Linear elastic zone

Stress corresponding to point 'A' is yield stress.



50. The void ratio of a clay soil sample M decreased from 0.575 to 0.510 when the applied pressure is increased from 120 kPa to 180 kPa. For the same increment in pressure, the void ratio of another clay soil sample N decreases from 0.600 to 0.550. If the ratio of hydraulic conductivity of sample M to sample N is 0.125, then the ratio of coefficient of consolidation of sample M to sample N (round off to three decimal places) is

Civil Engineering

50. Ans: 0.095 Sol: Sample M $e_o = 0.575$ $e_f = 0.510$ $\Delta \sigma' = 180 - 120 = 60 \text{ kPa}$ $m_{v_1} = \frac{\Delta e}{1 + e_o} \times \frac{1}{\Delta \sigma'}$ $= \frac{0.575 - 0.51}{1 + 0.575} \times \frac{1}{60}$ $\therefore m_{v_1} = 6.878 \times 10^{-4} \text{ m}^2/\text{kN}$ Sample N $e_o = 0.560$ $e_f = 0.55$ $\Delta \sigma' = 60 \text{ kPa}$ $m_{v_2} = \frac{\Delta e}{1 + e_o} \times \frac{1}{\Delta \sigma'}$ $= \frac{0.6 - 0.55}{1 + 0.60} \times \frac{1}{60}$ $\therefore m_{v_2} = 5.208 \times 10^{-4} \text{ m}^2/\text{kN}$

Given:
$$\frac{K_1}{K_2} = 0.125$$
 \therefore $C_v = \frac{K}{m_v \gamma_w}$
 $\frac{C_{v_1}}{C_{v_2}} = \frac{K_1}{K_2} \times \frac{m_{v_2}}{m_{v_1}}$
 $= 0.125 \times \frac{5.20 \times 10^{-4}}{6.878 \times 10^{-4}}$
 $\therefore \frac{C_{v_1}}{C_{v_2}} = 0.0946 \simeq 0.095$





C S

AIR – 1

EE:9

AIR – 2

ME:7

EC:9

Total Selections in Top 10 58

CS:**7**

AGARWAL

CE:**7**

and many more...

ADIGAUR

AIR – 9

SHARMA

IN : 6 **PI:9 XE:4**

ANJAN TIWA AIR – <mark>8</mark>

- 51. The value of $\lim_{x\to\infty} \frac{x \ln(x)}{1+x^2}$ is
 - (a) ∞ (b) 0.5
 - (c) 0 (d) 1.0

51. Ans: (c)

Sol:

 $\lim_{x \to \infty} \frac{x \ln(x)}{1 + x^2} = \frac{\infty}{\infty} \rightarrow \text{Indeterminate form}$

Using L'Hospital rule, we get

$$\lim_{x \to \infty} \frac{x \cdot \frac{1}{x} + \ln(x)}{2x} = \lim_{x \to \infty} \frac{1 + \ln x}{2x} = \frac{\infty}{\infty}$$

Apply L'Hospital rule again, we get $\lim_{x \to \infty} \frac{1/x}{2} = 0$

 $\therefore \lim_{x \to \infty} \frac{x \ln(x)}{1 + x^2} = 0$

52. The hyetograph in the figure corresponds to a rainfall event of 3 cm.



If the rainfall event has produced a direct runoff of 1.6 cm, the ϕ -index of the event (in mm/hour, round off to one decimal place) would be _____

52. Ans: 4.2

Sol: Given Data: P = 3 cm, t = 3.5 hoursR = 1.6 cm = 16 mm

t(Hrs)	0-0.5	0.5-1	1-1.5	1.5-2	2-2.5	2.5-3	3-3.5
i, mm/ hr	12	4.5	15	14	4	7.5	3
P,mm	6	2.25	7.5	7	2	3.75	1.5

To Find ϕ -Index: Trial 1: Assume $t_e = 3.5$ hrs $P_e = 6 + 2.25 + 7.5 + 7 + 2 + 3.75 + 1.5 = 30$ mm ϕ_1 -Index = $\frac{P_e - R}{t_e} = \frac{30 - 16}{3.5} = 4$ mm/hr Eliminate intensities 4 mm/hr & 3 mm/hr which doesn't produces runoff

Trial-2: Assume $t_e = 2.5$ hrs $P_e = 30 - [2+1.5] = 26.5$ mm ϕ_2 -Index $= \frac{P_e - R}{t_e} = \frac{26.5 - 16}{2.5} = 4.2$ mm/hr

- 53. In general, the CORRECT sequence of surveying operations is
 - (a) Reconnaissance \rightarrow Field observations \rightarrow Data analysis \rightarrow Map making
- 199(b) Reconnaissance \rightarrow Data analysis \rightarrow Field observations \rightarrow Map making
 - (c) Data analysis → Reconnaissance → Field
 observations → Map making
 - (d) Field observations → Reconnaissance → Data analysis → Map making

53. Ans: (a)

Sol: Reconnaissance \rightarrow Site visit Field observation \rightarrow Preliminary/Detailed Survey

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54. A solid circular torsional member OPQ is subjected to torsional moments as shown in the figure (not to scale). The yield shear strength of the constituent material is 160 MPa.		using a proportional weir at the outlet end of the chamber, the minimum length of the chamber (in m, in integer) to remove 0.25 mm particles completely
$\int \frac{2 \text{ kN.m}}{1 \text{ kN.m}} \frac{1 \text{ kN.m}}{0.1 \text{ m}} + \frac{2 \text{ kN.m}}{1 \text{ m}} \frac{1 \text{ kN.m}}{0.8 \text{ m}}$ $\int \frac{1 \text{ m}}{1 \text{ m}} \frac{1 \text{ m}}{0.5 \text{ m}} 1$	R IA	55. Ans: 9 Sol: $d = 0.25 \text{ mm}$ $S = 2.7$ $V_s = 2.5 \text{ cm/sec}$ $B = 0.5 \text{ m}$ $Q = 9720 \text{ m}^3/\text{day}$ $H = 0.75 \text{ m}$ $v_H = 0.3 \text{ m/sec}$ $L = ?$ 100% removal For 100% removal $\frac{H}{v_s} \le \frac{L}{v_H} \Rightarrow \frac{H}{v_s} = \frac{L}{v_H}$ $\frac{0.75}{2.5 \times 10^{-2}} = \frac{L}{0.3}$ $\Rightarrow L = 9 \text{ m}$
55. A grit chamber of rectangular cross-section is to be designed to remove particles with diameter of 0.25 mm and specific gravity of 2.70. The terminal settling velocity of the particles is estimated as 2.5 cm/s. The chamber is having a width of 0.50 m and has to carry a peak wastewater flow of 9720 m ³ /d giving the depth of flow as 0.75 m. If a flow- through velocity of 0.3 m/'s has to be maintained		

