



# ACE

## Engineering Academy

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### Branch: CIVIL ENGINEERING \_MOCK-D SOLUTIONS

01. Ans: (A)

02. Ans: 0.34 (Range 0.32 to 0.36)

Sol: Grade compensation for BG curve = 0.04%  
per degree curve

$$\text{Total grade compensation} = 0.04 \times 4 \\ = 0.16\%$$

$$\therefore \text{Gradient provided} = 0.5 - 0.16 \\ = 0.34\%$$

03. Ans: (C)

Sol: As per IRC camber provided for WBM,

$$\text{heavy rainfall is } 3\% = \frac{1}{33}.$$

$$\therefore \text{Height of crown} = \frac{w}{2N} = \frac{3.8}{2 \times 33} = 0.0575 \text{ m} \\ = 57.5 \text{ mm} \approx 58 \text{ mm}$$

04. Ans: 618.15 Range: 618 to 619

$$\text{Sol: } \frac{q_f}{q_p} = \frac{B_f}{B_p}$$

$$\frac{q_f}{287} = \frac{1.4}{0.65}$$

$$q_f = 618.15 \text{ kN/m}^2$$

05. Ans : 2.09 Range: 2 to 2.10

$$\text{Sol : } S_n = \frac{C}{F_c \cdot \gamma H}$$

$$0.181 = \frac{115}{F_c \times 20.2 \times 15}$$

$$F_c = 2.10$$

06. Ans: 2 no range

Sol: The probability density function of uniform distribution is

$$f(x) = \begin{cases} 1, & 0 < x < 1 \\ 0, & \text{otherwise} \end{cases}$$

$$E(y) = E[-2 \log_e x]$$

$$= \int_0^1 -2 \log_e x f(x) dx$$

$$= -2 \int_0^1 \log_e x dx$$

$$= -2 \{x \log_e x - x\}_0^1$$

$$= -2 \{(0-1) - (0)\}$$

$$= 2$$

07. Ans: 300 Range: 299.2 to 300

$$\text{Sol: } Q = \frac{W \cdot h}{F[S + C]} = \frac{22.5 \times 1200}{6[2.54 + 12.5]} = 300 \text{ kN}$$

08. Ans: (C)

$$\text{Sol: } \therefore \lim_{x \rightarrow 0} \frac{\tan(ax)}{x} = a$$

$$\text{Now, } \lim_{x \rightarrow 0} \frac{\tan(4x)}{4x} = \frac{1}{4} \lim_{x \rightarrow 0} \frac{\tan(4x)}{x}$$

$$\therefore \lim_{x \rightarrow 0} \frac{\tan(4x)}{4x} = \frac{1}{4} (4) = 1$$

09. Ans: 0

Sol: There is no effect due to the change in level of water in the lake on effective stress at any point below the bed of lake.



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10. Ans: (C)

11. Ans: (B)

Sol: In a short column subjected to pure axial loading, the strain variation is uniform with a value of 0.002.

12. Ans: 15.39 Range 15.2 to 15.5

Sol:  $F_v$  = weight of volume of liquid contained in semi-circular gate

$$F_v = \rho g V$$

$$= 1000 \times 9.8 \times \frac{\pi \times R^2}{2} \times 1$$

$$F_v = 15.39 \text{ kN}$$

13. Ans: 1280 no range

Sol: Given that  $|A_{4 \times 4}| = 5$

$$\therefore |K A_{n \times n}| = K^n |A_{n \times n}|$$

$$\Rightarrow |(-4) A| = (-4)^4 |A_{4 \times 4}| \text{ for } n = 4$$

$$\Rightarrow |(-4) A_{4 \times 4}| = (256) (5)$$

$$\therefore |(-4) A_{4 \times 4}| = 1280$$

14. Ans: 166.67 ppm Range: (166-167)

Sol: BOD = Depletion of oxygen  $\times$  Dilution factor

$$= 3 \text{ ppm} \times \frac{100}{1.8}$$

$$= 166.67 \text{ ppm}$$

15. Ans: (C)

16. Ans: (B)

Sol: Addition of water imparts permanent hardness.

17. Ans: 2000

$$\text{Sol: } \frac{E}{R} = \frac{f_{\max}}{y_{\max}}$$

$$\frac{200 \times 10^3}{100} = \frac{f_{\max}}{1}$$

$$f_{\max} = 2000 \text{ MPa}$$

18. Ans: (B)

Sol: The condition for exactness of a differential equation

$$M(x, y) dx + N(x, y) dy = 0 \text{ is } \frac{\partial M}{\partial y} = \frac{\partial N}{\partial x}$$

Given that  $M(x, y) = 3xy^2 + k^2 x^2 y$  and  $N(x, y) = kx^3 + 3x^2 y$

$$\text{Consider } \frac{\partial M}{\partial y} = \frac{\partial N}{\partial x}$$

$$\Rightarrow 6xy + k^2 x^2 = 3kx^2 + 6xy$$

$$\Rightarrow k^2 = 3k \text{ (or) } k^2 - 3k = 0$$

$$\Rightarrow k = 0, 3$$

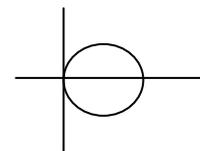
$\therefore$  The non zero value of  $k$  is 3

19. Ans: (B)

Sol: State of stress on the bottom fibre of a simply supported beam at mid span is in pure tension as shown below.



The corresponding Mohr's circle is touching to y-axis on positive side.





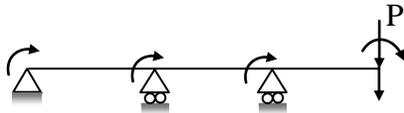
**20. Ans: 144000 Range: 144000 to 144000**

$$\text{Sol: } E_L = \underbrace{(60 \times 1000 \times 20)}_{\text{Area}} \times \underbrace{0.8}_{\text{pan coeff}} \times \underbrace{\frac{0.5}{100}}_{\frac{m}{\text{day}}} \times \underbrace{30}_{\text{day}}$$

$$= 144000 \text{ m}^3$$

**21. Ans: (A)**

**Sol:** Number of joint  $j = 4$



Number of members,  $m = 3$

Number of independent external reaction components,  $r = 4$

$$D_k = 3 \times 4 - (4 + 3) = 5$$

**22. Ans: (C)**

**23. Ans: (D)**

**24. Ans: 0.25**

**no range**

**Sol:** Given

$$\int_0^x f(t) dt = -2 + \frac{x^2}{2} + 4x \sin(2x) + 2 \cos(2x)$$

Differentiating both sides of above w.r.t 'x',

$$\text{we get } \frac{d}{dx} \left[ \int_0^x f(t) dt \right] = -0 + \frac{2x}{2} + 4 \sin(2x) + 8x \cos(2x) - 4 \sin(2x)$$

$$\Rightarrow \left( \frac{d}{dx}(x) \right) [f(x)] - \left( \frac{d}{dx}(0) \right) [f(0)]$$

$$= x + 8x \cos(2x)$$

$$\Rightarrow f(x) = x + 8x \cdot \cos(2x)$$

$$\therefore \frac{1}{\pi} f\left(\frac{\pi}{4}\right) = \frac{1}{\pi} \left[ \frac{\pi}{4} + 8 \left( \frac{\pi}{4} \right) \cdot \cos\left(\frac{2\pi}{4}\right) \right]$$

$$= \frac{1}{4} = 0.25$$

**25. Ans: (D)**

**26. Ans: (B)**

**Sol:** Given that  $A = (a_{ij})_{n \times n}$ ,

$$\text{where } a_{ij} = \begin{cases} (n+1)^2 - i, & \forall i = j \\ 0 & , \forall i \neq j \end{cases}$$

$$\Rightarrow A = \begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{bmatrix}$$

$$= \begin{bmatrix} 15 & 0 & 0 \\ 0 & 14 & 0 \\ 0 & 0 & 13 \end{bmatrix}_{3 \times 3} \quad \text{for } n = 3$$

$\Rightarrow A_{3 \times 3}$  is a diagonal matrix & its eigen values are its diagonal elements 15, 14, 13.

If  $\lambda_1, \lambda_2, \lambda_3$  are the eigen values of  $A_{3 \times 3}$  matrix then the eigen values of matrix  $A_{3 \times 3}^2$  are  $\lambda_1^2, \lambda_2^2$  and  $\lambda_3^2$ .

$\therefore$  The eigen values of a required matrix  $A^2$  are  $(15)^2, (14)^2$  and  $(13)^2$  (i.e., 225, 196, 169)

**27. Ans: 0.255**

**Range: 0.24 - 0.27**

**Sol:**

Time (1)	Total stream flow in cumec (2)	Base flow in cumec (3)	Direct runoff = (2) - (3)
0	4.8	4.8	0
2	5.1	4.8	0.3
4	6.5	4.8	1.7
6	7.4	4.8	2.6
8	10.2	4.8	5.4
10	8.8	4.8	4
12	7.4	4.8	2.6
14	4.8	4.8	0



Catchment area,  $A = 400 \text{ ha}$

$$= 400 \times 10^4 \text{ m}^2$$

$$\text{Volume of runoff, } V = \left[ \frac{O_1 + O_n}{2} + \sum O \right] \Delta t$$

$$= \left[ \left( \frac{0+0}{2} \right) + (0.3+1.7+2.6+5.4+4+2.6) \right] \times 2 \times 60 \times 60$$

$$= 11.95 \times 10^4 \text{ m}^3$$

$$\text{Depth of Runoff} = \frac{\text{Volume of Runoff}}{\text{Catchment area}}$$

$$= \frac{11.95 \times 10^4}{400 \times 10^4}$$

$$= 0.0298 \text{ m} = 2.98 \text{ cm}$$

$$\phi_{\text{index}} = \frac{P_e - R}{t_e}$$

Rainfall,  $P_e = 4 \text{ cm}$

$$\phi_{\text{index}} = \frac{4 - 2.98}{4} = 0.255 \text{ cm/hr}$$

**28. Ans: 163.35 (Range 162 to 165)**

**Sol:**  $V_1 = 72 \text{ kmph} = 20 \text{ m/s}$

$V_2 = 54 \text{ kmph} = 15 \text{ m/s}$

$$(\text{SSD})_{\text{car1}} = v_1 t + \frac{v_1^2}{2gf\eta}$$

$$= 20 \times 2.5 + \frac{20^2}{2 \times 9.81 \times 0.7 \times 0.6}$$

$$= 98.54 \text{ m}$$

$$(\text{SSD})_{\text{car2}} = v_2 t + \frac{v_2^2}{2gf\eta}$$

$$= 15 \times 2.5 + \frac{15^2}{2 \times 9.81 \times 0.7 \times 0.6}$$

$$= 64.81 \text{ m}$$

$\therefore$  Total sight distance required

$$= \text{SSD}_1 + \text{SSD}_2$$

$$= 98.54 + 64.81$$

$$= 163.35 \text{ m}$$

**29. Ans: 6.75 Range: 6.50 – 7.00**

**Sol:** Radius of Plate 'a' =  $\frac{30}{2} = 15 \text{ cm}$

$$p = \frac{P}{\pi a^2} = \frac{1490}{\pi \times 15^2} = 2.108 \text{ kg/cm}^2$$

$p = \text{contact pressure}$

**For standard plate of Dia 75 cm:**

Pressure on the surface is not uniformly distributed

$$E_s = 1.18 \frac{p}{\Delta}$$

$p = \text{pressure}$

$$E_s = 1.18 K_a$$

$\therefore$  For a given sub grade  $E_s$  is constant

$\therefore K_a = \text{constant}$

$$K_{30} \cdot a_{30} = K_{75} \cdot a_{75}$$

$$K_{30} = \frac{p}{\Delta} = \frac{2.108}{0.125} = 16.864 \text{ kg/cm}^3$$

$$16.864 \times 15 = K_{75} \times \frac{75}{2}$$

$$\Rightarrow K_{75} = 6.7456$$

$$K_{75} \approx 6.75 \text{ kg/cm}^3$$

**30. Ans: 2 Range: No Range**

**Sol:** Given that  $f(x, y) = x^2 + 2y^2$  ..... (1)

with  $y - x^2 + 1 = 0$  ..... (2)

From (2), we write  $y = x^2 - 1$  ..... (3)

Put (3) in (1), we get

$$f(x, y) = x^2 + 2y^2 = x^2 + 2(x^2 - 1)^2$$

$$= x^2 + 2[x^4 - 2x^2 + 1]$$

$$\text{Let } g(x) = 2x^4 - 3x^2 + 2$$

$$\text{Then } g'(x) = 8x^3 - 6x \text{ and } g''(x) = 24x^2 - 6$$

Consider  $g'(x) = 0$

$$\Rightarrow 8x^3 - 6x = 0$$



$\therefore x = 0, \frac{\sqrt{3}}{2}, \frac{-\sqrt{3}}{2}$  are stationary points.

At  $x = 0, g''(0) = -6 < 0$

At  $x = \pm \frac{\sqrt{3}}{2}, g''\left(\pm \frac{\sqrt{3}}{2}\right) = 12 > 0$

$\therefore x = 0$  is a local point of maxima.

Hence, the maximum value of the function

$f(x, y)$  at  $x = 0$  is

$$f(x, y) = f(x, x^2 - 1) = f(0, -1) = 0 + 2[0 - 0 + 1] = 2$$

**31. Ans: (C)**

**Sol:**  $V = 80$  kmph,  $H_t = 3$  sec

$$q = \frac{3600}{H_t} = \frac{3600}{3} = 1200 \text{ Veh / hr}$$

$q = k.V$

$$k = \frac{1200}{80} = 15 \text{ km / veh}$$

Distance between two vehicle

$$= \frac{1000}{K} = \frac{1000}{15} = 66.67 \text{ m}$$

**32. Ans: 52.58 Range: 52 to 53**

**Sol:** The increase stress,

$$\begin{aligned} \bar{\sigma}_o + \Delta\bar{\sigma} &= 60 + 70 \\ &= 130 \text{ kN/m}^2 \end{aligned}$$

$$\Delta H = \frac{C_r.H_o}{1+e_o} \log \frac{\bar{\sigma}_c}{\bar{\sigma}} + \frac{C_c.H_o}{1+e_o} \log \frac{\bar{\sigma}_o + \Delta\bar{\sigma}}{\bar{\sigma}_c}$$

$$\Delta H = \frac{0.03 \times 4000}{1+0.87} \log \frac{110}{60} + \frac{0.23 \times 4000}{1+0.87} \log \left( \frac{130}{110} \right)$$

$$\Delta H = 52.58 \text{ mm}$$

**33. Ans: 13.14 (Range:13.10 to 13.20)**

**Sol:**

$$w_s = \left[ w_1 - \left( \frac{V_1 - V_d}{w_d} \right) \gamma_w \right] \times 100$$

$$w_1 = \left[ \frac{w - w_d}{w_d} \right] = \left[ \frac{29.4 - 17.5}{17.5} \right] = 0.68$$

$$w_s = \left[ 0.68 - \left( \frac{19.2 - 9.6}{17.5} \right) \times 1 \right] \times 100 = 13.14\%$$

**34. Ans: 3.24**

**Sol:**  $n_f = 4.5$

$n_d = 12$

$$q = K.H. \frac{n_f}{n_d}$$

$$= 5 \times 10^{-3} \times 10^{-2} \times 2 \times \frac{4.5}{12}$$

$$= 3.75 \times 10^{-5} \text{ cum/s/m length of the}$$

piling

$$= 3.75 \times 60 \times 60 \times 24 \times 10^{-5}$$

$$= 3.24 \text{ cum/day/m length}$$

**35. Ans: (B)**

**36. Ans: 1.52 Range: No Range**

**Sol:** Consider  $\int_C \bar{f} \cdot d\bar{r} = \int_{(0,0)}^{(1,1)} \left[ \sqrt{x} dx + (x+y^3) dy \right]$

..... (1)

Given that  $C: x = t^2, y = t^3, 0 \leq t \leq 1$  } ..... (2)

$\Rightarrow dx = 2t dt, dy = 3t^2 dt$

Using (2), (1) becomes

$$\int_C \bar{f} \cdot d\bar{r} = \int_{t=0}^1 \left[ (t)(2t) dt + (t^2 + t^9)(3t^2) dt \right]$$



$$\Rightarrow \int_C \bar{f} \cdot d\bar{r} = \int_{t=0}^1 [2t^2 + 3t^4 + 3t^{11}] dt$$

$$\Rightarrow \int_C \bar{f} \cdot d\bar{r} = \left( \frac{2t^3}{3} + \frac{3t^5}{5} + \frac{3t^{12}}{12} \right)_0^1$$

$$\therefore \int_C \bar{f} \cdot d\bar{r} = \left( \frac{2}{3} + \frac{3}{5} + \frac{3}{12} \right) = 1.52$$

**37. Ans: (B)**

**Sol:** Mass specific gravity,  $S = \frac{\gamma_d}{\gamma_w}$

$$= \frac{1.4}{1} = 1.40$$

Readily available depth of water,

$$d_w = S \cdot d \text{ [FC - OM]}$$

$$d_w = 1.40 \times 70 [0.23 - 0.15] = 7.84 \text{ cm}$$

$$\text{Water to be applied} = \frac{d_w}{\eta_a} = \frac{7.84}{0.80} = 9.8 \text{ cm}$$

**38. Ans: (A)**

**Sol:** The required MOI of the first horizontal stiffness

$$I = Ct_w^3$$

C = actual distance between vertical stiffener.

$t_w$  = minimum thickness of web

$$C = 1200 \text{ mm}$$

$$t = 10 \text{ mm}$$

$$I = 1200 \times 10^3$$

$$I = 1.2 \times 10^6 \text{ mm}^4$$

**39. Ans: 12.14 Range: 12 to 13**

**Sol:** Area of tensile steel =  $4 \times \frac{\pi}{4} \times 16^2$   
= 804.25 mm<sup>2</sup>

Limiting depth of neutral axis for Fe415 steel ( $x_{u,lim}$ ) = 0.48d = 0.48 × 350 = 168mm

Actual depth of neutral axis ( $x_u$ )

$$0.36 f_{ck} b x_u = 0.87 f_y A_{st}$$

$$x_u = \frac{0.87 f_y A_{st}}{0.36 f_{ck} b} = \frac{0.87 \times 415 \times 804.25}{0.36 \times 25 \times 200}$$

$$= 161.32 \text{ mm} < x_{u,lim}$$

Hence the section is under reinforced

Moment of resistance

$$= 0.36 f_{ck} b x_u (d - 0.42 x_u)$$

$$= 0.36 \times 25 \times 200 \times 161.32 (350 - 0.42 \times 161.32) = 81.95 \text{ kNm}$$

Working moment of resistance = 81.95/1.5  
= 54.64 kNm

Permissible service load =  $\frac{54.64 \times 8}{6^2}$   
= 12.14 kNm

**40. Ans: 2.4 Range: 2.3 to 2.5**

**Sol:**  $\eta_0 = \frac{P}{\rho g Q H}$

$$Q = \frac{20 \times 10^6}{0.9 \times 10 \times 10^3 \times 36} = 61.728 \text{ m}^3 / \text{s}$$

$$\psi = \frac{V_f}{\sqrt{2gH}}$$

$$V_f = \psi \sqrt{2gH}$$

$$= 0.6 \times \sqrt{2 \times 10 \times 36}$$

$$V_f = 16.099 \text{ m/s}$$

$$Q = \frac{\pi}{4} (D_0^2 - D_h^2) V_f$$

$$\frac{D_0}{D_h} = 2.5$$

$$61.728 = \frac{\pi}{4} \times \left( D_0^2 - \frac{D_0^2}{(2.5)^2} \right) \times 16.099$$

$$D_0 = 2.4 \text{ m}$$

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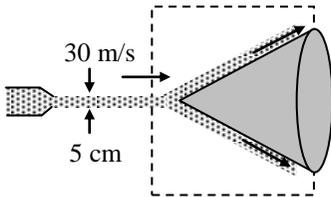


**41. Ans: (A)**

**Sol:** The mass flow rate of water jet is

$$\dot{m} = \rho AV$$

$$= 1000 \times \frac{\pi}{4} \times (0.05)^2 \times 30 = 58.9 \text{ kg/s}$$



By momentum equation for steady flow

$$F_{Rx} = \dot{m}V \cos\theta - \dot{m}V = \dot{m}V(\cos\theta - 1)$$

$F_{Ry} = 0$  (Due to symmetry about x-axis)

$$\text{Then } F_{Rx} = 58.9 \times 30 \times (\cos 45^\circ - 1)$$

$$= -518 \text{ N}$$

**42. Ans: (B)**

**Sol:** Given  $\frac{d}{dx} \left( x \frac{dy}{dx} \right) = x$  ..... (1)

With  $y(1) = 0$  ..... (2)

And  $y'(1) = 0$  ..... (3)

Now, integrating on both sides of (1), we get

$$x \frac{dy}{dx} = \frac{x^2}{2} + C_1$$

$$\Rightarrow \frac{dy}{dx} = \frac{x}{2} + \frac{C_1}{x}$$
 ..... (4)

Using (3), (4) becomes

$$0 = \frac{1}{2} + \frac{C_1}{1} \text{ (or) } C_1 = -\frac{1}{2}$$
 ..... (5)

Using (5), (4) becomes

$$\frac{dy}{dx} = \frac{x}{2} - \frac{1}{2x}$$

$$\Rightarrow y = \frac{x^2}{4} - \frac{1}{2} \log x + c$$
 ..... (6)

Using (2), (6) becomes

$$0 = \frac{1}{4} - \frac{1}{2}(0) + C \text{ (or) } C = -\frac{1}{4}$$
 ..... (7)

$\therefore$  The solution of (1) from (6) and (7) is

$$y = y(x) = \frac{x^2}{4} - \frac{1}{2} \log(x) - \frac{1}{4}$$

$$\text{Hence, } y(2) = 1 - \frac{1}{2} \log(2) - \frac{1}{4}$$

$$= \frac{3}{4} - \frac{1}{2} \log(2)$$

**43. Ans: (A)**

**Sol:** The spillway behaves like rectangular notch

$\therefore$  discharge per unit width

$$(q)_a = \frac{2}{3} C_d \sqrt{2g} H^{3/2}$$

H is head of water above crest level

$$\therefore H = 153.5 - 150$$

$$H = 3.5 \text{ m}$$

$$q = \frac{2}{3} \times 0.73 \times \sqrt{2 \times 9.81} \times (3.5)^{3/2}$$

$$q = 14.115 \text{ m}^3/\text{sec}/\text{m}$$

given depth at Toe is 0.44 m ( $y_1$ )

Let  $y$  be the required tail water depth then

$$\frac{2q^2}{g} = y_1 y_2 (y_1 + y_2)$$

$$\frac{2 \times 14.115^2}{9.81} = 0.44 y_2 (0.44 + y_2)$$

$$y_2 = 9.39 \text{ m}$$

Answer can be obtained by substituting options.

**44. Ans: 0.67**

**Range: 0.66-0.68**

**Sol:** Freeman's formula:

$$Q = 1136 \left( \frac{P}{5} + 10 \right)$$

$$= 1136 \left( \frac{168}{5} + 10 \right)$$

$$= 49,529.6 \text{ lit/min}$$



Buston's formula:

$$Q = 5663\sqrt{P}$$

$$= 5663\sqrt{168}$$

$$= 73,400.87 \text{ lit/min}$$

$$\frac{(Q)_{\text{Freeman}}}{(Q)_{\text{Buston}}} = \frac{49,529.6}{73,400.87} = 0.67$$

**45. Ans: (A)**

**Sol:** Average coefficient of runoff: k

$$k = \frac{\sum kA}{A}$$

$$\frac{(0.87 \times 15) + (0.43 \times 18) + (0.23 \times 34) + (0.20 \times 17) + (0.15 \times 16)}{15 + 18 + 34 + 17 + 16}$$

$$= 0.3441$$

$$\text{Rainfall intensity, } i = \frac{888}{30 + 45}$$

$$= 11.84 \text{ mm/hr}$$

Using Rational formula

$$Q_p = \frac{kiA}{360}$$

$$= \frac{0.3441 \times 11.84 \times 14}{360}$$

$$= 0.158 \text{ m}^3/\text{sec}$$

**46. Ans: 0.11 Range: 0.1 to 0.2**

**Sol:** Total possible outcomes for both faces even  
= (2, 2), (2, 4), (2, 6), (4, 2), (4, 4), (4, 6),  
(6, 2), (6, 4), (6, 6) = 9

Total favorable outcome for sum smaller than 6 = (2, 2)

P (sum is less than 6 given both faces are even) =  $\frac{1}{9} = 0.11$

**47. Ans: (A)**

**Sol:**  $E = \frac{\sum P_i E_i}{100}$

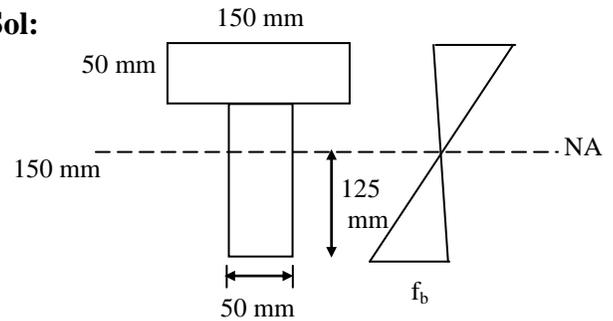
$$= \frac{(30 \times 6540) + (55 \times 17830) + (10 \times 7500) + (5 \times 21,300)}{100}$$

$$= 13,583.5 \text{ kJ/kg}$$

**48. Ans: (A)**

**49. Ans: (A)**

**Sol:**



Bending stress at the bottom fibre of the

$$\text{beam is } f_b = \frac{M}{I}(y_b) = \frac{3400 \times 10^3}{5312.5 \times 10^4}(125)$$

$$f_b = 8 \text{ MPa}$$

Tensile/compressive force in the cross-section is = avg. stress  $\times$  area of the cross section below the neutral axis

$$= \left(\frac{8+0}{2}\right)(50 \times 125) = 25 \text{ kN}$$

# HEARTY CONGRATULATIONS TO OUR **ESE - 2019** TOP RANKERS



**TOTAL SELECTIONS** in Top 10: **33**  
(EE: **9**, E&T: **8**, ME: **9**, CE: **7**) and many more...



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50. Ans: (C)

Sol: Slope at free end 'D' = slope due to loading '3P' at B + slope due to loading '2P' at C + slope due to loading 'P' at D

$$\begin{aligned} &= \frac{3PL^2}{2EI} + \frac{2P(2L)^2}{2EI} + \frac{P(3L)^2}{2EI} \\ &= \frac{20PL^2}{2EI} = \frac{10PL^2}{EI} \end{aligned}$$

51. Ans: (C)

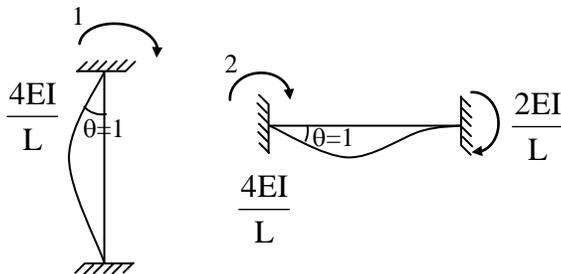
Sol: By analysis of bar chart critical path can not be found out.

The length of the bar for a particular activity has significance of time as bar chart is time scaled and the length of the bar will signify .

52. Ans: (D)

Sol: To generate stiffness matrix first fix all co ordinates

For Ist column

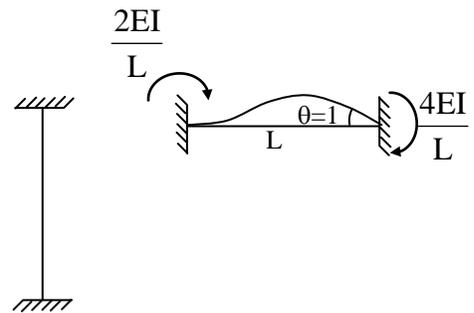


$$\begin{aligned} \therefore K_{11} &= \frac{4EI}{L} + \frac{4EI}{L} \\ &= \frac{4E(2I)}{5} + \frac{4E(2I)}{4} \end{aligned}$$

$$K_{11} = 3.6EI$$

$$K_{21} = \frac{2E(2I)}{4} = EI$$

For 2<sup>nd</sup> column:



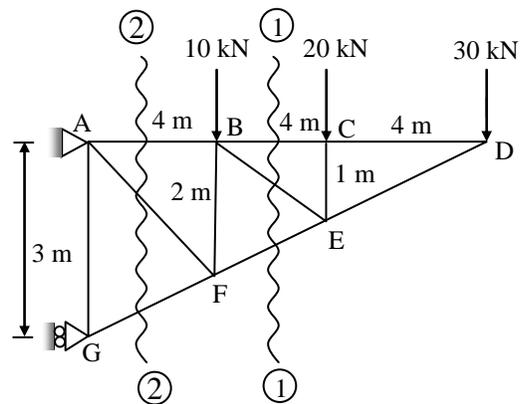
$$\therefore K_{12} = \frac{2E(2I)}{4} = EI$$

$$K_{22} = \frac{4E(2I)}{4} = 2EI$$

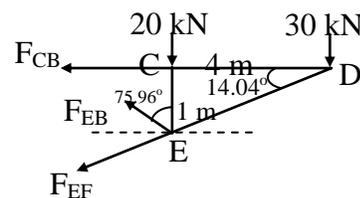
$$\therefore [K] = \begin{bmatrix} 3.6EI & EI \\ EI & 2EI \end{bmatrix}$$

53. Ans: (C)

Sol:



Cutting section (1) – (1)

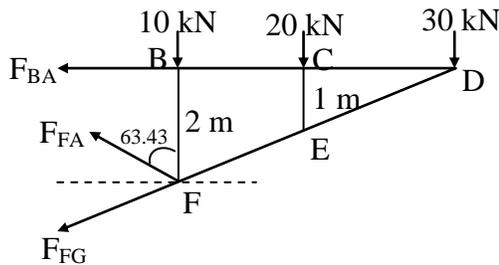




$$F_{EB} \cos (75.96) \times 4 + F_{EB} \sin (75.96) \times 1 = 20 \times 4$$

or,  $F_{EB} = 41.23 \text{ kN}$  (tensile)

Cutting section (2) – (2)



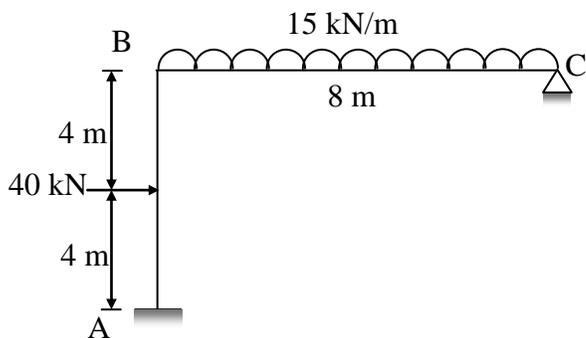
$$+\square \Sigma M_D = 0$$

$$F_{FA} \cos (63.43) \times 8 + F_{FA} \sin (63.43) \times 2 = 10 \times 8 + 20 \times 4$$

or,  $F_{FA} = 29.81 \text{ kN}$  (tensile)

**54. Ans: (D)**

**Sol:**



$$MF_{AB} = -MF_{BA} = -\frac{Pl}{8} = -40 \times \frac{8}{8} = -40 \text{ kNm}$$

$$MF_{BC} = -MF_{CB} = -\frac{wl^2}{12} = -\frac{15 \times 8^2}{12} = -80 \text{ kNm}$$

$$M_{AB} = MF_{AB} + \frac{4EI}{l} \theta_A + \frac{2EI}{l} \theta_B - \frac{6EI}{l^2} \Delta = -40 + 0.25 EI \theta_B \quad (\theta_A = 0, \Delta = 0)$$

$$M_{BA} = 40 + \frac{4EI}{l} \theta_B + \frac{2EI}{l} \theta_A - \frac{6EI}{l^2} \Delta = 40 + 0.5EI \theta_B$$

$$M_{BC} = MF_{BC} + \frac{4EI}{l} \theta_B + \frac{2EI}{l} \theta_C - \frac{6EI}{l^2} \Delta = -80 + 0.5EI \theta_B + 0.25 \theta_C$$

$$M_{CB} = MF_{CB} + \frac{4EI}{l} \theta_C + \frac{2EI}{l} \theta_B - \frac{6EI}{l^2} \Delta = 80 + 0.25EI \theta_B + 0.5EI \theta_C$$

**55. Ans: (C)**

**Sol:** Weight mean

$$= 47^\circ 40' + \frac{40 \times 1 + 38 \times 2 + 37 \times 2}{1 + 2 + 2}$$

$$= 47^\circ 40' 38''$$

$$\therefore \text{variance } v_1 = 47^\circ 40' 40'' - 47^\circ 40' 38''$$

$$= 2''$$

$$v_2 = 47^\circ 40' 38'' - 47^\circ 40' 38''$$

$$= 0$$

$$v_3 = 47^\circ 40' 37'' - 47^\circ 40' 38''$$

$$= -1$$

Standard deviation:

$$\therefore \sigma_w = \pm \sqrt{\frac{\sum (wv)^2}{n-1}}$$

$$= \pm \sqrt{\frac{(1 \times 2)^2 + (2 \times (-1))^2}{3-1}} = \sqrt{\frac{8}{2}}$$

$$= \pm 2''$$

**56. Ans: (B)**

**Sol:** (so) is wrong because they mean the same.

**57. Ans: (C)**

**58. Ans: (A)**



**59. Ans: (D)**

**Sol:** Capacity of the tank =  $(12 \times 13.5) = 162$  litres

Capacity of each bucket = 9 litres.

Number of buckets needed =  $162/9 = 18$

**60. Ans: (D)**

**Sol:** Volume of Cuboid = length  $\times$  breadth  $\times$  height

Number of cuboids

$$= \frac{(\text{Volume of cuboids}) \text{ formed from}}{(\text{Volume of cuboids}) \text{ taken}}$$

$$= \frac{18 \times 15 \times 12}{5 \times 3 \times 2} = 108$$

**61. Ans: (B)**

**Sol: At the most case:** Let the numbers be  $\{-45, 1, 1, 1, \dots, 1\}$ .

Average is 0. So, at the most 44 numbers may be  $> 0$ .

**At the least case:** Let the numbers be  $\{45, -1, -1, -1, \dots, -1\}$ .

Average is 0. So, at the least 1 number may be  $> 0$ .

**62. Ans: (B)**

**Sol:** Perimeter = Distance covered in 8 min.

$$= 12000 \times \frac{8}{60} \text{ m} = 1600 \text{ m.}$$

Let length =  $3x$  metres and breadth =  $2x$  metres.

Then,  $2(3x + 2x) = 1600$  or  $x = 160$ .

$\therefore$  Length = 480 m and Breadth = 320 m

$\therefore$  Area =  $(480 \times 320) \text{ m}^2 = 153600 \text{ m}^2$

**63. Ans: B**

**Sol:** Consider CP as 100%.

Loss 15%  $\Rightarrow$  So, SP = 85%

Gain 15%  $\Rightarrow$  So, New SP = 115%

Given  $115\% - 85\% = 30\% = 450$

$$\frac{100}{30} \times 450 = 1500$$

**64. Ans: (A)**

**Sol:** GDP at the beginning of 2013 is equal to the GDP at the end of 2012

$\Rightarrow$  GDP growth rate in 2012 = 7%

GDP at the end of 2011 = GDP at the beginning of 2012 = \$1 trillion

$\therefore$  GDP at the beginning of 2013

$$= \frac{100 + 7}{100} \times 1 \text{ trillion}$$

$$= \frac{107}{100} = \$1.07 \text{ trillion}$$

**65. Ans: (A)**

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