

# GATE | PSUs

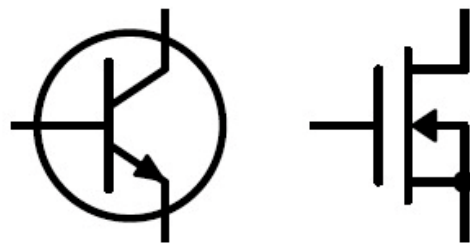


## ELECTRONICS & COMMUNICATION ENGINEERING

---

### Analog Circuits

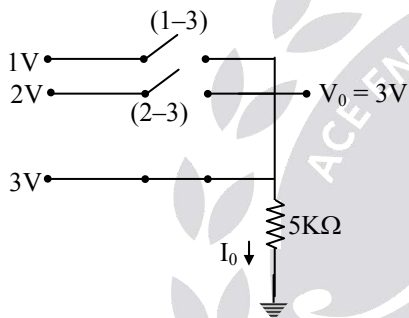
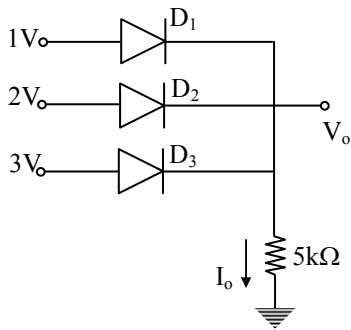
**Text Book :** Theory with worked out Examples  
and Practice Questions



# Analog Circuits

*(Solutions for Text Book Practice Questions)*

**01.**  
**Sol:**

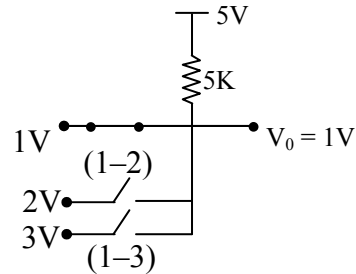
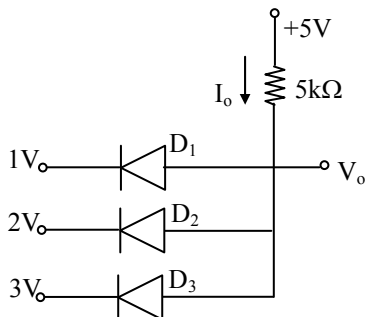


⇒ D<sub>1</sub>, D<sub>2</sub> are reverse biased and D<sub>3</sub> is forward biased.

i.e., D<sub>3</sub> only conducts.

$$\therefore I_o = 3/5K = 0.6mA$$

**02.**  
**Sol:**



⇒ D<sub>2</sub> & D<sub>3</sub> are reverse biased and 'D<sub>1</sub>' is forward biased.

i.e., D<sub>1</sub> only conduct

$$\therefore I_o = \frac{5-1}{5K} = 0.8mA$$

**03.**

**Sol:** Let diodes D<sub>1</sub> & D<sub>2</sub> are forward biased.

⇒ V<sub>o</sub> = 0 volt

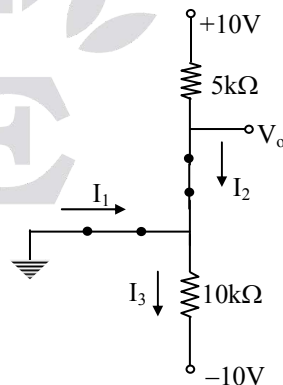
$$I_2 = \frac{10-0}{5K} = 2mA$$

$$I_3 = \frac{0-(-10)}{10K} = 1mA$$

Apply KVL at nodes 'V<sub>o</sub>':

$$-I_1 + I_3 - I_2 = 0$$

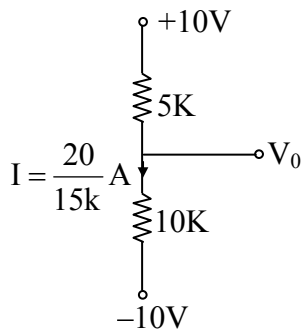
$$\Rightarrow I_1 = -(I_2 - I_3) = -1mA$$



So, D<sub>1</sub> is reverse biased & D<sub>2</sub> is forward biased

⇒ 'D<sub>1</sub>' act as an open circuit & D<sub>2</sub> is act as short circuit.

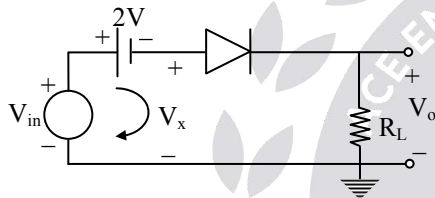
Then circuit becomes



$$\Rightarrow V_0 = 10k \times \left(\frac{20}{15k}\right) - 10$$

$$\therefore V_0 = 3.33V$$

**04.**  
**Sol:**



Apply KVL to the loop:

$$V_{in} - 2 - V_x = 0$$

$$\Rightarrow V_x = V_{in} - 2 \text{ ---- (1)}$$

Given,  $V_{in}$  range =  $-5V$  to  $5V$

$$\Rightarrow V_x \text{ range} = -7V \text{ to } 3V \text{ [}\because \text{ from eq (1)]}$$

Diode ON for  $V_x > 0V$

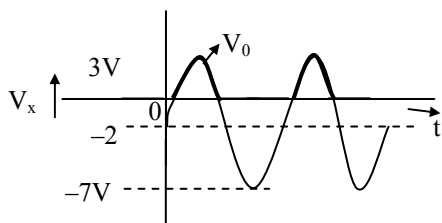
$$\Rightarrow V_0 = V_x$$

Diode OFF for  $V_x < 0V$

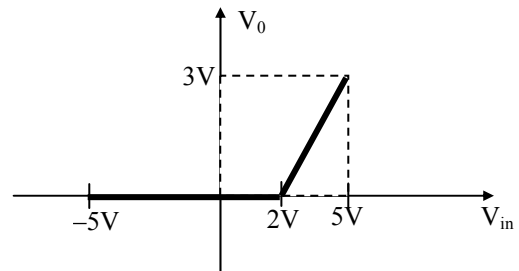
$$\Rightarrow V_0 = 0V$$

$$\therefore V_0 \text{ range} = 0 \text{ to } 3V$$

**Output wave form:**

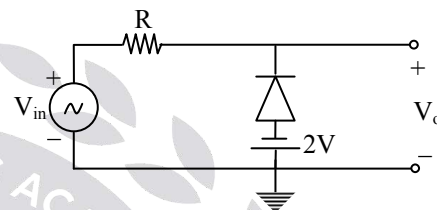


**Transfer characteristics:**



**05.**

**Sol:**

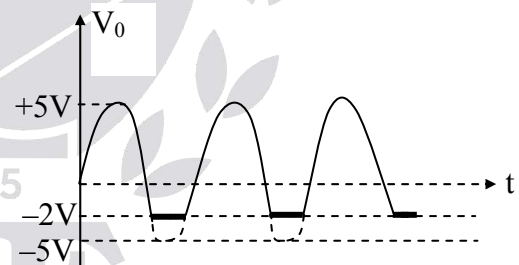


For  $V_i < -2V$ olt, Diode ON

$$\Rightarrow V_0 = -2V$$

For  $V_i > -2V$ olt, Diode OFF

$$\Rightarrow V_0 = V_i$$



**06.**

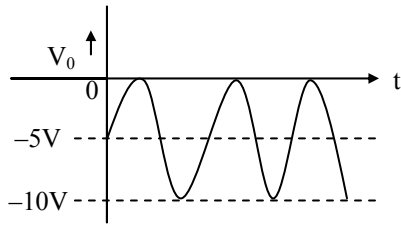
**Sol:** For positive half cycle diode Forward biased and Capacitor start charging towards peak value.

$$\Rightarrow V_C = V_m = 5V$$

$$\Rightarrow V_0 = V_{in} - V_C = V_{in} - 5$$

$$V_{in} \text{ range} = -5V \text{ to } +5V$$

$\therefore V_0 \text{ range} = -10\text{V to } 0\text{V}$



**07.**

**Sol:** For +ve cycle, diode 'ON', then capacitor starts charging

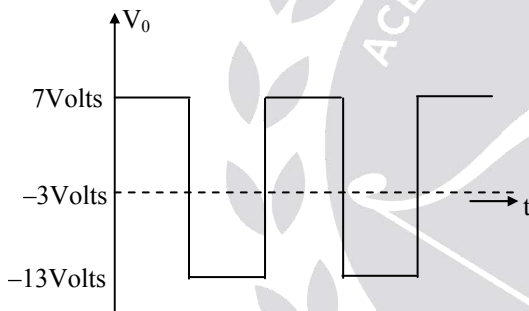
$$\Rightarrow V_C = V_m - 7 = 10 - 7 = 3\text{V}$$

Now diode OFF for rest of cycle

$$\begin{aligned} \Rightarrow V_0 &= -V_C + V_{in} \\ &= V_{in} - 3 \end{aligned}$$

$V_{in} \text{ range} : -10\text{V to } +10\text{V}$

$\therefore V_0 \text{ range} : -13\text{V to } 7\text{V}$



**08.**

**Sol:** Always start the analysis of clamping circuit with that part of the cycle that will forward bias the diodes this diode is forward bias during negative cycle.

For negative cycle diode ON, then capacitor starts charging

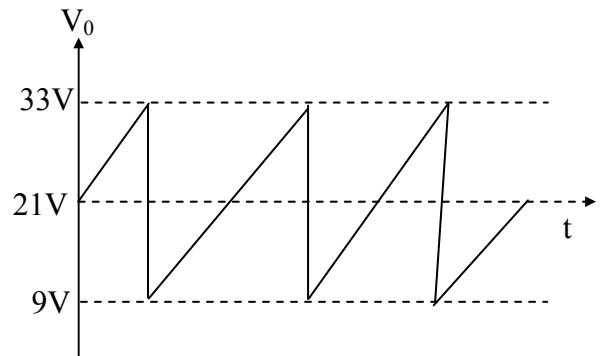
$$\begin{aligned} \Rightarrow V_C &= V_P + 9 \\ &= 12 + 9 = 21\text{V} \end{aligned}$$

Now diode OFF for rest of cycle.

$$\begin{aligned} \Rightarrow V_0 &= V_C + V_{in} \\ &= 21 + V_{in} \end{aligned}$$

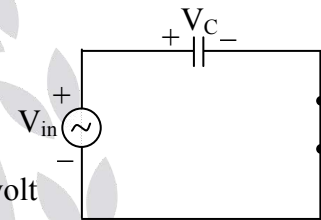
$V_{in} \text{ range} : -12 \text{ to } +12\text{V}$

$V_0 \text{ range} : 9\text{V to } 33\text{V}$



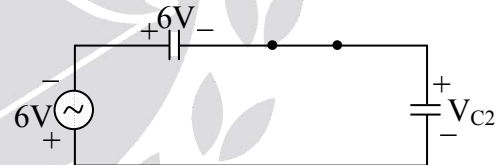
**09.**

**Sol:** During positive cycle,  $D_1$  forward biased &  $D_2$  Reverse biased.



$$V_{C1} = V_{in} = 6\text{volt}$$

During negative cycle,  $D_1$  reverse biased &  $D_2$  forward biased.

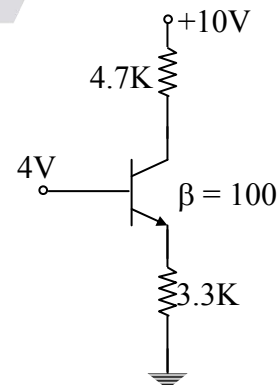


$$V_{C2} = -6 - 6 = -12\text{V}$$

Capacitor  $C_2$  will charge to negative voltage of magnitude 12V

**10.**

**Sol:**



Given,

$$V_B = 4V$$

$$V_{BE} = 0.7$$

$$V_B - V_E = 0.7$$

$$V_E = V_B - 0.7 = 3.3V$$

$$\Rightarrow I_E = \frac{3.3}{3.3K\Omega} = 1mA$$

Let transistor in active region

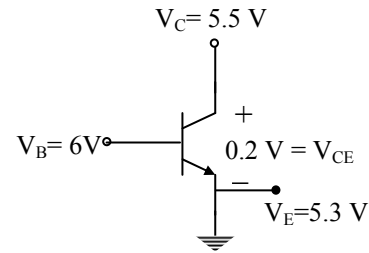
$$\Rightarrow I_C = \beta / (\beta + 1) \cdot I_E = 0.99mA$$

$$I_B = I_C / \beta = 9.9\mu A$$

$$V_C = 10 - 4.7 \times 10^3 \times 0.99 \times 10^{-3} = 5.347V$$

$$\Rightarrow V_C > V_B$$

$\therefore$  Transistor in the active region.



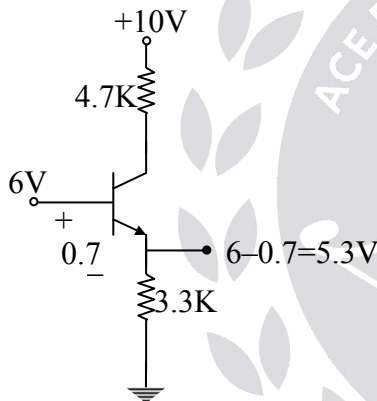
$$\Rightarrow I_C = \frac{10 - 5.5}{4.7K} = 0.957mA$$

$$I_B = 1.6 - 0.957 = 0.643mA$$

$$\beta = \frac{I_C}{I_B} = \frac{0.957mA}{0.643mA} = 1.483$$

$$\beta_{forced} < \beta_{active}$$

11.  
Sol:



$$V_E = V_B - V_{BE} = 6 - 0.7 = 5.3V$$

$$I_E = \frac{5.3}{3.3K} = 1.6mA$$

Let transistor is active region

$$\Rightarrow I_C = \frac{\beta}{(1 + \beta)} I_E$$

$$I_C = 1.59mA$$

$$V_C = 2.55V$$

$$\Rightarrow V_C < V_B$$

$\therefore$  Transistor in saturation region

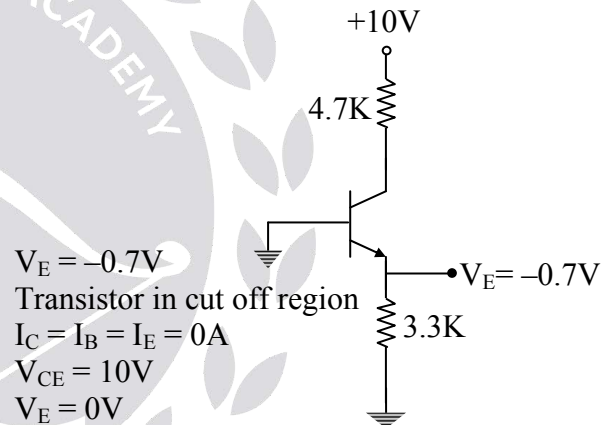
$$\Rightarrow V_{CE(sat)} = 0.2V$$

$$V_C - V_E = 0.2$$

$$V_C = 5.3 + 0.2$$

$$\Rightarrow V_C = 5.5V$$

12.  
Sol:



$$V_E = -0.7V$$

Transistor in cut off region

$$I_C = I_B = I_E = 0A$$

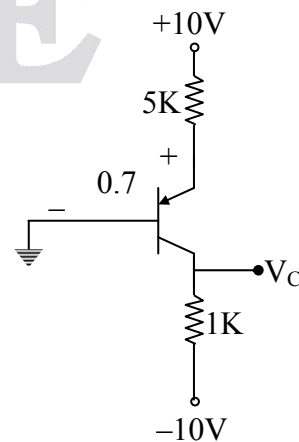
$$V_{CE} = 10V$$

$$V_E = 0V$$

$$V_C = 10V$$

$$V_B = 0V$$

13.  
Sol:



$$V_E = 0.7V \quad [\because V_B = 0V]$$

$$\Rightarrow I_E = \frac{10 - 0.7}{5K} = 1.86mA$$

Let transistor in active region.

$$\Rightarrow I_C = \frac{\beta}{(\beta + 1)} I_E = 1.84mA$$

$$\Rightarrow V_C = -10 + 1K \times 1.84m$$

$$V_C = -8.16V$$

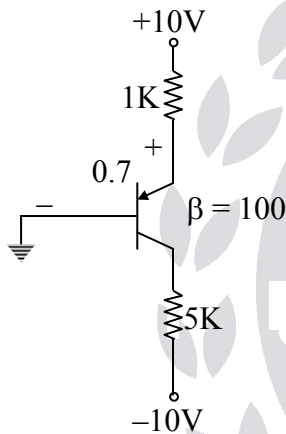
$$V_{EC} = V_E - V_C = 8.86V$$

$$V_{EC} > V_{EB}$$

$\therefore$  Transistor in active region

14.

Sol:



Let transistor in active region

$$V_E = 0.7V \quad [\because V_B = 0V]$$

$$I_E = \frac{10 - 0.7}{1k} = 9.3mA$$

$$I_C = \frac{\beta}{\beta + 1} I_E = 9.2mA$$

$$\Rightarrow V_C = -10 + 5K \times 9.2m$$

$$V_C = 36V$$

$$V_{EC} < V_{EB}$$

Transistor in saturation region

$$\Rightarrow V_{EC} = 0.2$$

$$V_E - V_C = 0.2 \Rightarrow V_C = 0.5V$$

$$\Rightarrow I_C = \frac{0.5 + 10}{5K} = 2.1mA$$

$$I_B = I_E - I_C = 7.2mA$$

$$\beta_{\text{forced}} = \frac{I_{C(\text{sat})}}{I_B}$$

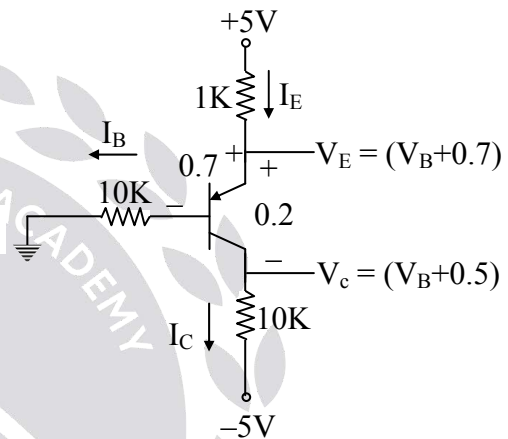
$$= \frac{2.1}{7.2}$$

$$= 0.29$$

$\beta_{\text{forced}} < \beta_{\text{active}}$  i.e., saturation region

15.

Sol:



$$I_E = I_C + I_B$$

$$\Rightarrow \frac{5 - (V_B + 0.7)}{1k} = \frac{(V_B + 0.5) + 5}{10k} + \frac{V_B}{10k}$$

$$10(5 - V_B - 0.7) = V_B + 0.5 + 5 + V_B$$

$$43 - 10V_B = 2V_B + 5.5$$

$$V_B = \frac{43 - 5.5}{12} = 3.125V$$

$$I_B = \frac{3.125}{10K} = 0.3125mA$$

$$V_C = V_B + 0.5 = 3.625V$$

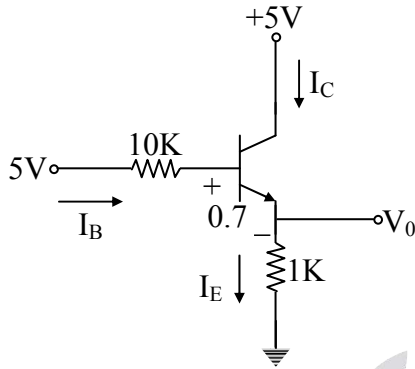
$$V_E = 3.825V$$

$$\therefore I_E = 1.175mA$$

$$\therefore I_C = 0.862mA$$

16.

**Sol:** Here the lower transistor (PNP) is in cut off region.



Apply KVL to the base emitter loop:

$$5 - 10K \cdot I_B - 0.7 - 1K \cdot (1 + \beta)I_B = 0$$

$$\Rightarrow I_B = \frac{4.3}{(101)K + 10K} = 38.73 \mu A$$

$$I_C = 3.87 \text{ mA}$$

$$I_E = 3.91 \text{ mA}$$

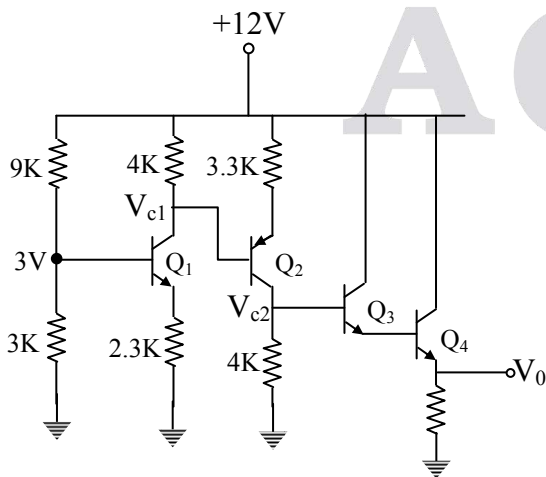
$$\Rightarrow V_E = V_0 = I_E(1k) = 3.91 \text{ V}$$

$$V_C = 5 \text{ V}$$

$$V_B = 5 - 10 \text{ k} (I_B) = 4.61 \text{ V}$$

17.

**Sol:**



$$I_{C_1} = I_{E_1} = \frac{2.3 \text{ V}}{2.3 \text{ k}} = 1 \text{ mA}$$

$$V_{C_1} = 12 \text{ V} - 4 \times 10^3 \times 1 \times 10^{-3} = 8 \text{ V}$$

$$V_{E_2} = 8 + 0.7 \text{ V} = 8.7 \text{ V}$$

$$I_{E_2} = \frac{12 \text{ V} - V_{E_2}}{3.3 \text{ k}} = \frac{12 \text{ V} - 8.7}{3.3 \text{ k}} = 1 \text{ mA}$$

$$V_{C_2} = 4 \text{ k} \times 1 \text{ mA} = 4 \text{ V}$$

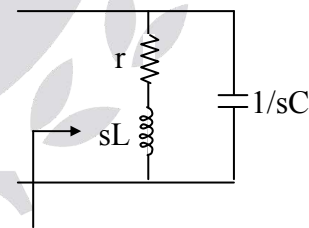
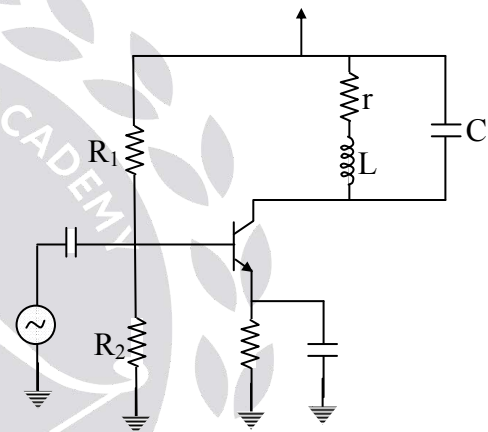
$$V_{E_3} = 4 \text{ V} - 0.7 = 3.3 \text{ V}$$

$$V_{E_4} = 3.3 - 0.7 = 2.6 \text{ V}$$

$$V_0 = 2.6 \text{ V}$$

18.

**Sol:**



$$Z_{eq} = \frac{1}{sC + \frac{1}{\frac{r + sL}{srC + s^2LC + 1}}} = \frac{r + sL}{(1 - \omega^2LC) + j\omega rC} = \frac{(r + j\omega L)[1 - \omega^2LC - j\omega rC]}{(1 - \omega^2LC)^2 + (\omega rC)^2}$$

$$= \frac{\omega^2 r L C + r - \omega^2 r L C + j\omega L [1 - \omega^2 L C] - j\omega r^2 C}{(1 - \omega^2 L C)^2 + (\omega r C)^2}$$

**Equate Imaginary terms:**

$$\omega L - \omega^3 L^2 C - \omega r^2 C = 0$$

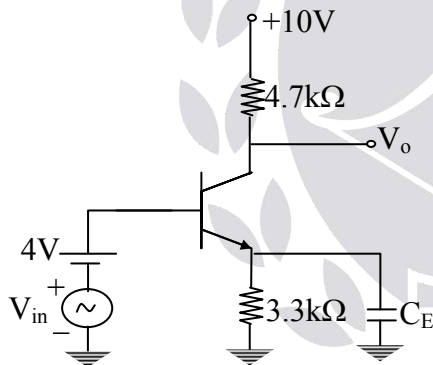
$$L - \omega^2 L^2 C - r^2 C = 0$$

$$\omega^2 L^2 C = L - r^2 C$$

$$\omega = \sqrt{\frac{1}{L C} - \frac{r^2 C}{L^2 C}}$$

$$\omega = \sqrt{\frac{1}{L C} - \left(\frac{r}{L}\right)^2}$$

**19.  
Sol:**



For D.C Analysis:

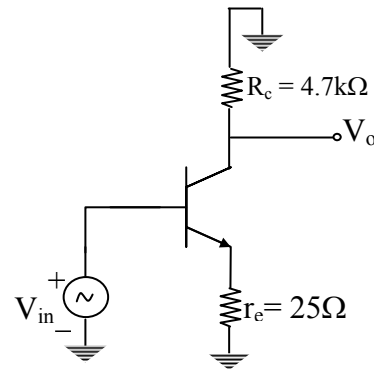
$$V_B = 4 \text{ V}$$

$$V_B - V_E = 0.7 \Rightarrow V_E = 4 - 0.7 = 3.3 \text{ V}$$

$$I_E = \frac{3.3}{3.3\text{k}} = 1\text{mA}$$

$$r_e = \frac{V_T}{I_E} = \frac{25\text{mV}}{1\text{mA}} = 25 \Omega$$

To apply small signal analysis set D.C source equal to zero.



$$\Rightarrow V_o = -i_c R_c$$

$$V_{in} = i_b r_\pi = i_b \beta r_e = i_c r_e$$

$$\therefore A_v = \frac{V_o}{V_i}$$

$$= \frac{-i_c R_c}{i_c r_e} = \frac{-R_c}{r_e} = \frac{-4.7\text{k}}{25} = -188$$

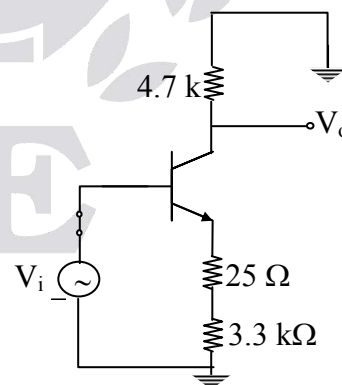
**20.**

**Sol:** D.C calculation is same as previous question

$$I_E = 1 \text{ mA}$$

$$r_e = 25 \Omega$$

Apply small signal analysis:



$$\frac{V_o}{V_i} = \frac{-R_c}{r_e + R_E} = \frac{-4700}{25 + 3300}$$

$$\therefore A_v = \frac{V_o}{V_i} = -1.413$$



21.

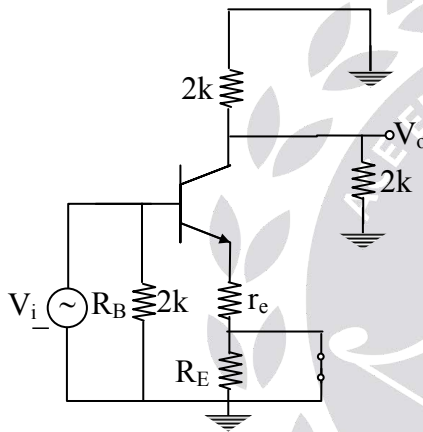
Sol: To calculate  $r_e$  value apply D.C analysis

$$I_E = \frac{V_{th} - V_{BE}}{R_E + \frac{R_{th}}{\beta + 1}}$$

$$= \frac{3 - 0.7}{2.3k + \frac{2k}{101}} = 0.991 \text{ mA}$$

$$r_e = \frac{V_T}{I_E} = \frac{25}{0.991} = 25.22 \Omega$$

Now apply small signal analysis:



$$A_v = \frac{V_o}{V_i} = \frac{-R_C}{r_e} = \frac{-(2k \parallel 2k)}{25.22} = -39.65$$

$$R_i = R_B \parallel \beta r_e$$

$$R_i = 1.116 \text{ k}\Omega$$

$$A_i = \frac{i_o}{i_i} = \frac{V_o}{R_L} \times \frac{R_i}{V_i} = A_v \times \frac{R_i}{R_L}$$

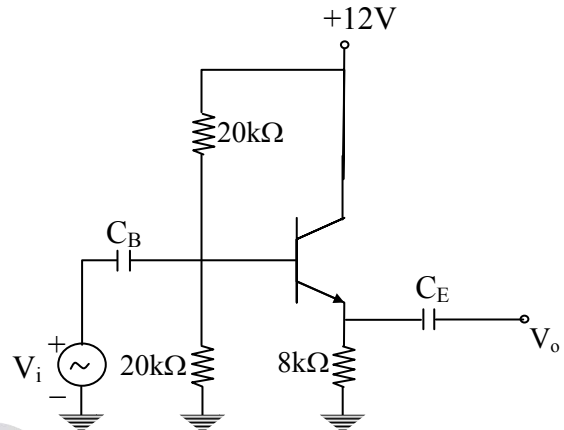
$$= \frac{-39.5 \times 1.116 \times 10^3}{2 \times 10^3}$$

$$= -22.322$$

$$R_o = R_C = 2 \text{ k}\Omega$$

22.

Sol:



Apply KVL at input Loop:

$$6 - 10k(I_B) - 0.7 - 8k(1 + \beta)I_B = 0$$

$$I_B = \frac{6 - 0.7}{10k + 8k \times 101} = 6.47 \mu\text{A}$$

$$I_E = 0.65 \text{ mA}$$

$$r_e = \frac{V_T}{I_E} = \frac{25}{0.65} = 38.5 \Omega$$

Apply small signal analysis

$$A_v = \frac{V_o}{V_i} = \frac{R_E}{r_e + R_E}$$

$$= 0.995$$

$$R_i = R_B \parallel \beta R_{E_{Total}}$$

$$R_{E_{Total}} = (R_E + r_e)$$

$$R_i = 10 \text{ k} \parallel 803.85 \text{ k}$$

$$= 9.87 \text{ k}\Omega$$

$$R_o = R_E \parallel r_e = 38.3 \Omega$$

23.

Sol:  $V_0 = -i_c R_C$

$$i_e \approx i_c = \frac{-V_i}{r_e}$$

$$V_0 = \left( \frac{V_i}{r_e} \right) R_C$$

$$\frac{V_0}{V_i} = \frac{R_C}{r_e}$$

Given  $I_E = 1\text{mA}$

$$\Rightarrow r_e = \frac{25\text{mV}}{1\text{mA}} = 25\Omega$$

$$A_V = \frac{R_C}{r_e}$$

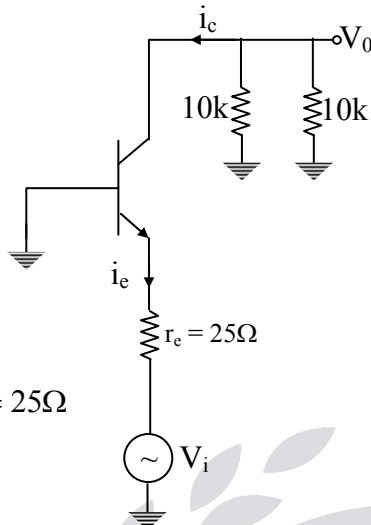
$$A_V = \frac{10\text{k} // 10\text{k}}{25} = \frac{5000}{25} = 200$$

$$R_0 = R_C = 10\text{k}\Omega$$

$$R_i = r_e = 25\Omega$$

$$A_I = \frac{i_0}{i_i} = \frac{v_0}{R_L} \times \frac{R_i}{v_i}$$

$$= A_V \times \frac{R_i}{R_L} = \frac{200 \times 25}{10^4} = 0.5$$



24.

Sol: For the given differential amplifier,

$$I_E = 1\text{mA}$$

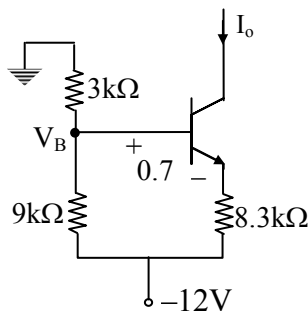
$$r_e = \frac{V_T}{I_E} = 25\Omega$$

$$A_d = \frac{V_0}{V_i} = \frac{-R_c}{r_e} = \frac{-3000}{25} \text{ (or) } -g_m R_c$$

$$A_d = -120$$

25.

Sol:



$$I_1 = \frac{0 - (-12)}{12\text{k}} = 1\text{mA}$$

$$I_1 = \frac{0 - V_B}{3\text{k}}$$

$$V_B = -3\text{V}$$

$$V_B - V_E = 0.7$$

$$V_E = V_B - 0.7$$

$$V_E = -3.7 \text{ Volt}$$

$$I_0 = \frac{-3.7 + 12}{8.3\text{k}}$$

$$I_0 = 1\text{mA}$$

$$I_E = 0.5\text{mA}$$

$$r_e = \frac{25\text{mV}}{0.5\text{mA}} = 50\Omega$$

$$A_d = \frac{-R_C}{r_e} = \frac{-2000}{50}$$

$$A_d = -40$$

26.

Sol: Voltage shunt feedback amplifier and

$$\frac{V_0}{V_{in}} = \frac{-R_f}{R_s} = \frac{-10\text{k}}{1\text{k}} \approx -10$$

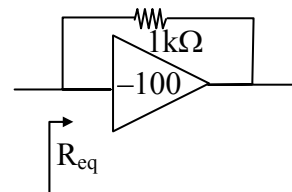
27.

Sol: Current - series feedback amplifier and

$$A_V \approx \frac{-R_C}{R_E} = \frac{-4.7\text{k}}{3.3\text{k}} = 1.4242$$

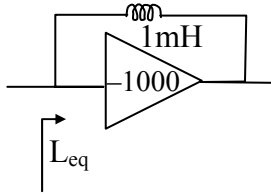
28.

Sol:



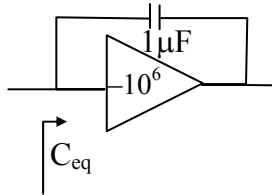
Using millers effect,

$$R_{eq} = \frac{1\text{k}}{1 + 100} = 9.9\Omega$$



$$L_{eq} = \frac{1\text{mH}}{1+1000} \approx 1\mu\text{H}$$

29.  
Sol:



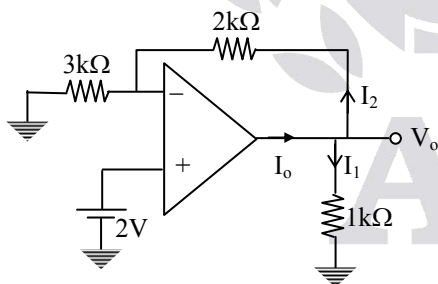
$$C_{eq} = 1\mu\text{F}(1+10^6) \approx 1\text{F}$$

30.

Sol:  $V_0 = \left(1 + \frac{R_f}{R_1}\right) V_i$

$$V_0 = \left(1 + \frac{2\text{k}}{3\text{k}}\right) 2$$

$$V_0 = \frac{10}{3} \text{ volt}$$



$$I_1 = \frac{V_0}{1\text{k}} = \frac{10}{3} \text{ mA} \quad \&$$

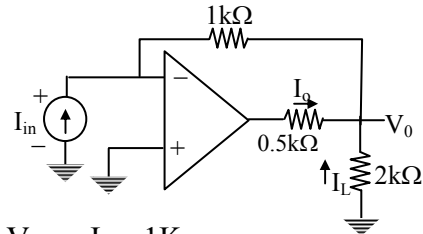
$$I_2 = \frac{V_0 - 2}{2\text{k}} = \frac{\frac{10}{3} - 2}{2\text{k}} = \frac{2}{3} \text{ mA}$$

$$\therefore I_0 = I_1 + I_2 = 4\text{mA}$$

31.

Sol:  $V_0 = \frac{-R_2}{R_1} V_{in}$

32.  
Sol:



$$V_0 = -I_{in} \times 1\text{K}$$

$$I_L = \frac{I_i \times 1\text{K}}{2\text{K}} = \frac{I_{in}}{2}$$

$$I_0 + I_{in} + I_L = 0$$

$$I_0 + I_{in} + \frac{I_{in}}{2} = 0$$

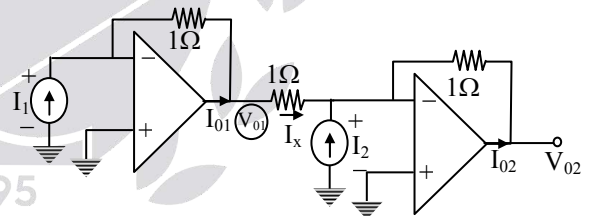
$$2I_0 + 2I_{in} + I_{in} = 0$$

$$2I_0 = -3I_{in}$$

$$\frac{I_0}{I_{in}} = \frac{-3}{2} = -1.5$$

33.

Sol:



$$V_{01} = -I_1$$

Apply KCL:

$$I_x + I_2 = \frac{0 - V_{02}}{1}$$

$$\frac{V_{01}}{1} + I_2 = -V_{02}$$

$$V_{01} + I_2 = -V_{02}$$

$$-I_1 + I_2 = -V_{02}$$

$$V_{02} = (I_1 - I_2) \text{ volt}$$

$$I_{01} + I_1 = I_x$$

$$I_{01} + I_1 = V_{01} \quad \left[ \because I_x = \frac{V_{01}}{1} \right]$$

$$I_{01} = V_{01} - I_1$$

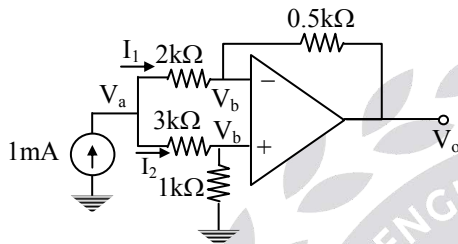
$$I_{01} = -2I_1 \quad \left[ \because V_{01} = -I_1 \right]$$

$$I_{02} = -(I_2 + I_x)$$

$$I_{02} = -(I_2 + V_{01})$$

$$I_{02} = (I_1 - I_2)A$$

**34.**  
**Sol:**



Apply KCL at  $V_a$ :

$$1m = \frac{V_a - V_b}{2k} + \frac{V_a - V_b}{3k}$$

$$1m = \frac{3V_a - 3V_b + 2V_a - 2V_b}{6k}$$

$$6 = 5V_a - 5V_b$$

$$V_a - V_b = \frac{6}{5}$$

$$V_a - V_b = 1.2 \text{ Volt}$$

$$I_1 = \frac{V_a - V_b}{2k} = \frac{1.2}{2k} = 0.6 \text{ mA}$$

$$I_2 = \frac{1.2}{3k} = 0.4 \text{ mA}$$

$$V_b = 0.4 \text{ mA} \times 1k = 0.4 \text{ Volt}$$

$$I_1 = \frac{V_b - V_o}{0.5k}$$

$$0.6 \text{ mA} = \frac{0.4 - V_o}{0.5k}$$

$$0.3 = 0.4 - V_o$$

$$\therefore V_o = 0.1 \text{ Volt}$$

**35.**

$$\text{Sol: } V_C = \frac{-I}{C} \cdot t = \frac{-10 \times 10^{-3}}{10^{-6}} \times 0.5 \times 10^{-3}$$

$$V_C = -5 \text{ Volt}$$

**36.**

**Sol:** Given open loop gain = 10

$$\frac{V_o}{V_i} = \frac{\left(1 + \frac{R_f}{R_1}\right)}{1 + \left(1 + \frac{R_f}{R_1}\right) \times \frac{1}{A_{OL}}}$$

$$\frac{V_o}{V_i} = \frac{(1+3)}{1 + \frac{4}{10}}$$

$$V_o = V_i \times \frac{4}{1 + \frac{4}{10}}$$

$$V_o = \frac{2 \times 4}{1 + \frac{4}{10}} = 5.715 \text{ Volt}$$

**37.**

$$\text{Sol: } \frac{V_o}{V_i} = \frac{-R_f/R_1}{1 + \frac{(1 + R_f/R_1)}{A_{OL}}}$$

$$\frac{V_o}{V_i} = \frac{-9}{1 + \frac{10}{10}}$$

$$\frac{V_o}{V_i} = \frac{-9}{2}$$

$$V_o = -4.5 \text{ Volt}$$

**38.**

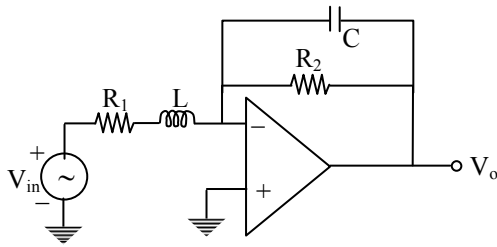
**Sol:**  $SR = 2\pi f_{\max} V_{0\max}$

$$V_{0\max} = \frac{SR}{2\pi f_{\max}} = \frac{10^6}{2\pi \times 20 \times 10^3} = 7.95 \text{ Volt}$$

$$V_o = A \times V_i \Rightarrow V_i = \frac{V_o}{A} = 79.5 \text{ mV}$$

39.

Sol:



$$z_2 = R_2 \parallel \frac{1}{sC} = \frac{R_2}{sCR_2 + 1}$$

$$z_1 = R_1 + sL$$

$$\left| \frac{V_o}{V_i} \right| = \frac{R_2}{(sCR_2 + 1)(R_1 + sL)}$$

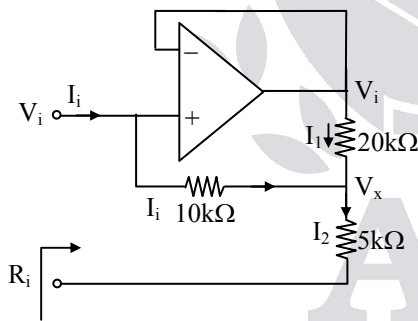
$$\left| \frac{V_o}{V_i} \right| = \frac{R_2}{(sCR_2 + 1)(R_1 + sL)}$$

It represent low pass filter with

$$\text{D.C gain} = \frac{R_2}{R_1}$$

40.

Sol: (i)



Apply KCL at  $V_x$  :

$$\frac{V_x}{5k} = I_i + I_1$$

$$\frac{V_x}{5k} = \frac{V_i - V_x}{10k} + \frac{V_i - V_x}{20k}$$

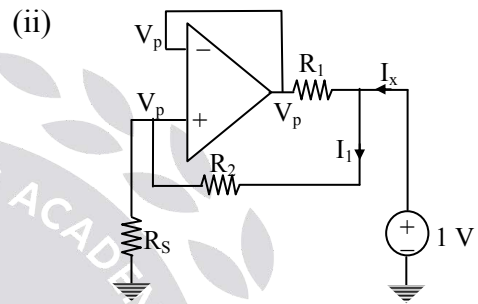
$$\frac{V_x}{5} = \frac{3V_i - 3V_x}{20}$$

$$V_x = \frac{3}{7} V_i$$

$$I_i = \frac{V_i - V_x}{10k}$$

$$I_i = \frac{V_i - \frac{3}{7} V_i}{10k}$$

$$\frac{V_i}{I_i} = 17.5k\Omega$$



$$R_0 = \frac{1}{I_x}$$

$$V_p = \frac{R_s}{R_2 + R_s}$$

$$I_x = \frac{1 - V_p}{R_2} + \frac{1 - V_p}{R_1}$$

$$I_x = (1 - V_p) \left( \frac{1}{R_2} + \frac{1}{R_1} \right)$$

$$I_x = \left( 1 - \frac{R_s}{R_2 + R_s} \right) \left( \frac{R_1 + R_2}{R_1 R_2} \right)$$

$$I_x = \frac{R_2}{R_2 + R_s} \left( \frac{R_1 + R_2}{R_1 R_2} \right)$$

$$\therefore R_0 = \frac{1}{I_x} = \left( \frac{R_s + R_2}{R_1 + R_2} \right) R_1$$

41.

**Sol:**  $V_E = V_{in}$

$$V_{CE} = V_C - V_E$$

$$V_{CE} = 15 - V_{in}$$

given  $V_{in}$  0 to 5 Volt

$\Rightarrow$  Transistor is in active region

$$I_E = I_0 = \frac{V_{in} + 15}{10} = \frac{17}{10} = 1.7 \text{ A} \quad [ \because V_{in} = 2 \text{ V} ]$$

$$I_B = \frac{I_0}{1 + \beta} = \frac{1.7}{100} \text{ A}$$

$$V_B = V_{in} + 0.7 = 2.7 \text{ V}$$

$$I_B = \frac{V_{op} - V_B}{100}$$

$$\frac{V_{op} - 2.7}{100} = \frac{1.7}{100}$$

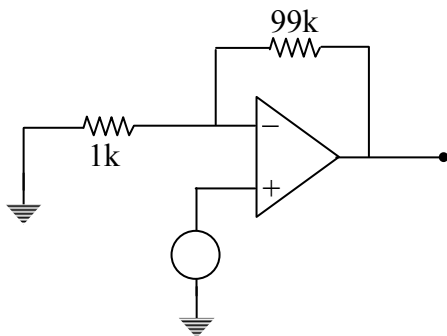
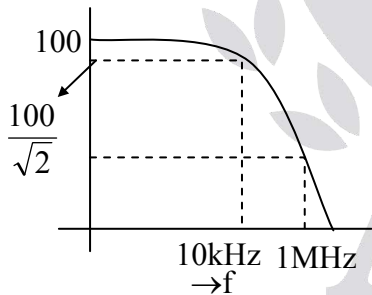
$$V_{op} = 4.4 \text{ Volt}$$

42.

**Sol:** Single stage:

$$\text{Gain} = 40 \text{ dB} = 100, f_T = 1 \text{ MHz} = \text{Gain BW}$$

$$\text{BW} \rightarrow f_{3\text{dB}} = \frac{f_T}{\text{Gain}} = \frac{10^6}{100} = 10 \text{ kHz}$$

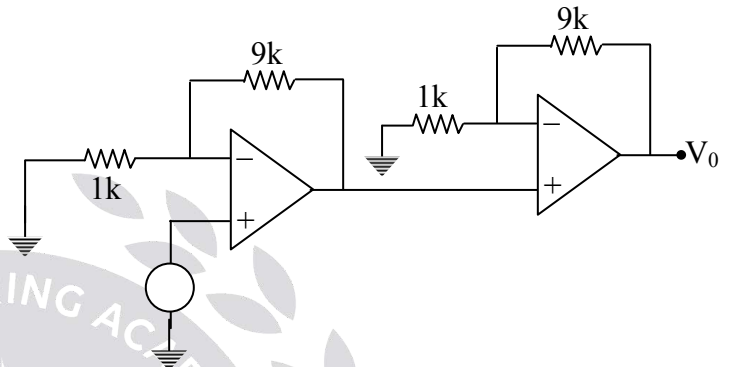


Two stages:



$$f_{3\text{dB}} = \frac{1\text{M}}{10} = 100 \text{ kHz}, \quad f_{3\text{dB}} = 100 \text{ kHz (for single stage)}$$

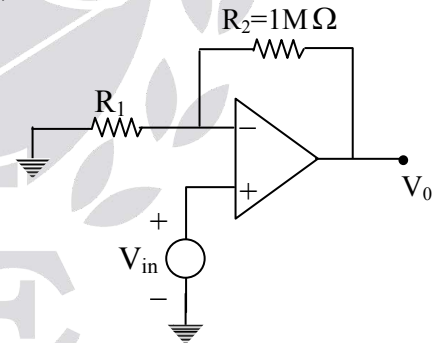
Two stages (Overall):



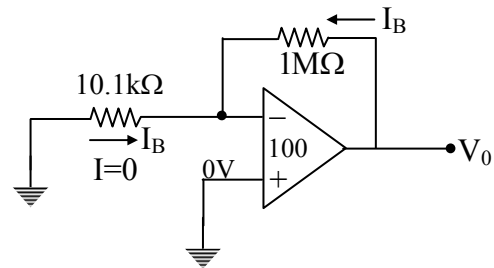
$$\begin{aligned} \text{Overall BW} &= f_{3\text{dB}} \sqrt{2^{1/2} - 1} \\ &= 100 \text{ k} (0.65) \\ &= 65 \text{ kHz} \end{aligned}$$

43.

**Sol:** (a)



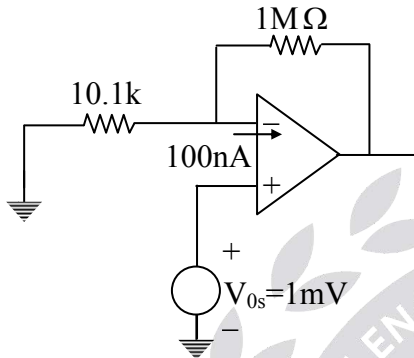
$$\text{Gain} = \frac{V_0}{V_{in}} = 1 + \frac{1\text{M}}{R_1} = 100 \Rightarrow R_1 = 10.1 \text{ k}\Omega$$



$$\begin{aligned} V_0 &= I_B(1M) \\ &= 100nA(1M) \\ &= 0.1V \end{aligned}$$

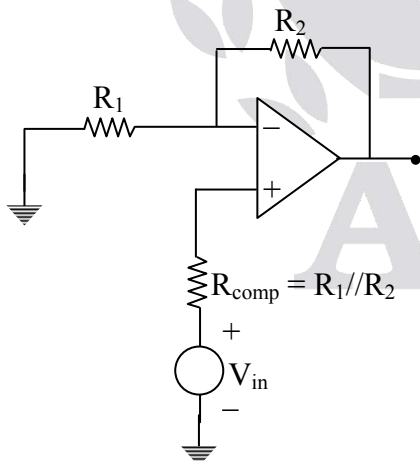
(b)

- op-amp draws current
- op-amp CKT the curve doesn't pass through '0' (transfer characteristics)



$$\begin{aligned} V_0 &= |V_{0 \text{ Bios current}}| + |V_{0 \text{ Offset Voltage}}| \\ &= 1M(I_B) + \left(1 + \frac{R_2}{R_1}\right) V_{os} \\ &= 1M(100nA) + 100(1mV) \\ &= 0.2V \end{aligned}$$

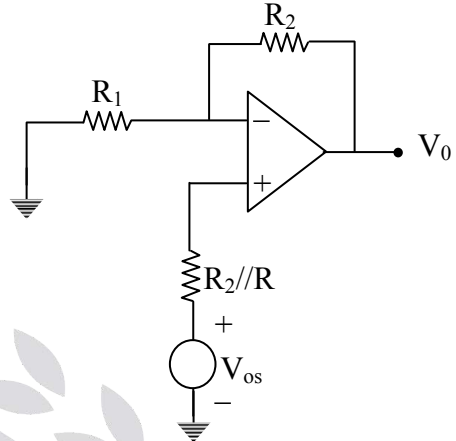
(c)



$$\begin{aligned} \rightarrow R_{comp} &= R_1/R_2, \text{ then } V_0 = (I_{B1} - I_{B2}) R_2 \\ &= I_{os} R_2 \\ V_0 &= (I_{B1} - I_{B2}) R_2 \\ &= I_{os} R_2 \\ &= 1/10 (I_B R_2) \end{aligned}$$

$$\begin{aligned} &= \frac{1}{10} 100nA(1M) \\ &= 0.01V \end{aligned}$$

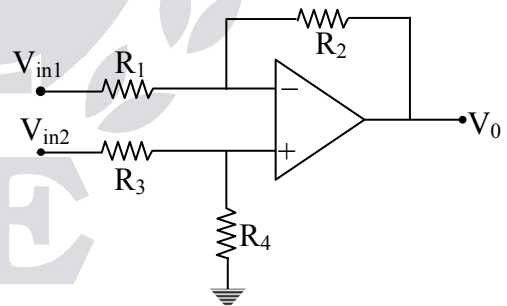
(d)



$$\begin{aligned} V_0 &= |V_{0 \text{ Offset Voltage}}| + |V_{0 \text{ Bios current}}| \\ &= 0.1 + 0.01 \\ &= 0.11 \end{aligned}$$

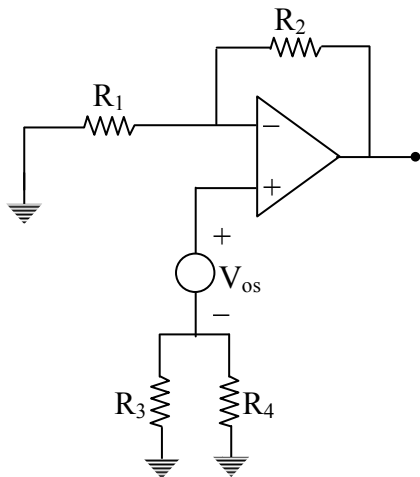
44.

**Sol:** Given  
 $R_1 = R_3 = 10k\Omega$   
 $R_2 = R_4 = 1M\Omega$



$$\begin{aligned} V_0 &= \frac{R_2}{R_1} (V_{in2} - V_{in1}) \\ &= \frac{1M}{10k} (V_{in2} - V_{in1}) \end{aligned}$$

Given  $V_{os} = 4mV$   
 $I_B = 0.3 \mu A$   
 $I_{os} = 50 nA$

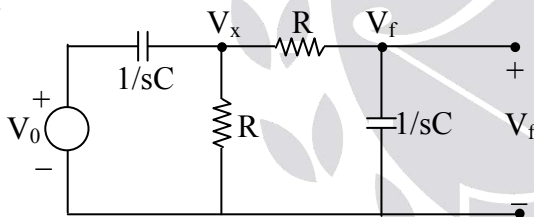


$$V_o = \left[ 1 + \frac{R_2}{R_1} \right] V_{os} + I_{os} R_2$$

$$= \left[ 1 + \frac{1M}{10k} \right] 4mV + 50nA [1M]$$

$$= 454mV$$

45.  
Sol:



KCL

$$\frac{V_x - V_0}{(1/sC)} + \frac{V_x}{R} + \frac{V_x - V_f}{R} = 0 \text{ -----(1)}$$

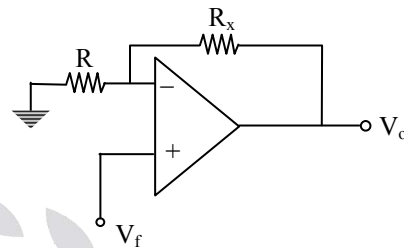
$$\frac{V_f - V_x}{R} + \frac{V_f}{(1/sC)} = 0 \text{ -----(2)}$$

From (1) and (2) eliminate  $V_x$

$$\beta = \frac{V_f}{V_0} = \frac{SCR}{[S^2C^2R^2 + 3SCR + 1]}$$

$$\beta = \frac{1}{\left[ 3 + SCR + \frac{1}{SCR} \right]}$$

$$\beta = \frac{1}{3 + j\left( \omega RC - \frac{1}{\omega RC} \right)} \quad (S = j\omega)$$



$$A = \frac{V_o}{V_f} = 1 + \frac{R_x}{R}$$

Loop gain = 1  $\rightarrow A = 1/\beta$

$$A\beta = 1$$

$$1 + \frac{R_x}{R} = 3 + j\left( \omega RC - \frac{1}{\omega RC} \right)$$

Equate imaginary parts

$$0 = \omega RC - \frac{1}{\omega RC}$$

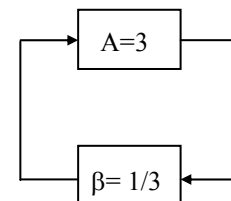
$$\omega^2 = \frac{1}{R^2C^2}$$

$$f = \frac{1}{2\pi RC} \text{ frequency of oscillation}$$

Equate

$$1 + \frac{R_x}{R} = 3$$

$$R_x = 2R$$





46.

**Sol:**  $\omega_0 = \frac{1}{\sqrt{LC}}$

$$\frac{V_F}{V_0} = \beta = \frac{0.5k}{R_x + 0.5}$$

$$A = 1 + \frac{9k}{1k} = 10$$

$A\beta = 1$  for sustained oscillations

$$\frac{0.5k}{R_x + 0.5k} \times 10 = 1$$

$$\therefore R_x = 4.5 \text{ k}\Omega$$

47.

**Sol:** Given  $\beta = \frac{1}{6}$

$$A = 1 + \frac{R_2}{R_1}$$

$A\beta = 1$  for sustained oscillations

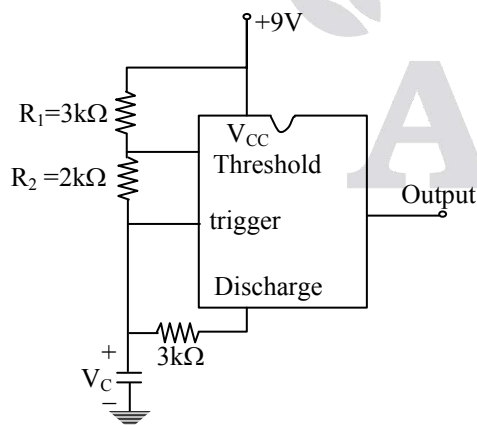
$$\left(1 + \frac{R_2}{R_1}\right) \cdot \frac{1}{6} = 1$$

$$\frac{R_2}{R_1} = 5$$

$$R_2 = 5 R_1$$

48.

**Sol:**



$$V_{th} = \frac{2}{3} V_{CC} = \frac{2}{3} \times 9 = 6 \text{ V}$$

$$V_{th} - V_C = 2 \times 10^3 \times I \quad \left( I = \frac{9-6}{3k} \right)$$

$$V_{th} - V_C = 2 \text{ V}$$

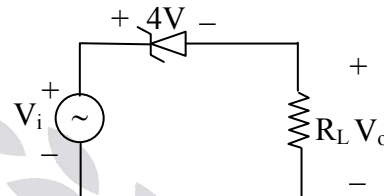
$$V_C = V_{th} - 2 = 4 \text{ V}$$

$$V_{trigger} = \frac{1}{3} V_{CC} = 3 \text{ V}$$

$$V_C = 3 \text{ V to } 4 \text{ V}$$

49.

**Sol:**



$$V_i = 8 \sin t \text{ V}$$

During -Ve cycle, Zener is Forward biased and act as short circuit.

$$\Rightarrow V_0 = V_i$$

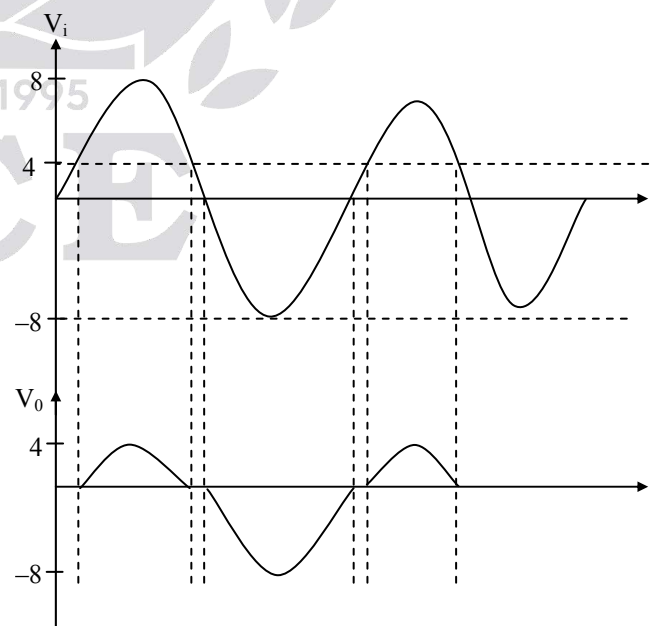
During + Ve cycle,

For  $0 < V_i < 4$ , Zener OFF Since Zener is not in break down

$$\Rightarrow V_0 = 0$$

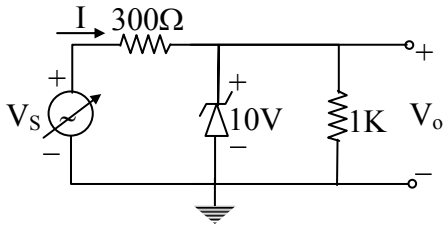
For  $V_i > 4$ , Zener is in break down.

$$\Rightarrow V_0 = V_i - 4$$



50.

Sol:



$$I_z = 1\text{mA to } 60\text{mA}$$

$$I = \frac{V_s - V_z}{300}$$

$$I_{\min} = \frac{V_{s\min} - 10}{300} \quad \text{--- (I)}$$

$$I_{\max} = \frac{V_{s\max} - 10}{300} \quad \text{--- (II)}$$

$$I_{\min} = I_{z\min} + I_L \left[ \because I_L + \frac{V_z}{1k} = 10\text{mA} \right]$$

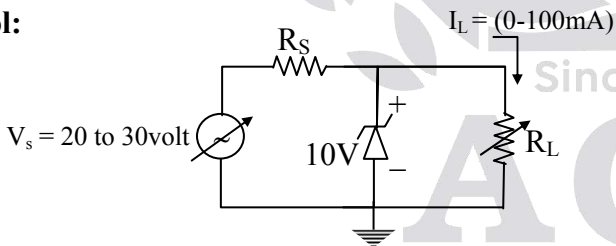
$$I_{\min} = 1\text{mA} + 10\text{mA} = 11\text{mA}$$

$$I_{\max} = 60\text{mA} + 10\text{mA} = 70\text{mA}$$

From equation (1) and (2) required range of  $V_s$  is 13.3 to 31 volt.

51.

Sol:



The current in the diode is minimum when the load current is maximum and  $v_s$  is minimum.

$$R_s = \frac{V_{s\min} - V_z}{I_{z\min} + I_{L\max}}$$

$$R_s = \frac{20 - 10}{(10 + 100)\text{mA}}$$

$$R_s = 90.9\Omega$$

$$I_{z\max} = \frac{30 - 10}{90.9} = 0.22\text{A} \left[ \because I_{L\min} = 0\text{A} \right]$$

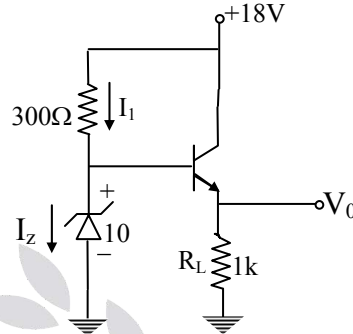
$$P_z = V_z I_{z\max}$$

$$P_z = 10 \times 0.22$$

$$P_z = 2.2\text{W}$$

52.

Sol:



$$V_B = 10\text{volt}$$

$$V_E = 10 - 0.7 = 9.3\text{volt}$$

$$I_E = 9.3\text{mA}$$

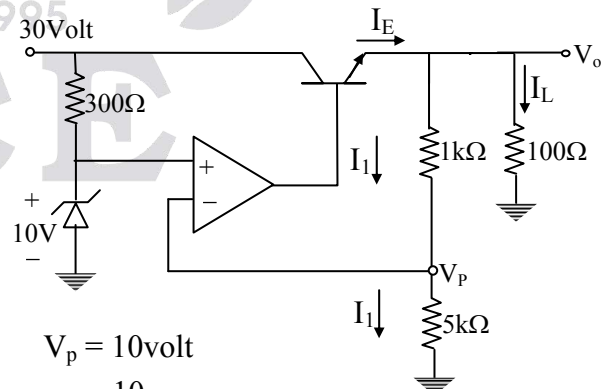
$$I_B = \frac{I_E}{1 + \beta} = \frac{9.3\text{mA}}{101} = 92.07\mu\text{A}$$

$$I_1 = \frac{18 - 10}{300} = 26.67\text{mA}$$

$$I_z = I_1 - I_B = 26.57\text{mA}$$

53.

Sol:



$$V_p = 10\text{volt}$$

$$I_1 = \frac{10}{5k} = 2\text{mA}$$

$$\Rightarrow V_o = (6k) I_1 = 12\text{V} = V_E$$

$$V_C = 30\text{volt}$$

$$\Rightarrow V_{CE} = V_C - V_E = 18 \text{ volt.}$$

$$I_E = I_1 + I_L$$

$$I_E = 2\text{m} + \frac{12}{100} = 122\text{mA}$$

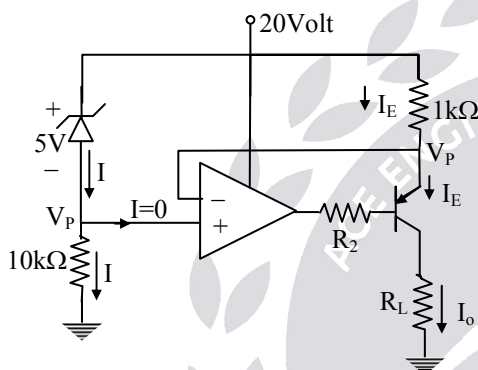
$$\Rightarrow I_C = \frac{\beta}{1+\beta} I_E$$

$$\Rightarrow I_C = 0.120\text{Amp}$$

$$\Rightarrow P_T = I_C \times V_{CE}$$

$$\therefore P_T = 2.17\text{W}$$

**54. Sol:**



$$I = \frac{20 - 5}{10\text{k}} = \frac{15}{10} \text{ mA}$$

$$V_P = 10\text{k} \times I = 15\text{volt}$$

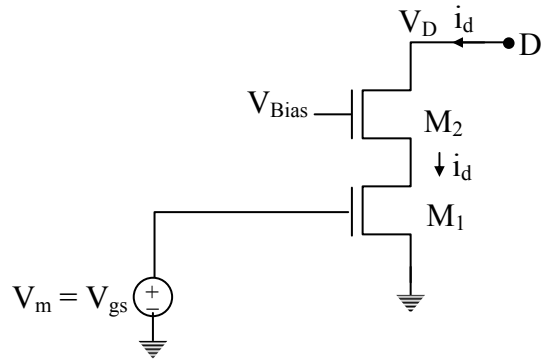
$$I_C = \frac{20 - V_P}{1\text{k}} = \frac{20 - 15}{1\text{k}} = 5\text{mA}$$

$$\beta \text{ large} \Rightarrow I_B \approx 0\text{A}$$

$$\therefore I_C = I_0 = 5\text{mA}$$

**55. Ans: (c)**

**Sol:** The circuit given is the MOS cascode amplifier, Transistor  $M_1$  is connected in common source configuration and provides its output to the input terminals (i.e., source) of transistor  $M_2$ . Transistor  $M_2$  has a constant dc voltage,  $V_{bias}$  applied at its gate. Thus the signal voltage at the gate of  $M_2$  is zero and  $M_2$  is operating as a CG amplifier. Which is current Buffer.

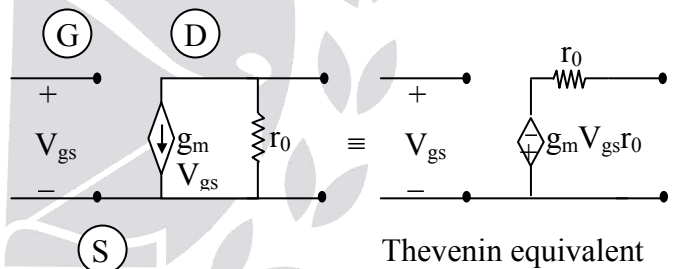


Overall transconductance

$$g_m = \frac{i_d}{V_{gs}} = \left[ \frac{\partial i_D}{\partial V_{GS}} \right] = \frac{i_{d1}}{V_{gs1}} = g_{m1}$$

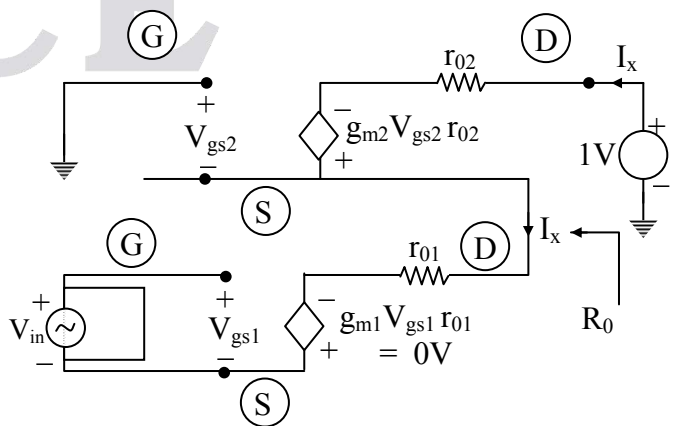
The overall (approximate) transconductance of the cascode amplifier is equal to the transconductance of common source amplifier  $g_{m1}$ .

**AC model of MOSFET**



Thevenin equivalent

Let us find the output resistance  $R_0 = \frac{1V}{I_x}$



By KVL  $V_{gs2} + I_x r_{01} = 0$

$$V_{gs2} = -I_x r_{01} \text{ -----(1)}$$

By KVL

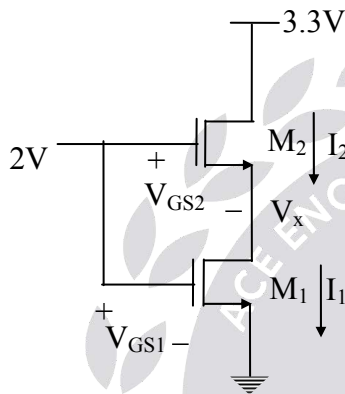
$$-1 + I_x r_{02} - g_m r_{02} V_{gs2} + I_x r_{01} = 0$$

$$-1 + I_x r_{02} + g_m r_{02} I_x r_{01} + I_x r_{01} = 0$$

$$\therefore I_x = \frac{1}{r_{01} + r_{02} + g_m r_{02} r_{01}} \approx \frac{1}{g_m r_{01} r_{02}}$$

$$R_0 = \frac{1}{I_x} = g_m r_{01} r_{02}$$

**56.**  
**Sol:**



$$\left(\frac{W}{L}\right)_2 = 2 \left(\frac{W}{L}\right)_1$$

$V_{TH} = 1V$  for both  $M_1$  and  $M_2$

For  $M_2$  to be in saturation:

$$V_D > V_G - V_{TH}$$

$$3.3 > 2 - 1$$

$$3.3 > 1$$

So  $M_2$  will be in saturation if it is ON.

For  $M_1$  to be in saturation:

$$V_D > V_G - V_{TH}$$

$$V_x > 2 - 1$$

$V_x > 1V$  but if  $V_x$  is more than  $1V$ ,  $V_{GS2}$  becomes less than  $1V$ , which means  $M_2$  will be off so  $M_1$  can not be in saturation.

Now, We can conclude that  $M_1$  is in triode and  $M_2$  is in saturation

$$V_{GS1} = 2V$$

$$V_{DS1} = V_x$$

$$V_{GS2} = 2 - V_x$$

$$\text{Now, } I_1 = I_2$$

$$\mu_n C_{ox} \left(\frac{W}{L}\right)_1 \left[ (V_{GS1} - V_{TH}) V_{DS1} - \frac{1}{2} V_{DS1}^2 \right]$$

$$= \frac{1}{2} \mu_n C_{ox} \left(\frac{W}{L}\right)_2 (V_{GS2} - V_{TH})^2$$

$$V_x - \frac{1}{2} V_x^2 = (2 - V_x)^2$$

$$3V_x^2 - 6V_x + 2 = 0$$

$$V_x = 0.42V, -1.58V$$

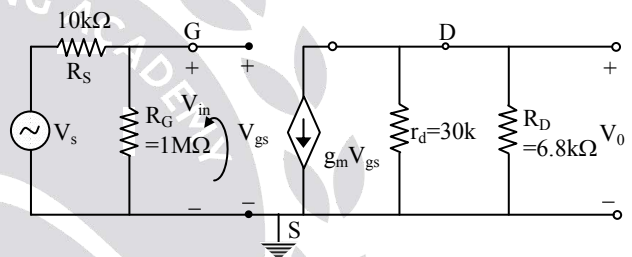
$V_x$  cannot be more than  $1V$ , since  $M_2$  will become off

$$\text{So, } V_x = 0.42V$$

**57.**

**Sol:** Given  $I_{DSS} = 10\text{ mA}$ ,  $V_p = -5V$ ,

$$V_{GG} = -2V \text{ and } r_d = 30\text{ k}\Omega$$



$$V_0 = -g_m V_{gs} (r_d || R_D)$$

$$\therefore A_v = -g_m (r_d || R_D)$$

$$I_D = I_{DSS} \left[ 1 - \frac{V_{GS}}{V_p} \right]^2$$

$$V_G = -2V$$

$$V_{GS} = -2 - 0 = -2V (\because V_s = 0V)$$

$$I_D = 10m \left[ 1 - \frac{-2}{-5} \right]^2$$

$$I_D = 3.6\text{ mA}$$

$$g_m = \frac{2\sqrt{I_D I_{DSS}}}{V_p}$$

$$= \frac{2\sqrt{(3.6m)(10m)}}{5} = \frac{2 \times 6m}{5} = 2.4\text{ms}$$

$$\therefore A_v = -(2.4 \times 10^{-3}) [30\text{ k} || 6.8\text{ k}]$$

$$\frac{V_0}{V_{gs}} = A_v = -13.3$$

$$V_{gs} = \frac{10^6}{10^6 + 10^4} V_s$$

$$= 0.99 V_s$$

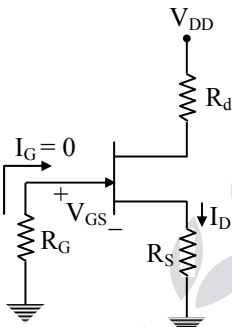
$$\frac{V_0}{V_s} = A_{V_s}$$

$$= -13.3 \times 0.99$$

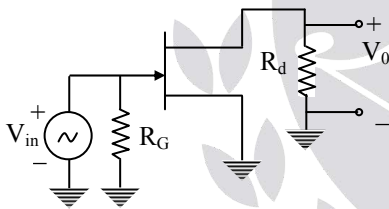
$$= -13.16$$

58.

**Sol: DC Equivalent**



**AC Equivalent**



Device equation

$$(i) I_{DS} = I_{DSS} \left[ 1 - \frac{V_{GS}}{V_P} \right]^2$$

$$\Rightarrow 0.8 \text{ mA} = 1.65 \text{ mA} \left[ 1 - \frac{V_{GS}}{-2} \right]^2$$

$$\Rightarrow V_{GSQ} = -0.607 \text{ V}$$

$$(ii) g_m = \frac{\partial I_{DS}}{\partial V_{GS}} = 2I_{DSS} \left[ 1 - \frac{V_{GSQ}}{V_P} \right] \left[ -\frac{1}{V_P} \right]$$

$$= 2(1.65 \text{ mA}) \left[ 1 - \frac{0.607}{2} \right] \left[ \frac{1}{2} \right]$$

$$= 1.149 \text{ ms}$$

$$(iii) V_G = V_{GS} + I_{DS}R_S = 0$$

$$\Rightarrow -0.607 + 0.8 \text{ mA}(R_S) = 0$$

$$R_S = \frac{-0.607}{-0.8 \text{ mA}} = 758.75 \Omega$$

$$(iv) \text{Voltage gain } (A_V) = -g_m R_d$$

$$\text{Gain (dB)} = 20 \log A_V$$

$$20 = 20 \log A_V$$

$$\Rightarrow A_V = 10$$

$$\Rightarrow 10 = g_m R_d$$

$$\Rightarrow 10 = (1.149 \text{ m})R_d$$

$$\therefore R_d = 8.7 \text{ k}\Omega$$

Since 1995

**ACE**