## ESE- 2020 (Prelims) - Offline Test Series <br> Test- 3 <br> CIVIL ENGINEERING

## SUBJECT: STRUCTURAL ANALYSIS \& DESIGN OF STEEL STRUCTURES SOLUTIONS

## 01. Ans: (c)

Sol: Minimum thickness of web plate, when web plate is directly exposed to weather and accessible for cleaning and painting $\mathrm{t}_{\mathrm{w}}$ is 6 mm .

Plate girder with vertical stiffener, first and second horizontal stiffener are required as per IS800:1984 when the depth to thickness ratio of web is in between 250 to 400

$$
\begin{aligned}
250 & <\frac{\mathrm{d}_{2}}{\mathrm{t}_{\mathrm{w}}} \leq 400 \quad\left(\mathrm{t}_{\mathrm{w}}=6 \mathrm{~mm}\right) \\
\frac{\mathrm{d}_{2}}{\mathrm{t}_{\mathrm{w}}} & \leq 400 \\
\mathrm{~d}_{2} & \leq 400 \times \mathrm{t}_{\mathrm{w}} \\
& \leq 400 \times 6 \\
& \leq 2400 \mathrm{~mm}
\end{aligned}
$$

Maximum depth of web plate $\mathrm{d}_{2}=\mathrm{d}=2400 \mathrm{~mm}$

## 02. Ans: (d)

Sol: Stress due to concentric load $P$ is

$$
f_{a}=\frac{P}{A}=\frac{P}{L \times B}
$$

Bending stress due to bending moment M is

$$
\begin{aligned}
f_{b}= \pm \frac{M}{I} \times y & = \pm \frac{P \times e}{\frac{B \times L^{3}}{12}} \times \frac{L}{2} \\
& = \pm \frac{6 \times P \times e}{B \times L^{2}}
\end{aligned}
$$

Combined stress due to P and M is
$f_{a} \pm f_{b}=\frac{P}{L \times B} \pm \frac{6 \times P \times e}{B \times L^{2}}=\frac{P}{L \times B}\left(1 \pm \frac{6 \times e}{L}\right)$
Tensile stress below the base plate to be developed substantial, when e $>\mathrm{L} / 3$

## 03. Ans: (d)

Sol: When slope of roof $\theta>10^{0}$
The minimum live load on roof truss as per IS875

For roofs sloping $>\mathbf{1 0}^{\mathbf{0}}$
(i) For roof membrane, sheets or purlins: $750 \mathrm{~N} / \mathrm{m}^{2}$ less $20 \mathrm{~N} / \mathrm{m}^{2}$ for every degree increase in slope over $10^{\circ}$ subjected to a minimum of $400 \mathrm{~N} / \mathrm{m}^{2}$.

Note: The live load shall not be taken less than $400 \mathrm{~N} / \mathrm{m}^{2}$.

Live load per square meter area
$=750-20 \times\left(\theta-10^{0}\right)$ not less than $400 \mathrm{~N} / \mathrm{m}^{2}$
04. Ans: (a)

## Sol:


05. Ans: (d)


$$
\begin{aligned}
\text { Carry over factor }= & \frac{\text { Carry over moment }}{\text { Applied moment }} \\
& =\frac{\mathrm{M} / 2}{\mathrm{M}}=\frac{1}{2}
\end{aligned}
$$

6. Ans: (b)


Maximum compressible force

$$
=30\left[\frac{1}{2} \times 5.33 \times 0.29\right]=23.186 \mathrm{kN}
$$

## 07. Ans: (a)

Sol:

- Equilibrium of structure is considered in method of section.
- For pin-jointed plane frame, number of equilibrium equations are 3 i.e $\Sigma \mathrm{H}=0$, $\Sigma \mathrm{V}=0 \& \Sigma \mathrm{M}=0$
- Using these three equilibrium equations, we can find three unknowns at a time.

8. Ans: (a)

Sol: An increase in load ' $w$ ' will not increase the moment at the fixed end but will increase the moment in the beam as in a simply supported beam.

## 09. Ans: (d)

Sol: Span of pulin $l$ (i.e spacing of truss) $=4.5 \mathrm{~m}$

$$
=4500 \mathrm{~mm}
$$

Minimum leg with of angle purlin parallel to the slope of roof not less than $1 / 60$

$$
=4500 / 60=75 \mathrm{~mm}
$$

Minimum leg with of angle purlin normal to the slope of roof not less than $1 / 45$

$$
=4500 / 45=100
$$

## 10. Ans: (b)

Sol: Shear stress in weld due to concentric load $\mathrm{q}_{1}=50 \mathrm{MPa}$
Shear stress in weld due to due to in plane moment $\mathrm{q}_{2}=120 \mathrm{MPa}$
Fillet welded connection is designed for maximum resultant shear stress between $\mathrm{q}_{1}$ and $\mathrm{q}_{2}$ is $\mathrm{q}_{\mathrm{Rmax}}$ is maximum at top right corner of fillet weld group and $\theta=45^{\circ}$

$$
\begin{aligned}
\mathrm{q}_{\mathrm{R} \max } & =\sqrt{\mathrm{q}_{1}^{2}+\mathrm{q}_{1}^{2}+2 \times \mathrm{q}_{1} \times \mathrm{q}_{2} \cos \theta} \\
\mathrm{q}_{\mathrm{R} \max } & =\sqrt{50^{2}+120^{2}+2 \times 50 \times 120 \times \cos 45^{0}} \\
& =159.32 M P a \approx 160 \mathrm{MPa}
\end{aligned}
$$

## 11. Ans: (a)

Sol: Maximum free BM, M $=\frac{W a b}{L}$


Sum of fixed end moments

$$
\begin{aligned}
& =\frac{\mathrm{Wab}^{2}}{\mathrm{~L}^{2}}+\frac{\mathrm{Wa}^{2} \mathrm{~b}}{\mathrm{~L}^{2}} \\
& =\frac{\mathrm{Wab}}{\mathrm{~L}^{2}}[\mathrm{~b}+\mathrm{a}] \quad[\mathrm{L}=\mathrm{a}+\mathrm{b}] \\
& =\frac{\mathrm{Wab}}{\mathrm{~L}}=\mathrm{M}
\end{aligned}
$$

12. Ans: (b)

Sol: Beam mechanism


$$
\mathrm{P}_{\mathrm{u}} \times \mathrm{L} \theta=6 \mathrm{M}_{\mathrm{P}} \theta
$$

$$
P_{u}=\frac{6 M_{P}}{L}
$$

## 13. Ans: (c)

Sol:


Area under compression $=$ Area under tension
$4000+10(\mathrm{~h}-10)=10(510-\mathrm{h})$
$\mathrm{h}=60 \mathrm{~mm}$ from top
$510-60=450 \mathrm{~mm}$ from bottom

# SSC-JE (Paper-II) MAINS 2018 

## OFFLINE TEST SERIES

Streams: Civil | Electrical | Mechanical

* FULL LENGTH MOCK TEST-1

Exam Date: 01.12.2019
Exam Timing: 6:00 pm to 8:00 pm
2. FULL LENGTH MOCK TEST-2

Exam Date: 15.12.2019
Exam Timing: 6:00 pm to 8:00 pm
$\checkmark$ All tests will be conducted in Question Paper Booklet format.

- Test Series will be conducted at all our centres.


> (C) 040-48539866 / 040-40136222 testseries@aceenggacademy.com

# ISRO * <br> ONLINE TEST SERIES 

No. of Tests : 15
Subject Wise Tests : 12 | Mock Tests : 3
Indian Space Research Organisation (ISRO)
Recruitment of Scientist/Engineer 'SC'
ELECTRONICS | MECHANICAL | COMPUTER SCIENCE
『 starts from $5^{\text {th }}$ November 2019
All tests will be available till 12-01-2020.
(C) 040-48539866 / 040-40136222 « testseries@aceenggacademy.com

## 14. Ans: (c)

Sol: Design strength of bolt $\mathrm{V}_{\mathrm{db}}=60 \mathrm{kN}$
Critical bolt is one is farthest from C.G of bolt group and close to the applied load line, hence bolt 2 is critical.

Vertical shear force in each bolt due to P is
$\mathrm{F}_{\mathrm{a}}=\frac{\mathrm{P}}{\mathrm{n}}=\frac{\mathrm{P}}{4}=0.25 \mathrm{P}$
Shear force in critical bolt due to twisting moment is $\mathrm{F}_{\mathrm{m}, 2}=\frac{\mathrm{Mr}_{2}}{\sum \mathrm{r}^{2}}$
$r_{1}=r_{2}=r_{3}=r_{4}=120 / 2=60 \mathrm{~mm}$

$$
\mathrm{F}_{\mathrm{m}, 2}=\frac{\mathrm{P} \times 180 \times 60}{4 \times 60^{2}}=0.75 \mathrm{P}
$$

The maximum resultant shear force in bolt 2

$$
\text { is } \mathrm{F}_{\mathrm{Rmax}}=\mathrm{F}_{\mathrm{R} 2}=\mathrm{F}_{\mathrm{a}}+\mathrm{F}_{\mathrm{m} 2}
$$

$$
=0.25 \mathrm{P}+0.75 \mathrm{P}=\mathrm{P}
$$

For safety of critical bolt, the design criteria as per IS800, $\mathrm{F}_{\text {rmax }} \leq \mathrm{V}_{\mathrm{db}}$
Equating $\mathrm{F}_{\mathrm{rmax}}=\mathrm{V}_{\mathrm{db}}=60 \mathrm{kN}$
15. Ans: (c)

Sol: As per IS 875 Part 3 Wind Loads
$\mathrm{V}_{\mathrm{Z}}=$ Design wind velocity in $\mathrm{m} / \mathrm{sec}$ at a height z
$\mathrm{V}_{\mathrm{z}}=\mathrm{k}_{1} \cdot \mathrm{k}_{2} \cdot \mathrm{k}_{3} \cdot \mathrm{~V}_{\mathrm{b}}$
$\mathrm{k}_{1}=$ probability or risk factor
$\mathrm{k}_{2}=$ terrain, height and structure size factor.
$\mathrm{K}_{3}=$ topography factor .

## 16. Ans: (a)

Sol: Apply unit moment at 'A'


$$
\begin{aligned}
& \delta_{11}=\frac{L}{3 \mathrm{EI}} \\
& \delta_{21}=\frac{-\mathrm{L}}{6 \mathrm{EI}}
\end{aligned}
$$


$\delta_{21}=-\frac{L}{6 E I}$
$\delta_{22}=\frac{\mathrm{L}}{3 \mathrm{EI}}$
$\delta=\left[\begin{array}{cc}\frac{L}{3 E I} & -\frac{L}{6 E I} \\ \frac{-L}{6 E I} & \frac{L}{3 E I}\end{array}\right]$
17. Ans: (b)

Sol: Joint equilibrium equation at ' $B$ '

$$
\begin{aligned}
\mathrm{M}_{\mathrm{BA}} & +\mathrm{M}_{\mathrm{BC}}=0 \\
\mathrm{M}_{\mathrm{BA}} & =\mathrm{M}_{\mathrm{FBA}}+\frac{2 \mathrm{EI}}{\mathrm{~L}}\left[2 \theta_{\mathrm{B}}+\not \mathrm{A}_{\mathrm{A}}^{0}-\frac{3 \not \varnothing^{0}}{\mathrm{~L}}\right] \\
& =\frac{\mathrm{WL}}{8}+\frac{4 \mathrm{EI} \theta_{\mathrm{B}}}{\mathrm{~L}} \\
& =\frac{10 \times 4}{8}+\mathrm{EI} \theta_{\mathrm{B}} \\
\mathrm{M}_{\mathrm{BA}} & =5+\mathrm{EI} \theta_{\mathrm{B}} \\
\mathrm{M}_{\mathrm{BC}} & =\mathrm{M}_{\mathrm{FBC}}^{0}+\frac{2 \mathrm{EI}}{\mathrm{~L}}\left[2 \theta_{\mathrm{B}}+\not \mathrm{C}_{\mathrm{C}}^{0}-\frac{38}{\mathrm{~L}}\right]^{0} \\
& =\mathrm{EI} \theta_{\mathrm{B}}
\end{aligned}
$$

$$
\begin{aligned}
& \mathrm{M}_{\mathrm{BA}}+\mathrm{M}_{\mathrm{BC}}=0 \\
& 5+\mathrm{EI} \theta_{\mathrm{B}}+\mathrm{EI} \theta_{\mathrm{B}}=0 \\
& \theta_{\mathrm{B}}=\frac{-2.5}{\mathrm{EI}}
\end{aligned}
$$

## 18. Ans: (c)

Sol: Effective length about major axis

$$
\mathrm{KL}_{z z}=1.0 \times \mathrm{L}
$$

Effective length about minor axis

$$
\mathrm{KL}_{\mathrm{yy}}=0.5 \times \mathrm{L}
$$

Radius of gyration about minor axis

$$
\mathrm{r}_{\mathrm{zz}}=60 \mathrm{~mm}
$$

Radius of gyration about major axis

$$
\mathrm{r}_{\mathrm{yy}}=15 \mathrm{~mm}
$$

Limiting slenderness ratio of column (KL/r) $=180$

Effective slenderness ratio about minor axis $(0.5 \mathrm{~L} / 15)=180$
$\mathrm{L}=5400 \mathrm{~mm}=5.4 \mathrm{~m}$

## 19. Ans: (d)

Sol: Non dimensional effective slenderness ratio of steel column $\lambda=\sqrt{\frac{f_{y} \times\left(\frac{K L}{r}\right)^{2}}{\pi^{2} E}}$
$\lambda$ depends on material ( $\mathrm{f}_{\mathrm{y}}, \mathrm{E}$ ),
radius of gyration (cross sectional property)
$r_{\text {min }}=\sqrt{\frac{I_{\text {min }}}{A}}$

Effective length of column (end conditions) and unsupported length of column depends on lateral bracing)
20. Ans: (d)

Sol: Battens are used in built up column to join two column components together, so that the joined column components with battens behaves as a single steel component to shear the applied compressive load uniformly on components.
21. Ans: (b)

Sol: $\frac{\mathrm{C}}{\mathrm{r}_{\text {min }}} \ngtr 0.7 \frac{\mathrm{~kL}}{\mathrm{r}}$ of built up column
Where $\mathrm{C}=$ maximum spacing of batten of built up column

C $\ngtr 0.7 \times 25 \times 50$
$\mathrm{C} \ngtr 875 \mathrm{~mm}$
22. Ans: (b)

Sol: Restrain the structure initially in the given coordinate directions (1,2,3)


Given unit displacement in the direction of
(1)

$\Rightarrow \mathrm{P}=\frac{\mathrm{AE}}{\ell}$
$\mathrm{K}_{11}=\frac{\mathrm{AE}}{\ell}+\frac{12 \mathrm{EI}}{\ell^{3}}$
23. Ans: (d)

Sol: Effective length of fillet weld $\mathrm{L}_{\mathrm{w}}=200 \mathrm{~mm}$
$\mathrm{L}_{\mathrm{w} 1}+\mathrm{L}_{\mathrm{w} 2}=\mathrm{L}_{\mathrm{w}}=200 \mathrm{~mm}$
To have moment free welded connection, the C.G of weld group and C.G of load line must be on same line

Consider moment of weld section about C.G of weld group

$$
\left(\frac{\mathrm{P}_{1}}{\mathrm{P}_{2}}\right)=\left(\frac{\mathrm{L}_{\mathrm{w} 1}}{\mathrm{~L}_{\mathrm{w} 2}}\right)=\left(\frac{25}{100-25}\right)=\frac{1}{3}
$$

$$
\mathrm{L}_{\mathrm{w} 1}=0.5 \mathrm{~L}_{\mathrm{w} 2}---(2)
$$

From Equation (1) and Equation (2)
$\mathrm{L}_{\mathrm{w} 1}=50 \mathrm{~mm}$
$\mathrm{L}_{\mathrm{w} 2}=150 \mathrm{~mm}$
$\mathrm{L}_{\mathrm{w} 1} / \mathrm{Lw}^{2}=0.33$

## 24. Ans: (d)

Sol: Maximum tensile load $(\mathrm{P})=$ Safe tensile strength of main tie $\mathrm{P}_{\mathrm{t}}$
$\mathrm{P}_{\mathrm{t}}=\mathrm{A}_{\mathrm{net}} \times \sigma_{\mathrm{at}}=\mathrm{A}_{\mathrm{g}} \times \sigma_{\mathrm{at}}$
Permissible axial tensile stress

$$
\begin{aligned}
\sigma_{\mathrm{at}} & =1.33 \times 0.6 \mathrm{f}_{\mathrm{y}} \\
& =1.33 \times 0.6 \times 250=200 \mathrm{Mpa} \\
\mathrm{P}_{\mathrm{t}} & =2 \times 1150 \times 200=460000 \mathrm{~N}=460 \mathrm{kN}
\end{aligned}
$$

## 25. Ans: (a)

Sol: The tensile load carrying capacity of lug angle ( $\mathrm{P}_{\mathrm{l}}$ )
$\mathrm{P}_{l}=1.2 \times$ tensile strength of outstanding leg of an angle tie $=1.2 \times \mathrm{P}_{\mathrm{o}}$

$$
\begin{aligned}
\mathrm{P}_{\mathrm{o}} & =\mathrm{A}_{\mathrm{o}} \times \sigma_{\mathrm{at}} \\
& =(100-10 / 2) \times 10 \times 150=142.5 \times 10 \mathrm{~N} \\
& =142.5 \mathrm{kN} \\
\mathrm{P}_{l} & =1.2 \times \mathrm{P}_{\mathrm{o}}=1.2 \times 142.5=171 \mathrm{kN}
\end{aligned}
$$

26. Ans: (d)

Sol: $\mathrm{U}=\int_{0}^{\rho} \frac{\mathrm{M}^{2} \mathrm{dx}}{2 E I}$

$$
\begin{aligned}
& \mathrm{U}=\mathrm{U}_{\mathrm{AB}}+\mathrm{U}_{\mathrm{BC}} \\
& \mathrm{U}=\int_{0}^{\ell} \frac{\left(\frac{\mathrm{P} \ell}{2}\right)^{2} \mathrm{dx}}{2 \mathrm{EI}}+\int_{0}^{\ell / 2} \frac{(\mathrm{Px})^{2} \mathrm{dx}}{2 \mathrm{EI}} \\
& \mathrm{U}=\frac{7}{48} \frac{\mathrm{P}^{2} \ell^{3}}{\mathrm{EI}}
\end{aligned}
$$

## 27. Ans: (c)

## 28. Ans: (d)

Sol: For two hinged semicircular arch carrying a concentrated load W at crown, the horizontal thrust, $\mathrm{H}=\frac{\mathrm{W}}{\pi}$

H is independent of radius
Thus, the ratio is $1: 1: 1$
29. Ans: (b)
30. Ans: (d)

Sol: In bracket type connection, due to out plane beam reaction produces bending moment and concentric load on bolt group.
Concentric load causes shear force in bolt and bending moment is produces tensile force in bolt, hence bolt in a bolt group should be designed for shear force and tensile force.

## 31. Ans: (d)

Sol: Ratio of flexural strength of semi compact section to flexural strength of plastic section of steel beam in case of laterally restrained beam

$$
\begin{aligned}
\left(\frac{\mathbf{M}_{\mathrm{d}, \mathrm{~s}}}{\mathbf{M}_{\mathrm{d}, \mathrm{~s}}}\right) & =\left(\frac{\mathrm{Z}_{\mathrm{e}} \times \mathrm{f}_{\mathrm{y}} / \gamma_{\mathrm{m} 0}}{1.2 \times \mathrm{Z}_{\mathrm{e}} \times \mathrm{f}_{\mathrm{y}} / \gamma_{\mathrm{m} 0}}\right)=\left(\frac{1}{1.20}\right) \\
& =0.83
\end{aligned}
$$

## 32. Ans: (b)

Sol: Strength of rivets per pitch $\left(\mathrm{P}_{\mathrm{r}}\right)=\mathrm{n} \times$ Rivet
Value $=2 \times 45=90 \mathrm{kN}=90 \times 10^{3} \mathrm{~N}$
Nominal diameter of rivet $\phi=20 \mathrm{~mm}$
Gross diameter of rivet $d=20+1.5$

$$
=21.5 \mathrm{~mm}
$$

Tensile strength of plate per pitch

$$
\begin{aligned}
\mathrm{P}_{\mathrm{t}}=\mathrm{A}_{\mathrm{net}} \times \sigma_{\mathrm{at}} & =(\mathrm{p}-\mathrm{n} \times \mathrm{d}) \times \mathrm{t} \times \sigma_{\mathrm{at}} \\
& =(\mathrm{p}-1 \times 21.5) \times 10 \times 150
\end{aligned}
$$

To have maximum efficiency of riveted connection by equating $\mathrm{P}_{\mathrm{r}}=\mathrm{P}_{\mathrm{t}}$
$90 \times 10^{3}=(\mathrm{p}-1 \times 21.5) \times 10 \times 150$
Pitch $(\mathrm{p})=81.5 \mathrm{~mm} \approx 80 \mathrm{~mm}$
33. Ans: (c)

Sol: $\mathrm{DF}_{\mathrm{BA}}=\frac{\frac{4}{12}}{\frac{4}{12}+\frac{4}{12}}=0.5=\mathrm{DF}_{\mathrm{BC}}$
$\mathrm{DF}_{\mathrm{CB}}=\frac{\frac{4}{12}}{\frac{4}{12}+\frac{4}{8}}=0.4, \mathrm{DF}_{\mathrm{CD}}=0.6$
$\mathrm{FEM}_{\mathrm{BC}}=-\frac{10 \times 12^{2}}{12}=-120 \mathrm{kNm}$
$\mathrm{FEM}_{\mathrm{CD}}=\frac{-125 \times 8}{8}=-125 \mathrm{kNm}=-\mathrm{FEM}_{\mathrm{DC}}$

## 34. Ans: (b)

Sol: Displacement methods
(i) Slope deflection method
(ii) Stiffness method

Force methods
(i) Method of consistent deformation
(ii) Flexibility method
35. Ans: (d)

Sol: $\mathrm{D}_{\mathrm{s}}=\mathrm{r}-2=5-2=3$

36. Ans: (a)

Sol:


$$
\begin{aligned}
\mathrm{MF}_{\mathrm{AB}} & =-\mathrm{MF}_{\mathrm{BA}}=-\frac{\mathrm{w} \ell^{2}}{12}=-20 \times \frac{8^{2}}{12} \\
& =-106.67 \mathrm{kNm}
\end{aligned}
$$

$$
\mathrm{M}_{\mathrm{AB}}=\mathrm{MF}_{\mathrm{AB}}+\frac{4 \mathrm{EI}}{\mathrm{~L}} \theta_{\mathrm{A}}+\frac{2 \mathrm{EI}}{\mathrm{~L}} \theta_{\mathrm{B}}-\frac{6 \mathrm{EI}}{\mathrm{~L}^{2}} \Delta
$$

$$
=-106.67+\frac{\mathrm{EI}}{4} \theta_{\mathrm{B}} \quad\left(\text { as } \theta_{\mathrm{A}}=0, \Delta=0_{-}\right.
$$

$$
\mathrm{M}_{\mathrm{BA}}=\mathrm{MF}_{\mathrm{BA}}+\frac{2 \mathrm{EI}}{\mathrm{~L}} \theta_{\mathrm{A}}+\frac{4 \mathrm{EI}}{\mathrm{~L}} \theta_{\mathrm{B}}-\frac{6 \mathrm{EI}}{\mathrm{~L}^{2}} \Delta
$$

$$
=106.67+\frac{\mathrm{EI}}{2} \theta_{\mathrm{B}} \quad\left(\text { as } \theta_{\mathrm{A}}=0, \Delta=0\right)
$$

37. Ans: (b)
38. Ans: (b)

Sol:


Plastic section modulus of I section girder about minor axis $\left(\mathrm{Z}_{\mathrm{py}}\right)$

$$
\begin{aligned}
& Z_{p y}=b_{f} \times t_{f} \times \frac{b_{f}}{2} \times 2+\frac{t_{w}}{2\left(h-2 \times t_{f}\right)} \times \frac{t_{w}}{4} \times 2 \\
& Z_{p y}=b_{f} \times t_{f} \times b_{f}+t_{w} \times d \times \frac{t_{w}}{4} \\
& Z_{p y}=A_{f} \times b_{f}+\frac{A_{w}}{4} \times t_{w}
\end{aligned}
$$

[Area of flange $\left(A_{f}\right)=b_{f} \times t_{f}$ \& Area of web $\left.\left(A_{w}\right)=d \times t_{w}\right]$
39. Ans: (d)

Sol: The shear force is maximum near support, due to heavy support reaction, the web of plate girder is behaves as thin column and Due to maximum compressive stress at centre of web plate under heavy support reaction, the web plate of plate girder buckle vertically, such buckling is called bearing or vertical buckling of web plate
40. Ans: (d)

Sol:

$\mathrm{MF}_{\mathrm{AC}}=-\frac{\mathrm{Pab}^{2}}{\ell^{2}}=-\frac{36 \times 2 \times 4^{2}}{6^{2}}=-32 \mathrm{kNm}$
$\mathrm{MF}_{\mathrm{CA}}=+\frac{\mathrm{Pa}^{2} \mathrm{~b}}{\ell^{2}}=\frac{36 \times 2^{2} \times 4}{6^{2}}=16 \mathrm{kNm}$
$\mathrm{MF}_{\mathrm{CD}}=-\mathrm{MF}_{\mathrm{DC}}=-\frac{\mathrm{w} \ell^{2}}{12}=-\frac{6 \times 6^{2}}{12}=-18 \mathrm{kNm}$

$$
\begin{aligned}
& \mathrm{MF}_{\mathrm{DB}}=-\mathrm{MF}_{\mathrm{BD}}=-\frac{12 \times 6^{2}}{12}=-36 \mathrm{kNm} \\
& \begin{aligned}
& \mathrm{M}_{\mathrm{AC}}=\mathrm{M}_{\mathrm{FAC}}+\frac{2 \mathrm{EI}}{\mathrm{~L}}\left(2 \not \theta_{\mathrm{A}}+\theta_{\mathrm{C}}\right) \\
&=-32+\frac{2 \mathrm{EI}}{6} \theta_{\mathrm{C}} \\
&=-32+\frac{\mathrm{EI}}{3} \theta_{\mathrm{C}} \\
& \begin{aligned}
\mathrm{M}_{\mathrm{DB}} & =-36+\frac{2 \mathrm{EI}}{6}\left(2 \theta_{\mathrm{D}}\right) \\
& =-36+\frac{2 \mathrm{EI} \theta_{\mathrm{D}}}{3}
\end{aligned}
\end{aligned} . \begin{array}{l}
\text { ( }
\end{array}
\end{aligned}
$$

41. Ans: (c)

Sol: The condition for maximum shear force due to wheel loads shall be place as shown in figure (i.e one of the wheel load on should be placed at support)


Taking moment about support B

$$
\begin{aligned}
\mathrm{R}_{\mathrm{A}} & \times 8=200 \times 8+200 \times(8-3) \\
\mathrm{R}_{\mathrm{A}} & =\frac{[200 \times 8+200 \times(8-3)}{8} \\
& =325 \mathrm{kN}
\end{aligned}
$$

## 42. Ans: (c)

Sol:


Hence the kinematic indeterminacy $=11$
43. Ans: (d)
$15 \mathrm{kN} / \mathrm{m}$
Sol:
Sol:

$$
\begin{aligned}
& \mathrm{MF}_{\mathrm{AB}}=-\mathrm{MF}_{\mathrm{BA}} \\
&=-\frac{\mathrm{P} \ell}{8}=-40 \times \frac{8}{8}=-40 \mathrm{kNm} \\
& \mathrm{MF}_{\mathrm{BC}}=-\mathrm{MF}_{\mathrm{CB}}
\end{aligned}=-\frac{\mathrm{w} \ell^{2}}{12}=-\frac{15 \times 8^{2}}{12}=-80 \mathrm{kNm}
$$

$$
\mathrm{M}_{\mathrm{AB}}=\mathrm{MF}_{\mathrm{AB}}+\frac{4 \mathrm{EI}}{\ell} \theta_{\mathrm{A}}+\frac{2 \mathrm{EI}}{\ell} \theta_{\mathrm{B}}-\frac{6 \mathrm{EI}}{\ell^{2}} \Delta
$$

$$
=-40+0.25 \operatorname{EI} \theta_{\mathrm{B}} \quad\left(\theta_{\mathrm{A}}=0, \Delta=0\right)
$$

$$
\mathrm{M}_{\mathrm{BA}}=40+\frac{4 \mathrm{EI}}{\ell} \theta_{\mathrm{B}}+\frac{2 \mathrm{EI}}{\ell} \theta_{\mathrm{A}}-\frac{6 \mathrm{EI}}{\ell^{2}} \Delta=40+0.5 \mathrm{EI} \theta_{\mathrm{B}}
$$

$$
\mathrm{M}_{\mathrm{BC}}=\mathrm{MF}_{\mathrm{BC}}+\frac{4 \mathrm{EI}}{\ell} \theta_{\mathrm{B}}+\frac{2 \mathrm{EI}}{\ell} \theta_{\mathrm{C}}-\frac{6 \mathrm{EI}}{\ell^{2}} \Delta
$$

$$
=-80+0.5 \mathrm{EI} \theta_{\mathrm{B}}+0.25 \theta_{\mathrm{C}}
$$

$$
\mathrm{M}_{\mathrm{CB}}=\mathrm{MF}_{\mathrm{CB}}+\frac{4 \mathrm{EI}}{\ell} \theta_{\mathrm{C}}+\frac{2 \mathrm{EI}}{\ell} \theta_{\mathrm{B}}-\frac{6 \mathrm{EI}}{\ell^{2}} \Delta
$$

$$
=80+0.25 \mathrm{EI} \theta_{\mathrm{B}}+0.5 \mathrm{EI} \theta_{\mathrm{C}}
$$

44. Ans: (c)

Sol: The slenderness of a tension member to be limited as per IS800, to take care stress reversals, to control the self weight of deflections and to prevent lateral vibrations
45. Ans: (b)

Sol: Limiting slenderness ratio of compression
flange $\left(\frac{\mathrm{KL}}{\mathrm{r}_{\text {min }}}\right)=250$
Effective length of rigidly supported beam
$\mathrm{KL}=0.65 \mathrm{~L}=\mathrm{L}$
Minimum radius of gyration $r_{\text {min }}=r_{y y}$ $=10.4 \mathrm{~mm}$
$\frac{\mathrm{KL}}{\mathrm{r}_{\text {min }}}=\frac{\mathrm{KL}}{\mathrm{r}_{\mathrm{yy}}}=250$
$\frac{0.65 \mathrm{~L}}{\mathrm{r}_{\mathrm{yy}}}=250$
$\mathrm{L}=\frac{250 \times 10.4}{0.65}=4000 \mathrm{~mm}$
46. Ans: (b)

Sol:
D


$$
\begin{aligned}
& \mathrm{K}_{\mathrm{AD}}=\frac{4(\mathrm{EI})}{\mathrm{L}}, \mathrm{~K}_{\mathrm{AB}}=\frac{4(4 \mathrm{EI})}{\mathrm{L}}, \mathrm{~K}_{\mathrm{AC}}=\frac{4(5 \mathrm{EI})}{\mathrm{L}} \\
& \therefore \mathrm{~K}=\mathrm{K}_{\mathrm{AD}}+\mathrm{K}_{\mathrm{AB}}+\mathrm{K}_{\mathrm{AC}}=\frac{40 \mathrm{EI}}{\mathrm{~L}} \\
& \therefore \mathrm{DF}_{\mathrm{AB}}=\frac{\mathrm{K}_{\mathrm{AB}}}{\mathrm{~K}}=0.4
\end{aligned}
$$

## 47. Ans: (b)

Sol: $\mathrm{K}_{\mathrm{OA}}=\frac{4 \mathrm{EI}}{\mathrm{L}} \rightarrow$ Far End fixed

$$
\mathrm{K}_{\mathrm{OB}}=\frac{3 \mathrm{EI}}{\mathrm{~L}} \rightarrow \text { Far End pinned }
$$

## For OD:



No moment can be resisted by OD as can be seen
$\therefore \mathrm{K}_{\mathrm{OD}}=0$

## For OC:



Applying 1st moment + Area theorem

$$
\theta_{\mathrm{C}}-\theta_{\mathrm{O}}=\frac{\mathrm{ML}}{\mathrm{EI}} \text {, but } \theta_{\mathrm{C}}=0
$$

$\therefore\left|\theta_{\mathrm{O}}\right|=\frac{\mathrm{ML}}{\mathrm{EI}} \quad \Rightarrow \mathrm{M}=\frac{\mathrm{EI}}{\mathrm{L}}\left|\theta_{\mathrm{O}}\right|$
$\therefore \mathrm{K}_{\mathrm{OC}}=\frac{\mathrm{EI}}{\mathrm{L}}$
Hence $\mathrm{DF}_{\mathrm{OA}}=\frac{4}{4+3+1+0}=0.5$
48. Ans: (d)

Sol: $\mathrm{DF}_{\mathrm{BA}}=\frac{\frac{3(2)}{6}}{\frac{3(2)}{6}+\frac{3}{4}}=\frac{4}{7}$
$\mathrm{DF}_{\mathrm{BC}}=\frac{3}{7}$
$\mathrm{FEM}_{\mathrm{AB}}=-\mathrm{FEM}_{\mathrm{BA}}=-60$
$\mathrm{FEM}_{\mathrm{BC}}=-33.75$
$\mathrm{FEM}_{\mathrm{CB}}=11$

|  | AB | BA | BC | CB |
| :---: | :---: | :---: | :---: | :---: |
| DF |  | $4 / 7$ | $3 / 7$ |  |
| FFM | -60 | 60 | -33.75 | 11.25 |
| Dist | 60 | -15 | -11.25 | -11.25 |
| C.O |  | 30 | -5.625 |  |
| Dist |  | -13.93 | -10.45 |  |
|  | 0 | 61.1 | -61.1 | 0 |

Balance at exterior hinge support
49. Ans: (c)

Sol: There are number of advantages of bolted joints over riveted joints. The noise nuisance, the preheating of rivets, the labour cost, replacement of faulty rivet and for same strength lesser number of bolts, minimum erection time and overall cost of bolted joint is minimum.
50. Ans: (d)

Sol: Under axial loads fillet welds, slot and plug weld are generally designed for shear stresses only and but welds are designed for axial stresses.
51. Ans: (d) 52. Ans: (c)
53. Ans: (a)

Sol:

| 1 | 2 | 3 |
| :---: | :---: | :---: |
| 4 | 5 | 6 |
| 7 | 8 | 9 |
| 10 | 11 | 12 |
|  |  |  |

Total number of support reactions

$$
=3+2+1+3=9
$$

$\therefore$ Degree of external indeterminacy

$$
=9-3=6
$$

Number of closed loops in the structure $=12$
$\therefore$ Degree of internal indeterminacy

$$
\begin{aligned}
& =3 \mathrm{C}[\mathrm{C}=\text { no of closed loops }] \\
& =3 \times 12=36
\end{aligned}
$$

Hence degree of static indeterminacy

$$
=6+36=42
$$

## 54. Ans: (c)

Sol: Effective length of fillet weld
$\mathrm{L}_{\mathrm{w}}=2 \times 100+75=275 \mathrm{~mm}$

Effective throat thickness
$\mathrm{t}_{\mathrm{t}}=\mathrm{K} \times \mathrm{S}=0.7 \times 6=4.2 \mathrm{~mm}$
Design force $\mathrm{P}=$ Design Shear strength of fillet weld $\left(\mathrm{P}_{\mathrm{dw}}\right)$

$$
\begin{aligned}
& P=P_{d w}=\frac{L_{w} \times t_{t} \times f_{u}}{\sqrt{3} \times \gamma_{m w}} \\
&=\frac{275 \times 4.2 \times 410}{\sqrt{3} \times 1.25}=218.72 \times 10^{3} \mathrm{~N} \\
&=218.72 \mathrm{kN}
\end{aligned}
$$

55. Ans: (c)

Sol: number of nodes $=13$
degrees of freedom per node $=2$
no. of restraints $=3$
K. $1=13 \times 2-3$

$$
=26-3=23
$$


56. Ans: (a)

Sol: The Williot - Mohr diagram is a graphical method to obtain an approximate value for displacement of a structure which submitted to certain load.

## 57. Ans: (a)

Sol: $m=5, r=4, j=4$
$D_{\text {si }}=m-2 \mathrm{j}+3=0$
$\mathrm{D}_{\text {se }}=\mathrm{r}-3=1$
$\mathrm{D}_{\mathrm{s}}=0$
Horizontal reactions $\left(\mathrm{H}_{\mathrm{B}}\right)$ at B will be taken as redundant
$+\rightarrow$ Tensile
$-\rightarrow$ Compressive
Due to External Load:


Due to Unit Load:


$$
\mathrm{H}_{\mathrm{B}}=-\frac{\Sigma \mathrm{N}_{\mathrm{n}} \mathrm{~L}}{\Sigma \mathrm{n}^{2} \mathrm{~L}}=-\frac{0}{0}=0 \mathrm{kN}
$$

58. Ans: (b)

Sol: When low percentage of carbon added to iron with other elements the yield stress of steel, ultimate tensile stress of steel and hardness of steel is lesser and ductility of steel \& toughness of steel is increased. Hence option (b) is correct.

# TEST YOUR PREP IN A REAL TEST ENVIRONMENT 

## Pre GAIJ - 2020

## Date of Exam : 18 ${ }^{\text {th }}$ January 2020 Last Date to Apply: 31 ${ }^{\text {st }}$ December 2019

Highlights:

- Get real-time experience of GATE-20 test pattern and environment
- Virtual calculator will be enabled.
- Post exam learning analytics and All India Rank will be provided.
- Post GATE guidance sessions by experts.
- Encouraging awards for GATE-20 toppers.


# SSC-JE (Paper-I) <br> OOnline Test Series 

Staff Selection Commission - Junior Engineer
No. of Tests : 20
Subject Wise Tests: 16|Mock Tests-4
Civil|Electrical|Mechanical

## AVAILABLE NOW

All tests will be available till SSC 2019 Examination
59. Ans: (d)

Sol: Permissible tensile stress of steel as per IS 800:1984 $\sigma_{a t}=0.6 \mathrm{f}_{\mathrm{y}}$
Permissible average stress of steel as per IS800:1984 $\tau_{\mathrm{vf}}=0.4 \mathrm{f}_{\mathrm{y}}$
The ratio of permissible axial tensile stress to average shear stress $=\frac{0.6 f_{y}}{0.4 f_{y}}=1.5$
60. Ans: (b)

Sol: $m=6, r 3, j=4$
$D_{s i}=m-2 j+3=6-8+3=1$
$\mathrm{D}_{\text {se }}=\mathrm{r}-3=3-3=0$
$\mathrm{D}_{\mathrm{s}}=1$
61. Ans: (c)

Sol: Here, $\quad m=11, r=3, j=6$
$\mathrm{D}_{\mathrm{si}}=\mathrm{m}-2 \mathrm{j}+3=11-12+3=2$
$\mathrm{D}_{\mathrm{se}}=\mathrm{r}-3=3-3=0$
$\mathrm{D}_{\mathrm{s}}=2+0=2$
Hence, statically indeterminate to degree 2.
62. Ans: (a)
63. Ans: (d)

Sol: $\mathrm{V}_{\mathrm{A}}+\mathrm{V}_{\mathrm{B}}=100 \mathrm{t}$
For right part ' BC '
$V_{B} \times 10=50 \times 5+\mathrm{H} \times 5$
For part 'AC'
$\mathrm{V}_{\mathrm{A}} \times 10=5 \times 10 \times 5+\mathrm{H} \times 5$
From equation (1) $+(2)$
$\mathrm{V}_{\mathrm{B}} \times 10=250+\mathrm{H} \times 5$
$\mathrm{V}_{\mathrm{A}} \times 10=250+\mathrm{H} \times 5$
$\left(\mathrm{V}_{\mathrm{A}}+\mathrm{V}_{\mathrm{B}}\right) \times 10=500+\mathrm{H} \times 10$
$100 \times 10=500+\mathrm{H} \times 10$
$H=50 t$

64. Ans: (d)

Sol:
$+\mathrm{n} \Sigma \mathrm{M}_{\left.\mathrm{Z}\right|_{\mathrm{E}}}=0$
$\mathrm{V}_{\mathrm{A}} \times 16=20 \times 12+40 \times 8+20 \times 4$
$\mathrm{V}_{\mathrm{A}}=40 \mathrm{kN}$
Taking section as per figure

$+\mathrm{n} \Sigma \mathrm{M}_{\mathrm{A}}=0$
$\left(\mathrm{F}_{\mathrm{FC}} \cos 45^{\circ}\right) \times 4+\left(\mathrm{F}_{\mathrm{FC}} \sin 45^{\circ}\right) \times 4+20 \times$ $4=0$
or, $\quad \mathrm{F}_{\mathrm{FC}}=-14.14 \mathrm{kN}$
As the truss is symmetric one,
Then, $\quad \mathrm{F}_{\mathrm{CG}}=\mathrm{F}_{\mathrm{CF}}$

$$
=-14.14 \mathrm{kN} \text { (compressive) }
$$

Joint C:

$\mathrm{F}_{\mathrm{CH}}+\mathrm{F}_{\mathrm{CG}} \sin 45+\mathrm{F}_{\mathrm{CF}} \sin 45=40$
$\mathrm{F}_{\mathrm{CH}}=60 \mathrm{kN}$ (Tensile)
65. Ans: (c)


Here, $m=7, r=3, j=5$
$\mathrm{D}_{\mathrm{si}}=\mathrm{m}-2 \mathrm{j}+3=7-10+3=0$
$\mathrm{D}_{\text {se }}=\mathrm{r}-3=3-3=0$
$\mathrm{D}_{\mathrm{s}}=0 \quad$ statically determinate
$\stackrel{+}{\uparrow} \Sigma \mathrm{F}_{\mathrm{Y}}=0 \quad \mathrm{~V}_{\mathrm{A}}=8+8=16 \mathrm{kN}$
$+\mathrm{n} \Sigma \mathrm{M}_{\left.\mathrm{Z}\right|_{\mathrm{A}}}=0$
$\mathrm{H}_{\mathrm{E}} \times 3-8 \times 3-8 \times 6=0$ or, $\mathrm{H}_{\mathrm{E}}=24 \mathrm{kN}$
$\mathrm{H}_{\mathrm{A}}=-24 \mathrm{kN}$

Joint A:

$\mathrm{F}_{\mathrm{AD}} \sin \theta=16$

$$
\mathrm{F}_{\mathrm{AD}}=\frac{16}{\sin 45}=22.627 \mathrm{kN}(\text { Tensile })
$$

66. Ans: (a)

Sol: For short joint lengths force in bolt in the bolted joint will be redistributed due to plastic action and the bolt will share the load equally. However in long joint, the shear distribution is non uniform, bolt at ends of the joint are forced more under tension, it may lead to failure of joint called unbuttoning.
67. Ans: (a)

Sol: It is assumed that the strength of longitudinal fillet welds and transverse fillet weld is same. Actually the strength of the transverse fillet weld is more than the longitudinal fillet weld, because a transverse fillet weld is stresses more uniformly for full length.

## HEARTY CONGRATULATIONS <br> TO OUR ESE - 2019 TOP RANKERS



## TOTAL SELECTIONS in Top 10: 33

(EE: 9, E\&T: 8, ME: 9, CE: 7) and many more...


# DIGITAL CLASSES for <br> ESE 2020/2021 General Studies \& Engineering Aptitude 

68. Ans: (c)

Sol: Generally gantry girder are designed as laterally unsupported beam unless the compression flange beam is laterally supported by either by catwalk or additional member (such girder is laterally supported gantry girder). Such arrangement increases the cost of girder and not provided to be economical.
69. Ans: (c)

Sol: Block shear failure of tension member at end of connection along path involving tension on one plane and shear on the perpendicular plane due to smaller length of connection for use of higher grade bolts.
70. Ans: (a) 71. Ans: (b)

## 72. Ans: (a)

Sol: Excessive deformation may create problems for roof drainage and they may cause twisting and distortion of connection and connected members and lead to high secondary stresses
73. Ans: (a)
74. Ans: (a)

Sol: Fillet weld closure to the minimum size of the weld are economical for the same strength. It is because the volume of material required for large size weld for the same strength will be several times of that required for smaller size
75. Ans: (c)

Sol: Statement I is true but statement II false.

