

Hyderabad | Delhi | Ahmedabad | Bhopal | Pune | Bhubaneswar | Bengaluru Lucknow | Patna | Chennai | Vijayawada | Vizag | Tirupathi | Kukatpally | Kolkata

# **GATE - 2019**

# Questions with Detailed Solutions

# ELECTRONICS & COMMUNICATION ENGINEERING

ACE Engineering Academy has taken utmost care in preparing the **GATE-2019** Examination solutions. Discrepancies, if any, may please be brought to our notice. ACE Engineering Academy do not owe any responsibility for any damage or loss to any person on account of error or omission in these solutions. ACE Engineering Academy is always in the fore front of serving the students, irrespective of the examination type (GATE/ESE/PSUs/PSC/GENCO/TRANSCO etc.,).

All Queries related to GATE- 2019 Solutions are to be sent to the following email address hyderabad@aceenggacademy.com | Contact Us: 040-23234418,19,20

Ķ	Engineering Publications	(2)	Electronics & Communication Engineering
	1	Section : General Ap	titude
01. 01	The boat arrived dawn. (a) Under (b) at	(c) on	(d) in
Sol:	Use preposition 'at' dawn		
		End of Solution	
02	When he did come home she	him lying dead on the roa	dside somewhere
•=	(a) concluded (b) notice	(c) looked	(d) pictured
<b>02.</b>	Ans: (d)		
Sol:	Pictured means to have a thought, u	nderstanding or idea about s <b>End of Solution</b>	something or someone.
03.	Five different books (P, Q, R, S, T) second, respectively from the right s arranged is	are to be arranged on a shel side of the shelf. The numbe	f. The books R and S are to be arranged first and er of different orders in which P, Q and T may be
	(a) 6 (b) 2	(c) 12	(d) 120
Sol:	Five different books = P, Q, R, S and $ \begin{array}{ccccccccccccccccccccccccccccccccccc$	d T from the given data, the	above books are arranged as follows
	Another Method:		
	From the given data R and S places a = 6 ways.	are fixed and remaining three	e books can be arranged in 3! ways (i.e.) $3 \times 2 \times 1$
	Hence Option (1) is correct.	End of Solution	
	The strategies that the company	to sell its products	house-to-house marketing.
04.	The shalegies that the company		- /
04.	(a) use, includes (b) uses, include	(c) uses, including	(d) used, includes

# RRB(JE)-2019



Common for all Streams No. of Tests : 20 Starts from 25<sup>th</sup> February 2019



CE | ME | EC | EE No. of Tests : 20 Starts from 6<sup>th</sup> May 2019

**()** 040 - 48539866 / 040 - 40136222

testseries@aceenggacademy.com

ACE Launches



# For B.Tech – CSE Students



# Placement Training

In **Level – 1 Companies** Short Term & Long Term Batches

	<b>ACE</b> Engineering Publications		$\begin{pmatrix} 4 \end{pmatrix}$	Electronics & Commun	ication Engineering
05.	It would take one	machine 4 hours to com	plete a production or	der and another machine 2	hours to complete the
	same order. If bot	h machines work simult	aneously at their resp	bective constant rates, the ti	me taken to complete
	the same order is	hours.			
	(a) 3/4	(b) 2/3	(c) 7/3	(d) 4/3	

#### 05. Ans: (d)

6-3

**Sol:** Machine one  $(M_1)$  can take to complete production = 4 hours

Second Machine  $(M_2)$  can take to complete production = 2 hours

$$\begin{split} M_1 &= 4 \text{ hours, } 1 \text{ hours} = \frac{1}{4}^{\text{th}} \text{ production} \\ M_2 &= 2 \text{ hours, } 1 \text{ hours} = \frac{1}{2}^{\text{th}} \text{ production} \\ \text{In one hour } (M_1 + M_2) = \frac{1}{4} + \frac{1}{2} = \frac{1+2}{4} = \frac{3}{4}^{\text{th}} \end{split}$$

 $\therefore$  M<sub>1</sub> and M<sub>2</sub> can take to complete production =  $\frac{4}{3}$  hours

**End of Solution** 

06. Five people P, Q, R, S and T work in a bank. P and Q don't like each other but have to share an office till T gets a promotion and moves to the big office next to the garden. R, who is currently sharing an office with T wants to move to the adjacent office with S, the handsome new intern. Given the floor plan, what is the current location of Q, R and T?

(O = Office, WR = Washroom)

WR	$O_1$	O <sub>2</sub>	O <sub>3</sub>	$O_4$	(b)	WR	O <sub>1</sub>	O <sub>2</sub>	O <sub>3</sub>	O <sub>4</sub>
	P, Q		<b>R</b> , T	S	-		<b>P</b> , <b>Q</b>		Т	<b>R</b> , S
Mana	ger		Teller	Teller		Mana	ger	]	Teller	Teller
		Entry	1	2				Entry	1	2
Garde	'n			•		Garde	n	•	•	
W/D	0,	0.	0,	0,	] (c)	WD	0,	0.	0,	0,
WR	$\mathbf{O}_1$ $\mathbf{P}$	$egin{array}{c} O_2 \\ m{Q} \end{array}$	O <sub>3</sub> <b>R</b>	$egin{array}{c} \mathbf{O}_4 \\ \mathbf{S} \end{array}$	) (c)	WR	O <sub>1</sub> <b>P</b> , <b>Q</b>	O <sub>2</sub>	O <sub>3</sub> <b>R</b>	$egin{array}{c} \mathbf{O}_4 \\ \mathbf{S} \end{array}$
WR	O <sub>1</sub> <b>P</b>	$\mathbf{Q}^2$	O <sub>3</sub> <b>R</b>	O <sub>4</sub> S	(c)	WR	O <sub>1</sub> <b>P</b> , <b>Q</b>	O <sub>2</sub>	O <sub>3</sub> <b>R</b>	O <sub>4</sub> S
WR Mana	O <sub>1</sub> P	O <sub>2</sub> <b>Q</b>	O <sub>3</sub> <b>R</b> Teller	O <sub>4</sub> S Teller 2	(c)	WR Manaj	O <sub>1</sub> P, Q	0 <sub>2</sub>	O <sub>3</sub> <b>R</b> Teller	O <sub>4</sub> S Teller
WR	O <sub>1</sub> P	O <sub>2</sub> Q Entry	O <sub>3</sub> <b>R</b> Teller 1	O <sub>4</sub> S Teller 2	(c)	WR Mana, T	O <sub>1</sub> P,Q	O <sub>2</sub> Entry	O <sub>3</sub> <b>R</b> Teller 1	O <sub>4</sub> S Teller 2

ACE Engineering Publications Hyderabad + Delhi + Bhopal + Pune + Bhubaneswar + Lucknow + Patna + Bengaluru + Chennai + Vijayawada + Vizag + Tirupati + Kolkata + Ahmedabad

	<b>EXACTE</b> Engineering Publications		5	GATE-19 EXAM PAF			
06.	Ans: (a)						
Sol:	Before getting promotion 'T' sharing with R and P and Q's are working together means they are in same office.						
	Option '2' is not correct due to T is sharing with R (i.e.) before getting promotion T is not worked alone.						
	Option '3' is not correct due to 'T' place of work is not defined.						
	Option '4' is also	not correct due to aft	er 'T' getting promotion	P and Q is are not working together.			
			End of Solution				
07.	Four people are st	anding in a line facin	g you. They are Rahul, M	lathew, Seema and Lohit. One is an engineer, o			
	is a doctor, one a t	eacher and another a	dancer. You are told that				
	1. Mathew is not s	standing next to Seen	na				
	2. There are two p	eople standing betwe	en Lohit and the enginee	r			
	3. Rahul is not a d	octor	C C				
	4. The teacher and	I the dancer are stand	ing next to each other				
	5. Seema is turnin	g to her right to spea	k to the doctor standing r	lext to her			
	Who among them	is an engineer?					
	(a) Mathew	(b) Rahul					
	(c) Seema	(d) Lohit					
07.	Ans: (a)						
Sol:	Four peoples are l	Rahu, Mathew, Seen	a and Lohit and in the g	roup one engineer, one is a doctor, one a teac			
	and another a dan	cer.					
	Statement 1:						
	Seema Mathew						
	Statement 2:						
	Lohit		_				
		En	gineer				
	Statement 3:						
	Rahul $\neq$ doctor						
	Statement 4:						
	Teacher (or) Danc	er Dancer (or) Teacl	<u>ner</u>				
	Statement 5:						
	Seema						
	Doctor						
	From above condi	tions, the following	line can be formed				
	Lohit	Seema	Rahul	Mathew			
	$\downarrow$	$\downarrow$	$\downarrow$	$\downarrow$			
	Doctor	Teacher/Dancer	Teacher/Dancer	Engineer			
	From above, an er	ngineer in the group i	s Mathew.	-			
	Hence option '1' i	s correct.					

6

08. The bar graph in Panel(a) shows the propagation of male and female illiterates in 2001 and 2011. The proportions of males and females in 2001 and 2011 are given in Panel(b) and (c), respectively. The total population did not change during this period.

The percentage increase in the total number of literates from 2001 to 2011 is \_\_\_\_\_.



#### 08. Ans: (b)

(a) 35.43

Sol: Panel (a), Bar diagram represents, proportion of illiterates (%) dark shaded represents female and male illiterates in 2001 and light shaded represents female and male illiterates in 2011. Panel (b) and panel (c) male and females in 2001 and 2011 respectively.

Assume population in 2001 = 100 nos

from given data, population in 2011 also 100.

From the given Bar charts and pie charts, the following table can be possible.

	20	01	2011		
	Males	Females	Males	Females	
Total	60	40	50	50	
Illiterates	50% of 60 = 30	60% of 40 = 24	40% of 50 = 20	40% of 50 = 20	
Literates	60 - 30 = 30	40 - 24 = 16	50 - 20 = 30	50 - 20 = 30	

Total literates in 2001 = 30 + 16 = 46

Total literates in 2011 = 30 + 30 = 60

: The percentage increase in the total number of literates from 2001 to  $2011 = \frac{60-46}{46} \times 100$ 

$$= \frac{14}{60} \times 100 = 30.43\%$$

#### )

09. "Indian history was written by British historians – extremely well documented and researched, but not always impartial. History had to serve its purpose: Everything was made subservient to the glory of the Union Jack. Latter-day Indian scholars presented a contrary picture."

7

From the text above, we can infer that:

Indian history written by British historians \_\_\_\_

- (a) was not well documented and researched and was always biased
- (b) was well documented and not researched but was always biased
- (c) was well documented and researched but was sometimes biased
- (d) was not well documented and researched and was sometimes biased

#### 09. Ans: (c)

**Sol:** Other choices are irrelevant

#### **End of Solution**

10. Two design consultants, P and Q, started working from 8 Am for a client. The client budgeted a total of USD 3000 for the consultants. P stopped working when the hour hand moved by 210 degrees on the clock. Q stopped working when the hour hand moved by 240 degrees. P took two tea breaks of 15 minutes each during her shift, but took no lunch break. Q took only one lunch break for 20 minutes, but no tea breaks. The market rate for consultants is USD 200 per hour and breaks are not paid. After paying the consultants, the client shall have USD remaining in the budget.

\_\_\_\_ remaining in the t

- (a) 000.00
- (b) 166.67

(c) 300.00

(d) 433.33

#### 10. Ans: (b)

**Sol:** P and Q started work at 8 am

P makes an angle of 210° Q makes an angle of 240°

hours hand makes an angle of 30° for each hours (i.e.)  $\frac{360^{\circ}}{12} = 30^{\circ}$ 

 $P \rightarrow 210^{\circ} \text{ and } Q \rightarrow 240^{\circ}$ 

Tea break time of  $P = 15 \min \times 2 = 30 \min$ 

Lunch break time of Q = 20 min

P's working hours including breaks =  $\frac{210}{30}$  = 7 hours

Q's working hours including breaks =  $\frac{240}{30}$  = 8 hours

P's net working hours (excluding breaks) = 7 hrs - 30 min = 6 hrs 30 min

O's net working hours (excluding breaks) = 8 hrs - 20 min = 7 hrs 40 min

P's and Q's total working hours = 6 hrs 30 min + 7 hrs 40 min = 14 hrs 10 min

Total amount payed to consultants =  $14 \text{ hrs} \times 200 + \frac{10}{60} \times 200 = 2800 + 33.34 = 2833.33$ 

The remaining amount with client from the budget = 3000 - 2833.33 = 166.67 USD

Electronics & Communication Engineering

#### Section : Electronics & Communication Engineering

8

01. For an LTI system, the Bode plot for its gain is as illustrated in the figure shown. The number of system poles  $N_p$  and the number of system zeros  $N_z$  in the frequency range 1 Hz  $\leq f \leq 10^7$  Hz is



Sol:

ACE Engineering Publications





9

At f = 10Hz  $\rightarrow$  1pole (- 20 dB/dec) f = 10<sup>2</sup> Hz  $\rightarrow$  (-40 dB/dec)  $\rightarrow$  2 poles f = 10<sup>3</sup> Hz  $\rightarrow$  (+20 dB/dec)  $\rightarrow$  1 zero f = 10<sup>4</sup> Hz  $\rightarrow$  (+40 dB/dec)  $\rightarrow$  2 zeros f = 10<sup>5</sup> Hz  $\rightarrow$  (-40 dB/dec)  $\rightarrow$  2 poles f = 10<sup>6</sup> Hz  $\rightarrow$  (-20 dB/dec)  $\rightarrow$  1 pole N<sub>p</sub> = 6 , N<sub>z</sub> = 3

#### **End of Solution**

02. Let Y(s) be the unit-step response of a causal system having a transfer function  $G(s) = \frac{3-s}{(s+1)(s+3)}$ 

that is,  $Y(s) = \frac{G(s)}{s}$ . The forced response of the system is (a) u(t) (b) 2u(t) (c) 2u(t) - 2e<sup>-t</sup> u(t) + e<sup>-3t</sup> u(t) (d) u(t) - 2e<sup>-t</sup> u(t) + e<sup>-3t</sup> u(t) **02.** Ans: (a) Sol:  $Y(s) \rightarrow$  Unit step response of a causal system

$$Y(s) = \frac{G(s)}{s} = \frac{3-s}{(s+1)(s+3)s}$$
  
$$\downarrow_{ILT} = \frac{-2}{s+1} + \frac{1}{s+3} + \frac{1}{s}$$
  
$$y(t) = -2 e^{-t} u(t) + e^{-3t} u(t) + u(t).$$
 So, the forced response of the system is u(t)  
End of Solution

03. Let H(z) be the z-transform of a real-valued discrete-time signal h[n]. If P(z) = H(z) H( $\frac{1}{z}$ ) has a zero at  $z = \frac{1}{2} + \frac{1}{2}j$ , and P(z) has a total of four zeros, which one of the following plots represents all the zeros correctly?







#### 03. Ans: (a)

**Sol:** H(z) is Z-transform of real valued discrete time signal h(n)

If H(z) has a zero at  $z_1 = \frac{1}{2} + \frac{j}{2}$ The remaining zeros are  $z_2 = z_1^* = \frac{1}{2} - \frac{j}{2}$  $z_3 = \frac{1}{z_1} = 1 - j$  $z_4 = \left(\frac{1}{z_1}\right)^* = 1 + j$ 

The pole zero plot is



**End of Solution** 

04. The correct circuit representation of the structure shown in the figure is

12



#### 04. Ans: (a)

**Sol:** As per the fabrication structure given BJT is npn transistor with base to collector of nn<sup>+</sup> material means act as P-N diode from base to collector i.e at base usually 'n' material acts as p-type with respect to n<sup>++</sup> and n<sup>++</sup> act as n-type material with respect to n-material

#### **End of Solution**

ACE Engineering Publications Hyderabad + Delhi + Bhopal + Pune + Bhubaneswar + Lucknow + Patna + Bengaluru + Chennai + Vijayawada + Vizag + Tirupati + Kolkata + Ahmedabad

#### To WIN The RACE... Join ACE...





# SUMMER SHORT TERM BATCHES

GATE+PSUs - 2020

## HYDERABAD

29<sup>th</sup> April | 06<sup>th</sup> May | 11<sup>th</sup> May 18<sup>th</sup> May | 26<sup>th</sup> May | 02<sup>nd</sup> June 2019

## **ADMISSIONS ARE OPEN**

EARLY BIRD OFFER : Register on or Before 31" March 2019 : 3000/- Off

Electronics & Communication Engineering

05. The families of curves represented by the solution of the equation  $\frac{dy}{dx} = -\left(\frac{x}{y}\right)^n$ For n = -1 and n = +1, respectively, are

- (a) Circles and Hyperbolas
- (b) Parabolas and Circles
- (c) Hyperbolas and Circles
- (d) Hyperbolas and Parabolas
- 05. Ans: (c)

**Sol:** Given  $\frac{dy}{dx} = -\left(\frac{x}{y}\right)^n$ 

ACE

 $\Rightarrow$  y<sup>n</sup> dy +x<sup>n</sup> dx = 0 ( use variable separable method)

By Integrating  $\frac{y^{n+1}}{n+1} + \frac{x^{n+1}}{n+1} = \frac{c^{n+1}}{n+1}$  For  $(n \neq -1)$ 

 $\Rightarrow$  y<sup>n+1</sup> + x<sup>n+1</sup> = c<sup>n+1</sup>

**Clearly for n = 1**  $x^2 + y^2 = c^2 \Rightarrow$  circle

For  $\mathbf{n} = -1$   $\frac{dy}{dx} = -\left(\frac{x}{y}\right)^{-1} = -\frac{y}{x}$ 

$$\Rightarrow x \, dy + y \, dx = 0$$

$$\Rightarrow d(xy) = 0$$

By Integrating  $\rightarrow xy = c \rightarrow Hyperbola$ 

#### **End of Solution**

14

06. The baseband signal m(t) shown in the figure is phase-modulated to generate the PM signal  $\phi(t) = \cos(2\pi f_c t + k m(t))$ . The time t on the x-axis in the figure is in milliseconds. If the carrier frequency is  $f_c = 50$  kHz and  $k = 10\pi$ , then the ratio of the minimum instantaneous frequency (in kHz) to the maximum instantaneous frequency (in kHz) is (rounded off to 2 decimal places).





15

#### 06. Ans: 0.75

Sol:  $f_i = f_c + \frac{k}{2\pi} \frac{d}{dt} m(t)$   $f_{max} = f_c + \frac{k}{2\pi} \frac{d}{dt} m(t)_{max}$   $f_{min} = f_c + \frac{k}{2\pi} \frac{d}{dt} m(t)_{min}$ given  $f_c = 50 \text{ kHz}, \text{ } \text{k} = 10\pi \Rightarrow \frac{k}{2\pi} = 5$   $\frac{dm(t)}{dt}\Big|_{min} = -1 \text{k}, \frac{dm(t)}{dt}\Big|_{max} = 2 \text{k}$  $\frac{f_{min}}{f_{max}} = \frac{50 \text{k} + 5 \text{k}}{50 \text{k} + 10 \text{k}} = \frac{45 \text{k}}{60 \text{k}} = 0.75$ 

#### **End of Solution**

07. he figure shows the high-frequency C-V curve of a MOS capacitor (at T = 300K) with  $\Phi_{ms} = 0$  V and no oxide charges. The flat-band, inversion, and accumulation conditions are represented, respectively, by the points



- (..) **(**, -., -
- (b) Q, P, R
- (c) R, P, Q
- (d) P, Q, R

#### 07. Ans: (a)

Sol: Given C-V characteristics of MOS capacitor with p-type substrate for high frequencies.

Point-P possible in accumulation mode

- Point-Q possible in flat band mode
- Point-R possible in inversion mode
- So, option (1) is correct

### ACE

16

08. The value of the integral  $\int_0^{\pi} \int_y^{\pi} \frac{\sin x}{x} dx dy$ , is equal to \_\_\_\_\_.

#### 08. Ans: 2

Sol: 
$$\int_{y=0}^{\pi} \left[ \int_{x=y}^{\pi} \frac{\sin x}{x} dx \right] dy$$
  
Change the order of integration, then  
x: 0 to  $\pi$   
y: 0 to x  
$$\int_{x=0}^{\pi} \left[ \int_{y=0}^{y=x} \frac{\sin x}{x} dy \right] dx$$
$$= \int_{x=0}^{\pi} \frac{\sin x}{x} dx = -\cos x \mid_{0}^{\pi}$$
$$= -(-1-1)$$
$$= 2$$



**End of Solution** 

09. The number of distinct eigenvalues of the matrix 
$$A = \begin{bmatrix} 2 & 2 & 3 & 3 \\ 0 & 1 & 1 & 1 \\ 0 & 0 & 3 & 3 \\ 0 & 0 & 0 & 2 \end{bmatrix}$$
 is equal to \_\_\_\_\_.

#### 09. Ans: 3

Ans: 3 Given that A =  $\begin{bmatrix} 2 & 2 & 3 & 3 \\ 0 & 1 & 1 & 1 \\ 0 & 0 & 3 & 3 \\ 0 & 0 & 0 & 2 \end{bmatrix}$ Sol:

> The given matrix is an upper triangular matrix. It's eigen values are Just diagonal elements only.

- $\therefore$  Eigen values are 2, 1, 3, 2
- $\therefore$  Number of distinct eigen values = 3

#### **End of Solution**

- 10. A standard CMOS inverter is designed with equal rise and fall times ( $\beta_n = \beta_n$ ). If the width of the pMOS transistor in the inverter is increased. What would be the effect on the LOW noise margin (N M<sub>1</sub>) and the HIGH noise marging N  $M_{H}$ ?
  - (a) No change in the noise margins.
  - (b) N  $M_{\rm L}$  decreases and N  $M_{\rm H}$  increases.
  - (c) N  $M_{\rm L}$  increases and N  $M_{\rm H}$  decreases.
  - (d) Both N  $M_{\rm L}$  and N  $M_{\rm H}$  increase.

ACE Engineering Publications Hyderabad + Delhi + Bhopal + Pune + Bhubaneswar + Lucknow + Patna + Bengaluru + Chennai + Vijayawada + Vizag + Tirupati + Kolkata + Ahmedabad



The behavior of the CMOS inverter for static conditions of operation is described by the voltage transfer characteristics (VTC) and for dynamic operation condition is described by the time response during switching conditions.

$$\begin{split} V_{OH} &= V_{DD} \\ V_{IL} &= \frac{2V_o \cdot |V_{Top}| \cdot V_{DD} + k_r V_{Ton}}{1 + k_r} \\ V_o &= V_{in} \cdot V_{Top} + \sqrt{(V_{in} \cdot V_{DD} - V_{Top})^2 + k_r (V_{in} \cdot V_{top})^2} \\ k_r &= \frac{\beta_n}{\beta_p} = \frac{\mu_n c_{ox} \left(\frac{W}{L}\right)_n}{\mu_p c_{ox} \left(\frac{W}{L}\right)_p} \\ V_{IH} &= \frac{V_{DD} + V_{Top} + k_r (2V_o + V_{Top})}{1 + k_r} \\ V_o &= V_{in} \cdot V_{Ton} + \sqrt{(V_{in} \cdot V_{Ton})^2 + \frac{1}{k_r} [V_{in} \cdot V_{DD} - V_{Top}]^2} \\ V_{OL} &= 0 \\ NM_L &= V_{IL} \cdot V_{OL} \\ NM_H &= V_{OH} \cdot V_{IH} \\ \therefore W_p \uparrow \rightarrow NM_L \uparrow \\ W_n \uparrow \rightarrow NM_H \downarrow \end{split}$$

#### **End of Solution**

11. In the circuit shown,  $V_s$  is a square wave of period T with maximum and minimum values of 8 V and -10V, respectively. Assume that the diode is ideal and  $R_1 = R_2 = 50\Omega$ .

The average value of  $V_L$  is \_\_\_\_\_ volts (rounded off to 1 decimal place).





(18)

#### 11. Ans: -3

#### Sol:



 $\frac{T}{2} < t < T$ 



So, output waveform is



#### **End of Solution**

12. The value of the contour integral  $\frac{1}{2\pi j} \oint \left(z + \frac{1}{z}\right)^2 dz$  evaluated over the unit circle |z| = 1 is \_\_\_\_\_\_. **12.** Ans: 0

Sol: Given  $\frac{1}{2\pi J} \oint_{C} \left(z + \frac{1}{z}\right)^2 dz$  C is |z| = 1 $\oint_{C} \left(z + \frac{1}{z}\right)^2 dz = \oint_{C} \frac{(z^2 + 1)^2}{z^2} dz$ 

(19

z = 0 is singular point lies inside of the curve C, |z| = 1By Cauchy's Integral formula

$$\oint_{C} \frac{(z^2+1)^2}{z^{1+1}} = \frac{1}{2\pi J} \frac{f^{1}(z)}{1!} \bigg|_{at\,z=0}$$

Here  $f(z) = (z^2 + 1)^2$ 

$$f^{1}(z) = 2(z^{2} + 1) 2z \Longrightarrow f^{1}(0) = 0$$
  
:  $\frac{1}{2\pi J} \oint_{C} \frac{(z^{2} + 1)^{2}}{z^{2}} dz = \frac{1}{2\pi J} \times 0 = 0$ 

#### **End of Solution**

- 13. Consider the signal  $f(t) = 1 + 2\cos(\pi t) + 3\sin(\frac{2\pi t}{3}) + 4\cos(\frac{\pi}{2}t + \frac{\pi}{4})$ , where t is in seconds. Its fundamental time period, in seconds, is \_\_\_\_\_.
- 13. Ans: 12

Sol: 
$$f(t) = 1 + 2\cos(\pi t) + 3\sin\left(\frac{2\pi}{3}t\right) + 4\cos\left(\frac{\pi}{2}t + \frac{\pi}{4}\right)$$
$$\omega_0 = GCD\left(\pi, \frac{2\pi}{3}, \frac{\pi}{2}\right)$$
$$= GCD\left(\frac{6\pi}{6}, \frac{4\pi}{6}, \frac{3\pi}{6}\right)$$
$$= \frac{\pi}{6}$$

Time period T =  $\frac{2\pi}{\omega_0}$  = 12secs

Alternate method

(i) 
$$\omega_1 = \pi$$
  $\omega_2 = \frac{2\pi}{3}$   $\omega_3 = \frac{\pi}{2}$   
 $\frac{2\pi}{T_1} = \pi \Rightarrow T_1 = 2$   $\frac{2\pi}{T_2} = \frac{2\pi}{3} \Rightarrow T_2 = 3$   $\frac{2\pi}{T_3} = \frac{\pi}{2} \Rightarrow T_3 = 4$   
(ii)  $\frac{T_1}{T_2} = \frac{2}{3}$   
 $\frac{T_1}{T_3} = \frac{2}{4} = \frac{1}{2}$ 

(iii) L.C.M of denominators of step (ii)

$$=$$
 L.C.M (3, 2)  $=$  6

(iv)  $T = (L. C. M) T_1 = (2) (6) = 12 \text{ secs}$ 

(20)

Electronics & Communication Engineering

14. Let Z be an exponential random variable with mean 1. That is, the cumulative distribution function of Z is given by

$$F_{z}(x) = \begin{cases} 1 - e^{-x} & \text{if } x \ge 0 \\ 0 & \text{if } x < 0 \end{cases}$$

Then Pr(Z > 2 | Z > 1), rounded off to two decimal places, is equal to \_\_\_\_\_.

#### 14. Ans: 0.3679

Sol: Given that Z is exponential distribution with cumulative function  $F_z(x) = 1 - e^{-x}$   $x \ge 0$ 

0 x < 0

We know that probability density function

$$f_{z}(x) = F'_{z}(x) = e^{-x} \quad x \ge 0$$
  

$$0 \quad x < 0$$
  

$$P(z > 2/z > 1) = \frac{P((z \ge 2) \cap (z \ge 1))}{P(z \ge 1)}$$
  

$$= \frac{\int_{1}^{\infty} e^{-x} dx}{\int_{1}^{\infty} e^{-x} dx}$$
  

$$= \frac{(-e^{-x})_{2}^{\infty}}{(-e^{-x})_{1}^{\infty}}$$
  

$$= \frac{-(e^{-\infty} - e^{-2})}{-(e^{-\infty} - e^{-1})} = \frac{e^{-2}}{e^{-1}}$$
  

$$= e^{-1}$$
  

$$= 0.3679$$

#### **End of Solution**

15. In the circuit shown, what are the values of F for EN = 0 and EN = 1, respectively?



# GATE-19 EXAM PAP

#### 15. Ans: (a)

- **Sol:** Case-1: When enable = 0, both MOSFETs are off, hence F = Hi-Z
  - Case-2: When enable = 1, inputs of both MOSFETs is  $\overline{D}$  i.e.,
  - $\rightarrow$  If D = 0 is  $\Rightarrow$  n-channel MOSFET is on, p-channel MOSFET is off so F = 0,
  - $\rightarrow$  If D = 1  $\Rightarrow$  PMOS-on, NMOS-off. thus, F = V<sub>DD</sub> = logic 1

i.e, when  $E = 1 \Rightarrow F = D$ 

#### **End of Solution**

In the circuit shown, the clock frequency, i.e., the frequency of the CLK signal, is 12 kHz. The frequency of the signal at Q<sub>2</sub> is \_\_\_\_\_ kHz.



#### 16. Ans: 4

**Sol:** Given  $D_1 = \overline{Q}_1 \overline{Q}_2$ ,  $D_2 = Q_1$ 

CLK	Present state		Flipflops inputs		Next state	
	Q <sub>1</sub>	Q <sub>2</sub>	D <sub>1</sub>	D <sub>2</sub>	Q <sub>1</sub>	Q <sub>2</sub>
	0	0	1	0	1	0
	1	0	0	1	0	1
	0	1	0	0	0	0

So, the circuit counts 00,10,01,.....

Hence, the frequency at  $Q_2$  is  $\frac{f_{CLK}}{3} = \frac{12}{3} = 4kHz$ 

#### **End of Solution**

17. What is the electric flux  $(\int \vec{E}.d\hat{a})$  through a quarter-cylinder of height H (as shown in the figure) due to an infinitely long line charge along the axis of the cylinder with a charge density of Q?





(22)

#### 17. Ans: (b)

Sol: Electric flux  $= \int_{S} \vec{E}.d\vec{a}$ we know electric field due to line charge  $\vec{E} = \frac{\rho_{L}}{2\pi\epsilon_{0}\rho}\hat{a}_{\rho}$ Given  $\rho_{L} = Q$   $\vec{E} = \frac{Q}{2\pi\epsilon_{0}\rho}\hat{a}_{\rho}$ So  $\int_{S} \vec{E}.d\vec{a} = \int_{S} \frac{Q}{2\pi\epsilon_{0}\rho}\hat{a}_{\rho}.d\vec{a}$   $= \frac{Q}{2\pi\epsilon_{0}\rho}\int_{S} da$   $= \frac{Q}{2\pi\epsilon_{0}\rho}$  (surface area of the given portion)  $\int_{S} \vec{E}.d\vec{a} = \frac{Q}{2\pi\epsilon_{0}\rho} \left(\frac{2\pi\rho H}{4}\right)$  $= \frac{QH}{4\epsilon_{0}}.$ 

18. Which one of the following functions is analytic over the entire complex plane?

(a) 
$$e^{1/z}$$
 (b)  $\ln(z)$   
(c)  $\frac{1}{1-z}$  (d)  $\cos(z)$ 

#### 18. Ans: (d)

**Sol:** (a)  $e^{1/z}$  is NOT analytic at z = 0

(b)  $\ell$ nz is NOT analytic in Domain D = {z / x \le 0, y = 0}

(c) 
$$\frac{1}{1-z}$$
 is NOT analytic at  $z = 1$ 

 $\therefore$  cosz is analytic every where in the complex plane.

#### **End of Solution**

- 19. A linear Hamming code is used to map 4-bit messages to 7-bit codewords. The encoder mapping is linear. If the message 0001 is mapped to the codeword 0000111, and the message 0011 is mapped to the codeword 1100110, then the message 0010 is mapped to
  - (a) 1100001
  - (b) 1111000
  - (c) 0010011
  - (d) 1111111

#### **19.** Ans: (a)

Sol: A code is said to be linear if the algebraec sum of two codes is also another code

 $0001 \rightarrow 0000111$   $0011 \rightarrow 1100110$   $0010 \quad 1100001$ So, 0010 is mapped into 1100001



Starts from **30<sup>th</sup> March 2019.** Test Series will be conducted at all our centres

# APPSC-AEE (Prelims) Online Test Series

# No. of Tests : 18

Topic Wise Tests : 15 | Mock Tests - 3 Civil | Mechanical | Electrical

## **Available Now**

All Tests will be available till 18<sup>th</sup> February 2019

🕓 040 - 48539866 / 040 - 40136222 🛛 🗳 tes

testseries@aceenggacademy.com

(24

20 In the table shown, List-I and List II, respectively, contain terms appearing on the left-hand side and the right-hand side of Maxwell's equations (in their standard form). Match the left-hand side with the corresponding right-hand side.

List I		List I	Ι	
1	∇ . D	Р	0	
2	$\nabla \times E$	Q	ρ	
3	∇.B	R	$-\frac{\partial \mathbf{B}}{\partial t}$	
4	$\nabla  imes H$	S	$J + \frac{\partial D}{\partial t}$	
(a) $1 - Q$ , $2 - I$ (c) $1 - P$ , $2 - R$	$\begin{array}{c} R, 3 - P, 4 - S \\ R, 3 - Q, 4 - S \end{array}$	(b) 1 (d) 1	-Q, 2-S, 3-I -R, 2-Q, 3-S	P, 4 – R 8, 4 – P

#### 20. Ans: (a)

ACE

**Sol:** 1.  $\nabla . \vec{D} = \rho$  (Q)  $\rightarrow$  Gauss's Law

- 2.  $\nabla \times \vec{E} = \frac{-\partial \vec{B}}{\partial t}$  (R)  $\rightarrow$  Faraday's Law
- 3.  $\nabla . \vec{B} = 0$  (P)  $\rightarrow$  Gauss's Law for magnetic fields
- 4.  $\nabla \times \vec{H} = J + \frac{\partial \vec{D}}{\partial t}$  (S)  $\rightarrow$  Ampere's Law

#### **End of Solution**

21. Consider the two-port resistive network shown in the figure. When an excitation of 5 V is applied across Port 1, and Port 2 is shorted, the current through the short circuit at Port 2 is measured to be 1 A (sec(a) in the figure). Now, if an excitation of 5 V is applied across Port 2, and Port 1 is shorted (sec(b) in the figure). What is the current through the short circuit at Port 1?



ACE	(25)	GATE-19 EXAM PAPER
Engineering Publications		

#### 21. Ans: (a)

**Sol:** This is direct application of <u>reciprocity theorem</u> - which states, in any linear passive bilateral network excited by a single source. The ratio of response to excitation remains constant even if the position of <u>source</u> and <u>Load</u> are <u>interchanged</u>.





So, answer is 1 Amp

#### **End of Solution**

22. Radiation resistance of a small dipole current element of length  $\ell$  at a frequency of 3 GHz is 3 ohms. If the length is changed by 1%, then the percentage change in the radiation resistance, rounded off to two decimal places, is  $\frac{9}{6}$ 

#### 22. Ans: 2

**Sol:** Given f = 3GHz

$$\begin{split} R_{rad} &= 3\Omega \\ \frac{\Delta \ell}{\ell} \times 100 = 1 \\ \frac{\Delta R}{R} \times 100 = ? \\ R_{rad} &= 80\pi^2 \left(\frac{\ell}{\lambda}\right)^2 \\ R_{rad} &\alpha \, \ell^2 \\ \frac{\Delta R_{rad}}{R_{rad}} \times 100 = 2\frac{\Delta \ell}{\ell} \times 100 \\ &= 2(1) \\ \frac{\Delta R_{rad}}{R_{rad}} \times 100 = 2\% \end{split}$$

26

Electronics & Communication Engineering

23. Which one of the following options describes correctly the equilibrium band diagram at T = 300 K of a Silicon pnn <sup>+</sup>p<sup>++</sup> configuration shown in the figure?



27

#### 23. Ans: (c)

- **Sol:**  $\rightarrow$  The device is not biased hence fermi level should be constant.
  - $\rightarrow$  In P type fermi level should be closer to Ev.
  - $\rightarrow$  In N type fermi level should be closer to Ec.
  - $\rightarrow$  In P<sup>++</sup> fermi level penetrates into valence band.

#### **End of Solution**

24. In the circuit shown, A and B are the inputs and F is the output. What is the functionality of the circuit?





Electronics & Communication Engineering

А	В	N <sub>1</sub>	N <sub>2</sub>	P <sub>1</sub>	P <sub>2</sub>	F(Output)
0	0	OFF	OFF	ON	ON	1
1	0	ON	OFF	OFF	ON	0
0	1	OFF	ON	ON	OFF	0
1	1	ON	ON	OFF	OFF	1

: Given diagram is XNOR.

#### **End of Solution**

28

25. If X and Y are random variables such that E[2X+Y] = 0 and E[X+2Y] = 33, then E[X] + E[Y] =\_\_\_\_\_.

#### 25. Ans: 11

Sol: Given X,Y are Random variables

E(2X + Y) = 0 and E(X+2Y) = 33  $\Rightarrow 2E(X) + E(Y) = 0$ .....(1)  $\Rightarrow E(X) + 2 E(Y) = 33$ .....(2) By solving (1) and (2) E(Y) = 22 E(X) = -11 $\therefore E(X) + E(Y) = 22 - 11 = 11$ 

#### **End of Solution**

26. The dispersion equation of a waveguide, which relates the wavenumber k to the frequency  $\omega$ , is  $k(\omega) = (1/c)\sqrt{\omega^2 - \omega_0^2}$ 

where the speed of light  $c = 3 \times 10^8$  m/s, and  $\omega_0$  is a constant. If the group velocity is  $2 \times 10^8$  m/s, then the phase velocity is

- (a)  $2 \times 10^8 \,\text{m/s}$
- (b)  $4.5 \times 10^8 \,\mathrm{m/s}$
- (c)  $3 \times 10^8 \,\text{m/s}$
- (d)  $1.5 \times 10^8 \,\mathrm{m/s}$

#### 26. Ans: (b)

Sol: Given

wave number 
$$\beta = k(\omega) = \frac{1}{c}\sqrt{\omega^2 - \omega_0^2}$$

Group velocity ( $v_g$ ) = 2 ×10<sup>8</sup> m/s

Phase velocity  $(v_p) = \frac{\omega}{\beta}$ 

$$\mathbf{v}_{\mathrm{P}} = \frac{\boldsymbol{\omega} \mathbf{c}}{\sqrt{\boldsymbol{\omega}^2 - \boldsymbol{\omega}_0^2}}$$

we know

$$v_{g} = \frac{d\omega}{d\beta} = \frac{1}{\left(\frac{d\beta}{d\omega}\right)}$$
$$\beta = \frac{1}{c}\sqrt{\omega^{2} - \omega_{0}^{2}}$$

ACE Engineering Publications Hyderabad + Delhi + Bhopal + Pune + Bhubaneswar + Lucknow + Patna + Bengaluru + Chennai + Vijayawada + Vizag + Tirupati + Kolkata + Ahmedabad





29

$$\begin{aligned} \frac{d\beta}{d\omega} &= \frac{1}{c} \frac{1}{2\sqrt{\omega^2 - \omega_0^2}} 2\omega \\ \frac{d\beta}{d\omega} &= \frac{\omega}{c\sqrt{\omega^2 - \omega_0^2}} \\ \frac{1}{v_g} &= \frac{\omega}{c\sqrt{\omega^2 - \omega_0^2}} \\ \sqrt{\omega^2 - \omega_0^2} &= \frac{\omega v_g}{c} \\ &= \frac{\omega.2 \times 10^8}{3 \times 10^8} \\ \sqrt{\omega^2 - \omega_0^2} &= \frac{2\omega}{3} \end{aligned}$$
 so,  $v_p &= \frac{\omega c}{\sqrt{\omega^2 - \omega_0^2}} = \frac{\omega c}{\frac{2\omega}{3}} \\ v_p &= \frac{3}{2}c = \frac{3}{2}(3 \times 10^8) = 4.5 \times 10^8 \text{ m/s.} \end{aligned}$  (or)  
we know the relation  
 $v_p v_g = c^2 \\ v_p &= \frac{c^2}{v_g} \\ v_p &= \frac{(3 \times 10^8)^2}{2 \times 10^8} \end{aligned}$ 

 $v_p = 4.5 \times 10^8$  m/s.

#### **End of Solution**

27. It is desired to find three-tap causal filter which gives zero signal as an output to an input of the form  $x(n) = c_1 \exp\left(-\frac{j\pi n}{2}\right) + c_2 \exp\left(\frac{j\pi n}{2}\right)$ 

Where  $c_1$  and  $c_2$  are arbitrary real numbers. The desired three-tap filter is given by

$$h[0] = 1, h[1] = a, h[2] = b$$

And

h[n] = 0 for n < 0 or n > 2.

What are the values of the filter taps a and b if the output is y[n] = 0 for all n, when x[n] is as given above?

$$\xrightarrow{x[n]} \xrightarrow{n=0} y[n]=0$$

$$\xrightarrow{h[n]=\{1,a,b\}}$$

(a) $a = 1, b = 1$	(b) $a = -1, b = 1$
(c) $a = 0, b = 1$	(d) $a = 0, b = -1$

( 30

#### 27. Ans: (c)

Sol: Given 
$$x(n) = c_1 \exp\left(-\frac{j\pi n}{2}\right) + c_2 \exp\left(\frac{j\pi n}{2}\right)$$
  
and  $h(0) = 1$ ;  $h(1) = a$ ;  $h(2) = b$   
 $H(e^{j\omega}) = 1 + ae^{-j\omega} + be^{-j2\omega}$   
Given that  $y(n) = 0$  for all n  
From the given options by trail & errors of we make  $a = 0$  &  $b = 1$   
Due to  $c_1 e^{-\frac{j\pi n}{2}} \Rightarrow$  output  $= 1 + 0.e^{+\frac{j\pi}{2}} + e^{-j2\left(-\frac{\pi}{2}\right)} = 1 - 1 = 0$   
 $c_2 e^{\frac{j\pi n}{2}} \Rightarrow$  output  $= 1 + 0.e^{-\frac{j\pi}{2}} + e^{-j2\left(\frac{\pi}{2}\right)} = 1 - 1 = 0$   
End of Solution

28. Let the state-space representation of an LTI system be  $\dot{x}(t) = A x(t) + B u(t)$ , y(t) = C x(t) + d u(t) where A,B,C are matrices, d is a scalar, u(t) is the input to the system and y(t) is its output. Let  $B = \begin{bmatrix} 0 & 0 & 1 \end{bmatrix}^T$  and d = 0. which one of the following options for A and C will ensure that the transfer function of this LTI system is  $H(s) = \frac{1}{s} \frac{1}{s}$ 

$$(a) A = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ -3 & -2 & -1 \end{bmatrix} \text{ and } C = \begin{bmatrix} 0 & 0 & 1 \end{bmatrix}$$
$$(b) A = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ -1 & -2 & -3 \end{bmatrix} \text{ and } C = \begin{bmatrix} 0 & 0 & 1 \end{bmatrix}$$
$$(c) A = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ -3 & -2 & -1 \end{bmatrix} \text{ and } C = \begin{bmatrix} 1 & 0 & 0 \end{bmatrix}$$
$$(d) A = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ -1 & -2 & -3 \end{bmatrix} \text{ and } C = \begin{bmatrix} 1 & 0 & 0 \end{bmatrix}$$

Sol: 
$$H(s) = \frac{1}{s^3 + 3s^2 + 2s + 1}$$
  
 $\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \\ \dot{x}_3 \end{bmatrix} = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ -1 & -2 & -3 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} + \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix} \begin{bmatrix} u \end{bmatrix}$   
 $\begin{bmatrix} Y \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix}$ 



۲.	ACE
The second se	Engineering Publications
	Engineering Publications

(32

29. A germanium sample of dimensions 1 cm  $\times$  1 cm is illuminated with a 20 mW, 600 nm laser light source as shown in the figure. The illuminated sample surface has a 100 nm of loss-less Silicon dioxide layer that reflects onefourth of the incident light. From germanium interface, one-third is absorbed in the germanium layer, and onethird is transmitted through the other isde of the sample. If the absorption coefficient of germanium at 600 nm is  $3 \times 10^4$  cm–1 and the bandgap is 0.66 eV, the thickness of the germanium layer, rounded off to 3 decimal places, is  $\mu$ m.



**Sol:**  $1 - e^{-\alpha x} = 0.5$  $e^{-\alpha x} = 0.5$ 

$$e = 0.3$$

$$x = \frac{-\ln(0.5)}{\alpha} = \frac{-\ln(0.5)}{3 \times 10^4} cm$$

 $= 0.231 \ \mu m$ 

#### **End of Solution**

30. In the circuit shown, the breakdown voltage and the maximum current of the Zener diode are 20 V and 60 mA. respectively. The values of  $R_1$  and  $R_L$  are 200  $\Omega$  and 1 k $\Omega$ , respectively. What is the range of  $V_i$  that will maintain the Zener diode in the 'on' state?



(a) 18 V to 24 V (b) 22 V to 34 V

(c) 24 V to 36 V

(d) 20 V to 28 V

Sol:  

$$\frac{V_{I,min} - 20}{0.2k} = \frac{20}{1k}$$

$$V_{I,min} = 24V$$

$$\frac{V_{I,max} - 20}{0.2k} = 60mA + 20mA$$

$$V_{I,max} = 36V$$

ACE Engineering Publications Hyderabad + Delhi + Bhopal + Pune + Bhubaneswar + Lucknow + Patna + Bengaluru + Chennai + Vijayawada + Vizag + Tirupati + Kolkata + Ahmedabad

33

31. Let h[n] be a length-7 discrete-time finite impulse response filter, given by

$$h[0] = 4, h[1] = 3, h[2] = 2, h[3] = 1,$$
  
 $h[-1] = -3, h[-2] = -2, h[-3] = -1,$ 

and h[n] is zero for  $|n| \ge 4$ . A length-3 finite impulse response approximation g[n] of h[n] has to be obtained such that

$$E(h,g) = \int_{-\pi}^{\pi} |H(e^{j\omega}) - G(e^{j\omega})|^2 d\omega$$

is minimized, where  $H(e^{j\omega})$  and  $G(e^{j\omega})$  are the discrete-time Fourier transforms of h[n] and g[n], respectively. For the filter that minimizes E(h, g), the value of 10g[-1] + g[1], rounded off to 2 decimal places, is \_\_\_\_\_.

#### 31. Ans: - 27

Sol: To minimize energy in the error signal, there are different approaches like, Prony's method, pade approximation. As g(n) length is three samples. Assume samples as g(-1), g(0), and g(1). We can minimize E(h, g) by making h(n) = g(n) using rectangular window & Parseval's theorem of DTFT. Based on which 10g(-1) + g(1) = 10(-3) + 3 = -27.

#### **End of Solution**

32. In the circuit shown, the threshold voltages of the pMOS ( $|V_{tp}|$ ) and nMOS ( $V_{tn}$ ) transistors are both equal to 1 V. All the transistors have the same output resistance  $r_{ds}$  of 6 M $\Omega$ . The other parameters are listed below:

$$\mu_{n} C_{ox} = 60 \mu A/V^{2}; \left(\frac{W}{L}\right)_{nMOS} = 5$$
$$\mu_{n} C_{ox} = 30 \mu A/V^{2}; \left(\frac{W}{L}\right)_{pMOS} = 10$$

 $\mu_n$  and  $\mu_p$  are the carrier mobilities, and  $C_{ox}$  is the oxide capacitance per unit area. Ignoring the effect of channel length modulation and body bias, the gain of the circuit is \_\_\_\_\_\_

(rounded off to 1 decimal place).



32. Ans: -900

Sol: 
$$I_{DC} = \frac{1}{2} \mu_P C_{OX} \left( \frac{W}{L} \right)_P (V_{SGP} - |V_{TP}|)^2 = \frac{1}{2} \times 30 \frac{\mu A}{V^2} \times 10 \times (2 - 1)^2 V^2$$
  
 $= 150 \mu A$   
 $g_{mn} = \sqrt{2I_{DC} \mu_n C_{OX} \left( \frac{W}{L} \right)_N} = \sqrt{2 \times 150 \mu A \times 60 \frac{\mu A}{V^2} \times 5}$   
 $= 300 \mu S$   
 $A_v = -g_m (r_{ds} || r_{ds}) = -300 \times 3 = -900$ 

(34

33. Consider a causal second-order system with the transfer function

$$G(s) = \frac{1}{1+2s+s^2}$$

with a unit-step  $R(s) = \frac{1}{s}$  as an input. Let C(s) be the corresponding output. The time taken by the sytem output c(t) to reach 94% of its steady-state value lim c(t), rounded off to two decimal places, is

(a) 4.50 (b) 3.89 (c) 2.81 (d) 5.25

Sol: 
$$G(s) = \frac{1}{1+2s+s^2}$$
  
 $G(s) = \frac{1}{(s+1)^2}$   
 $G(s) = \frac{1}{s(s+1)^2} = \frac{1}{s} - \frac{1}{(s+1)^2} - \frac{1}{s+1}$   
 $C(t) = (1 - te^{-t} - e^{-t})u(t)$   
 $\Rightarrow 94\%$  of ss value = 0.94  
 $0.94 = (1 - te^{-t} - e^{-t})$   
 $0.06 = e^{-t} (t+1)$   
 $\Rightarrow$  By option verification method  
Let  $t = 4.5$   
 $e^{-t} (t+1) = e^{-4.5} (1 + 4.5) = 0.06109 \approx 0.06$   
Thus option 4.5 is the Answer

#### **End of Solution**

#### 34. Consider the line integral

$$\int_{C} (xdy - ydx)$$

the integral being taken in a counterclockwise direction over the closed curve C that forms the boundary of the region R shown in the figure below. The region R is the area enclosed by the union of a  $2 \times 3$  rectangle and a semi-circle of radius 1. The line integral evaluates to





35

#### 34. Ans: (c)

Sol: By Greens theorem

$$\int_{C} \underbrace{xdy}_{N} - \underbrace{ydx}_{M} = \iint_{R} \left( \frac{\partial N}{\partial x} - \frac{\partial M}{\partial y} \right) dxdy$$
$$\Rightarrow \int_{C} \left( xdy - ydx \right) = \iint_{R} (1+1) dxdy$$
$$= \iint_{R} \int 2 dxdy$$

 $\Rightarrow \int_{C} (xdy - ydx) = 2 \times Area of the region$ 

= 2(Area of a rectangle + Area of a semi circle)

$$= 2\left[2 \times 3 + \frac{\pi(1)^2}{2}\right] = 2\left(6 + \frac{\pi}{2}\right)$$
$$= 2\frac{(12 + \pi)}{2}$$

 $= 12 + \pi$ 

**End of Solution** 

Electronics & Communication Engineering

35. The state transition diagram for the circuit shown is

ACE Engineering Publications











#### 35. Ans: (d)

Sol: 
$$Q(t + 1) = D$$
.....(1)  
 $D = \overline{(\overline{A} \ \overline{Q} + AQ)(Q)}$  .....(2)  
Substitute (2) in (1)  
 $Q(t + 1) = \overline{A}.\overline{Q}$   
So, if  $A = 0 \Rightarrow Q(t + 1) = 1$   
 $A = A \Rightarrow Q(t + 1) = \overline{Q}$   
If  $A = 0$ ,  $D = \overline{Q}.\overline{Q} = \overline{0} = 1$   
If  $A = 1$ ,  $D = \overline{QQ} = \overline{Q}$ 

ACE Engineering Publications Hyderabad + Delhi + Bhopal + Pune + Bhubaneswar + Lucknow + Patna + Bengaluru + Chennai + Vijayawada + Vizag + Tirupati + Kolkata + Ahmedabad

36

	(37)	GATE-19 EXAM PAPER
Engineering Publications		

36. In an ideal pn junction with an ideality factor of 1 at T = 300 K, the magnitude of the reverse-bias voltage required to reach 75% of its reverse saturation current, rounded off to 2 decimal places, is \_\_\_\_\_mV.

 $[k = 1.38 \times 10^{-23} \text{ JK}^{-1}, h = 6.625 \times 10^{-34} \text{ J-s}, q = 1.602 \times 10^{-19} \text{ C}]$ 

36. Ans: 35.87

Sol: 
$$I_R = 0.75 I_S$$
  
 $I_D = -0.75 I_S$   
 $I_S (e^{V_D/V_T} - 1) = -0.75 I_S$   
 $e^{V_D/V_T} = 0.25$   
 $V_D = V_T \ln(0.25)$   
 $V_R = -V_T \ln(0.25)$   
 $= -\frac{1.38 \times 10^{-23} \times 300}{1.6 \times 10^{-19}} \times -1.386$   
 $= 35.87 \text{ mV}$ 

#### **End of Solution**

37. The block diagram of a system is illustrated in the figure shown, where X(s) is the input and Y(s) is the output.

The transfer function 
$$H(s) = \frac{Y(s)}{X(s)}$$
 is  
 $X(s) + \underbrace{s}_{-} + \underbrace{1}_{s} + \underbrace{1}_{s}$ 

(a) 
$$H(s) = \frac{s+1}{s^2+s+1}$$
  
(b)  $H(s) = \frac{s^2+1}{s^3+2s^2+s+1}$   
(c)  $H(s) = \frac{s^2+1}{2s^2+1}$   
(d)  $H(s) = \frac{s^2+1}{s^3+s^2+s+1}$ 

37. Ans: (b)

Sol:



Electronics & Communication Engineering



38



38. Consider a six-point decimation-in-time Fast Fourier Transform (FFT) algorithm, for which the signal-flow graph corresponding to X[1] is shown in the figure. Let  $W_6 = \exp\left(-\frac{j2\pi}{6}\right)$ . In the figure, what should be the values of the coefficients  $a_1, a_2, a_3$  in terms of  $W_6$  so that X[1] is obtained correctly?



(a)  $a_1 = 1, a_2 = W_6 \cdot a_3 = W_6^2$ (b)  $a_1 = -1, a_2 = W_6^2, a_3 = W_6$ (c)  $a_1 = 1, a_2 = W_6^2, a_3 = W_6$ (d)  $a_1 = -1, a_2 = W_6, a_3 = W_6^2$ 

38. Ans: (a)

Sol: 
$$X(k) = \sum_{n=0}^{N-1=5} x(n) W_6^{kn}$$
  
=  $x(0) + x(1) W_6^k + x(2) W_6^{2k} + x(3) W_6^{3k} + x(4) W_6^{4k} + x(5) W_6^{5k}$ 

 $X(1) = x(0) + x(1) W_6^1 + x(2) W_6^2 + x(3) W_6^3 + x(4) W_6^4 + x(5) W_6^5$ 

39

Based on symmetry

$$W_{N}^{k+\frac{N}{2}} = -W_{N}^{k} \qquad W_{6}^{3} = -W_{6}^{0} = -1$$
$$W_{6}^{4} = -W_{6}^{1}$$
$$W_{6}^{5} = -W_{6}^{2}$$
From the SFG  
We can say  $a_{1} = 1$ 
$$a_{2} = W_{6}$$
$$a_{3} = W_{6}^{2}$$

#### **End of Solution**

39. Two identical copper wires W1 and W2, placed in parallel as shown in the figure, carry currents I and 2I, respectively, in opposite directions. If the two wires are separated by a distance of 4r, then the magnitude of the magnetic field  $\vec{B}$  between the wires at a distance r from W1 is



(a) 
$$\frac{\mu_0 I}{6\pi r}$$
  
(b)  $\frac{\mu_0^2 I^2}{2\pi r^2}$ 

(c) 
$$\frac{6\mu_0 I}{5\pi r}$$
(d) 
$$\frac{5\mu_0 I}{6\pi r}$$

#### **39.** Ans: (d)



Engineering Publications	40	Electronics & Communication Engineering
$ec{\mathbf{B}}=ec{\mathbf{B}}_1+ec{\mathbf{B}}_2$		
$\vec{\mathbf{B}}_1 = \frac{\mu_0 \mathbf{I}}{2\pi \mathbf{r}} \otimes$		
$\vec{\mathrm{B}}_2 = rac{\mu_0 2\mathrm{I}}{2\pi(3\mathrm{r})} \otimes$		
$ec{\mathbf{B}}=ec{\mathbf{B}}_1+ec{\mathbf{B}}_2$		
$\vec{\mathbf{B}} = \frac{\mu_0 \mathbf{I}}{2\pi r} \left[ 1 + \frac{2}{3} \right] \otimes$		
$ec{{f B}}={5\mu_{ m o}I\over 6\pi r}\otimes$		

#### **End of Solution**

- 40. Consider a differentiable function f(x) on the set of real numbers such that f(-1) = 0 and  $|f'(x)| \le 2$ . Given these conditions, which one of the following inequalities is necessarily true for all  $x \in [-2, 2]$ ?
  - (a)  $f(x) \le \frac{1}{2}|x+1|$  (b)  $f(x) \le \frac{1}{2}|x|$
  - (c)  $f(x) \le 2|x+1|$  (d)  $f(x) \le 2|x|$

#### 40. Ans: (c)

**Sol:** From the option (3)

if the max of f(x) = 2|x+1| then

$$f(x) = \begin{cases} 2(x+1) \text{if } x+1 \ge 0 \Rightarrow x \ge -1 \\ -2(x+1) \text{if } x+1 < 0 \Rightarrow x < -1 \end{cases}$$

 $f'(x) = \begin{cases} 2 & \text{if } x \ge -1 \\ -2 & \text{if } x < -1 \end{cases}$  $|f'(x)| \le 2 \text{ and } f(-1) = 0$ So, option (c) is correct.

#### **End of Solution**

41. Consider the homogeneous ordinary differential equation

$$x^{2} \frac{d^{2}y}{dx^{2}} - 3x \frac{dy}{dx} + 3y = 0,$$
  $x > 0$ 

with y(x) as a general solution. Given that

$$y(1) = 1$$
 and  $y(2) = 14$ 

the value of y(1.5), rounded off to two decimal places, is \_\_\_\_\_

#### 41. Ans: 5.25

Sol:  $x^2 \frac{d^2y}{dx^2} - 3x \frac{dy}{dx} + 3y = 0$ Given that y(1) = 1 y(2) = 14Put  $x = e^z$  (or)  $z = \ln x$ 

ACE Engineering Publications Hyderabad + Delhi + Bhopal + Pune + Bhubaneswar + Lucknow + Patna + Bengaluru + Chennai + Vijayawada + Vizag + Tirupati + Kolkata + Ahmedabad



41

 $\theta = \frac{d}{dz}$  ,  $xDy = \theta y$   $x^2D^2y = \theta(\theta-1)y$ 

... The given DE is equivalent to

$$\theta(\theta - 1) - 3\theta y + 3y = 0$$
  
$$\theta^2 y - 4 \theta y + 3y = 0$$
  
$$\therefore \frac{d^2 y}{dz^2} - 4\frac{dy}{dz} + 3y = 0$$

Axillary equation  $m^2 - 4m + 3 = 0$ (m - 1) (m - 3) = 0

$$\therefore m = 1, 3$$
  
The solution is  $y = C_1 e^z + C_2 e^{3z}$ 
$$\therefore y = C_1 x + C_2 x^3$$
$$y(1) = 1 \Rightarrow 1 = C_1 + C_2$$
$$y(2) = 14 \Rightarrow 14 = 2C_1 + 8C_2$$
By solving  $C_2 = 2, C_1 = -1$ 
$$\therefore y = -x + 2x^3$$
$$\therefore y(1.5) = -1.5 + 2(1.5)^3$$
$$= 5.25$$

**End of Solution** 

42. In the circuit shown,  $V_1 = 0$  and  $V_2 = V_{dd}$ . The other relevant parameters are mentioned in the figure. Ignoring the effect of channel length modulation and the body effect, the value of  $I_{out}$  is \_\_\_\_\_mA (rounded off to 1 decimal place).





#### 42. Ans: 6





#### **End of Solution**

43. The RC circuit shown below has a variable resistance R(t) given by the following expression:

 $R(t) = R_0 \left(1 - \frac{t}{T}\right) \text{ for } 0 \le t \le T$ 

where  $R_0 = 1\Omega$ , and C = 1 F. We are also given that T = 3 R<sub>0</sub>C and the source voltage is  $V_s = 1$ V. If the current at time t = 0 is 1 A, then the current I(t), in amperes, at time t = T/2 is \_\_\_\_\_ (rounded off to 2 decimal places).



43. Ans: 0.25 Sol: R(t)i(t) +  $\frac{1}{C}\int i dt = 1$ R(t) $\frac{di}{dt} + i(t)\frac{dR(t)}{dt} + i = 0$  $(1 - \frac{t}{3})\frac{di}{dt} + i(-\frac{1}{3}) + i = 0$ 

43

$$(3-t)\frac{di}{dt} + 2i = 0$$
  

$$(3-t)\frac{di}{dt} = -2i$$
  

$$\frac{di}{i} = \left(\frac{-2}{3-t}\right)dt$$
  

$$ln(i) = 2ln(3-t) + ln(c)$$
  

$$ln(i) = ln(3-t)^{2}c$$
  

$$i(t) = (3-t)^{2}c$$
  

$$i(0) = 1 = 3^{2}c$$
  

$$c = \frac{1}{9}$$
  

$$i(t) = \frac{1}{9}(3-t)^{2}$$
  

$$i(1.5) = \frac{1}{9}(1.5)^{2} = 0.25 \text{ A}$$

#### **End of Solution**

44. A single bit, equally likely to be 0 and 1, is to be sent across an additive white Gaussian noise (AWGN) channel with power spectral density N<sub>0</sub>/2. Binary signaling, with  $0 \rightarrow p(t)$  and  $1 \rightarrow q(t)$ , is used for the transmission, along with an optimal receiver that minimizes the bit-error probability.

Let  $\varphi_1(t)$ ,  $\varphi_2(t)$  form an orthonormal signal set.

If we choose  $p(t) = \varphi_1(t)$  and  $q(t) = -\varphi_1(t)$ , we would obtain a certain bit-error probability  $P_{b}$ .

If we keep  $p(t) = \varphi_1(t)$ , but take  $q(t) = \sqrt{E} \varphi_2(t)$ , for what value of E would we obtain the same bit-error probability P<sub>b</sub>?

(a) 3

- (b) 2
- (c) 1
- (d) 0

```
44. Ans: (a)
```

**Sol:** 0 is represented by p(t)

1 is represented by q(t)

 $\phi_1(t)$  and  $\phi_2(t)$  form are orthonormal signal set

 $p(t) = \phi_1(t)$ 

$$q(t) = -\phi_1(t)$$

The signal space diagram is

![](_page_43_Figure_2.jpeg)

$$d_{\min} = 2$$
  
If  $p(t) = \phi_1(t)$  and  $q(t) = \sqrt{E} \phi_2(t)$   
The signal space diagram is

![](_page_43_Figure_4.jpeg)

bit error probability will be same if the  $d_{min}$  is same

$$\sqrt{1 + E} = 2$$
$$1 + E = 4$$
$$E = 3$$

#### **End of Solution**

45. Consider a unity feedback system, as in the figure shown, with an integral compensator  $\frac{K}{s}$  and open-loop transfer function

$$G(s) = \frac{1}{s^2 + 3s + 2}$$

where K > 0. The positive value of K for which there are exactly two poles of the unity feedback system on the j $\omega$  axis is equal to \_\_\_\_\_ (rounded off to two decimal places).

![](_page_43_Figure_11.jpeg)

ACE Engineering Publications Hyderabad + Delhi + Bhopal + Pune + Bhubaneswar + Lucknow + Patna + Bengaluru + Chennai + Vijayawada + Vizag + Tirupati + Kolkata + Ahmedabad

44

45

#### 45. Ans: 6

Sol:  $G_{C}(s) = \frac{K}{s(s^{2}+3s+2)}$   $CE \rightarrow 1 + G_{C}(s) = 0$   $CE \rightarrow s^{3} + 3s^{2} + 2s + k = 0$   $s^{3}$  | 1 2  $s^{2}$  | 3 k  $s^{1}$  |  $\left(\frac{6-k}{3}\right) = 0$   $s^{0}$  | k  $AE \rightarrow 3s^{2} + 6 = 0$   $s = \pm j\sqrt{2}$ k = 6

#### **End of Solution**

46. In the circuit shown,  $V_s$  is a 10 V square wave of period T = 4 ms with R = 500  $\Omega$  and C = 10  $\mu$ F. The capacitor is initially uncharged at t = 0, and the diode is assumed to be ideal. The voltage across the capacitor ( $V_c$ ) at 3 ms is equal to \_\_\_\_\_ volts (rounded off to one decimal place).

![](_page_44_Figure_7.jpeg)

#### 46. Ans: 3.3

**Sol:**  $V_s = 10V$ 

$$V_{c}(t) = 10V (1 - e^{-t/R_{c}})$$
  

$$V_{c}(t = 2ms) = 10V(1 - e^{-\frac{2 \times 10^{-3}}{500 \times 10 \times 10^{-6}}})$$
  
= 3.3V  
T/2↔T: Diode is OFF  

$$V_{c}(t = 3ms) = 3.3V$$

![](_page_45_Picture_0.jpeg)

# HEARTY CONGRATULATIONS TO OUR ESE 2018 RANKERS

AIR

![](_page_45_Picture_2.jpeg)

![](_page_45_Picture_3.jpeg)

![](_page_45_Picture_4.jpeg)

![](_page_45_Picture_5.jpeg)

KARTHIK KOTTURU

TEKCHAND DESHWAL

SHANAVAS CP E&T

AIR

AIR

EE

EE

AIR

![](_page_45_Picture_6.jpeg)

AIR

![](_page_45_Picture_7.jpeg)

CHIRAG JHA

PUNIT SINGH CE

![](_page_45_Picture_9.jpeg)

![](_page_45_Picture_10.jpeg)

AIR

![](_page_45_Picture_11.jpeg)

AMAN JAIN ME

SRIJAN VARMA

![](_page_45_Picture_13.jpeg)

![](_page_45_Picture_14.jpeg)

![](_page_45_Picture_16.jpeg)

![](_page_45_Picture_17.jpeg)

![](_page_45_Picture_18.jpeg)

![](_page_45_Picture_20.jpeg)

![](_page_45_Picture_21.jpeg)

and many more ...

![](_page_45_Picture_23.jpeg)

AIR

AIR

AIR

MAYUR PATIL ME

RISHABH DUTT CE

ROHIT KUMAR CE

SOUVIK DEB ROY

![](_page_45_Picture_25.jpeg)

AIR

![](_page_45_Picture_26.jpeg)

![](_page_45_Picture_27.jpeg)

![](_page_45_Picture_28.jpeg)

![](_page_45_Picture_30.jpeg)

SURYASH GAUTAM E&T AIR

![](_page_45_Picture_32.jpeg)

![](_page_45_Picture_34.jpeg)

![](_page_45_Picture_35.jpeg)

![](_page_45_Picture_36.jpeg)

PRATHAMESH E&T

MILAN KRISHNA

![](_page_45_Picture_49.jpeg)

![](_page_45_Picture_50.jpeg)

![](_page_45_Picture_51.jpeg)

![](_page_45_Picture_52.jpeg)

![](_page_45_Picture_53.jpeg)

![](_page_45_Picture_55.jpeg)

AIR

![](_page_45_Picture_58.jpeg)

![](_page_45_Picture_59.jpeg)

![](_page_45_Picture_60.jpeg)

![](_page_45_Picture_62.jpeg)

![](_page_45_Picture_63.jpeg)

![](_page_45_Picture_65.jpeg)

![](_page_45_Picture_66.jpeg)

![](_page_45_Picture_67.jpeg)

![](_page_45_Picture_68.jpeg)

![](_page_45_Picture_69.jpeg)

![](_page_45_Picture_70.jpeg)

![](_page_45_Picture_71.jpeg)

![](_page_45_Picture_73.jpeg)

CHIRAG SINGLA ME

AIR

ANKIT GARG

![](_page_45_Picture_77.jpeg)

AIR

RATIPALLI NAGESWAR

AIR

![](_page_45_Picture_80.jpeg)

![](_page_45_Picture_87.jpeg)

GATE-19 EXAM PAPER

47

![](_page_46_Figure_2.jpeg)

(c) 1.8 and 1.2 (d) 2.4 and 1.2

47. Ans: (a)

ACE Engineering Publicatione

Sol: Given, 
$$V_{TN} = 0.6V$$
,  $\lambda = 0 \& V_{SB} = 0$   
 $\therefore V_{th} = V_{tho}$  (or)  $V_t = V_{to}$   
Since, N-MOS, current always flow from drain to source,  
 $\Rightarrow$  from fig (1)  
 $\therefore V_{G1} = 3V$ ,  $V_{D1} = 3V$ ,  $V_{TN} = 0.6V$   
Since, to ON N-MOS [E - mode],  
 $V_{GS} \ge V_{Th}$   
Let  $V_{GS} = V_{Th} \Rightarrow V_{G1} - V_{s1} = V_{Th}$   
 $\therefore V_{S1} = V_{G1} - V_{Th} = 2.4V$   
Since,  $V_{S1} = V_{G2} \Rightarrow V_{G2} = 2.4V$ ,  
 $\& V_{D2} = 3V$   
 $\therefore$  Let  $V_{GS2} = V_{Th} \Rightarrow V_{G2} - V_{S2} = V_{Th}$   
 $\therefore V_{S2} = V_{out1} = 2.4 - 0.6$   
 $= 1.8 V$ .  
Similarly from fig (2)  
 $V_{G1} = V_{G2} = V_{G3} = 3V \& V_{D1} = 3V$   
 $\therefore V_{S1} = V_{G1} - V_{Th} = 3 - 0.6 = 2.4V$   
 $\therefore V_{S1} = V_{O2} = 2.4V$ 

# 48Electronics & Communication Engineering $V_{S3} = V_{G3} - V_{Th} = 2.4V$ $V_{out2} = 2.4V$ $\therefore V_{o1} = 1.8V, V_{o2} = 2.4V$ End of Solution

48. A rectangular waveguide of width w and height h has cut-off frequencies for  $TE_{10}$  and  $TE_{11}$  modes in the ratio 1:2. The aspect ratio w/h, rounded off to two decimal places, is

48. Ans: 1.73 Sol:  $f_c|_{TE_{10}} = \frac{c}{2}\frac{1}{a}$   $f_c|_{TE_{11}} = \frac{c}{2}\sqrt{\frac{1}{a^2} + \frac{1}{b^2}}$ Given  $\frac{f_{cTE_{11}}}{f_{cTE_{11}}} = \frac{1}{2}$   $f_{cTE_{11}} = 2f_{cTE_{10}}$   $\frac{c}{2}\sqrt{\frac{1}{a^2} + \frac{1}{b^2}} = 2\frac{c}{2}\frac{1}{a}$ .  $\frac{1}{a^2} + \frac{1}{b^2} = \frac{4}{a^2}$   $\frac{1}{b^2} = \frac{3}{a^2}$   $(\frac{a}{b})^2 = 3$   $\frac{a}{b} = \sqrt{3}$  $\frac{a}{b} = 1.732$ 

#### **End of Solution**

49. Let a random process Y(t) be described as Y(t) = h(t) \* X(t) + Z(t), where X(t) is a white noise process with power spectral density S<sub>x</sub>(f) = 5 W/Hz. The filter h(t) has a magnitude response given by |H(f)| = 0.5 for -5 ≤ f≤ 5, and zero elsewhere. Z(t) is a stationary random process, uncorrelated with X(t), with power spectral density as shown in the figure. The power in Y(t), in watts, is equal to \_\_\_\_\_ W (rounded off to two decimal places).

![](_page_47_Figure_5.jpeg)

![](_page_48_Picture_0.jpeg)

49

#### 49. Ans: 17.5

#### Sol:

![](_page_48_Figure_5.jpeg)

Let us assume x(t)\*h(t) = w(t)

 $\mathbf{y}(t) = \mathbf{w}(t) + \mathbf{z}(t)$ 

$$\mathbf{R}_{_{\mathrm{YY}}}(\tau) = \mathbf{R}_{_{\mathrm{WW}}}(\tau) + \mathbf{R}_{_{ZZ}}(\tau) + \mathbf{R}_{_{\mathrm{WZ}}}(\tau) + \mathbf{R}_{_{ZW}}(\tau)$$

x(t) & z(t) are uncorrelated

$$R_{wz}(\tau) = R_{zw}(\tau) = 0$$
$$R_{YY}(\tau) = R_{ww}(\tau) + R_{zz}(\tau)$$
$$S_{YY}(f) = S_{ww}(f) + S_{zz}(f)$$

The power of y(t) is  $P_{Y} = \int_{-\infty}^{\infty} S_{YY}(f) df = \int_{-\infty}^{\infty} S_{WW}(f) df + \int_{-\infty}^{\infty} S_{ZZ}(f) df$  $S_{WW}(f) = |H(f)|^2 S_{X}(f)$ 

![](_page_48_Figure_12.jpeg)

#### **End of Solution**

50

50. In the circuit shown, if  $v(t) = 2 \sin(1000 t)$  volts,  $R = 1 k\Omega$  and  $C = 1 \mu F$ , then the steady-state current i(t), in milliAmperes (mA), is

![](_page_49_Figure_3.jpeg)

(a)  $2\sin(1000 t) + 2\cos(1000 t)$ (c)  $\sin(1000 \text{ t}) + \cos(1000 \text{ t})$ 

(b)  $\sin(1000 t) + 3 \cos(1000 t)$ (d)  $3 \sin(1000 t) + \cos(1000 t)$ 

**50**. Ans: (d)

Sol:

ACE Engineering Publication

![](_page_49_Figure_7.jpeg)

 $R = 1000 \Omega$ 

at  $\omega = 1000$  rad/sec

$$X_{\rm C} = \frac{-j}{\omega {\rm C}} = \frac{-j}{1000 \times \frac{1}{3} \times 10^{-6}}$$

$$X_C = -j3000\Omega$$

![](_page_49_Figure_12.jpeg)

51

#### GATE-19 EXAM PAPER

![](_page_50_Figure_3.jpeg)

$$Z_{T} = (900 - j \ 300) \parallel (1800 - j600)$$
$$Z_{T} = \frac{(1440000 - j1080000)}{(2700 - j900)}$$
$$Z_{T} = (600 - j200)\Omega$$

Finally

![](_page_50_Figure_6.jpeg)

So, 
$$i(t) = \frac{2\sin 1000t}{(600 - j200)} = \frac{2\sin 1000t}{632.455 \angle -18.434}$$

So,

$$i(t) = 3.162 \sin(1000t + 18.434^{\circ}) \text{ mA}$$

S(A + B) = sinA cosB + cosA sinB

So,

 $i(t) = 3.162 (sin1000t \cos 18.434 + \cos 1000t \sin 18.434) mA$ 

 $i(t) = (3 \sin 1000t + \cos 1000t) mA$ 

#### (OR)

ACE

![](_page_51_Figure_2.jpeg)

52

![](_page_51_Figure_3.jpeg)

$$Z_{eq} = Z || (Z + Z) = \frac{2}{3}Z$$

For parallel combination

![](_page_51_Figure_6.jpeg)

ACE

(53)

51. A CMOS inverter, designed to have a mid-point voltage  $V_1$  equal to half of  $V_{dd}$ , as shown in the figure, has the following parameters:

 $V_{dd} = 3 V$ 

 $\mu_{n}C_{\text{ox}} = 100 \mu A/V^{2}; V_{\text{tn}} = 0.7V$  for nMOS

 $\mu_{\rm p}C_{\rm ox}$  = 40  $\mu$  A/V²;  $\left|\,V_{\rm tp}\,\right|$  = 0.9V for pMOS

The ratio of  $\left(\frac{W}{L}\right)_{n}$  to  $\left(\frac{W}{L}\right)_{n}$  is equal to \_\_\_\_\_ (rounded off to 3 decimal places).

![](_page_52_Figure_8.jpeg)

51. Ans: 0.225 Sol:  $\mu_{n}C_{ox}\left(\frac{W}{L}\right)_{N}(1.5 - V_{TN})^{2} = \mu_{P}C_{ox}\left(\frac{W}{L}\right)_{P}(1.5 - |V_{TP}|)^{2}$   $100 \times \left(\frac{W}{L}\right)_{N} \times 0.8^{2} = 40 \times \left(\frac{W}{L}\right)_{P} \times 0.6^{2}$  $\frac{(W/L)_{N}}{(W/L)_{P}} = \frac{9}{16} \times \frac{4}{10} = 0.225$ 

![](_page_52_Figure_10.jpeg)

52. The quantum efficiency ( $\eta$ ) and responsivity (R) at a wavelenth  $\lambda$  (in  $\mu$ m) in a p-i-n photodetector are related by

(a) 
$$R = \frac{\lambda}{\eta \times 1.24}$$
 (b)  $R = \frac{1.24 \times \lambda}{\eta}$   
(c)  $R = \frac{\eta \times \lambda}{1.24}$  (d)  $R = \frac{1.24}{\eta \times \lambda}$ 

#### 52. Ans: (c)

Sol:  $R = \frac{\eta q}{hv} = \frac{\eta q\lambda}{hc}$   $R = \frac{\eta \lambda}{1.24}$ 

#### **End of Solution**

ACE Engineering Publications Hyderabad + Delhi + Bhopal + Pune + Bhubaneswar + Lucknow + Patna + Bengaluru + Chennai + Vijayawada + Vizag + Tirupati + Kolkata + Ahmedabad

Electronics & C		(54) Electronics &
-----------------	--	--------------------

53. A voice signal m(t) is in the frequency range 5 kHz to 15 kHz. The signal is amplitude-modulated to generate an AM signal  $f(t) = A(1+m(t)) \cos 2\pi f_c t$ , where  $f_c = 600$  kHz. The AM signal f(t) is to be digitized and archived. This is done by first sampling f(t) at 1.2 times the Nyquist frequency, and then quantizing each sample using a 256-level quantizer. Finally, each quantized sample is binary coded using K bits, where K is the minimum number of bits required for the encoding. The rate, in Megabits per second (rounded off to 2 decimal places), of

nunication Engineering

of the resulting stream of coded bits is \_\_\_\_\_ Mbps.

53. Ans: 11.81

**Sol:** Spectrum of the voice signal m(t) is

![](_page_53_Figure_5.jpeg)

The spectrum of modulated signal is

![](_page_53_Figure_7.jpeg)

Given sampling rate is 1.2 times Nquist rate

$$\begin{split} f_s &= 1.2 \ f_{\scriptscriptstyle N} \\ &= 1.2 \Big[ 2 f_{\scriptscriptstyle H} \Big] \\ [ Nquist rate= 2[highest frequency component present in the signal] \\ f_s &= 1.2 \Big[ 2 \times 615 k \Big] \\ &= 1476 \ k \ samples \ /sec \\ Number of quantization levels = 256 \\ Number of bits to encode the signal \\ n &\geq log_2^L \\ n &\geq 8 \\ min = 8 \\ R_h &= nf_s = 8 \Big[ 1476 k \Big] = 11.808 \ Mbps \end{split}$$

ACE

55

54. A random variable X takes values -1 and +1 with probabilities 0.2 and 0.8, respectively. It is transmitted across a channel output is Y = X + N. The noise N is independent of X, and is uniformly distributed over the interval [-2,2]. the receiver makes a decision

$$\hat{X} = \begin{cases} -1, \text{ if } Y \leq \theta \\ +1, \text{ if } Y > \theta \end{cases}$$

where the threshold  $\theta \in [-1,1]$  is chosen so as to minimize the probability of error  $\Pr[\hat{X} \neq X]$ . The minimum

probability of error, rounded off to 1 decimal place, is

#### 54. Ans: 0.1

**Sol:** P(-1) = 0.2, P(1) = 0.8

the pdf of noise is

![](_page_54_Figure_10.jpeg)

the received signal Y = X + NThe pdf if '1' is transmitted

![](_page_54_Figure_12.jpeg)

The pdf if -1 is transmitted

![](_page_54_Figure_14.jpeg)

The threshold voltage should lies between -1 and +1

$$\begin{split} P_{\rm e} &= 0.8 \int_{-\infty}^{V_{\rm TH}} \frac{1}{4} \, dz + 0.2 \int_{V_{\rm TH}}^{\infty} \frac{1}{4} \, dz \\ &= 0.8 \int_{-1}^{V_{\rm TH}} \frac{1}{4} \, dz + 0.2 \int_{V_{\rm TH}}^{1} \frac{1}{4} \, dz \end{split}$$

$$P_{\rm e} = 0.2 [V_{\rm TH} + 1] + 0.05 [1 - V_{\rm TH}]$$

 $V_{TH} = -1 \rightarrow P_e = 0.1$  $V_{TH} = 0 \rightarrow P_e = 0.25$  $V_{TH} = 1 \rightarrow P_e = 0.4$ So the minimum probability of error is 0.1

#### Electronics & Communication Engineering

55. Consider a long-channel MOSFET with channel length 1  $\mu$ m and width 10  $\mu$ m. The device parameters are acceptor concentration N<sub>A</sub> = 5 × 10<sup>16</sup> cm<sup>-3</sup>, electron mobility  $\mu_n = 800 \text{ cm}^2/\text{V-s}$ , oxide capacitance/area  $C_{ox} = 3.45 \times 10^{-7} \text{F/cm}^2$ , threshold voltage V<sub>T</sub> = 0.7 V. The drain saturation current (I<sub>Dsat</sub>) for a gate voltage of 5 V is \_\_\_\_\_ mA (rounded off to two decimal places). [ $\varepsilon_0 = 8.854 \times 10^{-14} \text{F/cm}$ ,  $\varepsilon_{si} = 11.9$ ]

56

55. Ans: 25.5  
Sol: 
$$I_{D,sat} = \frac{1}{2} \mu_n C_{ox} \times \frac{W}{L} (V_{GS} - V_{TH})^2$$
  
 $= \frac{1}{2} \times 800 \times 3.45 \times 10^{-7} \times \frac{10}{1} \times (5 - 0.7)^2$   
 $= 25.5 \text{ mA}$ 

ACE Engineering Publications

**End of Solution**