



ESE | GATE | PSUs



ELECTRICAL ENGINEERING

ELECTRICAL & ELECTRONIC MEASUREMENTS

Text Book : Theory with worked out Examples
and Practice Questions

Chapter 3 Electrical & Electronic Measurements

Solutions for Text Book Practice Questions

1. Error Analysis, Units & Standards

Solutions for Objective Practice Questions

01. Ans: (b)

$$\begin{aligned}\text{Sol: } \% \text{ LE} &= \frac{\text{FSV}}{\text{true value}} \times \% \text{GAE} \\ &= \frac{200 \text{ V}}{100 \text{ V}} \times \pm 2\% = \pm 4\%\end{aligned}$$

02. Ans: (d)

Sol: Variables are measured with accuracy
 $x = \pm 0.5\%$ of reading 80 (limiting error)
 $Y = \pm 1\%$ of full scale value 100
 (Guaranteed error)
 $Z = \pm 1.5\%$ reading 50 (limiting error)
 The limiting error for Y is obtained as guaranteed
 $\text{Error} = 100 \times (\pm 1/100) = \pm 1$
 Then % L.E in Y meter
 $20 \times \frac{x}{100} = \pm 1$
 $x = 5\%$
 Given $w = xy/z$, Add all %L.E s
 Therefore $= \pm (0.5\% + 5\% + 1.5\%)$
 $= \pm 7\%$

03. Ans: (d)

$$\begin{aligned}\text{Sol: } W_T &= W_1 + W_2 \\ &= 100 - 50 = 50 \text{ W} \\ \frac{\partial W_T}{\partial W_1} &= \frac{\partial W_T}{\partial W_2} = 1\end{aligned}$$

$$\text{Error in meter 1} = \pm \frac{1}{100} \times 100 = \pm 1 \text{ W}$$

$$\text{Error in meter 2} = \pm \frac{0.5}{100} \times 100 = \pm 0.5 \text{ W}$$

$$W_T = W_1 + W_2 = 50 \pm 1.5 \text{ W}$$

$$W_T = 50 \pm 3\%$$

04. Ans: (a)

Sol: For 10V total input resistance

$$R_v = \frac{V_{\text{fsd}}}{I_{\text{m fsd}}} = 10/100\mu\text{A} = 10^5 \Omega$$

$$\begin{aligned}\text{Sensitivity} &= R_v/V_{\text{fsd}} = 10^5/10 \\ &= 10\text{k}\Omega/\text{V}\end{aligned}$$

$$\text{For } 100\text{V } R_v = 100/100\mu\text{A} = 10^6 \Omega$$

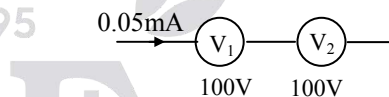
$$\begin{aligned}\text{Sensitivity} &= R_v/V_{\text{fsd}} = 10^6/100 \\ &= 10\text{ k}\Omega/\text{V}\end{aligned}$$

(or)

$$\text{Sensitivity} = \frac{1}{I_{\text{fsd}}} = \frac{1}{100 \times 10^{-6}} = 10\text{ k}\Omega/\text{V}$$

05. Ans: 150 V

Sol:



$$\begin{aligned}V_1 : & & V_2 : \\ S_{\text{dc1}} &= 10\text{ k}\Omega/\text{V} & S_{\text{dc2}} &= 20\text{ k}\Omega/\text{V}\end{aligned}$$

$$\begin{aligned}I_{\text{fsd}} &= \frac{1}{S_{\text{dc1}}} & I_{\text{fsd}} &= \frac{1}{S_{\text{dc2}}} \\ &= 0.1\text{mA} & &= 0.05\text{mA}\end{aligned}$$

The maximum allowable current in this combination is 0.05mA, since both are connected in series.

Maximum D.C voltage can be measured as

$$\begin{aligned}
 &= 0.05 \text{ mA } (10 \text{ k } \Omega/\text{V} \times 100 + 20 \text{ k } \Omega/\text{V} \times 100) \\
 &= 3000 \times 0.05 \\
 &= 150 \text{ V}
 \end{aligned}$$

06.

Sol: Internal impedance of 1st voltmeter

$$= \frac{100 \text{ V}}{5 \text{ mA}} = 20 \text{ k } \Omega$$

$$\begin{aligned}
 \text{Internal impedance of 2nd voltmeter} \\
 &= 100 \times 250 \text{ } \Omega/\text{V} = 25 \text{ k } \Omega
 \end{aligned}$$

$$\begin{aligned}
 \text{Internal impedance of 3rd voltmeters,} \\
 &= 5 \text{ k } \Omega
 \end{aligned}$$

$$\begin{aligned}
 \text{Total impedance across 120 V} \\
 &= 20 + 25 + 5 \\
 &= 50 \text{ k } \Omega
 \end{aligned}$$

$$\text{Sensitivity} = \frac{50 \text{ k } \Omega}{120 \text{ V}}$$

$$= 416.6 \text{ } \Omega/\text{V}$$

\Rightarrow Reading of 1st voltmeter

$$= \frac{20 \text{ k } \Omega}{416.6 \text{ } \Omega/\text{V}}$$

$$= 48 \text{ V}$$

Reading of 2nd voltmeter

$$= \frac{25 \text{ k } \Omega}{416.6 \text{ } \Omega/\text{V}}$$

$$= 60 \text{ V}$$

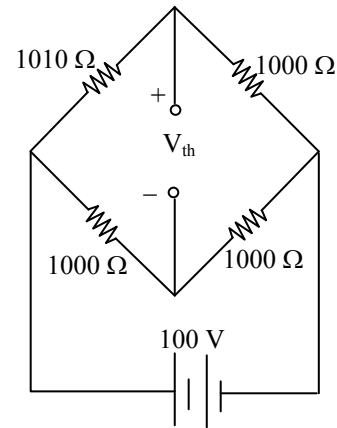
Reading of 3rd voltmeter

$$= \frac{5 \text{ k } \Omega}{416.6 \text{ } \Omega/\text{V}}$$

$$= 12 \text{ V}$$

07. **Ans: (b)**

$$\begin{aligned}
 \text{Sol: Bridge sensitivity} &= \frac{\text{Change in output}}{\text{Change in input}} \\
 &= \frac{V_{th}}{10 \text{ } \Omega}
 \end{aligned}$$



$$V_{th} = \frac{1010 \times 100}{2000} - \frac{1000 \times 100}{2000} = 0.25 \text{ V}$$

$$S_B = \frac{0.25 \text{ V}}{10 \text{ } \Omega} = 25 \text{ mV/ } \Omega$$

08. **Ans: (b)**

$$\text{Sol: Resolution} = \frac{200}{100} \times \frac{1}{10} = 0.2 \text{ V}$$

09. **Ans: (i) 41.97 (ii) 0.224 (iii) ± 0.1513**

$$\begin{aligned}
 \text{Sol: Mean } (\bar{X}) &= \frac{\sum x}{n} \\
 &= \frac{41.7 + 42 + 41.8 + 42 + 42.1 + 41.9 + 42.5 + 42 + 41.9 + 41.8}{10} \\
 &= 41.97
 \end{aligned}$$

$$SD = \sqrt{\frac{\sum d_n^2}{n-1}} \quad \text{for } n < 20 \quad d_n = \bar{X} - X_n$$

$$\begin{aligned}
 &\sqrt{\frac{(0.27)^2 + (-0.03)^2 + (-0.17)^2 + (-0.03)^2 + (-0.13)^2 + (0.07)^2 + (-0.53)^2 + (-0.03)^2 + (-0.13)^2 + (0.17)^2}{10-1}} \\
 &= 0.224
 \end{aligned}$$

$$\begin{aligned}
 \text{Probable error} &= \pm 0.6745 \times SD \\
 &= \pm 0.1513
 \end{aligned}$$

10. **Ans: (c)**

$$\begin{aligned}
 \text{Sol: Power} &= I^2 R = (2)^2 (100) \\
 &= 400 \text{ W}
 \end{aligned}$$

$$\% \text{ Error} = \pm \left[2 \left(\frac{\partial P}{\partial I} \right) + \frac{\partial P}{\partial R} \right] \times 100$$

$$= \pm 2 (1) \pm 0.2$$

$$= \pm 2.2\%$$

$$\text{Error} = \pm \frac{2.2}{100} \times 400$$

$$= \pm 8.8 \text{ W}$$

11. Ans: (c)

Sol: $R_T = R_1 + R_2 = 36 + 75 = 111 \Omega$

$$\Delta R_T = \left(\frac{5}{100} \times 36 \right) + \left(\frac{5}{100} \times 72 \right)$$

$$= 5.55 \Omega$$

$$R_T = 111 \pm 5.55 \Omega$$

12. Ans: (a)

Sol: $R = \frac{V}{I}$

$$\frac{\Delta R}{R} \times 100 = \frac{\Delta V}{V} \times 100 + \frac{\Delta I}{I} \times 100$$

$$\frac{\Delta R}{R} \times 100 = 2\% + 1\%$$

$$= 3\%$$

Solutions for Conventional Practice Questions

01.

Sol: (a) Sensitivity $|_{25^\circ\text{C}} = \frac{3.0 - 1.5}{100 - 50} = 30 \mu\text{m/kg}$

$$\text{Sensitivity}|_{40^\circ\text{C}} = \frac{3.5 - 1.9}{100 - 50} = 32 \mu\text{m/kg}$$

(b) Zero Drift = $0.3\text{mm} - 0\text{mm} = 0.3\text{mm}$

$$\text{Sensitivity Drift} = 32 \mu\text{m/kg} - 30 \mu\text{m/kg}$$

$$= 2 \mu\text{m/kg}$$

(c) zero Drift co-efficient = $\frac{0.3\text{mm}}{40^\circ\text{C} - 25^\circ\text{C}}$

$$= 20.0 \mu\text{m}/^\circ\text{C}$$

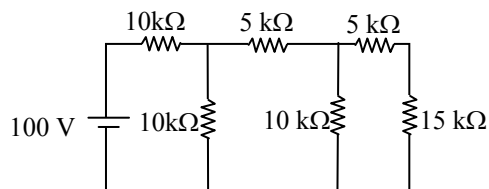
Sensitivity Drift co-efficient

$$= \frac{2 \mu\text{m/kg}}{40^\circ\text{C} - 25^\circ\text{C}}$$

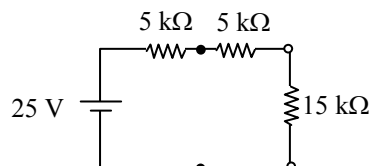
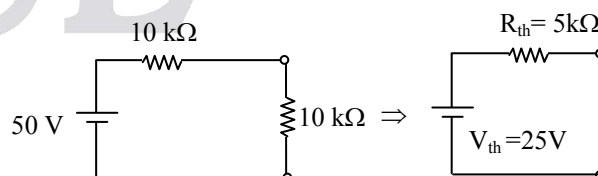
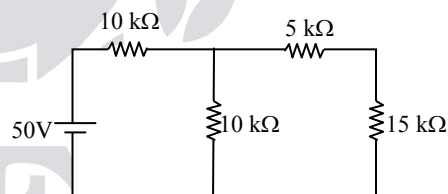
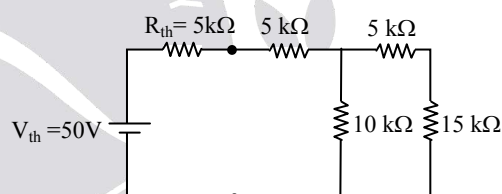
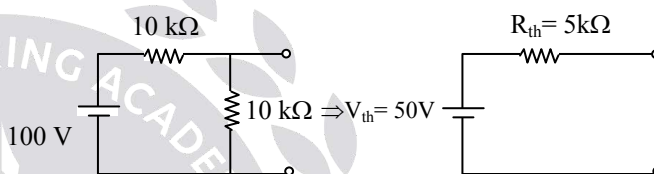
$$= 0.133 \mu\text{m/kg}/^\circ\text{C}$$

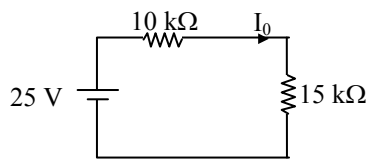
02.

Sol:



Using circuit minimizing techniques

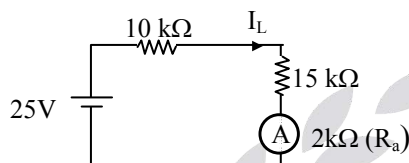




Value of current in 15kΩ

$$(I_0) = \frac{25V}{10k\Omega + 15k\Omega}$$

$$I_0 = 1 \text{ mA}$$



(A) reading (I_L)

$$= \frac{25V}{10k\Omega + 15k\Omega + 2k\Omega} = 926\mu A$$

$$I_L = 99\% I_0 \text{ (from the question data)}$$

$$I_L = 0.99 I_0, \quad I_L = \frac{1}{1 + \frac{R_a}{R_{ckt}}} I_0$$

$$\frac{I_L}{I_0} = \frac{1}{1 + \frac{R_a}{(10k + 15k\Omega)}}$$

$$\Rightarrow 0.99 = \frac{1}{1 + \frac{R_a}{25k\Omega}}$$

$$R_a = 250 \Omega$$

03. Ans: (a)

Sol: Accuracy → It indicates degree of closeness of measured value to the True value.

Precision: → Indicates the degree of closeness of measured values by an instrument for a fixed input quantity.

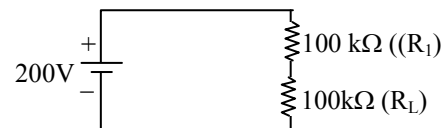
Sensitivity (s) → $\frac{\text{Change in output}}{\text{Change in input}}$

Unit of sensitivity depends on type of Instrument

For voltmeter sensitivity defined as $\frac{1}{I_{fsd}} \Omega/V$

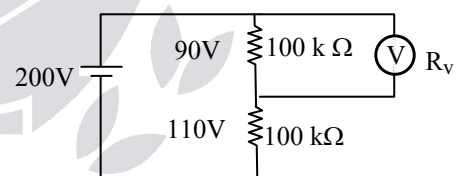
03. (b)

Sol:



$$V_{R1} = 200V \times \frac{100k\Omega}{100k + 100k} = 100V$$

A voltmeter when connected across either of two 100kΩ resistors (say upper one) acts as shunt for the portion of circuit. The voltmeter will then indicate a lower voltage drop than actually existed before the voltmeter was connected. This happens because of loading effect & mainly occurs with low sensitivity of Instrument. Assume voltmeter resistance as R_v .



Voltmeter Indication is '90 V'

$$R_{eq} = 100 \text{ k}\Omega // R_v = \frac{100k\Omega \times R_v}{100k\Omega + R_v}$$

$$R_{Total} = (R_{eq} + 100) \text{ k}\Omega,$$

Voltage division

$$90V = 200V \times \frac{R_{eq}}{100 + R_{eq}}$$

$$R_{eq} = 81.8 \text{ k}\Omega$$

$$R_{eq} = \frac{100k\Omega \times R_v}{100k\Omega + R_v}$$

$$\Rightarrow 81.8 \text{ k}\Omega = \frac{100\text{k}\Omega \times R_v}{100\text{k}\Omega + R_v}$$

$$R_v = 450 \text{ k}\Omega$$

04.
Sol: Ranges:

$$(A) \rightarrow (0 - 5) \text{ A}$$

$$(V) \rightarrow (0 - 250\text{V})$$

$$(W) \rightarrow (0 - 500 \text{ W})$$

Meter reading

$$I = 2.5\text{A} \pm 0.5\% \text{ fsd}$$

$$\Rightarrow I = 2.5 \pm 1\% \text{ of reading}$$

$$V = 115\text{V} \pm 0.5\% \text{ fsd}$$

$$\Rightarrow V = 115\text{V} \pm 1.086\% \text{ reading}$$

$$W = 220 \text{ W} \pm 1\% \text{ fsd}$$

$$\Rightarrow W = 220\text{W} \pm 2.27\% \text{ reading}$$

$$\cos\phi = \frac{P}{VI}$$

$$\ln \cos\phi = \ln p - \ln v - \ln I$$

$$\frac{1}{\cos\phi} = \frac{1}{P} \cdot \frac{dp}{d\cos\phi} - \frac{1}{V} \cdot \frac{dv}{d\cos\phi} - \frac{1}{I} \cdot \frac{dI}{d\cos\phi}$$

$$\frac{\Delta \cos\phi}{\cos\phi} = \frac{\Delta P}{P} - \frac{\Delta V}{V} - \frac{\Delta I}{I}$$

$$\frac{\Delta \cos\phi}{\cos\phi} \times 100 = \frac{\Delta P}{P} \times 100 + \frac{\Delta V}{V} \times 100 + \frac{\Delta I}{I} \times 100$$

$$= 2.27\% + 1.086\% + 1\%$$

$$= 4.356\% \rightarrow \text{max. uncertainty}$$

05.
Sol: Expected value (A_T) = 20mA

 Measured value (A_m) = 18mA

$$\text{i) Absolute error} = A_m - A_T = 2\text{mA}$$

$$\text{ii) Percentage error} = \frac{A_m - A_T}{A_T} \times 100 = -10\%$$

$$\text{iii) Relative Accuracy} = 1 - |\text{error}|$$

$$= 1 - |0.1| = 0.9$$

$$\text{iv) Percentage Accuracy} = 0.9 \times 100 = 90\%$$

 v) Precision of 6th measurement

$$(X_n = X_6) = 18\text{mA}$$

$$\% P = \left(1 - \left| \frac{X_n - \bar{X}}{\bar{X}} \right| \right) \times 100$$

$$\text{Avg}(\bar{X}) = \frac{(16 + 19 + 20 + 17 + 21 + 18 + 15 + 16 + 18 + 17) \text{ mA}}{10}$$

$$= 17.7 \text{ mA}$$

$$\% P = \left(1 - \left| \frac{18\text{mA} - 17.7\text{mA}}{17.7\text{mA}} \right| \right) \times 100$$

$$= 98.3\%$$

06.

$$\text{Sol: Absolute error} = 1.14 \text{ k}\Omega - 1.2 \text{ k}\Omega$$

$$= -0.06 \text{ k}\Omega$$

$$\text{Absolute error} = 1.26 \text{ k}\Omega - 1.2 \text{ k}\Omega$$

$$= 0.06 \text{ k}\Omega$$

$$\text{Tolerance} = \pm 0.06 \text{ k}\Omega$$

Maximum resistance at 25°C is 1.26 kΩ

Temperature coefficient = +500 PPM/°C

 Let $R_1 = 1.26 \text{ k}\Omega$ at 25°C

$$= \frac{+500}{1,000,000} \times 1.26 \text{ k}\Omega = +0.63 \text{ }\Omega/\text{°C}$$

$$\text{Change in temperature } (\Delta T) = 75^\circ\text{C} - 25^\circ\text{C}$$

$$= 50^\circ\text{C}$$

The maximum resistance at 75°C

$$= 1.26 \text{ k}\Omega + 0.63 \text{ }\Omega/\text{°C} \times 50^\circ\text{C}$$

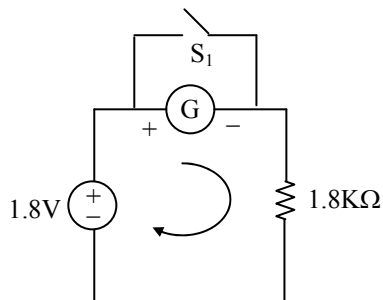
$$= 1.291 \text{ k}\Omega$$

2. Basics of Electrical Instruments

Solutions for Objective Practice Questions

01. Ans: (d)
Sol: The pointer swings to 1 mA and returns, settles at 0.9 mA i.e, pointer has oscillations. Hence,

the meter is under-damped. Now the current in the meter is 0.9 mA.



Applying KVL to circuit,

$$1.8 \text{ V} - 0.9 \text{ mA} \times R_m - 0.9 \text{ mA} \times 1.8 \text{ k}\Omega = 0$$

$$1.8 \text{ V} - 0.9 \times 10^{-3} R_m - 1.62 = 0$$

$$R_m = \frac{0.18}{0.9 \times 10^{-3}} = 200 \Omega$$

02. Ans: 32.4° and 21.1°

Sol: $I_1 = 5 \text{ A}$, $\theta_1 = 90^\circ$; $I_2 = 3 \text{ A}$, $\theta_2 = ?$

$\theta \propto I^2$ (as given in Question)

(i) Spring controlled

$$\theta \propto I^2$$

$$\frac{\theta_2}{\theta_1} = \left(\frac{I_2}{I_1} \right)^2$$

$$\Rightarrow \frac{\theta_2}{90} = \left(\frac{3}{5} \right)^2$$

$$\theta_2 = 32.4^\circ$$

(ii) Gravity controlled

$$\sin \theta \propto I^2$$

$$\frac{\sin \theta_2}{\sin \theta_1} = \left(\frac{I_2}{I_1} \right)^2$$

$$\frac{\sin \theta_2}{\sin 90} = \left(\frac{3}{5} \right)^2$$

$$\Rightarrow \frac{\sin \theta_2}{1} = 0.36$$

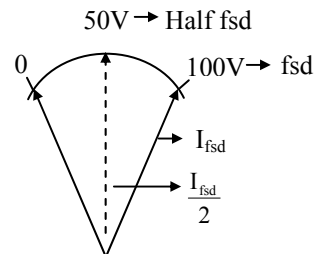
$$\theta_2 = \sin^{-1} (0.36) = 21.1^\circ$$

3. Electromechanical Indicating Instruments

Solutions for Objective Practice Questions

01. Ans: (c)

Sol:



$$S = \frac{1}{1000} \Omega / \text{volt}$$

$$S = \frac{1}{I_{\text{fsd}}} \Omega / \text{V}$$

$$I_{\text{fsd}} = \frac{1}{S} = \frac{1}{1000} = 1 \text{ mA}$$

$$100 \text{ V} \rightarrow 1 \text{ mA}$$

$$50 \text{ V} \rightarrow ? = 0.5 \text{ mA}$$

02. Ans: (a)

Sol:

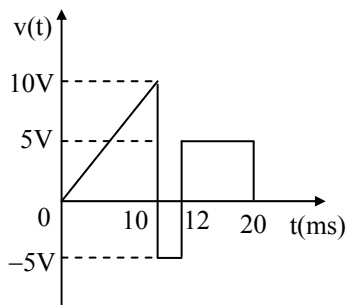
	1°C↑	10°C	T_c	θ
Spring stiffness(K_c)	0.04%↓	0.4%↓	0.4%↓	0.4%↑
			T_d	θ
Strength of magnet (B)	0.02%↓	0.2%↓	0.2%↓	0.2%↓

$$\text{Net deflection } (\theta_{\text{net}}) = 0.4\% \uparrow - 0.2\% \downarrow = 0.2\% \uparrow$$

Increases by 0.2%

03. Ans: (a)

Sol:



PMMC meter reads Average value

$$V_{\text{avg}} = \frac{\left(\frac{1}{2} \times 10 \times 10\text{ms}\right) + (-5\text{V} \times 2\text{ms}) + (5\text{V} \times 8\text{ms})}{20\text{ms}}$$

$$= \frac{50 - 10 + 40}{20} = 4\text{V}$$

(or)

$$\begin{aligned} \text{Avg. value} &= \frac{1}{20} \left[\int_0^{10} (1)t \, dt - \int_{10}^{12} 5 \, dt + \int_{12}^{20} 5 \, dt \right] \\ &= \frac{1}{20} \left[\left[\frac{t^2}{2} \right]_0^{10} - 5[t]_{10}^{12} + 5[t]_{12}^{20} \right] \\ &= 4\text{V} \end{aligned}$$

04. Ans: 3.6 MΩ

Sol: $V_m = (0 - 200)\text{V}$; $S = 2000\text{ Ω/V}$

$$V = (0 - 2000)\text{V}$$

$$\begin{aligned} R_m &= S \times V_m \\ &= 2000\text{ Ω/V} \times 200\text{V} \\ &= 400000\text{ Ω} \end{aligned}$$

$$\begin{aligned} R_{\text{se}} &= R_m \left(\frac{V}{V_m} - 1 \right) \\ &= 400000 \left(\frac{2000}{200} - 1 \right) \\ &= 3.6\text{ MΩ} \end{aligned}$$

05. Ans: (c)

$$\text{Sol: } T_d = \frac{1}{2} I^2 \frac{dL}{d\theta}$$

$$K_c \theta = \frac{I^2}{2} \frac{dL}{d\theta}$$

$$25 \times 10^{-6} \times \theta = \frac{25}{2} \times \left(3 - \frac{\theta}{2} \right) \times 10^{-6}$$

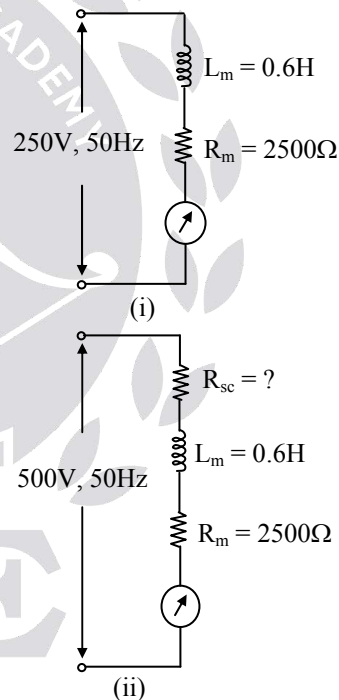
$$2\theta = 3 - \frac{\theta}{2}$$

$$\frac{5}{2} \theta = 3$$

$$\theta = 1.2\text{ rad}$$

06. Ans: 2511.5 Ω

Sol:



Current is same in case (i) & (ii)

In case (i),

$$\begin{aligned} I_m &= \frac{250\text{V}}{\sqrt{R_m^2 + (\omega L_m)^2}} \\ &= \frac{250\text{V}}{\sqrt{(2500)^2 + (2\pi \times 50 \times 0.6)^2}} = 0.0997\text{ A} \end{aligned}$$

In case (ii),

$$I_m = \frac{250 \text{ V}}{\sqrt{(R_m + R_{se})^2 + (\omega L_m)^2}}$$

$$0.0997 \text{ A} = \frac{500 \text{ V}}{\sqrt{(2500 + R_{se})^2 + (2\pi \times 50 \times 0.6)^2}}$$

$$\sqrt{(2500 + R_{se})^2 + 35.53 \times 10^3} = \frac{500}{0.0997}$$

$$\sqrt{(2500 + R_{se})^2 + 35.53 \times 10^3} = 5.015 \times 10^3$$

$$R_{se} = 2511.5 \Omega$$

07. Ans: 0.1025 μF

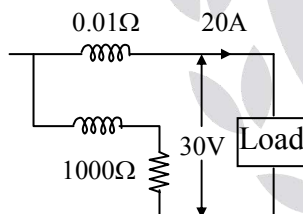
Sol: $C = \frac{0.41 L_m}{R_{se}^2}$

$$C = \frac{0.41 \times 1}{(2 \text{ k}\Omega)^2}$$

$$= 0.1025 \mu\text{F}$$

08. Ans: (c)

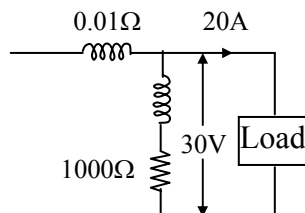
Sol: MC – connection



Error due to current coil

$$= \frac{20^2 \times 0.01}{(30 \times 20)} \times 100 = 0.667\%$$

LC – connection



Error due to potential coil

$$= \frac{(30^2 / 1000)}{(30 \times 20)} \times 100$$

$$= 0.15\%$$

As per given options, 0.15% high

09. Ans: (c)

Sol: $R_{load} = \frac{V}{I}$

$$= \frac{200}{20} = 10 \Omega$$

For same error $R_L = \sqrt{R_C \times R_V}$

$$\therefore 100 = 10 \times 10^3 \times R_C$$

$$\Rightarrow R_C = 0.01 \Omega$$

10. Ans (d)

Sol: From Δ le $\tan \beta = \frac{X_p}{r_p} = \frac{2\pi \times 50 \times 0.5}{1000} = 0.157$

$$\tan \beta = 0.157$$

$$\cos \phi = 0.7$$

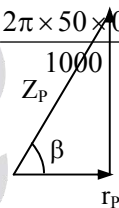
$$\phi = \cos^{-1}(0.7)$$

$$\tan \phi = \tan [\cos^{-1}(0.7)] = 1.02$$

$$\therefore \% \text{ error} = + (\tan \phi \times \tan \beta \times 100)$$

$$= + (1.02 \times 0.157 \times 100)$$

$$= 16\%$$



11. Ans: (a)

Sol: $i(t) = 3 + 4\sqrt{2} \sin 314t$

PMMC reads average value.

$$\therefore \text{Average value} = 3 \text{ A}$$

12. Ans: (b)

Sol: Hot wire ammeter reads RMS value

$$I_{rms} = \sqrt{2^2 + \left(\frac{4}{\sqrt{2}}\right)^2}$$

$$= 3.46 \text{ A}$$

13. Ans: (d)

Sol: Moving Iron Ammeter, $\theta \propto I^2$

For 1 A dc $\rightarrow 20^\circ$

$I_1 = 1 \text{ A}$, $\theta_1 = 20^\circ$

For $3 \sin 314 t \rightarrow ?$

MI Ammeter measures the rms value of AC current

$$I_2 = \frac{I_m}{\sqrt{2}} = \frac{3}{\sqrt{2}}, \quad I_2 = \frac{3}{\sqrt{2}}, \quad \theta_2 = ?$$

$$\frac{\theta_2}{\theta_1} = \frac{I_2^2}{I_1^2}$$

$$\frac{\theta_2}{20} = \frac{(3/\sqrt{2})^2}{(1)^2}$$

$$\Rightarrow \theta_2 = 90^\circ$$

14. Ans: (a)

Sol: $V_{dc} = I_{dc} \times 10 \Omega$

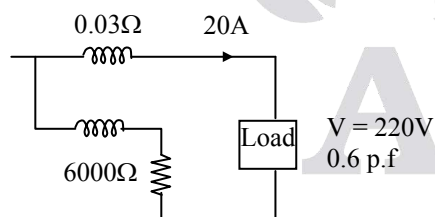
$$= \left(\frac{12+5}{2} \right) \times 10$$

$$= 85 \text{ V}$$

15. Ans: (b)

Sol: Given that,

$R_c = 0.03 \Omega$, $R_p = 6000 \Omega$



$$\% \text{ Error} = \frac{I_L^2 r_c}{VI \cos \phi} \times 100$$

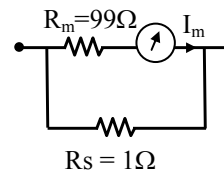
$$= \frac{20^2 \times 0.03}{220 \times 20 \times 0.6} \times 100$$

$$= 0.45\%$$

Solutions for Conventional Practice Questions

01.

Sol:



(a) $I_m = I_{fsd} = 0.1 \text{ mA}$

* Voltage across instrument $= I_m R_m$

$$= 0.1 \text{ mA} \times 99 \Omega$$

$$= 9.9 \text{ mV}$$

* $I_{sh} = \frac{9.9 \text{ mV}}{1 \Omega} = 9.9 \text{ mA}$

* $I_{total} = I = I_m + I_{sh} = 10 \text{ mA}$

(b) $I_m = 0.5 I_{fsd}$

$$= 0.5 \times 0.1 \text{ mA} = 0.05 \text{ mA}$$

* voltage across instrument

$$= I_m R_m = 0.05 \times 99 \text{ mV}$$

$$= 4.95 \text{ mV}$$

$$I_{sh} = \frac{4.95 \text{ mV}}{1 \Omega} = 4.95 \text{ mA}$$

$$I_{total} = 0.05 + 4.95 = 5 \text{ mA}$$

(c) $0.25 I_{FSD} = I_m = 0.25 \times 0.1 = 0.025 \text{ mA}$

Voltage across instrument

$$= I_m R_m = 2.475 \text{ mV}$$

$$I_{sh} = \frac{2.475}{1 \Omega} = 2.475 \text{ mA}$$

$$I = I_m + I_{sh} = 2.5 \text{ mA}$$

02.

Sol: Voltage across instrument for full scale deflection $= 100 \text{ mV}$.

Current in instrument for full scale

deflection, $I = \frac{V}{R} = \frac{100 \times 10^{-3}}{20} = 5 \times 10^{-3} \text{ A}$

Deflecting torque, $T_d = BINA = BIN(\ell \times d)$

$$= 100 \times B \times 30 \times 10^{-3} \times 25 \times 10^{-3} \times 5 \times 10^{-3}$$

$$= B \times 375 \times 10^{-6}$$

\therefore Controlling torque for a deflection $\theta = 120^\circ$

$$T_c = K\theta = 0.375 \times 10^{-6} \times 120$$

$$= 45 \times 10^{-6} \text{ N-m}$$

At final steady position, $T_d = T_c$

$$\text{or } 375 \times 10^{-6} \times B = 45 \times 10^{-6}$$

\therefore Flux density in the air gap,

$$B = \frac{45 \times 10^{-6}}{375 \times 10^{-6}} = 0.12 \text{ Wb/m}^2$$

Resistance of coil winding, $R_c = 0.3 \times 20 = 6 \Omega$

Length of mean turn

$$l = 2(L+d) = 2(30+25) = 110 \text{ mm}$$

Let a be the area of cross-section of wire and P be the resistivity

Resistance of coil, $R_c = N \rho / a$

\therefore Area of cross-section of wire

$$a = \frac{100 \times 1.7 \times 10^{-8} \times 110 \times 10^{-3}}{6} \times 10^6$$

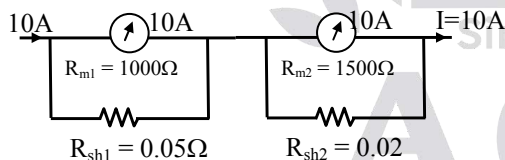
$$= 31.37 \times 10^{-3} \text{ mm}^2$$

$$\text{Diameter of wire, } d = \left[\left(\frac{4}{\pi} \right) (31.37 \times 10^{-3}) \right]^{\frac{1}{2}}$$

$$= 0.2 \text{ mm}$$

03.

Sol:



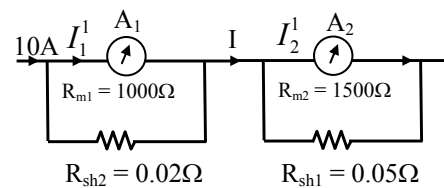
(Fig) with normal connections load is kept constant

$$I_1 = 10 \text{ A} \times \frac{0.05\Omega}{1000 + 0.05}$$

$$= 4.999 \times 10^{-4} = 0.5 \text{ mA}$$

$$I_2 = 10 \text{ A} \times \frac{0.02}{1500 + 0.02} = 1.333 \times 10^{-4}$$

$$= 0.133 \text{ mA}$$



With shunt connections interchanged

$$I_1^1 = 10 \text{ A} \times \frac{0.02}{1000 + 0.02} = 0.199 \text{ mA}$$

$$I_2^1 = 10 \text{ A} \times \frac{0.05}{1500 + 0.05} = 0.33 \text{ mA}$$

$$0.49 \text{ mA} \rightarrow 10 \text{ A}$$

$$0.19 \text{ mA} \rightarrow ?$$

$$\Rightarrow A_1 = \frac{0.19}{0.49} \times 10 = 3.87 \text{ A}$$

$$0.13 \text{ mA} \rightarrow 10 \text{ A}$$

$$0.33 \text{ mA} \rightarrow ?$$

$$\Rightarrow A_2 = \frac{0.33 \text{ mA}}{0.13 \text{ mA}} \times 10 \text{ A} = 25.38 \text{ A}$$

04.

Sol: (a) The internal resistance of 5Ω is due to copper only

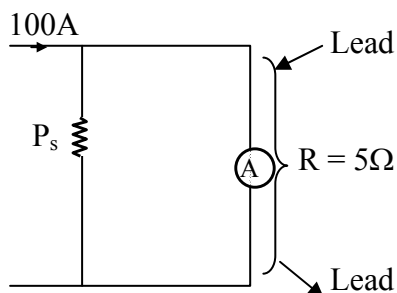
(b) A 4Ω manganin swamping resistor is used in series with a copper resistor of 1Ω . Assume the temperature coefficient of copper as $0.004 \text{ ohm}/^\circ\text{C}$ and that of manganin $0.00015 \text{ ohm}/^\circ\text{C}$

(c) When the whole of the 5Ω constitute the resistance in the copper of the instrument coil and lead as shown in the figure.

$$\text{Instrument current} = 0.015 \text{ A}$$

$$\therefore \text{shunt current} = 100 - 0.015$$

$$= 99.985 \text{ A}$$



PD across the shunt = 0.015×5

$$= 0.075 \text{ V}$$

$$\therefore \text{Shunt resistance} = \frac{0.075}{99.985}$$

$$= 0.00075 \, \Omega \text{ (manganin wire)}$$

Then the shunt resistance at 10°C temperature rise

$$= 0.00075 \times (1 + 10 \times 0.00015)$$

$$= 0.000751 \, \Omega$$

The instrument resistance after 10°C rise in temperature

$$= 5 \times (1 + 10 \times 0.004)$$

$$= 5.2\Omega$$

The instrument current corresponding to 100 A input. In inverse proportion to the resistance forming the parallel circuit, A and B will be.

$$= \frac{0.000751}{5.20075} \times 100 = 0.01444\text{A}$$

and the instrument reading

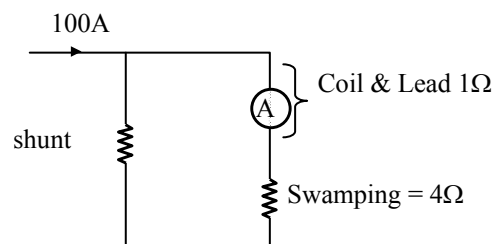
$$= \frac{100}{0.015} \times 0.01444 = 96.27 \text{ A}$$

\therefore Percentage error due to temperature rise

$$= 100 - 96.27 \text{ or } 3.73\% (10 \text{ W})$$

(b) The connections in this case are as shown
resistance of the instrument $\rightarrow 100\Omega$

Circuit after 10°C rise in temperature



$$= 1 \times (1 + 10 \times 0.004) + 4 \times (1 + 10 \times 0.00015)$$

$$= 5.046 \, \Omega$$

The shunt resistance after 10°C rise in temperature is still the same, that is 0.000751Ω

Instrument current corresponding to 100A
input

$$= \frac{0.000751}{5.046751} \times 100 = 0.01488\%$$

And the instrument reading

$$= \frac{100}{0.015} \times 0.01488 = 99.2 \text{ A}$$

\therefore Percentage error due to the temperature rise

$$= 100 - 99.2 \text{ or } 0.8\% (10W)$$

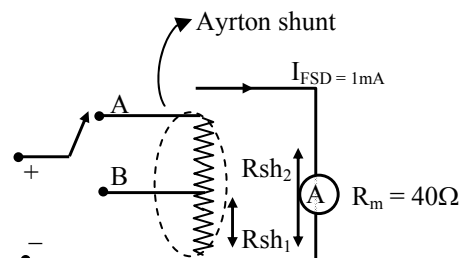
[This shows the great advantage of using a swamping resistance in parallel with the shunt]

05.

Sol: $R_m = 40\Omega$, $I_{FSD} = 1\text{mA}$

(0 - 10mA)

$$R_{sh1} = \frac{R_m}{m-1} = \frac{40}{\left(\frac{10mA}{1mA} - 1\right)} = 4.44\Omega$$



* (0–50mA)

$$R_{sh} = \frac{R_m + R_{sh1}}{M_2} = \frac{40\Omega + 4.44}{50\text{mA}/1\text{mA}} = 0.88\Omega$$

06.

Sol: $L = (10 + 50 - 2\theta^2) \mu\text{H}$

$$\frac{dL}{d\theta} = (5 - 4\theta) \mu\text{H per radian and also}$$

$$\frac{dL}{d\theta} = \frac{2K\theta}{I^2}$$

$$\therefore (5 - 4\theta) \times 10^{-6} = \frac{2k\theta}{I^2}$$

Substituting $\theta = 30^\circ$ or $\frac{\pi}{6}$ radian and

$I = 5\text{A}$ in above expression, we have

$$\left[5 - 4 \times \frac{\pi}{6} \right] \times 10^{-6} = \frac{2k \times \frac{\pi}{6}}{(5)^2}$$

Or $K = 69.36 \times 10^{-6} \text{ N-m/radian}$

i.e., spring constant

$$= 69.36 \times 10^{-6} \text{ Nm/radian Ans}$$

Substituting $I = 10\text{A}$ and $K = 69.36 \times 10^{-6}$ in Equation (i) we have

$$(5 - 4\theta) \times 10^{-6} = \frac{2 \times 69.36 \times 10^{-6}}{10^2} \theta$$

Or $\theta = 0.928$ radian or 53.2° Ans

07.

Sol: It is given that

$$I = 4\theta^n$$

And we know that

$$\frac{dL}{d\theta} = \frac{2K\theta}{I^2} = \frac{2K\theta}{4^2 \theta^{2n}} = \frac{1}{8} k\theta^{1-2n}$$

Integrating above expression we have

$$L = \frac{k\theta^{2-2n}}{8(2-2n)} + A = \frac{k\theta^{2-2n}}{16(1-n)} + A \dots\dots(i)$$

Where A is constant of integration

When $I = 0$, deflection $\theta = 0$ and $L = 10 \times 10^{-3}$ or 0.01H

Substituting $I = 0$, $\theta = 0$

And $L = 0.01\text{H}$ in Equation (1) we have

$$0.01 = 0 + A$$

$$\text{or } A = 0.01$$

Substituting $A = 0.01$ in Equation (i) we have L

$$= \frac{k}{16(1-n)} \theta^{2-2n} + 0.01$$

$$= \frac{0.6}{16(1-n)} \theta^{2-2n} + 0.01 \text{ Ans}$$

[$\therefore K = 0.6 \text{ N-m/rad}$]

(ii) substituting $n = 0.75$ in above expression we have

$$L = \frac{0.6}{16(1-0.75)} \theta^{(2-2 \times 0.75)} + 0.01$$

$$= 0.15\theta^{0.5+0.01}$$

Substituting $L = 60 \times 10^{-3}$ or 0.06 in above expression we have

$$0.06 = 0.15 \theta^{0.5} + 0.01 \text{ or}$$

$$\text{deflection, } \theta = \left[\frac{0.05}{0.15} \right]^2$$

$$= 0.111 \text{ radian or } 6.37^\circ \text{ Ans}$$

$$\text{Current, } I = 4\theta^n = 4(0.111)^{0.75}$$

$$= 0.769 \text{ A}$$

08.

Sol: Current drawn by instrument when connected across 300 V ac

$$I_{ac} = 100\text{mA} = 0.1\text{A}$$

At 50 Hz supply Instrument reactance,

$$X_L = 2\pi fL = 2\pi \times 50 \times 0.8 = 251.33 \Omega$$

$$= \frac{200.7 - 200}{200} \times 100 = 0.35\% \text{ Ans}$$

09.

Sol: The deflecting torque, $T_d = \frac{1}{2} I^2 \frac{dL}{d\theta}$

$I = 1.4$ and 1.6 , about 1.5 on either side,

$$\text{then } \frac{dL}{d\theta} = \frac{577.8 - 576.6}{61.5 - 49.5}$$

$$= \frac{1.2}{12} = 0.1 \times 10^{-6} \text{ H/deg}$$

$$\text{Or } 0.1 \times 57.3 = 5.73 \times 10^{-6} \text{ H/rad}$$

$$\text{and } T_d = \frac{1}{2} \times 1.5^2 \times 5.73 \times 10^{-6}$$

$$= 6.44 \times 10^{-6} \text{ Nm}$$

10.

Sol: The rate of change of mutual inductance is

$$\frac{dM}{d\theta} = \frac{k\theta}{I^2} = \frac{0.1 \times 10^{-6} \times 110}{(10)^2}$$

$$= 0.11 \times 10^{-6} \text{ H/rad}$$

$$= 0.00192 \mu \text{ H/degree}$$

Final inductance = initial inductance + change in

$$\text{inductance} = 2.0 + 0.00192 \times 110 = 2.21 \mu \text{ H}$$

11

Sol: (i) 1. Frictional Error (Torque/weight):

- Potential coil has more number of turns so weight of moving coil is more.
- Then it has more frictional error as compared to M.C and M.I

2. Temperature Error:

- Because of presence of two coils net heat developed is more. Then temperature error is more as compared to other Instruments.

3. Frequency error:

- When it is used as a voltmeter (or) ammeter Net Inductance is more then the frequency error is more
- But when used as a wattmeter, inductance is very less, so frequency error is low.

Hysteresis & Eddy current error:

- Because of the use of air core, the hysteresis and eddy current errors are almost zero.
- Both fixed coil & moving coils are electro magnet so poor magnetic field is present
- The external magnetic field can easily distort the inside operating field. Hence stray magnetic field is more as compared to other types of metets.

Note: For portable wattmeter, to reduce the stray magnetic field error; iron shielding is used.

- For precision wattmeters, to reduce stray magnetic field error, static system is used. In this, two set of fixed coil and moving coils are used.

$$\text{(ii). } I(t) = 80 - 60\sqrt{2} \sin(\omega t + 30^\circ) \text{ A}$$

Dynamo Ammeter \rightarrow rms

$$\Rightarrow I_{\text{rms}} = \sqrt{\frac{1}{2\pi} \int_0^{2\pi} i^2 d\theta}$$

$$i^2 = 80^2 - (60\sqrt{2})^2 \sin^2\left(\theta + \frac{\pi}{6}\right) - 9600\sqrt{2}$$

$$\sin\left(\theta + \frac{\pi}{6}\right)$$

$$= 6400 - 7200 \sin^2\left(\theta + \frac{\pi}{6}\right) - 13576.4502$$

$$\sin\left(\theta + \frac{\pi}{6}\right)$$

$$= 6400 + 7200 \left[\frac{1 - \cos 2\left(\theta + \frac{\pi}{6}\right)}{2} \right]$$

$$- 13576.4502 \sin\left(\theta + \frac{\pi}{6}\right)$$

$$\Rightarrow DA = I_{\text{rms}}^2 = \sqrt{\frac{1}{2\pi} \int_0^{2\pi} i^2 d\theta}$$

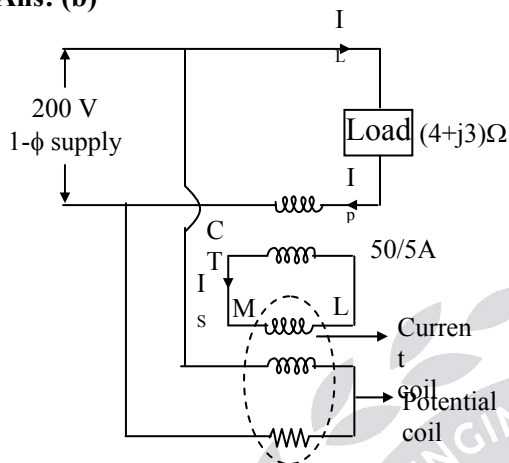
$$= 100 \text{ A}$$

4. Measurement of Power

Solutions for Objective Practice Questions

01. Ans: (b)

Sol:



Potential coil voltage = 200 V

C.T. primary current (I_p)

$$I_p = I_L = \frac{200 \text{ V}}{\sqrt{4^2 + 3^2} \tan^{-1}\left(\frac{3}{4}\right)}$$

$$I_p = I_L = \frac{200 \text{ V}}{5 \angle 36.86^\circ}$$

$$I_p = 40 \angle -36.86^\circ$$

$$\frac{I_p}{I_s} = \frac{50}{5}$$

$$\frac{40}{I_s} = \frac{50}{5}$$

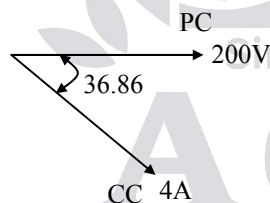
$$I_s = \frac{5}{50} \times 40 = 4 \text{ A}$$

C.T. secondary (I_s) = $4 \angle -36.86^\circ$

Wattmeter current coil = $I_c = 4 \angle -36.86^\circ$

Wattmeter reading

$$\begin{aligned} &= 200 \text{ V} \times 4 \times \cos(36.86^\circ) \\ &= 640.08 \text{ W} \end{aligned}$$



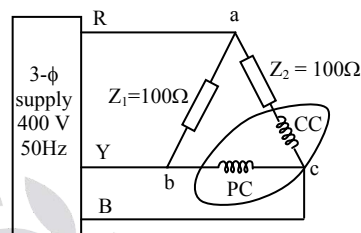
02. Ans: (c)

$$\text{Sol: } W = \frac{E_1}{\sqrt{2}} \times \frac{I_1}{\sqrt{2}} \cos \phi_1 + \frac{E_3}{\sqrt{2}} \times \frac{I_3}{\sqrt{2}} \cos \phi_3$$

$$W = \frac{1}{2} [E_1 I_1 \cos \phi_1 + E_3 I_3 \cos \phi_3]$$

03. Ans: (c)

Sol:



Based on R-Y-B

Assume abc phase sequence

$$V_{ab} = 400 \angle 0^\circ ; \quad V_{bc} = 400 \angle -120^\circ$$

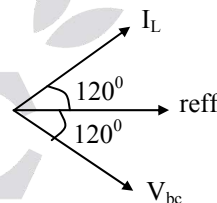
$$V_{ca} = 400 \angle -240^\circ \text{ or } 400 \angle 120^\circ$$

$$I_{ca} = I_L = \frac{(\text{line Voltage})}{Z_2}$$

$$= \frac{400 \angle 120^\circ}{100} = 4 \angle 120^\circ$$

Voltage across pressure coil = V_{bc}

$$= 400 \angle -120^\circ$$



Wattmeter reading

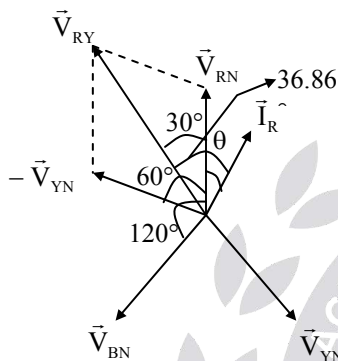
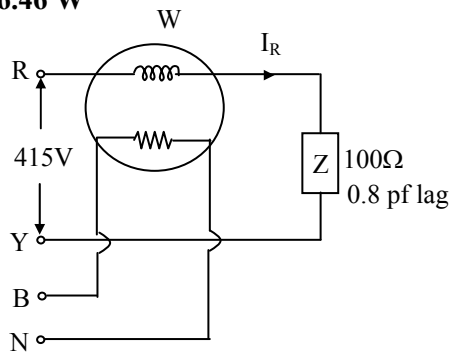
$$= I_L \times V_{bc} \cos(\angle I_L \text{ \& } V_{bc})$$

$$= 4 \times 400 \cos(240^\circ)$$

$$= 1600 \left(-\frac{1}{2}\right) = -800 \text{ W}$$

04. Ans: -596.46 W

Sol:



Current coil is connected in 'R_{phase}', it reads ' \tilde{I}_R ' current.

Potential coil reads phase voltage i.e., \tilde{V}_{BN}

$$W = \tilde{V}_{BN} \times \tilde{I}_R \times \cos(\tilde{V}_{BN} \cdot \tilde{I}_R)$$

$$V_L = 415 \text{ V}, V_{BN} = \frac{415}{\sqrt{3}} \text{ V}$$

$$I_R = \frac{V_{RY}}{Z} = \frac{415}{100} = 4.15 \text{ A}$$

$$\cos \phi = 0.8$$

$$\Rightarrow \phi = 36.86^\circ \text{ between } \tilde{V}_{RY} \text{ \& } \tilde{I}_R$$

$$\theta = 36.86^\circ - 30^\circ = 6.86^\circ$$

Now angle between \tilde{V}_{BN} and \tilde{I}_R

$$= 120 + 6.86 = 126.86^\circ$$

$$W = \frac{415}{\sqrt{3}} \times 4.15 \times \cos(126.86)$$

$$= -596.467 \text{ W}$$

05. Ans: (d)

Sol: $V_L = 400 \text{ V}, I_L = 10 \text{ A}$

$$\cos \phi = 0.866 \text{ lag}, \phi = 30^\circ$$

$$W_1 = V_L I_L \cos(30 - \phi)$$

$$W_2 = V_L I_L \cos(30 + \phi)$$

$$W_1 = 400 \times 10 \times \cos(30 - 30) = 4000 \text{ W}$$

$$W_2 = 400 \times 10 \times \cos(30 + 30) = 2000 \text{ W}$$

06. Ans: (b)

$$\text{Sol: } \phi = \tan^{-1} \left[\frac{\sqrt{3}(W_1 - W_2)}{(W_1 + W_2)} \right]$$

$$\text{Power factor} = \cos \phi$$

$$= 0.917 \text{ lag (since load is inductive)}$$

07. Ans: W = 519.61 VAR

Sol:

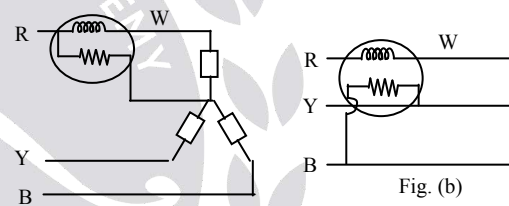


Fig. (a)

Fig. (b)

$$W = 400 \text{ watt}; W = V_{ph} I_{ph} \cos \phi$$

$$V_{ph} I_{ph} = 400/0.8$$

This type of connection gives reactive power

$$W = \sqrt{3} V_p I_p \sin \phi = \sqrt{3} \times \frac{400}{0.8} \times 0.6 = 519.6 \text{ VAR}$$

Solutions for Conventional Practice Questions

01.

Sol: Power calculated by freshman

$$P = I^2 R = (30.4)^2 \times 0.0105$$

$$= 9.70368 \text{ W}$$

True value of current (I_T) =

$$30.4\text{A} + \left(\frac{1.2}{100} \times 30.4\text{A} \right) = 30.77\text{A}$$

True value of resistance (R_T) =

$$0.0105\Omega + \left(\frac{0.3}{100} \times 0.0105\Omega \right) = 0.010532\Omega$$

$$\text{True power } (P_T) = (30.77)^2 \times 0.010532\Omega = 9.971\text{W}$$

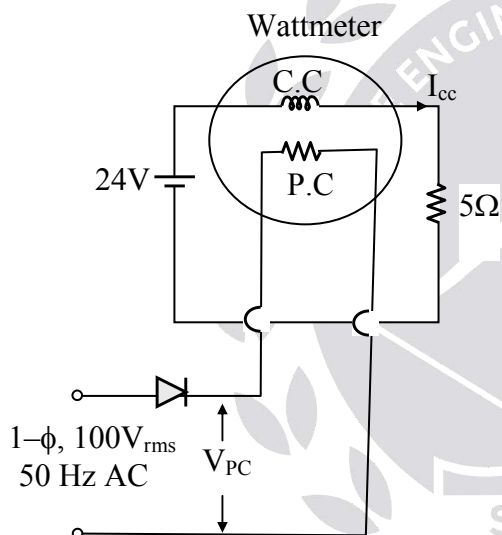
$$\frac{\text{True value of power}}{\text{power calculated by freshman}} \times 100$$

$$= \frac{9.971\text{W}}{9.70368} \times 100$$

$$= 102.75\%$$

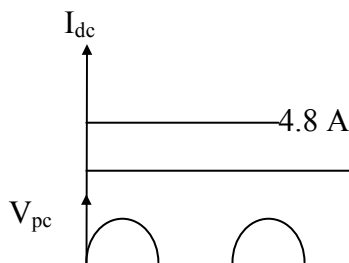
02.

Sol:



$$I_{dc} = I_{cc} = \frac{24\text{V}}{5\Omega} = 4.8\text{A}$$

$$V_{rms} = 100\text{V}, V_{max} = 100 \times \sqrt{2}$$



Wattmeter reading (W)

$$= \frac{1}{2\pi} \int_0^{2\pi} (V_{pc} \times I_{dc}) d\omega t$$

$$W = \frac{1}{2\pi} \left[\int_0^{\pi} (100\sqrt{2} \sin \omega t \times 4.8) d\omega t + \int_{\pi}^{2\pi} (0 \times 4.8) d\omega t \right]$$

$$= \frac{4.8 \times 100\sqrt{2}}{2\pi} \left[(-\cos \omega t)_0^{\pi} \right] = 216.07\text{W}$$

03.

$$\text{Sol: } W_m = (1 + \tan \phi \tan \beta) W_T$$

$$700\text{W} = (1 + \tan \phi \tan 2) W_T \text{ ----- (1)}$$

$$620\text{W} = (1 + \tan \phi \tan 1) W_T \text{ ----- (2)}$$

$$\Rightarrow \frac{(1)}{(2)} = \frac{35}{31} = \frac{(1 + \tan \phi \times 0.034)}{1 + \tan \phi \times 0.0174}$$

$$\Rightarrow (1 + \tan \phi \times 0.0174) 35$$

$$= (1 + \tan \phi \times 0.03492) 31$$

$$\Rightarrow 35 + 35 (\tan \phi \times 0.0174)$$

$$= 31 + 31 \tan \phi \times 0.03492$$

$$\Rightarrow 35 - 31 = 1.0852 \tan \phi - 0.609 \tan \phi$$

$$\Rightarrow 4 = 0.4762 \tan \phi$$

$$\Rightarrow \phi = 83.2108$$

$$\cos \phi = 0.1182$$

$$WT = \frac{700}{(1 + \tan 83.2108 \times \tan 2)} = 541.2407$$

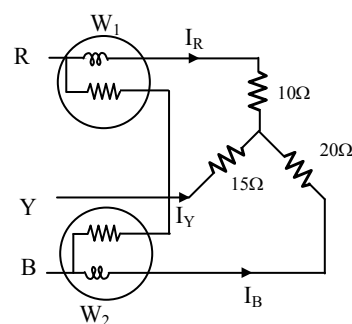
$$V = 240\text{V}$$

$$P = VI \cos \phi$$

$$\Rightarrow I = \frac{P}{V \cos \phi} = \frac{541.2407}{240 \times 0.1182} = 19.079\text{A}$$

04.

Sol:



Consider RYB phase sequence

$$V_R = \frac{440V}{\sqrt{3}} \angle 0^\circ = 254.03 \angle 0^\circ V$$

$$V_Y = 254.03 \angle -120^\circ V$$

$$V_B = 254.03 \angle -240^\circ V$$

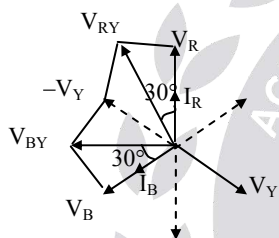
$$\Rightarrow I_R = \frac{V_R}{10\Omega} = \frac{254.03 \angle 0}{10\Omega} = 25.403 \angle 0$$

$$I_Y = \frac{V_Y}{15\Omega} = \frac{254.03 \angle -120}{15\Omega} = 16.935 \angle -120$$

$$I_B = \frac{V_B}{20\Omega} = \frac{254.03 \angle -240}{20\Omega} = 12.701 \angle -240 \text{ Acc}$$

ording to connections

W = P.C voltage × C.C current × cost of angle
between (P.C Voltage & CC current]



$$W_1 = V_{RY} \times I_R \cos (V_{RY} \& I_R)$$

$$W_1 = 440V \times 25.403 \times \cos 30$$

$$= 9679.84W$$

$$W_2 = V_{BY} \times \cos (V_{BY} \& I_B) \times I_B$$

$$= 440V \times 12.701 \times \cos 30$$

$$= 4839.73 W$$

$$3\phi \text{ Total } P = W_1 + W_2$$

$$= 14.519 \text{ kW}$$

05.

Sol: (i) $P_1 = 5000W$, $P_2 = -1000W$

$$\text{Total power } (P_T) = P_1 + P_2 \Rightarrow$$

$$5000 - 1000 = 4000W$$

Power Factor Angle (ϕ)

$$= \tan^{-1} \left[\sqrt{3} \frac{P_1 - P_2}{P_1 + P_2} \right]$$

$$\Rightarrow \tan^{-1} \left[\sqrt{3} \left[\frac{5000 - (-1000)}{5000 + 1000} \right] \right]$$

$$\Rightarrow \tan^{-1} \left[\sqrt{3} \left(\frac{6000}{4000} \right) \right] \Rightarrow \tan^{-1} \left[\frac{3\sqrt{3}}{2} \right] \phi$$

$$= 68.94^\circ$$

$$\therefore \text{Power Factor } \cos \phi = \cos (68.94^\circ)$$

$$= 0.3593$$

$$\approx 0.36 \text{ Lag}$$

(ii) Ans: Power consumed By each phase

$$= \frac{P_{\text{Total}}}{3} = \frac{4000}{3} = 1333.33W$$

In Δ connected system, voltage of each phase

$$V_{ph} = V_L = 440V$$

= supply voltage

→ current in each phase

$$= \frac{1333.33}{440 \times 0.36} = 8.41748 \text{ Amp}$$

→ Impedance of each phase

$$= \frac{440}{8.41748} = 52.27217 \Omega$$

→ Resistance of each phase

$$= \frac{1333.33}{(8.41748)^2} = 18.818 \Omega$$

→ Reactance (X) of each phase

$$= \sqrt{(52.27217)^2 - (18.818)^2}$$

$$= 48.7674 \Omega$$

→ In order that one of the wattmeter's should read zero, the power factor should be 0.5

$$\therefore \cos \phi = 0.5, \& \tan \phi = 1.73$$

$$\therefore \text{Reactance of circuit} \Rightarrow X = R \tan \phi$$

$$X = 18.818 \times 1.73 \Rightarrow X = 32.55514 \Omega$$

∴ Capacitive Reactance Required

$$= 48.7674 - 32.55514$$

$$= 16.21226$$

$$\text{Capacitance (C)} = \frac{1}{2\pi \times 50 \times 16.21226}$$

$$C = 196.33 \mu\text{F}$$

06.

Sol: Load power = $230 \times 5 \times 0.1 = 115\text{W}$

Load power factor $\cos\phi = 0.1$

$\therefore \phi = 84.26^\circ$ and $\sin\phi = 0.995$ and

$\tan\phi = 9.95$

→ Resistance of pressure coil circuit

$$R_p = 10000\Omega$$

→ Reactance of pressure coil circuit

$$= 2\pi \times 50 \times 100 \times 10^{-3} = 31.416\Omega$$

As the phase Angle of pressure coil circuit is small,

$$\beta = \tan\beta \approx \frac{31.416}{10000} = 3.1416 \times 10^{-3} \text{ rad}$$

$$= 0.0031416 \text{ rad}$$

→ When the pressure coil is connected on the load side the wattmeter measures power loss in pressure coil circuit in addition to load power

$$\text{True power} = VI\cos\phi = 230 \times 5 \times 0.1$$

$$= 115\text{W}$$

Let us consider only the effect of Inductance

Reading of wattmeter = true power

$$[1 + \tan\phi \tan\beta] = 115 [1 + 9.95 \times 0.00314]$$

$$= 118.593\text{W}$$

→ Power loss in pressure coil circuit =

$$\frac{V^2}{R_p} = \frac{230^2}{10000} = 5.29 \text{ W}$$

\therefore Reading of wattmeter considering

The power loss in pressure coil circuit

$$= 118.593 + 5.29 = 123.883$$

$$\text{Percentage error} = \frac{123.883 - 115}{115} \times 100$$

$$= 7.724\%$$

07.

Sol: $E_{RY} = 400 \angle 0^\circ$, $E_{YB} = 400 \angle -120^\circ$,

$$E_{BR} = 400 \angle 120^\circ,$$

$$I_{RY} = \frac{400}{30 - j40} = \frac{400}{50 \angle -53^\circ} = 8 \angle 53^\circ = 4.8 + j6.4$$

$$I_{RB} = \frac{400 \angle 120^\circ}{40}$$

$$\Rightarrow 10 \angle -60^\circ = I_{ML}$$

[wattmeter current coil current]

For the wattmeter pressure coil circuit

$$20 I_{RB} + V_1 V_2 - (-j40 I_{RY}) = 0$$

$$(i.e) 0 = 200 \angle -60^\circ + 40 \angle 90^\circ \times 8 \angle 53^\circ + V_1 V_2$$

$$\therefore -V_1 V_2 = 100 - j173 + 320 \angle 143^\circ$$

$$= 100 - j173 - 255.6 + j195.2$$

$$\therefore -V_1 V_2 = -155.6 + j20$$

$$V_1 V_2 = 155.6 - j20 = 156.9 \angle -7.3^\circ$$

$$\therefore \text{the reading of wattmeter} = I_{ML} \cdot V_1 V_2$$

$$= 10 \times 156.9 \times 10^{-3} \cos(52.7^\circ) \text{ kW}$$

$$= 0.94 \text{ kW}$$

08.

Sol: CBA → Phase sequence same as ACB phase sequence

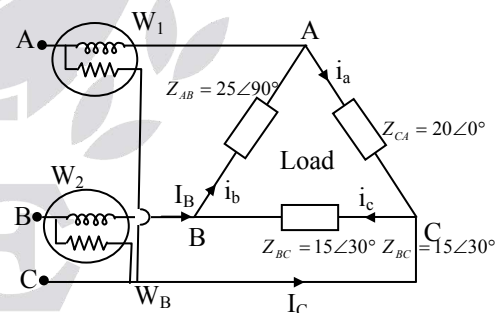


Fig.(b)

→ supply Line voltage = 230V

$$V_{AC} \angle 0^\circ = V_L \angle 0^\circ = 230 \angle 0^\circ$$

$$V_{CB} \angle -120^\circ = V_L \angle -120^\circ = 230 \angle -120^\circ$$

$$V_{BA} \angle -240^\circ = V_L \angle -240^\circ = 230 \angle -240^\circ$$

$$\text{Phase current (i}_a\text{)} = \frac{V_{AC} \angle 0^\circ}{20 \angle 0^\circ} = \frac{230 \angle 0^\circ}{20 \angle 0^\circ}$$

$$= 11.5 \angle 0^\circ \text{ A}$$

$$i_b = \frac{V_{BA} \angle -240^\circ}{25 \angle 90^\circ} = 9.2 \angle -330^\circ \text{ A}$$

$$i_c = \frac{V_{CB} \angle -120^\circ}{15 \angle 30^\circ} = \frac{230 \angle -120^\circ}{15 \angle 30^\circ} = 15.33 \angle -150^\circ \text{ A}$$

$$\text{Line current } (I_A) = i_a - i_b = [11.5 \angle 0^\circ - 9.2 \angle -330^\circ]$$

$$(I_A) = 11.5 - 9.2 \left[\frac{\sqrt{3}}{2} + \frac{j}{2} \right]$$

$$(I_A) = 11.5 - 7.96743 - j4.6$$

$$(I_A) = 3.53257 - j4.6 = 5.8 \angle -52.477^\circ$$

$$\begin{aligned} W_1 &= V_{pc} I_{cc} \cos [\angle V_{pc} \& I_{cc}] \\ &= V_{AC} \times I_A \cos [\angle V_{Ac} \& I_A] \\ &= 230 \times 5.8 \times \cos [52.477^\circ] \\ &= 812.512 \text{ W} \end{aligned}$$

$$\text{For } W_2 \text{ Reading: } I_B = i_b - i_c = 9.2 \angle -330^\circ - 15.33 \angle -150^\circ$$

$$I_B = 9.2 \left(\frac{\sqrt{3}}{2} + \frac{j}{2} \right) - 15.33 \left(\frac{-\sqrt{3}}{2} - \frac{j}{2} \right) = 21.2436 + j12.265$$

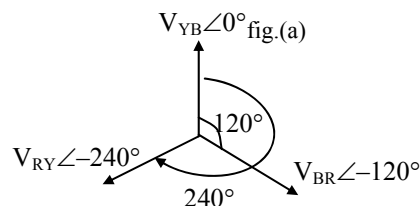
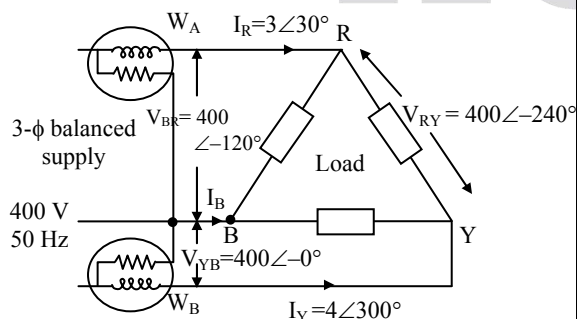
$$I_B = 24.53 \angle 30^\circ$$

$$V_{BC} = V_{CB} \angle \theta + 180^\circ = 230 \angle -120^\circ + 180^\circ$$

$$\begin{aligned} V_{PC} &= V_{BC} = 230 \angle +60^\circ \\ &= 230 \times 24.53 \cos (60^\circ - 30^\circ) \\ &= 5641.9 \times 0.866 \\ &= 4886.6 \text{ W} \end{aligned}$$

09.

Sol:



$$W_A = V_{RB} \times I_R \times \cos [\angle V_{RB} \& I_R]$$

$$V_{BR} = 400 \angle -120^\circ, \text{ But } V_{YB} \angle 0^\circ$$

$$V_{pc} = V_{RB} = 400 \angle -120^\circ + 180^\circ$$

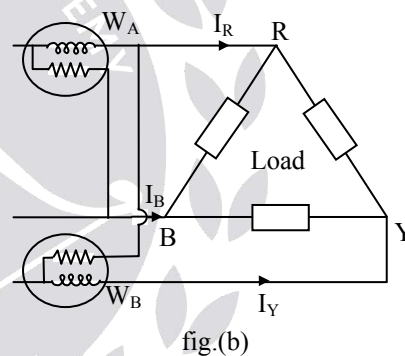
$$V_{RB} = 400 \angle +60^\circ = V_{PC}$$

$$\begin{aligned} W_A &= 400 \times 3 \times \cos (60^\circ - 30^\circ) \\ &= 1039.23 \text{ W} \end{aligned}$$

$$W_B = V_{PC} \times I_{CC} \times \cos (\angle V_{pc} \& I_{CC})$$

$$V_{pc} = V_{YB} = 400 \angle 0^\circ, I_{CC} = I_Y = 4 \angle 300^\circ$$

$$\begin{aligned} W_B &= 400 \times 4 \times \cos (-300^\circ) \\ &= 800 \text{ W} \end{aligned}$$



$$W_A = V_{PC} \times I_{CC} \times \cos (\angle V_{pc} \& I_{CC})$$

$$V_{PC} = V_{RB} = 400 \angle +60^\circ$$

$$I_{CC} = I_R = 3 \angle 30^\circ$$

$$W_A = 400 \times 3 \times \cos (60^\circ - 30^\circ)$$

$$W_A = 1039.23 \text{ W}$$

$$W_B = V_{PC} \times I_{CC} \times \cos (\angle V_{pc} \& I_{CC})$$

$$= V_{YR} \times I_Y \times \cos (\angle V_{YR} \& I_Y)$$

$$V_{PC} = V_{YR} = 400 \angle -240^\circ + 180^\circ$$

$$[\because V_{RY} = 400 \angle -240^\circ]$$

$$V_{YR} = 400 \angle -60^\circ, I_{CC} = I_Y = 4 \angle 300^\circ$$

$$W_B = 400 \times 4 \times \cos (-60^\circ - 300^\circ)$$

$$W_B = 1600 \text{ W}$$

5. Measurement of Energy
Solutions for Objective Practice Questions
01. Ans: (a)
Sol: Energy consumed in 1 minute

$$= \frac{240 \times 10 \times 0.8}{1000} \times \frac{1}{60} = 0.032 \text{ kWh}$$

Speed of meter disc

 = Meter constant in rev/kWhr \times Energy consumed in kWh/minute

$$= 400 \times 0.032$$

$$= 12.8 \text{ rpm (revolutions per minute)}$$

02. Ans: (a)
Sol: Energy consumed (True value)

$$= \frac{230 \times 5 \times 1}{1000} \times \frac{3}{60} = 0.0575 \text{ kWhr}$$

Energy recorded (Measured value)

$$= \frac{\text{No. of rev (N)}}{\text{meter constant (k)}}$$

$$= \frac{90 \text{ rev}}{1800 \text{ rev / kWhr}} = 0.05 \text{ kWhr}$$

$$\% \text{Error} = \frac{0.05 - 0.0575}{0.0575} \times 100$$

$$= -13.04\% = 13.04\% \text{ (slow)}$$

03. Ans: (c)
Sol: $V = 220 \text{ V}$, $\Delta = 85^\circ$, $I = 5 \text{ A}$

$$\text{Error} = VI [\sin(\Delta - \phi) - \cos \phi]$$

$$(1) \cos \phi = \text{UPF}, \phi = 0^\circ$$

$$\text{Error} = 220 \times 5 [\sin(85 - 0) - \cos 0]$$

$$= -4.185 \text{ W} \approx -4.12 \text{ W}$$

$$(2) \cos \phi = 0.5 \text{ lag}, \phi = 60^\circ$$

$$\text{Error} = 220 \times 5 [\sin(85 - 60) - \cos 60]$$

$$= -85.12 \text{ W}$$

04. Ans: (c)
Sol: Meter constant = 14.4 A-sec/rev

$$= 14.4 \times 250 \text{ W-sec/rev}$$

$$= \frac{14.4 \times 250}{1000} \text{ kW - sec/rev}$$

$$= \frac{14.4 \times 250}{1000 \times 3600} \text{ kWhr / rev}$$

$$\text{Meter constant} = \frac{1}{1000} \text{ kWhr / rev}$$

$$\text{Meter constant in terms of rev/kWhr} = 1000$$

05. Ans: (c)
Sol: Energy recorded (kWhr)

$$= \frac{5 \text{ rev}}{1200 \text{ rev / kWhr}}$$

$$= 4.1667 \times 10^{-3} \text{ kWhr}$$

$$\text{Energy} = 4.1667 \text{ Whr}$$

$$\text{Load power} = \frac{4.1667 \text{ Whr}}{75 \text{ sec}} = \frac{4.1667 \text{ Whr}}{\frac{75}{3600} \text{ hr}}$$

$$\text{Load power} = 200 \text{ W}$$

06. Ans: (d)
Sol: Energy recorded (measured value)

$$= \frac{51 \text{ rev}}{360 \text{ rev / kWhr}}$$

$$= 0.141667 \text{ kWhr}$$

Energy consumed (True value)

$$= \frac{10 \text{ kw} \times 50}{3600}$$

$$= 0.13889 \text{ kWhr}$$

$$\text{Error} = \frac{0.141667 - 0.13889}{0.13889} \times 100$$

$$= 1.999\% \approx +2\%$$

Solutions for Conventional Practice Questions

01.

Sol: Phantom loading: when the current rating of a meter under test is high, a test with actual loading assignments would involve a considerable waste of power. In order to avoid this, phantom loading is done. Phantom loading consists of supplying the pressure coil circuit from a circuit of required normal voltage, and the current coil circuit from a separate low voltage supply. It is possible to circulate the rated current through the current circuit with a low voltage supply as the impedance of this circuit is very low. With this arrangement, the total power supplied for the test is that due to small pressure coil current at normal voltage, plus that due to the current with low voltage. Therefore, power required for testing the meter with phantom loading is comparatively very small.

Given data:

$$V = 230V, \quad I = 12A$$

$$\cos\phi = 0.8 \text{ lag}, \quad K = 1200 \text{ rev/kWh},$$

$$N_1 = 1150 \text{ rev}$$

(i) Error in registration,

Actual kWh consumed

$$= 230 \times 12 \times 0.8 \times \frac{1}{2} \times 10^{-3}$$

$$= 1.104 \text{ kWh.}$$

\Rightarrow Actual revolutions registered

$$= k \times \text{kWh}$$

$$= 1200 \times 1.104$$

$$N_2 = 1324.8 \text{ Revolutions}$$

$$\text{Error registration} = \frac{N_2 - N_1}{N_2} \times 100$$

$$= \frac{1324.8 - 1150}{1324.8} \times 100$$

$$= 13.2\%$$

$$\text{(ii) Revolutions per minute} = \frac{1324.8}{60}$$

$$= 22.08$$

rev/min

$$\text{Revolutions registered/min} = \frac{1150}{30}$$

(half an hour measuring)

$$= 38.33 \text{ rev/min}$$

$$\% \text{ Error} = \frac{38.33 - 22.08}{22.08} \times 100$$

$$= 73.6\% \text{ (fast)}$$

Rectification: In energy meter, error in rpm can be rectified by bringing the braking magnet near to the centre of disc.

6. Bridge Measurement of R, L & C
Solutions for Objective Practice Questions

01. Ans: (a)

Sol: The deflection of galvanometer is directly proportional to current passing through circuit, hence inversely proportional to the total resistance of the circuit.

Let S = standard resistance

R = Unknown resistance

G = Galvanometer resistance

θ_1 = Deflection with S

θ_2 = Deflection with R

$$\therefore \frac{\theta_1}{\theta_2} = \frac{R + G}{S + G}$$

$$\Rightarrow R = (S + G) \frac{\theta_1}{\theta_2} - G$$

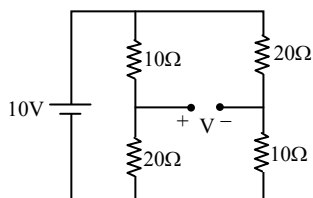
$$= (0.5 \times 10^6 + 10 \times 10^3) \left(\frac{41}{51} \right) - 10 \times 10^3$$

$$= 0.4 \times 10^6 \Omega$$

$$= 0.4 \text{ M}\Omega$$

02. Ans: (d)

Sol:



$$V = V_+ - V_-$$

$$= 10 \times \frac{20}{30} - 10 \times \frac{10}{30}$$

$$= 6.66 - 3.33 = 3.33 \text{ V}$$

03. Ans: (c)

Sol: The voltage across R_2 is

$$= E \frac{R_2}{R_1 + R_2} = \frac{E}{2}$$

The voltage across R_1 is

$$= E \frac{R_1}{R_1 + R_2} = \frac{E}{2}$$

$$\text{Now, } \frac{E}{2} = IR_3 + V$$

$$I = \frac{E - 2V}{2R_3} \Rightarrow I = \frac{E - 2V}{2R}$$

$$\text{and } \frac{E}{2} = IR_4$$

$$\frac{E}{2} = \left(\frac{E - 2V}{2R} \right) (R + \Delta R)$$

$$ER = (E - 2V) (R + \Delta R)$$

$$R + \Delta R = \frac{ER}{(E - 2V)}$$

$$\Delta R = \frac{ER}{(E - 2V)} - R$$

$$= \frac{ER - ER + 2VR}{(E - 2V)}$$

$$\Delta R = \frac{2VR}{(E - 2V)}$$

04. Ans: (c)

Sol: $R = \frac{0.4343 T}{C \log_{10} \left(\frac{E}{V} \right)}$

$$= \frac{0.4343 \times 60}{600 \times 10^{-2} \times \log_{10} \left(\frac{250}{92} \right)}$$

$$= \frac{26.058}{260.49 \times 10^{-12}}$$

$$R = 100.03 \times 10^9 \Omega$$

05. Ans: 0.118 μF, 4.26kΩ

Sol: Given: $R_3 = 1000 \Omega$

$$C_1 = \frac{\epsilon_0 \epsilon_r A}{d}$$

$$= \frac{2.3 \times 4\pi \times 10^{-7} \times 314 \times 10^{-4}}{0.3 \times 10^{-2}}$$

$$C_1 = 30.25 \mu\text{F}$$

$$\delta = 9^\circ \text{ for } 50 \text{ Hz}$$

$$\tan \delta = \omega C_1 r_1 = \omega L_4 R_4$$

$$\Rightarrow r_1 = 16.67 \Omega$$

$$\text{Variable resistor } (R_4) = R_3 \left(\frac{C_1}{C_2} \right)$$

$$R_4 = 4.26 \text{ k}\Omega, \quad C_4 = 0.118 \mu\text{F}$$

06. Ans: (a)

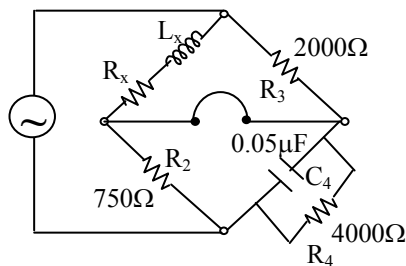
Sol: It is Maxwell Inductance Capacitance bridge

$$R_x R_4 = R_2 R_3$$

$$R_x = \frac{R_2 R_3}{R_4}$$

$$R_x = \frac{750 \times 2000}{4000}$$

$$R_x = 375 \Omega$$



$$\frac{L_x}{C_4} = R_2 R_3$$

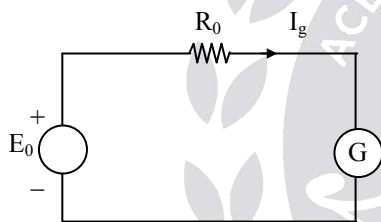
$$L_x = C_4 R_2 R_3$$

$$L_x = 0.05 \times 10^{-6} \times 750 \times 2000$$

$$L_x = 75 \text{ mH}$$

07. Ans: (a)

Sol: Thevenin's equivalent of circuit is



R_0 = Resistance of circuit looking into terminals b & d with a & c short circuited.

$$= \frac{RS}{R+S} + \frac{PQ}{P+Q} = \frac{1 \times 5}{1+5} + \frac{1 \times Q}{1+Q}$$

$$= 0.833 + \frac{Q}{1+Q} \text{ K}\Omega$$

$$\text{Now, } R_0 + G = \frac{24 \times 10^{-3}}{13.6 \times 10^{-6}}$$

$$= 1.765 \text{ k}\Omega$$

$$(\text{or}) R_0 = 1765 - 100 = 1665 \Omega$$

$$0.833 + \frac{Q}{1+Q} = 1.665$$

$$\Rightarrow Q = 4.95 \text{ k}\Omega$$

08.

Sol: Resistance of unknown resistor required for balance

$$R = (P/Q)S = (1000/100) \times 200 = 2000 \Omega.$$

In the actual bridge the unknown resistor has a value of 2005Ω or the deviation from the balance conditions is $\Delta R = 2005 - 2000 = 5 \Omega$.

Thevenin source generator emf

$$E_0 = E \left[\frac{R}{R+S} - \frac{P}{P+Q} \right] = 5 \left[\frac{2005}{2005+200} - \frac{1000}{1000+100} \right] = 1.0307 \times 10^{-3} \text{ V.}$$

Internal resistance of bridge looking into terminals b and d.

$$R_0 = \frac{RS}{R+S} + \frac{PQ}{P+Q} = \frac{2005 \times 200}{2005+200} + \frac{1000 \times 100}{1000+100} = 272.8 \Omega$$

Hence the current through the galvanometer

$$I_g = \frac{E_0}{R_0 + G} = \frac{1.0307 \times 10^{-3}}{272.8 + 100} \text{ A} = 2.77 \mu\text{A.}$$

Deflection of the galvanometer

$$\theta = S_i I_g = 10 \times 2.77 = 27.7 \text{ mm}/\Omega.$$

Sensitivity of bridge

$$S_B = \frac{\theta}{\Delta R} = \frac{27.7}{5} = 5.54 \text{ mm}/\Omega$$

09. Ans: (d)

Sol: $R_1 R_4 = R_2 R_3$

$$R_4 = \frac{R_2 R_3}{R_1}$$

$$= \frac{5 \times 100}{10} \pm (2\% + 5\% + 3\%)$$

$$= 50 \pm 10\% \Omega$$

10. Ans: (c)

Sol: Under balanced condition, current through Galvanometer is zero, then

$$R_{eq} = (120\Omega + 80\Omega) \parallel (120\Omega + 80\Omega)$$

$$= 100 \Omega$$

$$I_B = \frac{1V}{100\Omega} = 10 \text{ mA}$$

11. Ans: (c)

Sol: Sensitivity = $\frac{\text{Change in output}}{\text{Change in input}}$

$$= \frac{3 \text{ mm}}{6\Omega} = 0.5 \text{ mm}/\Omega$$

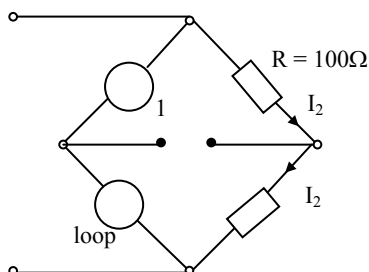
12. Ans: (d)

Sol: Changing the arms resistance by same value will not affect the Balance condition.

13. Ans: (a)

Sol: $V_1 = \sqrt{2} \cos(1000t) \text{ V}$

$$V_2 = 2 \cos(1000t + 45^\circ) \text{ V}$$



Under balanced condition,

$$V_1 = I_2 R$$

$$I_2 = \frac{V_1}{R} = \frac{\sqrt{2} \cos 1000t}{100}$$

$$\left. \begin{aligned} I_2 &= 10^{-2} \times \sqrt{2} \cos(1000t) \\ V_2 &= 2 \cos(1000t + 45^\circ) \end{aligned} \right\} \text{At } Z_x$$

'I₂' lags 'V₂' by 45°. So, Z_x has 'R' and 'L' in series.

$$R = Z \cos \theta = \frac{2}{10^{-2} \times \sqrt{2}} \cos 45^\circ = 100 \Omega$$

$$X_L = Z \sin \theta$$

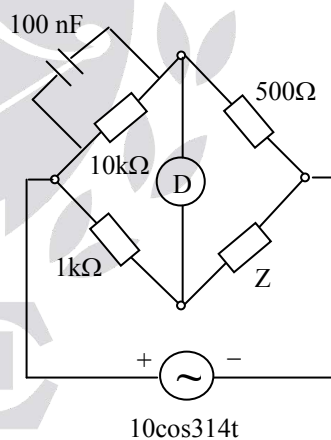
$$= \frac{2}{\sqrt{2} \times 10^{-2}} \sin 45^\circ = 100 \Omega$$

$$X_L = \omega L$$

$$L = \frac{X_L}{\omega} = \frac{100}{1000} = 0.1 \text{ H} = 100 \text{ mH}$$

14. Ans: (b)

Sol:



$$R \parallel \frac{1}{j\omega C} = \frac{R}{1 + j\omega RC}$$

$$\left(\frac{R}{1 + j\omega RC} \right) Z = 1k\Omega \times 500\Omega$$

$$\left(\frac{10k\Omega}{1 + j\omega \times 10k\Omega \times 100 \times 10^{-9}} \right) Z = 1k\Omega \times 500\Omega$$

$$\frac{10^4 \times Z}{1 + j\omega \times 10^{-3}} = 50 \times 10^4$$

$$Z = 50 + j\omega \times 0.05$$

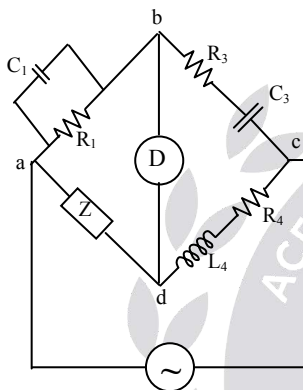
$$Z = R + j\omega L$$

$$R = 50 \Omega \text{ in series with } L = 0.05 \text{ H}$$

Solutions for Conventional Practice Questions

01.

Sol: The circuit diagram is shown below.



$$Z_1 = 303.3 \angle -72.4^\circ$$

$$Z_3 = 1049.5 \angle -17.7^\circ$$

$$Z_4 = 274.8 \angle 43.3^\circ$$

Using balance conditions,

$$Z_1 Z_4 = Z_2 Z_3 \rightarrow (1)$$

$$\theta_1 + \theta_4 = \theta_2 + \theta_3 \rightarrow (2)$$

$$Z_2 = 79.4 \text{ (from (1))}$$

$$\theta_2 = -11.4^\circ \text{ (from (2))}$$

$$\therefore Z_2 = 79.4 \angle -11.4^\circ$$

$$= 77.8 - j15.7$$

$$R = 77.8$$

$$X_C = 15.7$$

$$C = 10.2 \mu\text{F}$$

So, resistance of value 77.8Ω in series with C of value $10.2 \mu\text{F}$

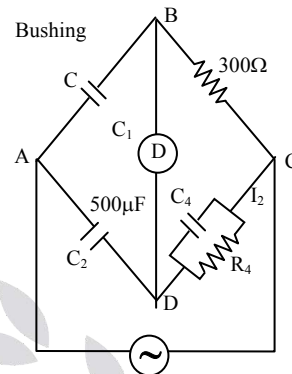
02.

Sol: Given data: $f = 50 \text{ Hz}$, $R_3 = 300 \Omega$,

$$C_2 = 500 \mu\text{F}, R_4 = 72.6 \Omega, C_4 = 0.148 \mu\text{F}$$

$$Z_1 Z_4 = Z_2 Z_3$$

$$Z_1 = Z_2 Z_3 Y_4$$



$$Z_1 = R_3 \times \frac{1}{j\omega C_2} \left[j\omega C_4 + \frac{1}{R_4} \right]$$

$$\frac{1}{j\omega C_1} = R_3 \frac{C_4}{C_2} + \frac{R_3}{j\omega C_2 R_4}$$

$$C_1 = C_2 \frac{R_4}{R_3} = 500 \times 10^{-12} \times \frac{72.6}{300} = 121 \text{ PF}$$

If we consider in bushing R_1 in series

$$R_1 R_4 \frac{-jR_3}{\omega C_1} = -\frac{jR_3}{\omega C_2} + \frac{R_3 R_4 C_4}{C_2}$$

$$R_1 = \frac{R_3 C_4}{C_2}, \quad C_1 = C_2 \frac{R_4}{R_3}$$

$$\text{Loss angle } \tan \delta = \omega C_1 R_1$$

$$= \omega \times \frac{R_3 C_4}{C_2} \times C_2 \frac{R_4}{R_3} = \omega C_4 R_4$$

$$= 2\pi \times 50 \times 72.6 \times 10^{-6} \times 0.148$$

$$\delta = 0.1934^\circ$$

03.

Sol: We know that $\epsilon_r = \frac{c_1 d}{\epsilon_0 A}$

$$\Rightarrow \frac{\epsilon_r \epsilon_0 A}{d} = c_1$$

$$\Rightarrow \frac{2.3 \times 8.854 \times 10^{-12} \times 314 \times 10^{-4}}{0.3 \times 10^{-2}} = c_1$$

$$\therefore c_1 = 213.145 \text{ pF}$$

$$r_1 = \frac{c_4}{c_2} R_3$$

$$R_4 = \frac{c_1}{c_2} R_3 = \frac{213.145 \text{ pF}}{50 \text{ pF}} \times 1000 = 4.269 \text{ k}\Omega$$

$$\tan \delta = 9^0$$

$$\delta = \tan^{-1}(9^0) = 1.46^0$$

$$\tan \delta = \omega c_4 R_4$$

$$0.1583 = \omega c_4 R_4$$

$$c_4 = \frac{0.1583}{2 \times \pi \times f \times R_4} = 0.1180 \text{ }\mu\text{F}$$

$$r_1 = \frac{c_4}{c_2} \times R_3 = \frac{0.1180 \text{ }\mu\text{F}}{50 \text{ pF}} \times 1000 = 2.36 \text{ M}\Omega$$

04.

Sol: Given

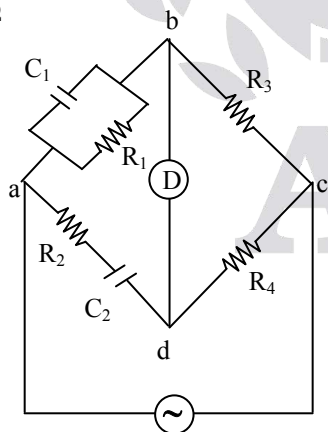
$$R_1 = 800 \text{ }\Omega$$

$$C_1 = 0.4 \text{ }\mu\text{F}$$

$$R_4 = 1200 \text{ }\Omega$$

$$R_2 = 500 \text{ }\Omega$$

$$C_2 = 1 \text{ pF}$$



This is Wien's bridge under balanced condition,

$$f = \frac{1}{2\pi\sqrt{R_1 R_2 C_1 C_2}} \text{ Hz}$$

$$\frac{R_4}{R_3} = \frac{R_2}{R_1} + \frac{C_1}{C_2}$$

$$\Rightarrow f = \frac{1}{2\pi\sqrt{800 \times 500 \times 0.4 \times 10^{-18}}} \text{ Mz}$$

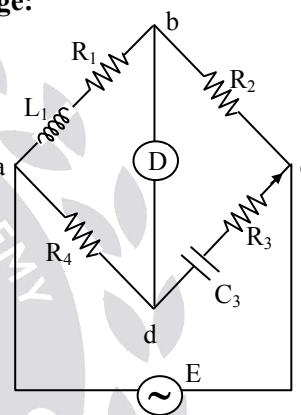
$$f = 397.9 \text{ kHz}$$

$$\text{also, } \frac{1200}{R_3} = \frac{500}{800} + \frac{0.4}{10^{-6}}$$

$$\Rightarrow R_3 = 3 \text{ m}\Omega$$

05.

Sol: Hay Bridge:



At balance condition, $Z_1 Z_4 = Z_2 Z_3$ and phase angles are also equal.

Here, phase null condition means phase angles are equal.

$$\theta_1 = \tan^{-1} \left(\frac{\omega L_1}{R_1} \right)$$

(Or)

$$\tan \theta_1 = \frac{\omega L_1}{R_1} = \text{Quality factor}$$

$$\tan \theta_c = \tan \theta_3 = \frac{1}{\omega C_3 R_3}$$

$$\theta_1 = \theta_3 \text{ (because } \theta_3 \text{ is negative)}$$

$$\frac{\omega L_1}{R_1} = \frac{1}{\omega C_3 R_3}$$

$$Q = \frac{\omega L_1}{R_1} = \frac{1}{\omega C_3 R_3}$$

$$\text{Here } Q = \frac{1}{\omega C_3 R_3}$$

Take 'I' is the current flowing in R_3 and ' C_3 '.

$$\text{So, } Q = \frac{I}{\omega C_3 (IR_3)}$$

$$\Rightarrow \frac{I}{\omega C_3} \times \frac{1}{IR_3}$$

$$\text{The potential drop in } C_3 = \frac{I}{\omega C_3} = V_{C_3}$$

\Rightarrow Voltage across ' C_3 '

IR_3 = voltage across resistor ' R_3 '

$$Q = \frac{\text{Voltage across } C_3}{\text{Voltage across } R_3}$$

$$= 0.005 \text{ A}$$

$$= 5 \text{ mA}$$

Total resistance of the battery circuit

= resistance of rheostat + resistance of slide wire

\therefore Resistance of rheostat

R_h = total resistance – resistance of slide wire

$$= \frac{3}{5 \times 10^{-3}} - 400$$

$$= 600 - 400$$

$$= 200 \Omega$$

04. Ans: (b)

Sol: Voltage drop per unit length

$$= \frac{1.45 \text{ V}}{50 \text{ cm}}$$

$$= 0.029 \text{ V/cm}$$

Voltage drop across 75 cm length

$$= 0.029 \times 75$$

$$= 2.175 \text{ V}$$

Current through resistor (I)

$$= \frac{2.175 \text{ V}}{0.1 \Omega}$$

$$= 21.75 \text{ A (or)}$$

$$75 \text{ cm} \rightarrow 0.1 \Omega$$

$$50 \text{ cm} \rightarrow ?$$

Slide wire resistance with standard cell

$$= \frac{50}{70} \times 0.1$$

$$= 0.067 \Omega$$

$$\text{Then } 0.067 \times I_w = 1.45 \text{ V}$$

$$I_w = \frac{1.45}{0.067}$$

$$= 21.75 \text{ A}$$

7. Potentiometers & Instrument Transformers

Solutions for Objective Practice Questions

01. Ans: (d)

Sol: Under null balanced condition the current flow in through unknown source is zero. Therefore the power consumed in the circuit is ideally zero.

02. Ans: (d)

Sol: Potentiometer is used for measurement of low resistance, current and calibration of ammeter.

03. Ans: (a)

Sol: Since the instrument is a standardized with an emf of 1.018 V with sliding contact at 101.8 cm, it is obvious that a length 101.8 cm represents a voltage of 1.018.

Resistance of 101.8 cm length of wire

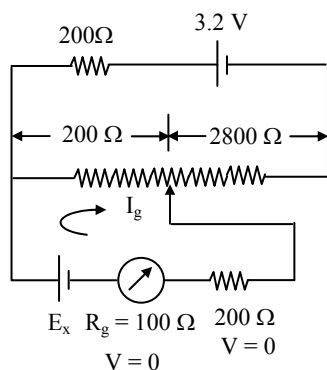
$$= (101.8/200) \times 400$$

$$= 203.6 \Omega$$

\therefore Working current $I_m = 1.018/203.6$

05. Ans: (a)

Sol:



Under balanced, $I_g = 0$

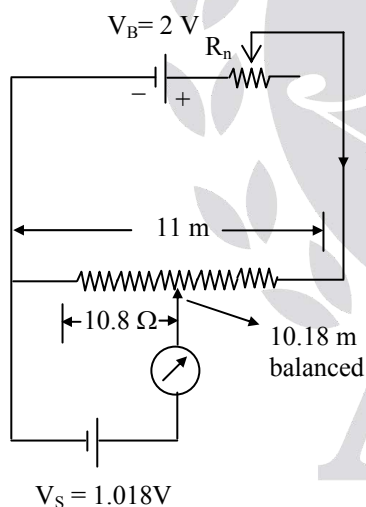
$$E_x = 3.2 \text{ V} \times \frac{200}{(200 + 200 + 2800)}$$

$$= 0.2 \text{ V}$$

$$E_x = 200 \text{ mV}$$

06. Ans: (a)

Sol:



Resistance $1 \Omega/\text{cm}$

For 11 m $\rightarrow 11 \Omega$

For 10m + 18cm $\rightarrow 10.8 \Omega$

$$I_w \times 10.8 \Omega = 1.018 \text{ V}$$

$$I_w = \frac{V_B}{R_n + I_r}$$

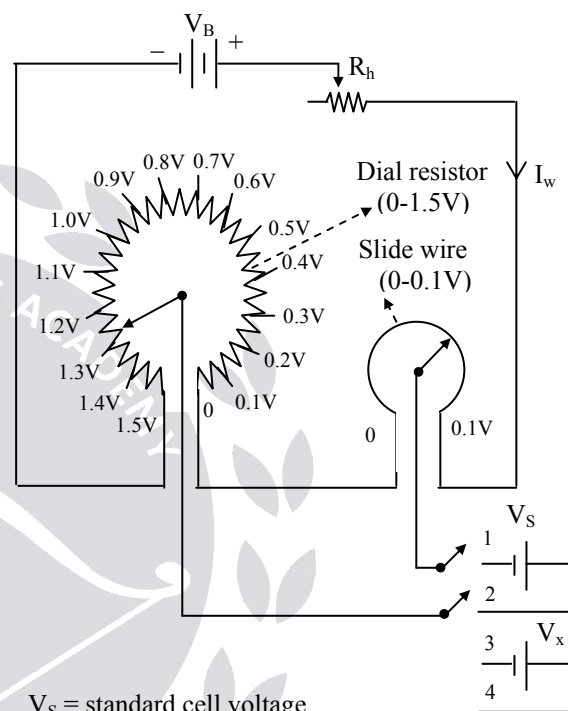
$$\Rightarrow 0.1 = \frac{2}{R_n + 11 \Omega}$$

$$R_n = \frac{2}{0.1} - 11$$

$$= 9 \Omega$$

07. Ans: (a)

Sol:



V_s = standard cell voltage

Dial resistor has 15 steps and each step is 10Ω

$$= 15 \times 10 \Omega = 150 \Omega$$

Slide wire resistance = 10Ω

Total resistance = $150 + 10 = 160 \Omega$

Working current (I_w) = 10 mA

Range of potentiometer

$$= 10 \text{ mA} \times 160 \Omega = 1.6 \text{ V}$$

Resolution of potentiometer

$$= \frac{\text{working current} \times \text{slide wire resistance}}{\text{slide wire length}}$$

$$= \frac{10 \text{ mA} \times 10 \Omega}{100 \text{ cm}}$$

$$= 0.001 \text{ V/cm}$$

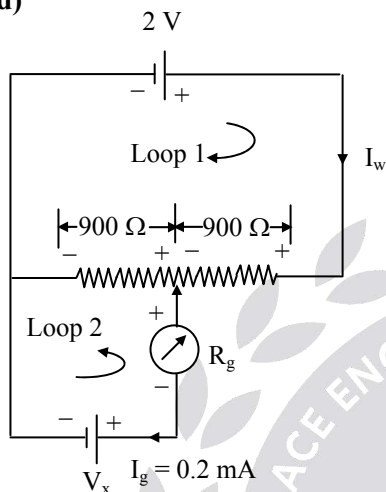
(1 div = 1 cm)

One fifth of a division can be read certainly.

$$\text{Resolution} = \frac{1}{5} \times 0.001 = 0.2 \text{ mV}$$

08. Ans: (d)

Sol:



Write KVL for loop 1

$$2V - 900 I_w - 900(I_w - 0.2\text{mA}) = 0$$

$$I_w = 1.211 \text{ mA}$$

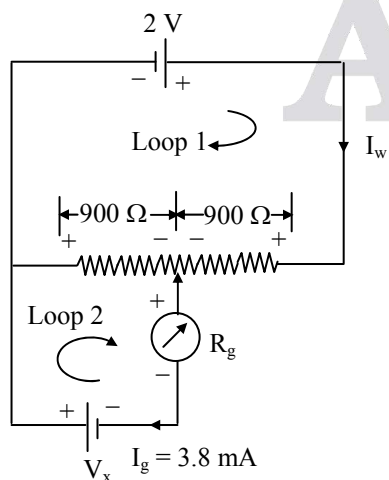
Write KVL for loop 2

$$V_x + 0.2 \text{ mA} \times R_g - 900(I_w - 0.2\text{mA}) = 0$$

$$V_x + 0.2 \times 10^{-3} R_g - 900(1.211 \times 10^{-3} - 0.2 \times 10^{-3}) = 0$$

$$V_x = 0.909 - 0.2 \times 10^{-3} R_g \quad \dots\dots\dots (1)$$

When V_x is reversed, the circuit is



Write KVL for loop (1)

$$2 - 900I_w - 900(I_w - 3.8\text{mA}) = 0$$

$$I_w = 3.011 \text{ mA}$$

Write KVL for loop (2)

$$V_x - 900(3.8\text{mA} - I_w) - 3.8\text{mA} \times R_g = 0$$

$$V_x - 900(3.8 \times 10^{-3} - 3.011 \times 10^{-3}) - 3.8 \times 10^{-3} R_g = 0$$

$$V_x = 0.710 + 3.8 \times 10^{-3} R_g \quad \dots\dots\dots (2)$$

Substitute (2) in eqn (1)

$$0.710 + 3.8 \times 10^{-3} R_g = 0.909 - 0.2 \times 10^{-3} R_g$$

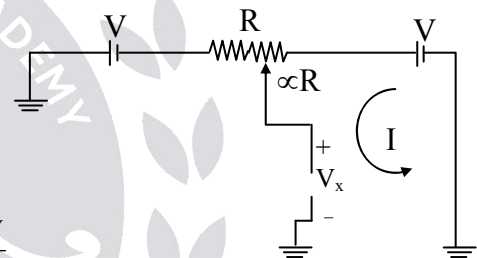
$$R_g = 49.72 \Omega \approx 50 \Omega$$

Substitute ' R_g ' value in eqn (2)

$$V_x = 0.710 + 3.8 \times 10^{-3} \times 50 = 0.9001 \text{ V}$$

09. Ans: (a)

Sol:



$$I = \frac{2V}{R}$$

Apply KVL in loop

$$-V + I\alpha R + V_x = 0$$

$$-V + \frac{2V}{R} \times \alpha R + V_x = 0$$

$$V - 2V\alpha = V_x$$

$$V_x = [1 - 2\alpha] V$$

10. Ans: (a)

Sol: $N_1 = 1$ $N_2 = 500$ $I_S = 5\text{A}$ Load $R_2 = 1\Omega$

Magnetizing ampere turns = 200 AT

$$I_0 = \frac{\text{Magnetizing ampere turns}}{\text{Primary turns}}$$

$$= \frac{200}{1} = 200 \text{ A}$$

Transformation ratio

$$n = \frac{N_2}{N_1}$$

$$= \frac{500}{1} = 500$$

The phase angle between primary & secondary current is

$$\theta = \frac{180}{\pi} \left(\frac{I_0 \cos(\alpha + \delta)}{n I_s} \right)$$

$$= \frac{180}{\pi} \left(\frac{200 \times \cos(0)}{500 \times 5} \right)$$

$$\approx 4.6^\circ \quad [\because (\alpha + \delta) \text{ is very small}]$$

11. Ans: (a)

Sol: % Ratio error = $\frac{K_n - R}{R} \times 100$

$$K_n = 200$$

$$R = \frac{I_p}{I_s} = \frac{100}{0.495} = 202.02$$

$$\% \text{ Ratio Error} = \frac{200 - 202.02}{202.02} \times 100$$

$$= -1\%$$

Solutions for Conventional Practice Questions

01.

Sol: The burden of secondary winding is purely resistive and therefore secondary winding PF is unity

$$\text{PF of exciting current} = 0.4$$

$$\cos(90 - \alpha) = 0.4$$

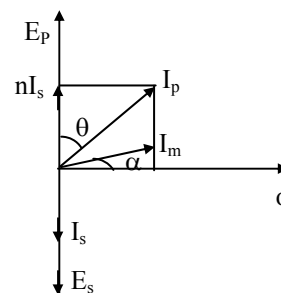
$$\alpha = 23.57$$

$$\text{Exciting current } I_0 = 1\text{A}$$

$$\text{Nominal ratio } K_n = \frac{1000}{5} = 200$$

Since there is no turn compensation, the turns ratio equal to the nominal ratio

$$n = K_n = 200$$



Rated secondary winding current, $I_s = 5\text{A}$

$$n I_s = 200 \times 5 = 1000\text{A}$$

Actual transformation Ratio

$$R = n + \frac{I_0}{I_c} \sin(\delta + \alpha)$$

$$= 200 + \frac{1}{5} \sin(0 + 23.57) = 200.08$$

$$\text{Ratio error} = \frac{K_n - R}{R} \times 100$$

$$= \frac{\text{Nominal Ratio} - \text{actual ratio}}{\text{actual ratio}} \times 100$$

$$= \frac{200 - 200.8}{200.8} \times 100 = -0.04\%$$

Phase angle error

$$\theta = \frac{180^\circ}{\pi} \left[\frac{I_0 \cos(\delta + \alpha)}{n I_s} \right]$$

$$= \frac{180^\circ}{\pi} \left[\frac{\cos(23.57)}{1000} \right]$$

$$= 0.0525$$

02.

Sol: Primary winding turns, $N_p = 1$

Secondary winding turns, $N_s = 300$

$$\text{Turns ratio, } n = \frac{N_s}{N_p} = 300$$

Secondary circuit burden impedance

$$= \sqrt{(1.5)^2 + (1.0)^2} = 1.8 \Omega$$

Secondary winding circuit

$$\cos \delta = \frac{1.5}{1.8} \text{ and } \sin \delta = \frac{1.0}{1.8} = 0.554$$

$$= 0.833$$

Secondary induced voltage

$$(E_s) = 5 \times 1.8 = 9.0V$$

Primary induced voltage

$$E_p = \frac{E_s}{300} = \frac{9}{300} = 0.03V$$

Loss component of current referred to primary winding.

$$I_c = \frac{\text{iron loss}}{E} = \frac{1.2}{0.03} = 40A$$

Magnetizing current, I_m

$$= \frac{\text{magnetizing mmf}}{\text{Primary winding turns}}$$

$$= \frac{100}{1} = 100A$$

Actual ratio, $R = n + \frac{I_0}{I_c} \sin(\delta + \alpha)$

$$= n + \frac{I_c \cos \delta + I_m \sin \delta}{I_s}$$

$$= 300 + \frac{40 \times 0.833 + 100 \times 0.555}{5}$$

$$= 317.6$$

$$K_n = n = 300$$

$$\text{Percentage Ratio} = \frac{K_n - R}{R} \times 100$$

$$= \frac{300 - 317.6}{317.6} \times 100 = -5.54\%$$

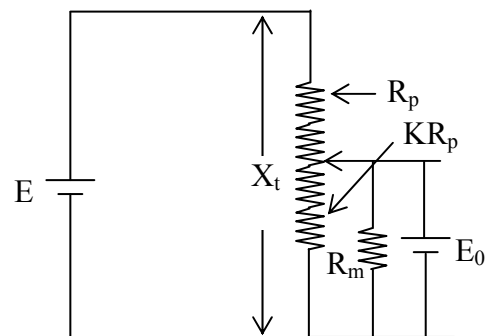
$$\text{Phase angle error } \theta = \frac{180^\circ}{\pi} \left(\frac{I_m \cos \delta - I_s \sin \delta}{n I_s} \right)$$

$$= \frac{180^\circ}{\pi} \left(\frac{100 \times 0.833 - 40 \times 0.555}{300 \times 5} \right)$$

$$= 2.34^\circ$$

03.

Sol: (a)



Given: $X_t = 120\text{mm}$, $R_p = 24\text{k}\Omega$, $X_i = 40\text{mm}$

So $K R_p = 8\text{k}\Omega$

Voltage V across $K R_p$ is

$$V = \frac{8}{24} E = 0.33E$$

After the connection of meter resistance

$$R_{eq} = K R_p \parallel R_m$$

$$\Rightarrow R_{eq} = \frac{15 \times 8}{15 + 8} = 5.211\text{k}\Omega$$

$$V_{eq} = \frac{5.211 \times E}{(24 - 8) + 5.211} = 0.2459E$$

$$\% \text{error} = \left(\frac{0.333 - 0.2459}{0.333} \right) \times 100 = 26.22\%$$

(b) To keep error within 3% V_{new} is the voltage developed across the common resistance of R_{eq} and R_{new} .

$$3 = \frac{(0.33 - V_{new})E}{0.33E} \times 100$$

$$V_{new} = 0.323E$$

$$\text{now } 0.323 = \frac{R_{new}}{16 + R_{new}} E$$

$$\Rightarrow R_{new} = 7.64\text{k}\Omega$$

$$\text{Now, } R_{max} = \frac{8R_{new}}{8 - R_{new}}$$

$$= \frac{8 \times 7.6442}{8 - 7.6442} = 172\text{k}\Omega$$

04.

Sol: Phase angle of pressure coil circuit (β) = $30'$

Phase angle of load = $\cos^{-1}(0.5) = 60^\circ$

Where

V = voltage across the load = 11 kV

I = load current = 100A

ϕ = Phase angle between current and voltage
= 60°

α = phase angle bandwidth

Currents in the current and pressure coils of watt meter

V_s = voltage across secondary of the potential transformer.

I_s = secondary current of current transformer.

I_p = current in the wattmeter pressure coil.

β = angle by which I_s lags V_s on account of inductance of pressure coil = $30' = 1/2^\circ$

δ = Phase angle of potential transformer = $45' =$

$$\frac{3^\circ}{4}$$

θ = phase angle of current transformer = $90' =$

$$1\frac{1}{2}^\circ$$

Phase angle between pressure coil current I_p and current I_s of wattmeter current coil

$$\alpha = \phi - \theta - \beta - \delta$$

$$= 60^\circ - \frac{3^\circ}{2} - \frac{1^\circ}{2} - \frac{3^\circ}{4} = 57.25^\circ$$

$$\text{Correction factor} = k = \frac{\cos \phi}{\cos \beta \cdot \cos \alpha}$$

$$= \frac{\cos 60^\circ}{\cos(0.5^\circ) \times \cos(57.25^\circ)} = 0.924$$

$$\text{Percentage ratio error} = \frac{k_n - R}{R} \times 100$$

$$\text{Actual ratio } R = \frac{k_n \times 100}{(100 + \text{percentage ratio error})}$$

$$\text{Actual ratio of C.T} = \frac{20 \times 100}{(100 - 0.2)} = 20.04$$

$$\text{Actual ratio of P.T} = \frac{100 \times 100}{(100 + 0.8)} = 99.2$$

Power of lead

$$= k \times \text{actual ratio of P.T} \times \text{actual ratio of C.T}$$

\times wattmeter \times wattmeter reading

$$(2) \text{ power of lead} = 11\text{kV} \times 0.5 \times 100$$

$$= 0.924 \times 20.4 \times 99.2 \times \text{wattmeter reading}$$

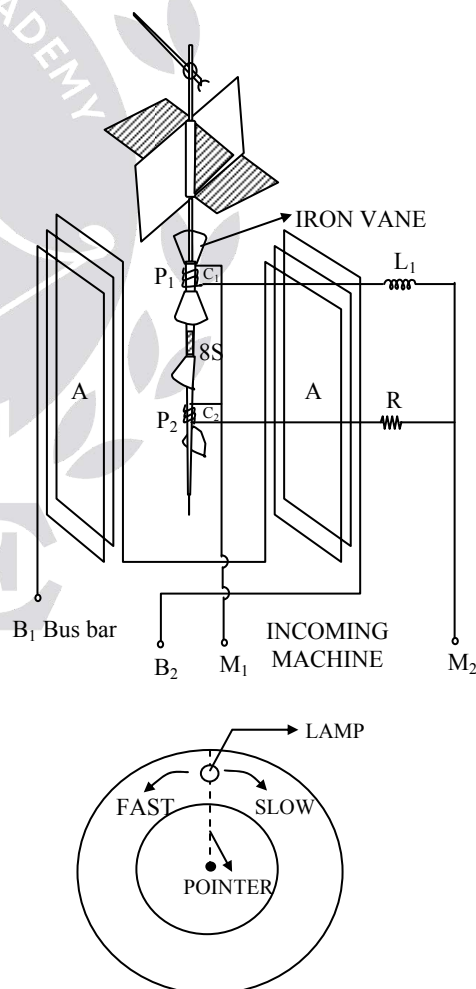
$$(3) \text{ Wattmeter reading} = 294.18 \text{ Watts}$$

8. Measurement of Frequency & Power factor

Solutions for Conventional Practice Questions

01.

Sol:



Constructional features of moving iron synchroscope:

- Figure above shows the construction of a moving iron synchroscope, which is due to Lip man.
- It has a fixed coil divided into two parts. This fixed coil A is designed for a small value of current and is connected in series with a resistance across two phases of the bus bar.
- There are two iron cylinders C_1 and C_2 mounted on the spindle. Each iron cylinder is provided with two iron vanes, whose axes are 180° out with each other.
- The iron cylinders are excited by two pressure coils P_1 and P_2 , which are connected to two phases of incoming machine.
- One of the coils has a series resistance and the other has a series inductance.
- This is done in order to create an artificial phase difference of 90° between the currents of two pressure coils.
- There are no control springs. The instrument is provided with a pointer which moves over a dial marked fast and slow.

Principle of working:

- When the Frequency of incoming machine is the same as that of the bus bars, the instrument behaves exactly like the corresponding form of the power factor meter.
- The deflection of the pointer from the plane of reference is equal to phase difference between the two voltages.
- However, if the frequencies of the two voltages are different, the pointer rotates

continuously at a speed corresponding to difference in frequency of the two voltages.

- The direction of rotation depends whether the incoming machine is too fast or too slow.
- Let v_1 and v_2 be the voltages of bus bar and incoming machine respectively.
- Let the frequencies of the two voltages be equal.

Torques produced by coils P_1 and P_2 are

$$T_1 = kv_1v_2\sin\theta\cos(\pm\alpha)$$

$$T_2 = kv_1v_2\sin(90^\circ - \theta)\cos(90^\circ \pm \alpha) \\ = kv_1v_2\cos\theta\sin(\pm\alpha)$$

Where

θ = deflection of the pointer from plane of reference. This plane of reference is the vertical position of the pointer.

α = phase angle between the two voltages.

- The two torques are in opposite direction, therefore, under equilibrium
 $T_1 = T_2$
 $kv_1v_2\sin\theta\cos(\pm\alpha) = kv_1v_2\cos\theta\sin(\pm\alpha)$ (or)
 $\theta = \pm\alpha$

- Thus the pointer is stationary and its deflection from plane of reference equals the phase difference between the two voltages.
- If the frequency of the incoming machine differs from that of the bus bars, the torques are

$$T_1 = kv_1v_2\sin\theta\cos(\pm\pi f't \pm \alpha)$$

And

$$T_2 = kv_1v_2\sin(90^\circ - \cos(90^\circ - (-2\pi f't \pm \alpha)) \\ = kv_1v_2\cos\theta\sin(\pm 2\pi f't \pm \alpha)$$

Where

$f' = f_2 - f_1$ = difference in two frequencies.

Hence at equilibrium

$$\sin\theta\cos(\pm 2\pi f't \pm \alpha) = \cos\theta\sin(\pm 2\pi f't \pm \alpha)$$

(or)

$$\theta = 2\pi f' t \pm \alpha$$

Thus, the moving system rotates with a frequency corresponding to difference in the two frequencies.

- The direction of rotation depends upon whether the frequency of incoming machine is higher (f' positive) or lower (f' negative) than the frequency at the bus bars
- The instant of synchronizing is when the pointer is stationary ($f' = 0$) and when it is at its vertical position.
- Moving iron synchrosopes are more common in use. They are cheap and their operation is simple and also they have a 360° scale.

02.

Sol: Construction and working principle of a single phase electro-dynamic power factor meter:

- The construction of a single phase electro-dynamometer type power factor is shown in below figure. It consists of a fixed coil, which acts as the current coil.
- This coil is split up into two parts and carries the current of the circuit under test. Therefore, the magnetic field produced by this coil is proportional to the main current.
- Two identical pressure coils A and B pivoted on a spindle constitute the moving system
- Pressure coil A has a non inductive resistance R connected in series with it, and coil B has highly inductive choke coil L connected in series with it.
- The two coils are connected across the voltage of the circuit. The values of R and L

are so adjusted that the two coils carry the same value of current at normal frequency. i.e. $R = \omega L$.

- The current through coil A is in phase with the circuit voltage, while that through coils B lags the voltage by an angle Δ which is nearly equal to 90°
- The angle between the planes of coils is also made equal to Δ . There is no controlling device. Connections to moving coils are made through thin silver or gold ligaments, which are extremely flexible and thus, give a minimum control effect on the moving system.
- In order to simplify the problem, we assume that the current through coil B lags the voltage by exactly 90° . Also that the angle between planes of coils is exactly 90° (i.e. $\Delta = 90^\circ$)
- Now, there will be two deflecting torques, one acting on coil A and the other on coil B. The coil windings are so arranged that the torques due to the two coils are opposite in direction.
- Therefore, the pointer will take up a position where these two torques are equal.
- Let us consider the case of a lagging power factor of $\cos\phi$

Deflecting torque acting on coil A is:

$$T_A = KVIM_{\max} \cos\phi \sin\theta$$

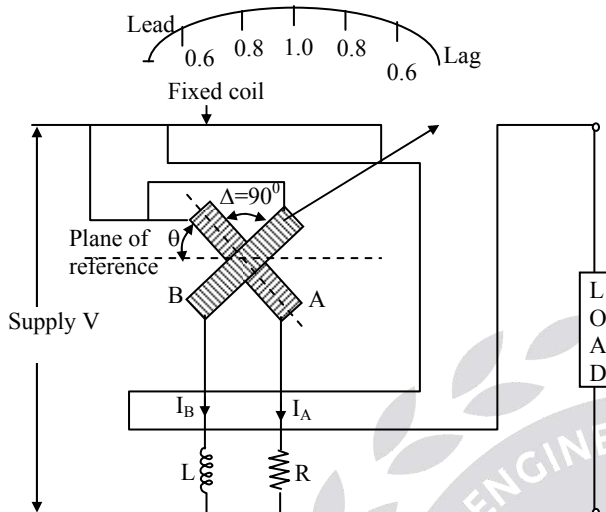
$\theta \rightarrow$ Angular deflection from the plane of reference,

$M_{\max} \rightarrow$ maximum value of mutual inductance between the two coils

This torque acts in the clockwise direction

Deflecting torque acting on coil B is:

$$T_B = KVIM_{\max} \cos(90^\circ - \phi) \sin(90^\circ + \theta) \\ = KVIM_{\max} \sin\phi \cos\theta$$



- This torque acts in the anticlockwise direction. The value of M_{\max} is the same in the two expressions, owing to similar constructions of the coils.
- The coils will take up such a position that the two torques are equal.

Hence at equilibrium $T_A = T_B$

$$KVIM_{\max} \cos\phi \sin\theta = KVIM_{\max} \sin\phi \cos\theta$$

$$\theta = \phi$$

\therefore The deflection of the instrument is a measure of phase angle of the circuit. The scale of the instrument can be calibrated directly in terms of power factor.

Comparison with Moving Iron type power factor Meter:

1. The working forces are very large in moving iron type power factor meter, whereas in electro-dynamometer type, working forces are very small

2. All coils in a moving iron instrument are fixed and therefore, the use of ligaments is eliminated.
3. The scale in moving iron instrument extends up to 360°
4. Moving iron instruments are simple and robust in construction, and also comparatively cheap
5. These instruments are less accurate than electro-dynamometer type.

9. Cathode Ray Oscilloscope

Solutions for Objective Practice Questions

01. Ans: (b)

Sol: Time period of one cycle = $\frac{8.8}{2} \times 0.5$

$$= 2.2 \text{ msec}$$

Therefore frequency = $\frac{1}{T} = \frac{1}{2.2 \times 10^{-3}}$

$$= 454.5 \text{ Hz}$$

The peak to peak Voltage = 4.6×100

$$= 460 \text{ mV}$$

Therefore the peak voltage $V_m = 230 \text{ mV}$

R.M.S voltage = $\frac{230}{\sqrt{2}} = 162.6 \text{ mV}$

02. Ans: (c)

Sol: In channel 1

The peak to peak voltage is 5V and peak to peak divisions of upper trace voltage = 2

Therefore for one division voltage is 2.5V

In channel 2, the no. of divisions for unknown voltage = 3

Divisions = 3, voltage/division = 2.5

$$\therefore \text{voltage} = 2.5 \times 3 = 7.5 \text{ V}$$

Similarly frequency of upper trace is 1kHz

So the time period T

$$(\text{For four divisions}) = \frac{1}{f}$$

$$T = \frac{1}{10^3} \Rightarrow 1 \text{ msec}$$

i.e., for four divisions time

period = 1m sec

In channel 2, for eight divisions of unknown waveform time period = 2m sec.

03. Ans: (c)

Sol: No. of cycles of signal displayed

$$\begin{aligned} &= f_{\text{signal}} \times T_{\text{sweep}} \\ &= 200\text{Hz} \times \left(10\text{cm} \times \frac{0.5\text{ms}}{\text{cm}} \right) = 1 \end{aligned}$$

i.e, one cycle of sine wave will be displayed.

$$\text{We know } V_{\text{rms}} = \frac{V_{\text{p-p}}}{2\sqrt{2}}$$

$$V_{\text{rms}} = \frac{N_v \times \text{Volt/div}}{2\sqrt{2}}$$

$$\Rightarrow N_v = \frac{2\sqrt{2} \times V_{\text{rms}}}{\text{Volt/div}}$$

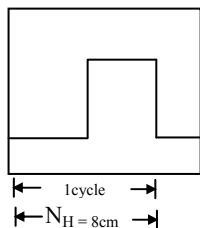
$$\Rightarrow N_v = \frac{2\sqrt{2} \times 300\text{mV}}{100\text{mv/cm}}$$

$$\Rightarrow N_v = 8.485\text{cm}$$

i.e 8.485cm required to display peak to peak of signal. But screen has only 8cm (vertical) As such, peak points will be clipped.

04. Ans: (b)

Sol:



→ Given data: Y input signal is a symmetrical square wave

$$f_{\text{signal}} = 25\text{KHz}, V_{\text{pp}} = 10\text{V}$$

→ Screen has 10 Horizontal divisions & 8 vertical divisions

which displays 1.25 cycles of Y-input signal.

$$\rightarrow V_{\text{pp}} = N_v \times \frac{\text{VOLT}}{\text{div}}$$

$$\Rightarrow \frac{\text{VOLT}}{\text{div}} = \frac{V_{\text{pp}}}{N_v} = \frac{10\text{V}}{5\text{cm}} = 2 \text{ Volt/cm}$$

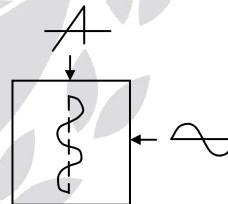
$$\rightarrow T_{\text{signal}} = N_H \text{ per cycle} \times \frac{\text{TIME}}{\text{div}}$$

$$\Rightarrow \frac{\text{TIME}}{\text{div}} = \frac{T_{\text{signal}}}{N_H \text{ per cycle}}$$

$$= \frac{1}{25\text{kHz} \times 8\text{cm}} = 5 \frac{\mu\text{s}}{\text{cm}}$$

05. Ans: (a)

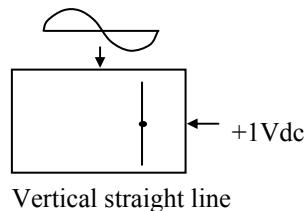
Sol: Frequency ratio is 2



∴ Two cycles of sine wave displayed on vertical time base

06. Ans: (a)

Sol:

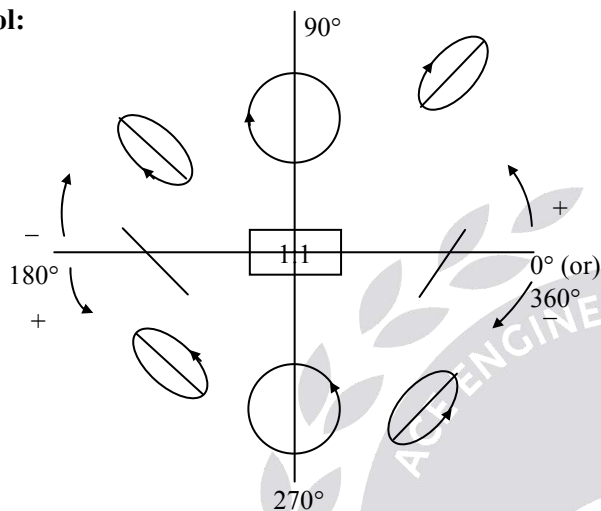


07. Ans: (a)

Sol: Since the coupling mode is set to DC the capacitance effect at the input side is zero. Therefore the waveform displayed on the screen is both DC and AC components.

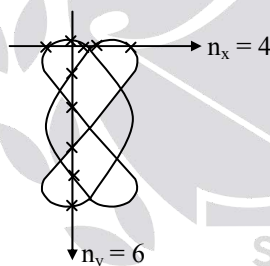
08. Ans: (d)

Sol:



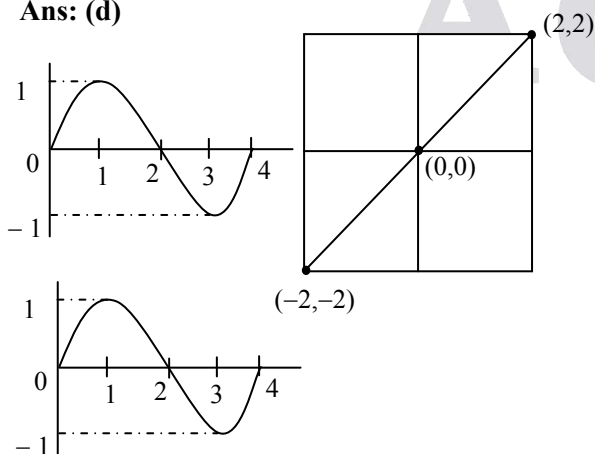
09. Ans: (b)

Sol: $f_y = \frac{n_x}{n_y} f_x$
 $= \frac{4}{6} \times 600 \text{ Hz}$
 $= 400 \text{ Hz}$



10. Ans: (d)

Sol:



Let $K_y = K_x = 2 \text{ Volt/div}$

t	V _y	V _x	d _y = k _y V _y	d _x = k _x V _x	points
0	0	0	0	0	(0,0)
1	1	1	2	2	(2,2)
2	0	0	0	0	(0,0)
3	-1	-1	-2	-2	(-2,-2)
4	0	0	0	0	(0,0)

By using these points draw the line which is a diagonal line inclined at 45° w.r.t the x-axis.

11. Ans: (d)

Sol: Voltage signal = $5 \sin(314t + 45^\circ)$

$$f_{\text{signal}} = \frac{314}{2\pi} \text{ Hz}$$

$$= 50 \text{ Hz}$$

No. of cycles of signal displayed

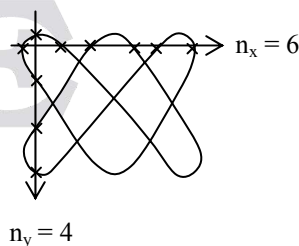
$$= f_{\text{signal}} \times T_{\text{sweep}}$$

$$= 50 \times 10 \times 5 \text{ ms/div}$$

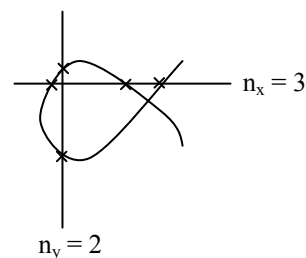
$$= 2.5$$

12. Ans: (d)

Sol:



$$\frac{f_y}{f_x} = \frac{6}{4} \Rightarrow \frac{3}{2}$$



$$\frac{f_y}{f_x} = \frac{3}{2}$$

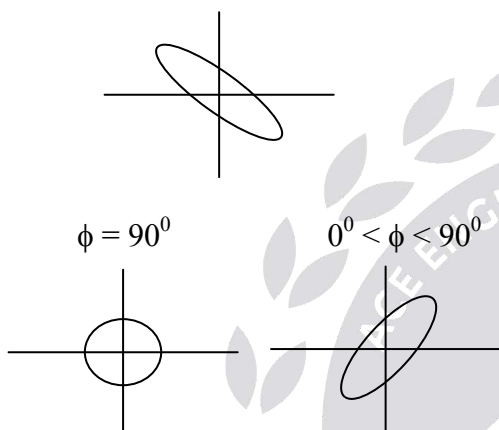
13. Ans: (a)

Sol: Lissajous figures are used for measurement of frequency and phase difference

14. Ans: (d)

Sol:

$$90^\circ < \phi < 180^\circ$$



Because of phase difference only figures changes from ellipse to circle and back to ellipse.

Solutions for Conventional Practice Questions

01.

Sol: We know: $t_m = \sqrt{t_s^2 + t_0^2}$ or $t_s = \sqrt{t_m^2 - t_0^2}$

Where, t_m = measured rise time

t_s = actual or true rise time of signal

t_0 = oscilloscope rise time

Given that: $t_0 = 15 \text{ ns}$ & $t_m = 20 \text{ ns}$

$$\therefore t_s = \sqrt{t_m^2 - t_0^2} = \sqrt{(20\text{ns})^2 - (15\text{ns})^2} = 13.23\text{ns}$$

Therefore, the actual rise time of signal is 13.23 ns

02.

$$\begin{aligned} \text{Sol: } v_x &= \sqrt{\frac{2eV_a}{m}} \\ &= \sqrt{\frac{2 \times 1.602 \times 10^{-19} \text{ C} \times 1000\text{V}}{9.11 \times 10^{-31} \text{ kg}}} \\ &= 1.87 \times 10^7 \text{ m/s} \end{aligned}$$

03.

Sol: given that:

Probe resistance, $R_p = 4\text{M}\Omega$

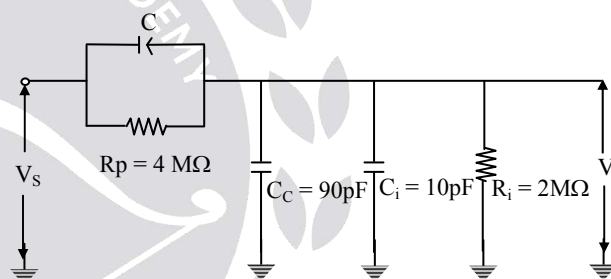
Probe capacitance, $C_p = C$

Cable capacitance, $C_c = 90\text{pF}$

CRO input resistance, $R_i = 2\text{M}\Omega$

CRO input resistance, $C_i = 10\text{pF}$

The equivalent circuit



We know $R_p C_p = R_i (C_c + C_i)$

$$\Rightarrow C_p = \frac{2\text{M}\Omega(90\text{pF} + 10\text{pF})}{4\text{M}\Omega} \Rightarrow C_p = 50\text{pF}.$$

$V_i = K \cdot V_s$ where K is attenuation factor

$$K = \frac{V_i}{V_s} = \frac{R_i}{R_p + R_i} \quad (\text{or}) \quad \frac{C_p}{C_p + (C_i + C_c)}$$

$$\therefore K = \frac{2\text{M}\Omega}{6\text{M}\Omega} \quad \text{or} \quad \frac{50\text{pF}}{150\text{pF}}$$

$$K = \frac{1}{3}$$

i.e., The test signal voltage will be attenuated by 3 times

04.

Sol: Given

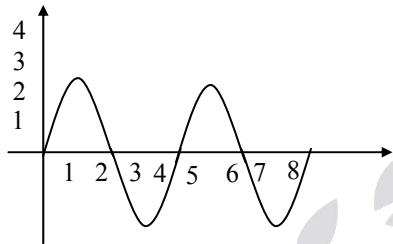
Vertical amplifier sensitivity = 5V/cm

Sweep speed = 50μs/cm

Peak – to Peak amplitude = 5.4 cm

Distance for two complete cycles = 8.4cm

From the above given data wave form can be constructed as shown below.



From the above wave form one cycle of wave form can be represented in 4.2 cm.

Voltage (Peak –Peak) = Vertical amplifier sensitivity × Peak to Peak amplitude.

$$= 5.4 \times \frac{5V}{cm} = 27V$$

$$\text{Rms voltage} = \frac{V_{p-p}}{2\sqrt{2}}$$

$$= \frac{27}{2\sqrt{2}} = 9.54V$$

Time period for one cycle

= sweep speed × distance for one cycle

= 50μs/cm × 4.2

= 210μs

$$\text{Frequency} = \frac{1}{\text{Time Period}} = \frac{1}{210 \times 10^{-6}}$$

$$= 4.76 \text{ kHz}$$

(b) Voltage applied to Horizontal axis = $V_{m1} \cos \omega t$

Voltage applied to vertical axis = $V_{m2} \sin \omega t$

When $\omega t = 0$ then ,

$$V_y = V_{m2} \sin (0) = 0; V_x = V_{m1} \cos(0) = V_{m1}$$

When $\omega t = 30^\circ$ then,

$$V_x = 0.866V_{m1}; V_y = 0.5 V_{m2}$$

When $\omega t = 60^\circ$ then,

$$V_x = 0.5V_{m1}; V_y = 0.866 V_{m2}$$

When $\omega t = 90^\circ$ then,

$$V_x = 0; V_y = V_{m2}$$

When $\omega t = 120^\circ$ then,

$$V_x = -0.5V_{m1}; V_y = 0.866 V_{m2}$$

When $\omega t = 150^\circ$ then,

$$V_x = -0.866V_{m1}; V_y = 0.5 V_{m2},$$

When $\omega t = 180^\circ$ then,

$$V_x = -V_{m1}; V_y = 0$$

When $\omega t = 210^\circ$ then,

$$V_x = -0.866 V_{m1}; V_y = -0.5 V_{m2}$$

When $\omega t = 240^\circ$ then,

$$V_x = -0.5V_{m1}; V_y = -0.866 V_{m2}$$

When $\omega t = 270^\circ$ then,

$$V_x = 0; V_y = -V_{m2}$$

When $\omega t = 300^\circ$ then,

$$V_x = 0.5V_{m1}; V_y = 0.866 V_{m2}$$

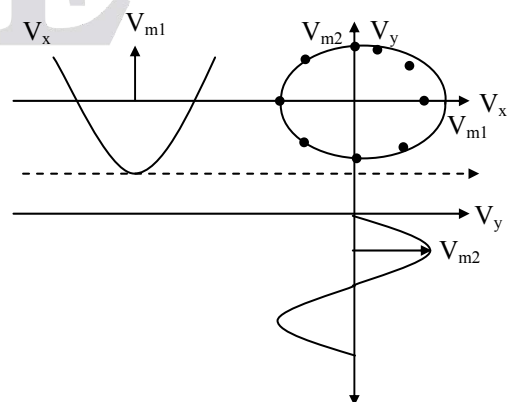
When $\omega t = 330^\circ$ then,

$$V_x = 0.866; V_{m1}; V_y = -0.5 V_{m2}$$

When $\omega t = 360^\circ$ then,

$$V_x = 1V_{m1}; V_y = 0$$

If we plot the above obtained V_y and V_x values on x-y plot for different angles then it can be represented as.



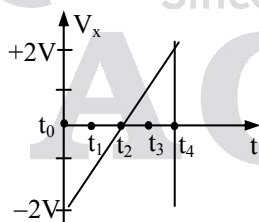
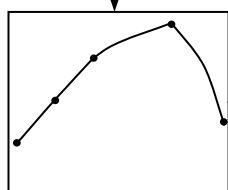
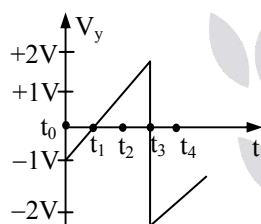
From the above plot we can conclude that

- When $V_{m1} \neq V_{m2}$ the trace will be an ellipse with 'x' axis as major axis when $V_{m1} > V_{m2}$ and with 'y' axis as major axis when $V_{m2} > V_{m1}$.
- When $V_{m1} = V_{m2}$ the trace will be a circle.

05.

Sol: Assume peak amplitude of saw tooth wave-form is 2V; the screen dimensions are 8 cm × 8 cm. The horizontal dial setting is 2 volt-cm. Given that y input saw tooth signal is leading x-input saw tooth signal by 90°.

t	V_x	V_y
t_0	-2V	-1V
t_1	-1V	0
t_2	0	+1V
t_3	+1V	+2V
t_4	+2V	-1V



06.

Sol: $V_a = 2000V$

Length of deflecting plates $l_d = 2$ cm

Distance between the plates (d) = 0.5 cm

Distance between centre of plates to the screen = 30 cm

Deflection height of the beam (D) = 3cm

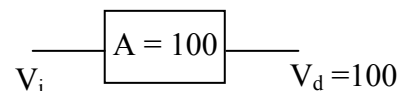
Gain of the amplifier (A) = 100

$$D = \frac{L \ell_d V_d}{2dV_a} \quad (\because V_d = \text{deflection voltage})$$

$$V_d = \frac{2dV_a \times D}{L \ell_d}$$

$$V_d = \frac{2 \times 0.5 \times 2000 \times 3}{30 \times 2}$$

$$V_d = 100 \text{ V}$$



$$\frac{V_d}{V_i} = 100$$

$$V_i = 1V$$

$$\text{Velocity of electron beam } (V_{ox}) = \sqrt{\frac{2qV_a}{m}}$$

q → Charge of an electron = $1.65 \times 10^{-19} \text{ C}$

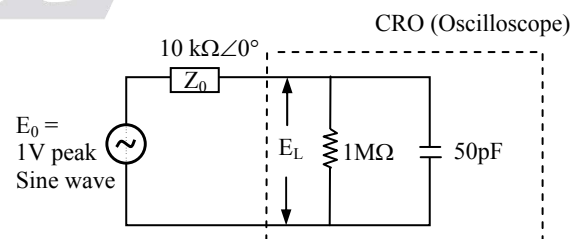
V_a → anode voltage required = 2000 V

m → mass of an electron = $9.1 \times 10^{-31} \text{ kg}$

$$V_{ox} = \sqrt{\frac{2qV_a}{m}} = \sqrt{\frac{2 \times 1.65 \times 10^{-19} \times 2000}{9.1 \times 10^{-31}}} = 26.93 \times 10^6 \text{ m/s}$$

07.

Sol:



(a) $f = 100 \text{ kHz}$:

$$X_C = \frac{1}{2\pi \times 100\text{kHz} \times 50\text{pF}}$$

$$= 32000 \Omega$$

Impedance of oscilloscope

$$(Z_L) = \frac{R \times (-jX_c)}{R - jX_c}$$

$$Z_L = \frac{10^6 \times (-j32000\Omega)}{10^6 - j32000\Omega}$$

$$= 32000\Omega \angle -90^\circ$$

Voltage indicated by CRO (E_L)

$$= \frac{E_0}{1 + Z_0 / Z_L}$$

$$E_L = \frac{1V \angle 0^\circ}{1 + \frac{10k\angle 0^\circ}{32000 \angle -90^\circ}}$$

$$= 0.954V \angle -17.4^\circ \text{ peak}$$

(b) $f = 1\text{MHz}$

$$X_C = \frac{1}{2\pi \times 1 \times 10^6 \times 50\text{pF}}$$

$$= 3200\Omega$$

Impedance of oscilloscope (Z_L)

$$Z_L = \frac{10^6(-j3200\Omega)}{10^6 - j3200\Omega}$$

$$= 3.2 \times 10^3 \angle -90^\circ$$

Voltage indicated by CRO (E_L)

$$= \frac{E_0}{1 + Z_0 / Z_L}$$

$$E_L = \frac{1V \angle 0^\circ}{1 + \frac{10k\Omega \angle 0^\circ}{3.2 \times 10^3 \angle -90^\circ}}$$

$$= 0.304V \angle -72.3^\circ$$

10. Digital Voltmeters

Solutions for Objective Practice Questions

01. Ans: (a)

Sol: The type of A/D converter normally used in a $3\frac{1}{2}$ digit multimeter is Dual-slope integrating type since it offers highest Accuracy, Highest Noise rejection and Highest Stability than other A/D converters.

02. Ans: (d)

Sol: DVM measures the average value of the input signal which is 1 V.

\therefore DVM indicates as 1.000 V

03. Ans: (c)

Sol: 0.2% of reading + 10 counts \rightarrow (1)

$$= 0.2 \times \frac{100}{100} + 10(\text{sensitivity} \times \text{range})$$

$$= 0.2 \times \frac{100}{100} + 10\left(\frac{1}{2 \times 10^4} \times 200\right)$$

$$= 0.2 + 0.1 = \pm 0.3 \text{ V}$$

$$\% \text{error} = \pm \frac{0.3}{100} \times 100 = 0.3\%$$

04. Ans: (d)

Sol: When $\frac{1}{2}$ digit is present voltage range becomes double. Therefore 1V can read upto 1.9999 V.

05. Ans: (d)

$$\text{Sol: Resolution} = \frac{\text{full-scale reading}}{\text{maximum count}} = \frac{9.999V}{9999}$$

$$= 1\text{mV}$$

06. Ans: (b)

Sol: Sensitivity = resolution \times lowest voltage range

$$= \frac{1}{10^4} \times 100 \text{ mV}$$

$$= 0.01 \text{ mV}$$

07. Ans: (c)

Sol: The DVM has $3\frac{1}{2}$ digit display

Therefore, the count range is from 0 to 1999 i.e., 2000 counts.

$$\text{Resolution} = \frac{\text{given voltage range}}{\text{Maximum count}}$$

$$= \frac{200\text{mV}}{2000} = 0.1\text{mV}$$

08. Ans: (a)

Sol: Resolution = $\frac{\text{max. voltage}}{\text{max. count}}$

$$= \frac{3.999}{3999} = 1\text{mV}$$

09. Ans: (b)

Sol: A and R are true, but R is not correct explanation for A.

10. Ans: (c)

Sol: When $\frac{1}{2}$ digit switched ON, then DVM will be able to read more than the selected range.

11. Ans: (b)

Sol: Given, $3\frac{1}{2}$ digit, FSD value of 200 mV

$$\text{Resolution} = \frac{200\text{mV}}{2000} = 0.1\text{mV}$$

$$\therefore \text{Error} = \frac{0.5}{100} \times 100\text{mV} + 5 \times 0.1\text{mV}$$

$$= \pm 1 \text{ mV}$$

\therefore The value lies between 99.0 mV & 101.0 mV

Solutions for Conventional Practice Questions

01.

Sol: The count range of $3\frac{1}{2}$ digit DVM is from 0 to 1999, i.e., 2000 counts.

Due to adding $\frac{1}{2}$ digit, the 1V range of this

DVM extended to 2V and 10V range extended to 20V.

$$\left. \begin{array}{l} \text{resolution of } 3\frac{1}{2} \text{ digit DVM} \\ \text{in 1V range of operation} \end{array} \right\} = \frac{1}{2 \times 10^3} \times 2\text{V}$$

$$= \frac{2\text{V}}{2000 \text{ counts}} = 1 \text{ mV}$$

$$\left. \begin{array}{l} \text{resolution of } 3\frac{1}{2} \text{ digit DVM} \\ \text{in 10V range of operation} \end{array} \right\} = \frac{1}{2 \times 10^3} \times 20\text{V}$$

$$= \frac{20\text{V}}{2000 \text{ counts}} = 10 \text{ mV.}$$

02.

Sol: We know: $V_m T_1 = V_{\text{ref}} T_2$

$$\Rightarrow V_m N_F = V_{\text{ref}} n$$

$$\Rightarrow V_m = \frac{V_{\text{ref}}}{N_F} \times n$$

$$= \frac{1000\text{V}}{1000} \times 762$$

$$= 762\text{V.}$$

03.

Sol: For analog multimeter

$$V_m = 10V, V_{FS} = 20V,$$

$$G.A.E = \pm 2\% \text{ of } V_{FS}$$

In question asking amount of error in% means limiting error.

$$\% \text{ Limiting error} =$$

$$\text{Measured value} \times \frac{x}{100} = \text{G.A.E value form}$$

Where $x \rightarrow \% \text{ limiting error}$

$$= 10 \times \frac{x}{100} = \frac{2}{100} \times (20)$$

$$\Rightarrow x = 4\%$$

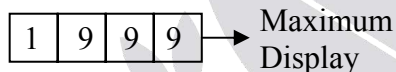
$$\therefore \% \text{ error} = 4\%$$

$$\Rightarrow \text{For } 3\frac{1}{2} \text{ digital multimeter, accuracy of}$$

$$\pm[0.5\% \text{ of reading} + 1 \text{ count}]$$

$$\Rightarrow \text{For 1 count} = \frac{V_{FS}}{\text{Maximum value of Display}}$$

$$\Rightarrow \text{For } 3\frac{1}{2} \text{ DMM,}$$



$$1 \text{ count} = \frac{20}{1999} = 0.01$$

$$= \pm \left[\frac{0.5}{100} \times (10) + 0.01 \right] = 0.06$$

This is absolute error

$$\therefore \% \text{ error} = \frac{0.06}{10} \times 100 = 0.6\%$$

11. Q- Meter

Solutions for Objective Practice Questions

01. Ans: (a)

$$\text{Sol: } C_1 = 300\text{pF} \quad C_2 = 200 \text{ pF}$$

$$Q = 1/(\omega C_1 R)$$

$$= 120 = 1/(C_2 + C_x)R$$

$$C_1 = C_2 + C_x$$

$$\therefore C_x = 100 \text{ pF}$$

02. Ans: (b)

$$\text{Sol: } \% \text{error} = -\frac{r}{r+R} \times 100$$

$$= -\frac{0.02}{0.02+10} \times 100 = -0.2\%$$

03. Ans: (c)

Sol: Q-meter consists of R, L, C connected in series.

\therefore Q-meter works on the principle of series resonance.

04. Ans: (b)

Sol: Given data: $C_d = 820 \text{ pF}$,

$$\omega = 10^6 \text{ rad/sec} \text{ \& } C = 9.18 \text{ nF}$$

$$\text{We know, } L = \frac{1}{\omega^2 [C + C_d]}$$

$$= \frac{1}{(10^6)^2 [9.18 \text{ nF} + 820 \text{ pF}]} = 100 \mu\text{H}$$

The inductance of coil tested with a Q-meter is $100 \mu\text{H}$.

05. Ans: (b)

Sol: A series RLC circuit exhibits voltage magnification property at resonance. i.e., the voltage across the capacitor will be equal to Q-times of applied voltage.

Given that V = applied voltage and
 V_0 = Voltage across capacitor

There fore, $Q = \frac{V_{c \max}}{V_{in}}$

$$\Rightarrow Q = \frac{V_0}{V}$$

06. Ans: (b)

Sol: $f_1 = 500 \text{ kHz}$; $f_2 = 250 \text{ kHz}$

$C_1 = 36 \text{ pF}$; $C_2 = 160 \text{ pF}$

$$n = \frac{250 \text{ kHz}}{500 \text{ kHz}}$$

$$\Rightarrow n = 0.5$$

$$C_d = \frac{36 \text{ pF} - (0.5)^2 160 \text{ pF}}{(0.5)^2 - 1}$$

$$= 5.33 \text{ pF}$$

07. Ans: (c)

Sol: $Q = \frac{\text{capacitor voltmeter reading}}{\text{Input voltage}}$

$$= \frac{10}{500 \times 10^{-3}}$$

$$= 20$$

08. Ans: i \rightarrow (c), ii \rightarrow (a)

Sol: (i) $C_d = \frac{C_1 - n^2 C_2}{n^2 - 1}$

$$= \frac{360 - 288}{3}$$

$$= 24 \text{ pF}$$

(ii) $L = \frac{1}{\omega_1^2 [C_1 + C_d]}$

$$= \frac{1}{[2\pi \times 500 \times 10^3]^2 [24 + 360] \times 10^{-6}} = 264 \mu\text{H}$$

09. Ans: (b)

Sol: $Q_{\text{true}} = Q_{\text{meas}} \left(1 + \frac{r}{R_{\text{coil}}} \right)$

$$Q_{\text{actual}} = Q_{\text{observed}} \left[1 + \frac{R}{R_s} \right]$$

10. Ans: (c)

Sol: $1 + \frac{C_d}{C} = \frac{Q_{\text{true}}}{Q_{\text{measured}}}$

$$\Rightarrow \frac{C_d}{C} = \frac{245}{244.5} - 1$$

$$= 2.044 \times 10^{-3}$$

$$\Rightarrow \frac{C}{C_d} = 489$$

11. Ans: (b)

Sol: Q-meter works on the principle of series resonance

$$V_c = Q \times V_{in}$$

\therefore Both A & R are individually true but R is not the correct explanation of A.

Solutions for Conventional Practice Questions

01.

Sol: Given that: $f_1 = 3 \text{ MHz}$ & $C_1 = 251 \text{ pF}$

$f_2 = 6 \text{ MHz}$ & $C_2 = 50 \text{ pF}$

$$\therefore n = \frac{f_2}{f_1} = \frac{6 \text{ MHz}}{3 \text{ MHz}} = 2$$

After inserting the test coil into socket of Q – meter, the resonance is obtained for the first time at 3 MHz with tuning capacitance set to 251 pF. Then, the frequency is doubled (i.e., $n = 2$) and, the resonance is obtained for the second time at 6 MHz with tuning capacitance set to 50 pF.

$$\begin{aligned}\text{We know: } C_d &= \frac{C_1 - n^2 C_2}{n^2 - 1} \\ &= \frac{251\text{pF} - (2)^2 50\text{pF}}{(2)^2 - 1} \\ &= \frac{251\text{pF} - 200\text{pF}}{3}\end{aligned}$$

$$\Rightarrow C_d = 17\text{pF}.$$

\therefore The self capacitance or distributed capacitance of coil is found to be 17pF.

02.

Sol: The effective Q-of the coil, $Q_t = \frac{1}{\omega CR}$

$$\begin{aligned}&= \frac{1}{2\pi \times 1 \times 10^6 \times 60 \times 10^{-12} \times 10} \\ &= 265.258\end{aligned}$$

The indicated or calculated Q-of the coil

$$\begin{aligned}Q_{ind} &= \frac{1}{2\pi \times 1 \times 10^6 \times 60 \times 10^{-12} \times (10 + 0.02)} \\ &= 264.729\end{aligned}$$

$$\begin{aligned}\% \text{ error} &= \frac{Q_{ind} - Q_t}{Q_t} \times 100 \\ &= \frac{264.729 - 265.258}{265.258} \times 100 \\ &= -0.19943\%\end{aligned}$$

03.

Sol: Refer previous Q for working of Q – meter
given that: $f_1 = 1\text{MHz}$ & $C_1 = 1530\text{ pF}$

$$f_2 = 3\text{ MHz} \text{ \& } C_2 = 162\text{ pF}$$

$$n = \frac{f_2}{f_1} = \frac{3\text{MHz}}{1\text{MHz}} = 3$$

After inserting the test coil into socket of Q – meter, the resonance is obtained for the first time at 1MHz with tuning capacitor adjusted to 1530PF. Then the frequency is tripled (i.e., $n = 3$)

and the resonance is obtained for the second time at 3MHz with tuning capacitor adjusted to 162 pF.

$$\begin{aligned}\text{We know: } C_d &= \frac{C_1 - n^2 C_2}{n^2 - 1} \\ &= \frac{1530\text{pF} - (3) \times 162\text{pF}}{(3)^2 - 1} \\ &= \frac{1530\text{pF} - 486\text{pF}}{8}\end{aligned}$$

$$C_d = 9\text{ pF}$$

\therefore The self capacitance of the coil is 9 pF.

04.

Sol: Given distributed capacitance $C_d = 20\text{PF}$

Tuning capacitance at first resonance = $C_1 = 200\text{pF}$

Tuning capacitance at second resonance = $C_2 = ?$

First resonance frequency occurs at

$$\begin{aligned}f_1 &= \frac{1}{2\pi\sqrt{L(C_d + C_1)}} \\ &= \frac{1}{2\pi\sqrt{L(220)}}\end{aligned}$$

Second resonance frequency will be double the first resonance frequency

$$f_2 = 2f_1$$

$$\begin{aligned}f_2 &= \frac{1}{2\pi\sqrt{L(C_2 + C_d)}} = \frac{2 \times 1}{2\pi\sqrt{L(C_1 + C_d)}} \\ \Rightarrow \frac{1}{2\pi\sqrt{L(C_2 + C_d)}} &= \frac{2 \times 1}{2\pi\sqrt{L(C_1 + C_d)}}\end{aligned}$$

By cross multiplying and squaring

$$(C_1 + C_d) = 4 \times (C_2 + C_d)$$

By solving

$$C_2 = \frac{C_1 - 3C_d}{4} \dots\dots\dots (1)$$

By substituting values of C_d and C_1 in (1) then

$$C_2 = \frac{200 - 3 \times 20}{4} = \frac{200 - 60}{4}$$

$$= 35 \text{ pF}$$

Tuning capacitance at second resonance

$C_2 = 35 \text{ pF}$ and

Second resonance frequency will be double the first resonance frequency

$$f_2 = 2f_1$$

05.

Sol: $Q = \frac{\omega L}{R}$

$$Q = \frac{X_L}{R}$$

$$Q = \frac{100}{10} = 10$$

06.

Sol: Given that: $f_1 = 1 \text{ MHz}$, $C_1 = 210 \text{ pF}$,
 $Q_1 = 100$ and $f_2 = 2 \text{ MHz}$, $C_2 = 45 \text{ pF}$

$$n = \frac{2 \text{ MHz}}{1 \text{ MHz}} = 2$$

$$C_d = \frac{210 \text{ pF} - 2^2 \times 45 \text{ pF}}{2^2 - 1}$$

$$= \frac{210 \text{ pF} - 4 \times 45 \text{ pF}}{3} = 10 \text{ pF}$$

$$L = \frac{1}{(2\pi \times 1 \text{ MHz})^2 [210 \text{ pF} + 10 \text{ pF}]}$$

$$= 1.15 \times 10^{-4} \text{ H}$$

$$R_{\text{coil}} = \frac{2\pi \times 1 \text{ MHz} \times 1.1513 \times 10^{-4}}{100}$$

$$= 7.245 \Omega$$

12. Basics of Transducers

Solutions for Objective Practice Questions

01. **Ans: (d)**

Sol: piezo electric transducer is an active transducer

02. **Ans: (c)**

Sol: Active transducers do not require an auxiliary power source to produce their output. From given options thermocouple & solar cell pair transducers are active transducers as they produce output with no auxiliary power source.

03. **Ans: (d)**

Sol: Pressure → Piezoelectric crystal

Temperature → Thermistor

Displacement → Capacitive transducer

Stress → Resistance strain gauge

04. **Ans: (d)**

Sol: Thermocouple → Cold junction compensation

Strain gauge → DC bridge

Piezoelectric crystal → Charge amplifier

LVDT → Phase sensitive detector

05. **Ans: (b)**

Sol: Usually from transducers we get small output which is not sufficient for further processing, so in order to amplify that output we require signal conditioning circuit. finally to read the output we require recorder.

06. **Ans: (d)**

Sol: Bolometer → measurement of power at 500 MHz

Hot wire anemometer → measurement of flow of air around an aeroplane.

C-type bourdon tube → measurement of high pressure

Optical pyrometer → measurement of temperature of furnace.

07. Ans: (d)

Sol: Charge amplifier with very low bias current and high input impedance → piezoelectric sensor for measurement of static force

Voltage amplifier with low bias current and very high input impedance → Glass electrode PH sensor

Voltage amplifier with very high CMRR sensing applications → strain gauge in unipolar DC wheatstone bridge.

08. Ans: (b)

Sol: Mcleod gauge → Pressure

Turbine meter → Flow

Pyrometer → Temperature

Synchros → Displacement

09. Ans: (a)

Sol: Variable capacitance device → Pressure transducer

Orifice meter → Flow measurement

Thermistors → Temperature measurement

10. Ans: (b)

Sol: From given options diaphragm and pivot torque are employed for displacement measurement while thermistor and thermocouple not related to displacement measurement.

11. Ans: (a)

Sol: Instrumentation amplifier is used to amplify signals from transducer

12. Ans: (a)

Sol: LVDT gives linear output & also very accurate compare to any other transducer given in options.

13. Ans: (c)

Sol: The lower limit of useful working range of a transducer is determined by transducer error and noise.

14. Ans: (d)

Sol: From given options, thermocouple and thermopile, piezoelectric pick-up, photovoltaic cell are self generating type transducers.

Solutions for Conventional Practice Questions

01.

Sol: Transducers can be classified

- Based upon transduction principle
- as primary and secondary transducers
- as passive and active transducers
- as analog and digital transducers
- as transducers and inverse transducers

Based upon transduction principle

The transducers can be classified on the basis of principle of transduction as resistive, inductive, capacitive etc., depending upon how they convert the input quantity into resistance, inductance or capacitance respectively.

02.

Sol: Primary and Secondary Transducers:

The first transducer which converts physical phenomenon into displacement, pressure, velocity etc. which is to be accepted by next stage is known as “**Primary Transducer**”.

The output of the primary transducer is converted subsequently into a usable output by a device called “**Secondary Transducer**”

Passive and Active Transducers:

Passive transducers: They derive the power required for transduction from an auxiliary power source.

Eg: Resistive, inductive and capacitive transducers.

Active transducers: They do not require an auxiliary power source to produce their output. They are also known as self – generating type since they develop their own voltage or current output.

Eg: piezoelectric, photovoltaic etc.

Analog and digital Transducers:

Analog transducers: These transducers convert the input quantity into an analog output which is a continuous function of time.

Eg: LVDT, thermocouple etc.

Digital Transducers:-These transducers convert the input quantity into an electrical output which is in the form of pulses.

Transducers & Inverse Transducers

Transducer: A transducer can be broadly defined as a device which converts a non – electrical quantity into an electrical quantity.

Inverse transducer: An inverse transducer is defined as a device which converts an electrical quantity into a non – electrical quantity.

03.

Sol: In the direct method of measurement, the physical quantities like length or mass are measured directly by the measuring instruments. The indirect method of measurement comprises of various stages for the measurement of the physical quantity like temperature, pressure,

force etc, since they cannot be measured by the direct instruments. In this method, the transducer is used which is connected to a host of other instruments to convert one form of energy that cannot be measured into the other form that can be measured easily. The input and the output values are calibrated so that for all the value of output the value of the input can be calculated.

Transducer:

The transducers that convert the mechanical input signals into electrical output signals are called as electrical transducers. The output obtained from the electrical transducers can be read by the humans or it can given as input to the controllers.. The input given to the electrical transducers can be in the form of the displacement, strain, velocity, temperature, flow etc and the output obtained from them can be in the form of current, voltage and change in resistance, inductance and capacitance. The output can be measured easily and it is calibrated against the input, thus enabling the measurement of the value of the input.

- 1. Potentiometers:** They convert the change in displacement into change in the resistance, which can be measured easily.
- 2. Variable Capacitance Transducers:** These comprise of the two parallel plates between which there is dielectric material like air. The change in distance between the two plates produced by the displacement results in change in capacitance, which can be easily measured.
- 3. Variable Resistance Transducers:** There is change in the resistance of these sensors when certain physical quantity is applied to it. It is most commonly used in resistance

thermometers or thermistors for measurement of temperature.

4. **Magnetic sensors:** The input given to these sensors is in the form of displacement and the output obtained is in the form of change in inductance or reluctance and production of the eddy currents.
5. **Piezoelectric transducers:** When force is applied to these transducers, they produce voltage that can be measured easily. They are used for measurement of pressure, acceleration and force.
6. **Strain gauges:** When strain gauges are strained or stretched there is change in their resistance. They consist of the long wire and are able to detect very small displacements produced by the applied force or pressure.
7. **Photo electric transducers:** When the light is applied to these transducers, they produce voltage.
8. **Linear variable differential transformer (LVDT):** LVDT is the transformer consisting of the primary and the secondary coil. It converts the displacement into the change in inductance.
9. **Ultrasonic Transducers:** These transducers use the ultrasonic or ultrasound waves to measure parameters like fluid level, flow rate etc.

Apart from these, there are some more electrical type of transducers like moving coil type, changing dielectric type, changing core positions type etc.

i) Inductive transducer:

The inductive transducers work on the principle of the magnetic induction of magnetic material. Just as the resistance of the electric conductor depends on number of factors, the induction of

the magnetic material depends on a number of variables like the number of turns, of the coil on the material, the size of the magnetic material, and the permeability of the flux path. In the inductive transducers, the magnetic materials are used in the flux path and there are one or more air gaps. The change in the air gap also results in change in the inductance of the circuit and in most of the inductive transducers; it is used for the working of the instrument.

ii) Capacitive transducer. The capacitive transducer or sensor is nothing but the capacitor with variable capacitance. The capacitive transducer comprises of two parallel metal plates that are separated by the material such as air, which is called as the dielectric material. In the typical capacitor, the distance between the two plates is fixed, but in variable capacitance transducers, the distance between the two plates is variable.

In the instruments using capacitance transducers, the value of the capacitance changes due to change in the value of the input quantity that is to be measured. This change in capacitance can be measured easily and it is calibrated against the input quantity, thus the value if the input quantity can be measured directly.

The capacitance C between the two plates of capacitive transducers is given by:

$$C = \epsilon_0 \times \epsilon_r \times A / d$$

Where C is the capacitance of the capacitor or the variable capacitance transducer

ϵ_0 is the absolute permittivity

ϵ_r is the relative permittivity

The product of ϵ_0 and ϵ_r is also called as the dielectric constant of the capacitive transducer.

A is the area of the plates

d is the distance between the plates

It is clear from the above formula that capacitance of the capacitive transducer depends on the area of the plates and the distance between the plates. The capacitance of the capacitive transducer also changes with the dielectric constant of the dielectric material used in it.

Thus, the capacitance of the variable capacitance transducer can change with the change of the dielectric material, change in the area of the plates and the distance between the plates.

iii) Strain gauges: Strain gauges are devices whose resistance changes under the application of force or strain. They can be used for measurement of force, strain, stress, pressure, displacement, acceleration etc. It is often easy to measure the parameters like length, displacement, weight etc that can be felt easily by some senses. However, it is very difficult to measure the dimensions like force, stress and strain that cannot be really sensed directly by any instrument. For such cases, special devices called strain gauges are very useful.

There are some materials whose resistance changes when strain is applied to them or when they are stretched and this change in resistance can be measured easily. For applying the strain you need force, thus the change in resistance of the material can be calibrated to measure the applied force. Thus the devices whose resistance changes due to applied strain or applied force are called as the strain gauges.

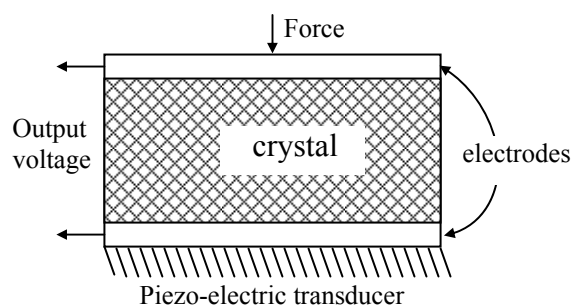
When force is applied to any metallic wire its length increases due to the strain. The more is the applied force, more is the strain and more is the increase in length of the wire. If L_1 is the initial length of the wire and L_2 is the final

length after application of the force, the strain is given as:

$$\varepsilon = (L_2 - L_1)/L_1$$

Further, as the length of the stretched wire increases, its diameter decreases. Now, we know that resistance of the conductor is the inverse function of the length. As the length of the conductor increases, its resistance decreases. This change in resistance of the conductor can be measured easily and calibrated against the applied force. Thus, strain gauges can be used to measure force and related parameters like displacement and stress. The input and output relationship of the strain gauges can be expressed by the term gauge factor or gauge gradient, which is defined as the change in resistance R for the given value of applied strain ε .

iv) Piezoelectric transducers



Piezo-electricity represents the property of a number of crystalline materials that cause the crystal to develop an electric charge or potential difference when subjected to mechanical forces or stresses along specific planes. Conversely, the crystal would undergo change in thickness (and thus produce mechanical forces) when charged electrically by a potential difference applied to its proper axis. Elements exhibiting piezo-electric qualities are sometimes known as electro restrictive elements.

A typical mode of operation of a piezo electric device for measuring varying force applied to a simple plate is shown in the fig. Metal electrodes are attached to the selected faces of a crystal in order to detect the electrical charge developed. The magnitude and polarity of the induced charge on the crystal surface is proportional to the magnitude and direction of the applied force and is given by

$$Q = KF$$

Where Q is the charge in coulomb, F is the impressed force in Newton's and K is the crystal sensitivity in C/N;

13. Resistive, Capacitive, Inductive Transducers

Solutions for Objective Practice Questions

01. Ans: (b)

Sol: For resistive potentiometer

$$\text{output } E_0 = K \times E_i$$

Where E_0 = output of the potentiometer

E_i = input of the potentiometer

02. Ans: (b)

Sol: In a resistance potentiometer, non linearity decreases with increase of load to potentiometer resistance because the output equation for potentiometer under loading condition is

$$E_0 = \frac{K}{1 + K(1 - K) \times \left(\frac{R_p}{R_m} \right)}$$

R_p = resistance of the potentiometer

R_m = resistance of the meter

03. Ans: (a)

Sol: In a resistance potentiometer high value of resistance lease to high value of sensitivity

04. Ans: (c)

Sol: Total temperature of POT = $T_{\text{ambient}} + T_{\text{pot}}$

$$T_{\text{pot}} = 30 \left(\frac{^\circ\text{C}}{\text{W}} \right) \times P$$

$$P = \frac{V^2}{R} = \frac{(10)^2}{100} = 1\text{W}$$

$$T_{\text{pot}} = 30 \left(\frac{^\circ\text{C}}{\text{W}} \right) \times 1\text{W}$$

$$= 30^\circ\text{C}$$

$$\text{Total temperature of POT} = 40 + 30 = 70^\circ\text{C}$$

05. Ans: (a)

Sol: Semiconductor strain gauge has a much higher gauge factor then that of a metal wire strain gauge because of piezo resistive effect.

06. Ans: (b)

Sol: We for quarter bridge strain measuring circuit

$$\text{the output } V_0 = \frac{V_i}{4} \times G_F \times \epsilon$$

$$\text{Here, } V_0 = 1 \text{ mV}$$

$$\text{Strain } (\epsilon) = 500 \times 10^{-6}$$

$$V_i = 4 \text{ V}$$

$$\text{Now } G_F = 2$$

07. Ans: (a)

Sol: For the given bending force we can say that configuration P is subjected to more tension compare to other two configurations.

08. Ans: (d)

$$\text{Sol: } G_f = 1 + 2 \times 0.35 = 1.70$$

09. Ans: (c)

Sol: For sinusoidal input output should have to be sinusoidal

10. Ans: (c)

Sol: Gauge factor $\frac{0.150/250}{1.5 \times 10^{-4}} = 4$

11. Ans: (b)

Sol: A gauge factor is a ratio of per unit change in resistance to per unit change in length

$$G.F = \frac{\Delta R / R}{\Delta L / L}$$

12. Ans: (b)

Sol: To receive the optimum output signal for shear strain, all the gauges should be placed at a position that is 45° in with respect to the longitudinal axis.

13. Ans: (c)

Sol: A strain gauge bridge sometimes excited with ac to avoid the power frequency pick-up.

14. Ans: (b)

Sol: $GF = 2$

$$\epsilon = 1 \times 10^{-6}$$

$$R = 120\Omega$$

$$\text{We know } = \frac{\Delta R}{R} = GF \epsilon$$

$$\Delta R = GF \epsilon R$$

$$= 2 \times 1 \times 10^{-6} \times 120$$

$$\Delta R = 240 \times 10^{-6} \Omega$$

15. Ans: (c)

Sol: The piezoresistive effect is a change in the electrical resistivity of a semi conductor or metal when mechanical strain is applied. Semiconductor strain gauges have higher piezoresistive coefficient so higher gauge factor.

16. Ans: (a)

Sol: In given diagram of LVDT, two secondary coils are so connected that output will always be added. So output is constant voltage graph.

17. Ans: (d)

Sol: LVDT has one primary coil and two secondary coils are connected in opposition, so that output must difference between two secondary output voltage.

18. Ans: (a)

Sol: LVDT is an inductive transducer which translates the linear motion into electrical signals.

19. Ans: (b)

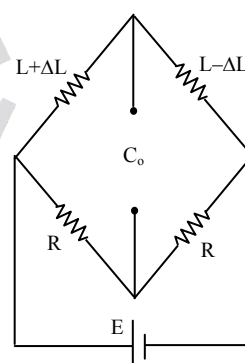
Sol: Air cored inductive transducers are suitable to use at higher frequencies

20. Ans: (d)

Sol: Inductive transducer in differential configuration of output is unaffected by External magnetic field temperature changes, variation of supply voltage & frequency.

21. Ans: (b)

Sol:



For push pull arrangement for L change change of inductance exhibited at output
 $= L + \Delta L - (L - \Delta L) = 2\Delta L$

22. Ans: (d)

Sol: An LVDT exhibits linear characteristics up to a displacement of ± 5 mm, linearly of 0.05 % has an infinite resolution and high sensitivity of the order of 40 V/mm.

23. Ans: (a)

Sol: To avoid the effect of fringing, the potential of the guard ring of a capacitance transducer hold at circuit potential. Ground is supposed to be a conduit to remove extraneous noise from the circuit.

24. Ans: (b)

Sol: The transfer function of capacitive transducer is given as

$$\frac{X_o(s)}{X_i(s)} = \frac{1}{\sqrt{1 + \left(\frac{1}{\tau\omega}\right)^2}}$$

So this resembles a high pass filter.

25. Ans: (a)

Sol: A strain gauge is an example of an electromechanical transducer in which displacement is used to vary the resistance. So we can say that both statement I & II are true as well as related.

26. Ans: (c)

Sol: Incase of strain gauge
 Statement –I is true but
 Statement –II is false.

Solutions for Conventional Practice Questions

01. Question not clear.

02.

Sol: Given data:

Gauge factor of given soft iron wire = 5.2

We know the relationship between gauge factor and Poisson's ratio

$$G_f = 1 + 2\nu$$

$$\nu = \frac{G_f - 1}{2} = \frac{5.2 - 1}{2} = \frac{4.2}{2} = 2.1$$

03.

Sol: Given data:

Conductor length $\ell = 24$ mm

Charge in length of conductor $\Delta \ell = 1$ mm

Diameter of the conductor $D = 1.5$ mm

Charge in diameter of conductor $\Delta D = 0.02$ mm

$$\text{Poisson's ratio } \nu = \frac{\text{lateral strain}}{\text{longitudinal strain}}$$

$$= \frac{\Delta D / D}{\Delta \ell / \ell}$$

$$= \frac{0.02 / 1.5}{1 / 24}$$

$$\nu = 0.32$$

$$\text{Gauge factor} = 1 + 2\nu$$

$$= 1 + (2 \times 0.32)$$

$$= 1.64$$

04.

Sol: Given data:

$$G_f = 2$$

$$\text{Stress} = 1000 \text{ (kg/cm}^2\text{)}$$

$$E = 2 \times 10^6 \text{ (kg/cm}^2\text{)}$$

Percentage change in Resistance of the strain gauge

$$\begin{aligned}
 &= \frac{\Delta R}{R} \times 100 \\
 &= \frac{G_f \times \text{stress}}{E} \times 100 \\
 &= \frac{2 \times 1000}{2 \times 10^6} \times 100 \\
 &= 0.1\%
 \end{aligned}$$

We know the relationship between gauge factor and Poisson's ratio

$$G_f = 1 + 2\nu$$

$$\nu = \frac{G_f - 1}{2} = \frac{2 - 1}{2} = 0.5$$

05.

Sol: Air gap after displacement of the armature

$$= 1.00 - 0.025 = 0.975 \text{ mm}$$

Since inductance is inversely proportional to the length of air gap, inductance with new gap

$$\text{would be} = \frac{1950}{0.975} = 2000 \mu\text{H}$$

$$\text{Change in inductance} = 2000 - 1950 = 50 \mu\text{H}$$

$$\text{Ratio} = \frac{\text{change in inductance}}{\text{original inductance}} = \frac{50}{1950} = 0.0256$$

$$\text{Ratio} = \frac{\text{displacement}}{\text{original gap}} = \frac{0.025}{1.0} = 0.025$$

Since the two ratios are equal, we can say that the change in inductance is linearly proportional to the displacements.

06.

Sol: Given data:

$$\text{LVDT rms output voltage} = 2.6 \text{ V}$$

$$\text{LVDT displacement} = 0.4 \mu\text{m}$$

Sensitivity of LVDT is

$$\begin{aligned}
 S &= \frac{\text{LVDT rms output voltage}}{\text{LVDT displacement}} \\
 &= \frac{2.6 \left(\frac{\text{V}}{\mu\text{m}} \right)}{0.4} = 6.5 \left(\frac{\text{V}}{\mu\text{m}} \right)
 \end{aligned}$$

07.

Sol: Given data:

$$\text{Sensitivity of given LVDT} = 60 \left(\frac{\text{V}}{\text{mm}} \right)$$

Bellow deflection = 0.15 mm for given pressure of $1.2 \times 10^6 \text{ (N/m}^2\text{)}$

$$\text{Given output voltage} = 4.5 \text{ V}$$

$$\text{Sensitivity of LVDT in } \left(\frac{\text{V}}{\text{N/m}^2} \right)$$

$$= 60 \left(\frac{\text{V}}{\text{mm}} \right) \times 0.15 (\text{mm}) \times \frac{1}{1.2 \times 10^6 \left(\frac{\text{N}}{\text{m}^2} \right)}$$

$$= 7.5 \left(\frac{\mu\text{V}}{\text{N/m}^2} \right)$$

Pressure when output voltage is 4.5 V is

$$= \frac{\text{output voltage}}{\text{sensitivity of LVDT}}$$

$$= \frac{4.5 (\text{V})}{7.5 \left(\frac{\mu\text{V}}{\text{N/m}^2} \right)}$$

$$= 6 \times 10^5 \text{ (N/m}^2\text{)}$$

08.

Sol: Given data:

LVDT output voltage in rms = 6(V) for displacement of $0.4 \times 10^{-3} \text{ (mm)}$

Voltmeter specification: 10 V voltmeter

Scale divisions = 100

$$\text{Division can be estimated} = \frac{2}{10} \text{ th division}$$

Sensitivity of the given LVDT

$$= \frac{\text{Voltage output}}{\text{input displacement}}$$

$$= \frac{6}{0.4 \times 10^{-3}} \left(\frac{\text{V}}{\text{mm}} \right)$$

$$S = 15000 \left(\frac{\text{V}}{\text{mm}} \right)$$

Resolution of voltmeter

$$= \frac{\text{voltmeter range}}{S \times \text{scaled division}} \times \frac{2}{10}$$

$$= \frac{10(V)}{15000 \left(\frac{V}{mm} \right) \times 100} \times \frac{2}{10}$$

$$R = 1.333 \times 10^{-6} (\text{mm})$$

09.

Sol: Given data:

Plate separation (x) under static condition = 0.05 mm

C_{static} capacitance under static condition
 $= 5 \times 10^{-12} (\text{F})$

Change in capacitance due to axial displacement
 $= 0.75 \times 10^{-12} (\text{F})$

We know the relationship between capacitance (C) and plate separation (x)

$$C \propto \frac{1}{x}$$

$$\frac{C_{\text{static}}}{C_{\text{static}} + \Delta C} = \frac{x_1}{x}$$

$$x_1 = x \times \frac{C_{\text{static}}}{C_{\text{static}} + \Delta C}$$

$$= 0.05 \times 10^{-3} \times \frac{5 \times 10^{-12}}{(5 \times 10^{-12}) + (0.75 \times 10^{-12})}$$

$$x_1 = 43.478 \mu\text{m}$$

$$\text{axial displacement} = x - x_1$$

$$= (0.05 \times 10^{-3}) - (43.478 \times 10^{-6})$$

$$= 0.006522 \text{ mm}$$

10.

Sol: Given data:

Area of quartz diaphragm = 750 mm^2

t_1 = separation distance between quartz diaphragm = 3.5 mm

$C = 370 \text{ pF}$ with no pressure with separation distance ' t_1 '

Δt_2 = deflection due to applied pressure

$\Delta t_2 = 0.6 \text{ mm}$ for the applied pressure of $900 \left(\frac{\text{km}}{\text{m}^2} \right)$

We know the relationship between

Capacitance (C) and separation distance (t) between the plates is

$$C \propto \frac{1}{t}$$

$$t_2 = t_1 - \Delta t_2$$

$$= 3.5 \text{ mm} - 0.6 \text{ mm}$$

$$t_2 = 2.9 (\text{mm})$$

$$\frac{C_1}{C_2} = \frac{t_2}{t_1}$$

$$C_2 = C_1 \frac{t_1}{t_2} = 370 \times 10^{-12} \times \frac{3.5 \times 10^{-3}}{2.9 \times 10^{-3}}$$

$$C_2 = 446.552 \text{ pF}$$

11.

Sol: Given data:

Capacitor overlapping area = $5 \times 10^{-4} (\text{m}^2)$

$C = 9.5 (\text{pF})$

$\epsilon_r = 81$

$\epsilon_0 = 8.854 \times 10^{-12} (\text{pF/m})$

We know that

$$C = \frac{\epsilon_0 \epsilon_r A}{d}$$

$$d = \frac{\epsilon_0 \epsilon_r A}{C}$$

$$= \frac{8.854 \times 10^{-12} \times 81 \times 5 \times 10^{-4}}{9.5 \times 10^{-12}} = 0.03775 (\text{m})$$

$$d = 37.75 (\text{mm})$$

$$\text{Sensitivity } S = \frac{\partial C}{\partial d} = - \frac{\epsilon_0 \epsilon_r A}{d^2}$$

$$= -\frac{8.854 \times 10^{-12} \times 81 \times 5 \times 10^{-4}}{(37.75 \times 10^{-3})^2}$$

$$S = -0.025 \times 10^{-8} \text{ (F/m)}$$

12.

Sol: Given data:

Separation distance (t_1) between diaphragm = 4 mm

For separation distance t_1 capacitance is 300 pF & oscillator frequency of 100 kHz.

P = applied pressure = 500 (kN/m²)

Δt_2 = average deflection for pressure

$P = 0.28$ mm

t_2 = separation distance after application of pressure P

$$\begin{aligned} t_2 &= t_1 - \Delta t_2 \\ &= 4 \text{ mm} - 0.28 \text{ mm} \\ &= 3.72 \text{ mm} \end{aligned}$$

Now we know the relationship between

C and t

$$C \propto \frac{1}{t}$$

$$\frac{C_1}{C_2} = \frac{t_2}{t_1}$$

$$C_2 = C_1 \frac{t_1}{t_2} = 300 \times 10^{-12} \times \frac{4 \times 10^{-3}}{3.72 \times 10^{-3}}$$

$$C_2 = 322.58 \text{ (pF)}$$

We know the relationship between frequency (f) & capacitance (C)

$$f \propto \frac{1}{C}$$

$$\frac{f_1}{f_2} = \frac{C_2}{C_1}$$

$$f_2 = \frac{f_1 C_1}{C_2} = 100 \times 10^3 \times \frac{300 \times 10^{-12}}{322.58 \times 10^{-12}}$$

$$f_2 = 93 \text{ kHz}$$

14. Piezo Electric Transducers

Solutions for Objective Practice Questions

01. **Ans: (a)**

Sol: For piezo electric transducer

$$\text{frequency} \propto \frac{1}{\text{cable length}}$$

$$f_{\text{new}} = \frac{f_{\text{old}}}{2} = \frac{1000}{2} = 500 \text{ Hz}$$

02. **Ans: (a)**

Sol: The output piezo electric transducer is a zero for static pressure.

03. **Ans: (a)**

Sol: For signal conditioning of piezo electric type transducer we require a charge amplifier

04. **Ans: (d)**

Sol: Piezoelectric transducers is used to measure dynamic pressure measurement while for static its output is zero millivolts.

05. **Ans: (a)**

Sol: $t = 2.5 \text{ mm}$

$$G = 0.05 \times \frac{V_m}{N}$$

$$P = 1.6 \times 10^5 \text{ N/m}^2$$

We know $\epsilon = gtp$

$$= 0.05 \times 2.5 \times 10^{-3} \times 1.6 \times 10^6$$

$$e_0 = 200 \text{ V}$$

06. **Ans: (c)**

Sol: The piezoelectric transducers vibrate at ultrasonic frequencies. Piezoelectric material is a type of electro acoustic transducer that converts electrical energy into mechanical and vice versa.

07. Ans: (a)

Sol: Piezoelectric crystal can be shown as electrical equivalent circuit in terms of L and C . Quartz, Rochelle salt, tourmaline are piezoelectric crystal. Also piezoelectric crystal exhibits the reverse effect of electrostriction.

08. Ans: (c)

Sol: Piezoelectric transducer used for dynamic displacement only and it is useless for static displacement. Piezoelectric materials have low dielectric constant.

Quartz dielectric constant is 4.2

09. Ans: (a)

Sol: Both Assertion and Reason are correct statements only But second is not related with first

Solutions for Objective Practice Questions

01.

Sol: Given $t = 2 \text{ mm}$

$$g = 0.05 \text{ Vm/N}$$

$$\frac{F}{A} = 15 \times 10^5 \text{ N/m}^2$$

We know

$$g = \frac{E_0 / t}{F / A}$$

$$\text{So } E_0 = g \times \frac{F}{A} \times t$$

$$= 0.05 \text{ Vm/N} \times 15 \times 10^5 \text{ N/m}^2 \times 2 \times 10^{-3}$$

$$= 150 \text{ V}$$

02.

Sol: Given data:

$$\text{Area of given crystal} = 36 \text{ mm}^2$$

$$\text{Thickness of given crystal} = 1.5 \text{ mm}$$

$$g = 0.012 \left(\frac{\text{Vm}}{\text{N}} \right)$$

$$\epsilon_r = 1400$$

$$E = 120 \times 10^{10} \text{ (N/m}^2\text{)}$$

$$F = 10 \text{ N}$$

(i) Output voltage $e_0 = g t$

$$= g t \frac{F}{A}$$

$$= 0.012 \times 1.5 \times 10^{-3} \times \frac{10}{36 \times 10^{-6}}$$

$$e_0 = 5 \text{ V}$$

(ii) Charge sensitivity $d = g \epsilon_0 \epsilon_r$

$$= 0.012 \times 8.854 \times 10^{-12} \times 1400$$

$$d = 148.75 \left(\frac{\text{pC}}{\text{N}} \right)$$

(iii) strain $\epsilon = \frac{\text{stress}}{E} = \frac{F}{AE}$

$$= 0.2315 \times 10^{-6}$$

$$= 0.2315 \text{ } \mu\text{strain}$$

(iv) charge generated $Q = dF$

$$= 148.75 \times 10^{-12} \times 10$$

$$Q = 1487.5 \text{ (pC)}$$

(v) Capacitance of pick up $C = \frac{Q}{V}$

$$= \frac{1487.5 \times 10^{-12}}{5}$$

$$= 297.5 \text{ (pF)}$$

03.

Sol: Charge sensitivity $d_{33} = d = 150 \times 10^{-12} \text{ C/N}$

$$C_{pz} = 25 \times 10^{-12} \text{ F}$$

$$R_{pz} = 10^{10} \Omega$$

Input force = $2 \text{ N } u(t)$ (step force)

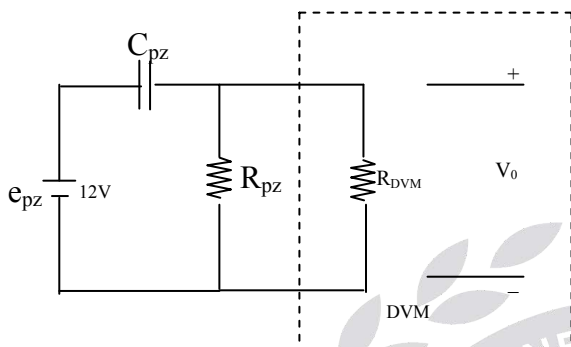
The Voltage generated

$$= \frac{\text{Charge Generated}}{C_{pz}}$$

$$e_{pz} = e_0 = \frac{d \times F}{C} = \frac{q}{c}$$

$$e_{pz} = \frac{150 \times 10^{-12} \text{ C/N} \times 2 \text{ N}}{25 \times 10^{-12}} = 12 \text{ V}$$

The equivalent circuit under the given condition is



$$\frac{V_0(S)}{e_{pz}(S)} = \frac{\tau s}{\tau s + 1}$$

$$\tau = C_{pz}(R_{pz} \parallel R_{DVM})$$

$$\tau = 20 \text{ PF } (10^{10} \Omega \parallel 10^{13} \Omega)$$

$$\tau = 25 \times 10^{-12} \times 999 \times 10^9 \Omega$$

$$\tau = 0.25 \text{ sec}$$

$$V_0(t) = e_{pz} \times e^{-t/\tau}$$

Where $V_0(t)$ is voltage across the Dvm .

Drop allowed from peak value i.e, 12 v is no more than 0.12v. Time at which V_0 falls to 11.88 V must be calculated.

Assigning $V_0(t) = 11.88 \text{ v}$

$$11.88 = 12 \times e^{-t/\tau}$$

$$\frac{11.8}{12} = e^{-t/\tau}$$

$$\Rightarrow \ln\left(\frac{11.88}{12}\right) = \frac{-t}{\tau}$$

$$\Rightarrow \frac{t}{\tau} = \ln\left(\frac{12}{11.88}\right)$$

$$\Rightarrow t = \tau \times \ln\left(\frac{12}{11.88}\right)$$

$$= 0.25 \ln\left(\frac{12}{11.88}\right) \text{ seconds}$$

$$\Rightarrow t = 2.512 \text{ m Seconds}$$

15. Measurement of Temperature

Solutions for Objective Practice Questions

01. Ans: (a)

Sol: Platinum resistance thermometer used to measure temperature in the range -200° C to 1000° C

Material	Minimum temperature	Maximum temperature
Platinum	-200° C	1000° C
Copper	-200° C	150° C
Nickel	-70° C	150° C
Tungsten	-200° C	850° C

02. Ans: (d)

Sol: RTD material must have

- (i) High temperature coefficient of resistance
- (ii) Higher resistivity
- (iii) Linear relationship between R and T
- (iv) Stability of the electrical characteristics of the material

03. Ans: (d)

Sol: Platinum has a constant volume of temperature coefficient in 0 to 100° C range.

Resistivity of platinum tends to increase less rapidly at higher temperatures.

Platinum has stability over higher range of temperature.

04. Ans: (b)

$$\text{Sol: } \alpha_{45^\circ\text{C}} = \left(\frac{R_2 - R_1}{T_2 - T_1} \right) \frac{1}{R_{45^\circ\text{C}}}$$

$$R_{45^\circ\text{C}} = \frac{R_1 + R_2}{2} = \frac{5 + 6.5}{2} = 5.75 \Omega$$

Here $R_1 = 5 \Omega$ at $T_1 = 30^\circ\text{C}$

$R_2 = 6.5 \Omega$ at $T_2 = 60^\circ\text{C}$

$$\alpha_{45^\circ\text{C}} = \left(\frac{6.5 - 5}{60 - 30} \right) \times \frac{1}{5.75} = 0.0087 (1/^\circ\text{C})$$

05. Ans: (d)

Sol: The resistance temperature characteristics of a temperature transducer is related to positive temperature coefficient thermistor.

06. Ans: (d)

Sol: Thermistors are well suited to precision temperature measurement. It is used in range of -100°C to 300°C . It has higher negative temperature coefficient of resistance.

07. Ans: (c)

Sol: A thermistor can exhibit either a negative change of resistance (NTC) or positive change of resistance (PTC) with increase of temperature depending upon the type of material used.

08. Ans: (b)

Sol: $R = 5000 \Omega$ at $T = 25^\circ\text{C}$, $\alpha = 0.04 (1/^\circ\text{C})$

$$R_{\text{lead}} = R [1 + \alpha (T_{\text{lead}} - T)]$$

$$10 = 5000 [1 + 0.04 (T - 25)]$$

$$T = 0.05^\circ\text{C}$$

09. Ans: (b)

Sol: Thermistors are essentially semiconductor devices that behaves as resistors with high negative temperature coefficient and are atleast 10 times as sensitive as the platinum resistance thermometer.

10. Ans: (b)

Sol: $\beta = 3000 \text{ K}$

$R = 1050 \Omega$ at $T = 27^\circ\text{C}$

$$= 300 \text{ K}$$

So temperature coefficient of resistances for the

$$\text{thermistor } \alpha = \frac{-\beta}{T^2} = \frac{-3000}{(300)^2} = -0.033 (\Omega/\Omega/^\circ\text{C})$$

11. Ans: (d)

Sol: In case of thermocouple we required a reference junction compensation to get stable and reliable output. Also thermocouple output is very small.

12. Ans: (a)

Sol: V_0 = output of thermocouple = 50 mV

R_t = thermocouple internal resistance = 50Ω

$R_{\text{lead}} = 10 \Omega$

r = PMMC internal resistance = 120Ω

So output voltage indicated by PMMC V_{PMMC} is

$$V_{\text{pmmc}} = \frac{r}{r + R_t + R_{\text{lead}}} \times V_0$$

$$= \frac{120}{120 + 50 + 10} \times 50 \times 10^{-3}$$

$$= \frac{120 \times 50 \times 10^{-3}}{180}$$

$$= 33.33 \text{ mV}$$

13. Ans: (d)

Sol:

Thermocouple	Temperature range(in $^\circ\text{C}$)
Copper-constantan	-200 to 350
Iron – constantan	-200 to 850
Alumel-Chromel	-200 to 1100
Platinum Rhodium	450 to 1500

14. Ans: (b)

Sol: Iron-constantan thermocouple is most suitable for temperature measurement in the range of 700 °C to 800° C.

15. Ans: (a)

Sol: Time to reach equilibrium

$$\text{Conditions } 5T = 10 \Rightarrow T = 2 \text{ sec}$$

$$\theta = \theta_0 [1 - e^{-t/T}]$$

$$0.5 = [1 - e^{-t/T}]$$

$$T = 1.39 \text{ sec}$$

Solutions for Conventional Practice Questions
01.

Sol: Temperature of thermistor at 2330 Ω is

$$\text{Here } R_T = 2330 \Omega$$

$$R_0 = 1050 \Omega$$

$$T = \text{unknown temperature at } 2330 \Omega$$

$$T_0 = 27^\circ\text{C} = 300^\circ\text{K}$$

$$R_T = R_0 e^{\beta \left(\frac{1}{T} - \frac{1}{T_0} \right)}$$

$$\ell_n \left(\frac{2330}{1050} \right) = 3140 \left(\frac{1}{T} - \frac{1}{300} \right)$$

$$0.7971 = 3140 \left(\frac{1}{T} - \frac{1}{300} \right)$$

$$T = 278.77^\circ\text{K}$$

$$T = 5.77^\circ\text{C}$$

This temperature corresponds to the resistance of 2330 Ω.

$$\text{Sensitivity } S = \frac{dR}{dT} = R_0 e^{\beta \left(\frac{1}{T} - \frac{1}{T_0} \right)} \times \left(\frac{-\beta}{T^2} \right)$$

$$= \frac{-R_T \beta}{T^2}$$

$$= \frac{-2330 \times 3140}{278.77^2}$$

$$S = -94.144 (\Omega/\text{K})$$

This is the required sensitivity of the given thermistor at a given operating point (2330 Ω and 278.77°C).

02.

Sol: Given data:

Sensitivity of copper with respect to platinum

$$S_{\text{CuPt}} = 7.4 \left(\frac{\mu\text{V}}{^\circ\text{C}} \right)$$

Sensitivity of constantan with respect to platinum

$$S_{\text{CnPt}} = -34.4 \left(\frac{\mu\text{V}}{^\circ\text{C}} \right)$$

Sensitivity of copper with respect to constantan

$$\begin{aligned} S_{\text{CuCn}} &= S_{\text{CuPt}} - S_{\text{CnPt}} \\ &= 7.4 \left(\frac{\mu\text{V}}{^\circ\text{C}} \right) - \left(-34.4 \left(\frac{\mu\text{V}}{^\circ\text{C}} \right) \right) \end{aligned}$$

$$S_{\text{CuCn}} = 41.8 \left(\frac{\mu\text{V}}{^\circ\text{C}} \right)$$

Now corresponding temperature difference in a thermocouple made up of copper and constantan junction for temperature difference of 250°C is

$$= S_{\text{CuCn}} \times 250^\circ\text{C}$$

$$= 41.8 \left(\frac{\mu\text{V}}{^\circ\text{C}} \right) \times 250^\circ\text{C} = 10.45 (\text{mV})$$

03.

Sol: Given data:

$$\alpha = 37.5 \left(\frac{\mu\text{V}}{^\circ\text{C}} \right)$$

$$\beta = 0.0045 \left(\frac{\mu\text{V}}{^\circ\text{C}} \right)$$

$$\theta_{\text{hot}} = 200^\circ\text{C}$$

$$\theta_{\text{cold}} = 0^\circ\text{C}$$

Now we know the thermocouple relationship between thermo-emf set up and temperature

difference between hot and cold junction is given by

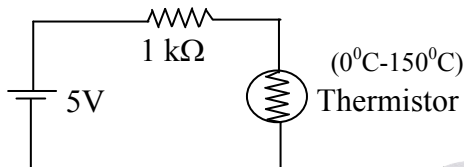
$$E = \alpha (Q_h - \theta_c) + \beta (\theta_h^2 - \theta_c^2)$$

$$= 37.5 \times 10^{-6} (200 - 0) + 0.0045 \times 10^{-6} (200^2 - 0^2)$$

$$= 7.68 \text{ mV}$$

04.

Sol:

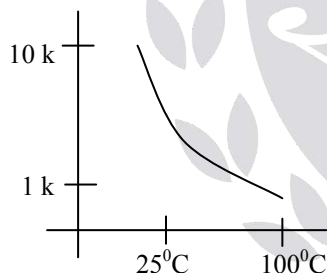


At 25°C the resistance of thermistor is 10kΩ

At 100°C the resistance of thermistor is 1kΩ

This thermistor is used in a temperature range of 0-150°C.

$$P = I^2 R = \frac{V^2}{R}$$



$$R_T = R_0$$

$$\ln \left[\frac{R_T}{R_0} \right] = \beta \left[\frac{1}{T} - \frac{1}{T_0} \right]$$

$$T_0 = 25^\circ\text{C} + 273 = 293\text{K and } R_0 = 10\text{k}\Omega$$

$$T = 100 + 273 = 373\text{K and } R_T = 1\text{k}\Omega$$

$$\ln \left[\frac{1}{10} \right] = \beta \left[\frac{1}{373} - \frac{1}{298} \right]$$

$$\beta = 3412.55 \text{ K}$$

Now

$$T_0 = 100^\circ\text{C} + 273 = 373 \text{ K and } R_0 = 1\text{K}\Omega$$

$$T = 150^\circ\text{C} + 273 = 473\text{K}$$

$$\ln \left[\frac{R_T}{1\text{k}\Omega} \right] = 3412.55 \left[\frac{1}{423} - \frac{1}{373} \right]$$

$$R_T = 339.12 \Omega$$

Thermistor resistor at 150°C

$$I = \frac{5\text{V}}{1\text{k} + R_T}$$

$$= \frac{5}{1339.12} = 3.733 \times 10^{-3}$$

$$P = I^2 \times R$$

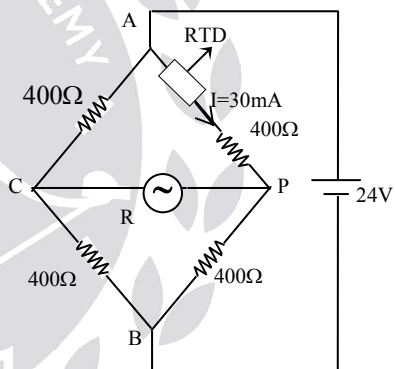
$$P = 4.72 \text{ mW}$$

05.

Sol: Given data:

$$R_1 = R_2 = R_3 = R_4 = 400\Omega; \quad \alpha = 0.042\Omega/^\circ\text{C}$$

$$T = 30^\circ\text{C}; \quad I = 30\text{mA}$$



Due to temperature rise of 30°C, increase in the resistance of sensor by = 0.042×30

$$= 1.26\Omega$$

So resistance of sensor branch become

$$= 400 + 1.26 = 401.26\Omega$$

Current through sensor is restricted is 30mA

Voltage across AB terminals

$$= 30[400 + 401.26] \times 10^{-3}$$

$$= 24.038 \approx 24\text{V (DC supply)}$$

Thevinins equivalent resistance across AB

$$\text{terminals} = (400 + 401.26) \parallel (400 + 400)$$

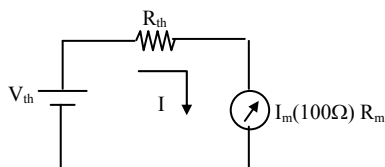
$$= (801.26) \parallel (800)$$

$$= \frac{801.26 \times 800}{801.26 + 800} = 400.3147 \Omega$$

$$V_{th} = 24 \times \left[\frac{400}{800} - \frac{400}{801.26} \right]$$

$$= 24[0.5 - 0.499] = 0.0188V$$

∴ I through the meter



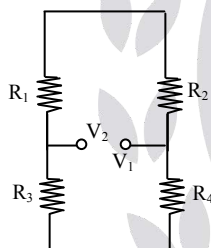
$$I = \frac{V_{th}}{R_{th} + R_m}$$

$$= \frac{0.0188}{400.3147 + 100} = 37.58 \mu A$$

$$\text{Deflection of the meter} = 37.58 \times 2^\circ = 75.16^\circ$$

06.

Sol:



Sensitivity 10 mV/ °C means change in 1°C in RTD corresponding to 10 mV change in Bridge output.

$$R_T = R_0 [1 + \alpha T]$$

$$= 100[1 + 0.00392(1-0)]$$

$$R_T = 100.392 \Omega$$

$$10 \text{ mV} = A_d [V_1 - V_2]$$

$$V_1 - V_2 = \left(\frac{R_4}{R_2 + R_4} \right) V - \left(\frac{R_3}{R_1 + R_3} \right) V$$

$$= 10 \left[\frac{150.392}{100.392 + 10k} - \frac{100}{100 + 10k} \right] = 0.3842 \text{ mV}$$

$$A_d = \frac{10}{0.3842} = 26.02$$

16. Measurement of Flow, Viscosity, Humidity

Solutions for Objective Practice Questions

01. Ans: (d)

Sol: In case of rotameter with increase in the flow rate, the float rises in the tube and there occurs an increase in the annular area between the float and the tube. So we can say that rotameter is a variable area device.

02. Ans: (a)

Sol: Flow rate in pitot tube is

$$Q = AV$$

$$= A \sqrt{\frac{2P_d}{\rho}}$$

$$\theta \propto \sqrt{P_d}$$

03. Ans: (c)

Sol:

Restrictors	Discharge coefficient
Orifice tube	0.60
Venturi tube	0.98
Flow nozzle	0.80

04. Ans: (b)

Sol: Rotary vane type transducer is an example of positive displacement flow meter.

05. Ans: (b)

Sol: Venturimeter has the lowest pressure drop for a given range of flow because venturimeter has highest coefficient of discharge about 0.98 .

06. Ans: (a)

Sol: In Rota meter, flow rate is directly proportional to height

$$Q \propto h$$

$$\therefore \frac{Q_1}{Q_2} = \frac{h_1}{h_2} = \frac{70 \text{ mm}}{20 \text{ mm}} = \frac{7}{2} = 3.5$$

07. Ans: (d)

Sol: During the flow through an orifice meter, the fluid jet on leaving the orifice contracts to minimum area at a section called vena-contracta, area of fluid jet at vena contracta is less than areas of the orifice & the two are related as area at vena contracta = $C_d \times$ orifice area.

$$= 0.6 \left(\frac{\pi d^2}{4} \right)$$

$$C_d \text{ of orifice} = 0.6$$

$$\text{Area of orifice} = \frac{\pi d^2}{4}$$

08. Ans: (a)

Sol: Pressure at throat of a venturi tube is lower compare to upstream pressure. While velocity at throat of a venturi tube is higher compare to velocity of flow at up stream.

09. Ans: (a)

Sol: In case of rotameter the weight of the float is balanced by the buoyancy and the drag force acting on the float. Volume flow rate sensitive to density changes of the fluid. By using rotameter volume flow rate of gas can be measured.

10. Ans: (c)

Sol: Flowing fluid density affected in orifice plate, rotameter, pitot static tube meter while flowing fluid density is not matter for measurement of flow in non obstruction type meter like electromagnetic flow meter.

11. Ans: (a)

Sol: When an electrically heated wire is placed in a flowing gas stream, heat is transferred from wire to the gas and hence the temperature of the wire reduces and due to this the resistance of the wire also changes. This change in resistance of the wire becomes a measure of flow rate.

12. Ans: (a)

Sol: Hot wire anemometer gives good result when the flowing fluid is exceptionally clean.

13. Ans: (c)

Sol: The turbine type flow meter used to measure totalisation of flow.

Solutions for Conventional Practice Questions

01.

Sol: For ultrasonic flow meter, the guiding equation is

$$\Delta t = \frac{2d V \cos \theta}{C^2}$$

$$10 \text{ n sec} = \frac{2 \times 25 \times 10^{-3} \times V \times \cos 60^\circ}{1000000}$$

$$\text{Velocity} = 0.4 \text{ m/sec}$$

02. Ans: 6.0 mV

$$\text{Sol: Given, } Q_v = \frac{400}{60} = 6.667 \text{ litre/sec}$$

$$l = 8 \text{ cm} = 0.08 \text{ m,}$$

$$B = 400 \text{ gauss} = 400 \times 10^{-4} \text{ tesla}$$

We know,

$$E = \frac{4B}{\pi l} Q_v \times 10^{-3} \text{ V} \approx 4.24 \text{ mV}$$

$$E_{\text{rms}} = \frac{2 \times 4.24}{\sqrt{2}} \text{ mv} = 6.0 \text{ mV}$$

17. Intermediate Quantity Measurements

Solutions for Objective Practice Questions

01. Ans: (d)

Sol: In seismic vibration sensor for measuring amplitude of vibration $\omega_n \ll \omega$ & slightly less than 1.

02. Ans: (d)

$$\text{Sol: } \omega_n = \sqrt{\frac{K}{M}}$$

Decreasing the mass in case of a seismic acceleration sensor while keeping all other parameters constant will increase the natural frequency, without affecting steady state sensitivity.

03. Ans: (a)

Sol: $M = 100 \mu\text{g}$

$F_n = 1\text{kHz}$

04. Ans: (a)

Sol: $f = 100 \text{ Hz}$; $X = 10 \text{ mm}$

$$\begin{aligned} \text{Peak acceleration of the seismic mass} &= \omega^2 x \\ &= (2\pi f)^2 x \\ &= (2\pi \times 100)^2 \times 10 \times 10^{-3} \\ &= 3947.84 \text{ (m/sec}^2\text{)} \end{aligned}$$

05. Ans: (a)

Sol: accelerometer input range

$$= 0 \text{ m/sec}^2 \text{ to } 98.1 \text{ (m/sec}^2\text{)}$$

$F = 30 \text{ Hz}$

$M = 0.01 \text{ kg}$

We know acceleration $= \omega^2 x$

$$x = \frac{\text{acceleration}}{\omega^2}$$

$$x_1 = 0\text{mm} \quad \text{to} \quad x_2 = \frac{98.1}{(2\pi \times 30)^2} = 2.76 \text{ mm}$$

06. Ans: (b)

Sol: In dc tachogenerators used for measurement of speed of a shaft, frequent calibration has to be done because the strength of permanent magnet decreases with age.

07. Ans: (c)

Sol: In a drag up type ac tachogenerator, the output voltage is modulated waveform.

08. Ans: (b)

Sol: $n_{\text{teeth}} = 60$; $N = \text{speed of shaft}$; $N = 25 \text{ rps}$;

We know

$$\text{Speed of shaft in rps} = \frac{\text{pulse rate}}{n_{\text{teeth}}}$$

$$25 = \frac{\text{pulses per second}}{60}$$

$$\text{Pulses per second} = 25 \times 60 = 1500$$

09. Ans: (b)

Sol: $f_r = \text{rotating frequency of motor}$

$$= \frac{1470}{60} = 24.5(\text{rps})$$

$F_f = \text{stroboscope flashing frequency}$

$$= 12.5 \text{ (fps)}$$

$$F_r - nf_f = 24.5 - nf_f$$

$$n = 2 f_r - nf_f = -30 \text{ rpm}$$

So star mark moves at a speed of 30 rpm against the direction of rotation.

10. Ans: (c)

$$\text{Sol: rpm} = \frac{\text{pulses per second}}{\text{number of teeth}} \times 60$$

$$\text{rpm} = \frac{\text{flash per minute}}{\text{number of teeth}}$$

$$N = \frac{F}{n}$$