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ESE- 2019 (Prelims) - Offline Test Series

Test - 13

#### MECHANICAL ENGINEERING

SUBJECT: Fluid Mechanics + Turbo Machinery + Thermodynamics and Heat Transfer — SOLUTIONS

#### 01. Ans: (a)

**Sol:**  $P_{reading} = P_{fluid} - P_{surrounding}$ 

Normally  $P_{surrounding} = P_{atm} = 0$ 

 $P_{reading} = 305 \text{ kPa}$ 

When  $P_{surrounding} = 650 \text{ mm Hg Vacuum}$ 

$$=\frac{650}{750}\times100$$

Then,

 $P_{\text{reading}} = 305 - (-86.67) = 391.67 \text{ kPa}$ 

#### 02. Ans: (d)

Sol:

- Thermal diffusivity of material is ability to conduct thermal energy relative to store thermal energy.
- Thermal diffusivity of liquid is less than that of gas.



As n decreases, W increases.

#### 04. Ans: (c)

Sol:





Initially,

$$P_A + \gamma_w \times 1.5 = P_{atm} + \gamma_{Hg} \times 0.1$$
-----(1)

When the pressure in A is doubled,

$$2P_{A} + \gamma_{w}(1.5 + x) = P_{atm} + \gamma_{Hg}(x + 0.1 + x)$$
-----(2)

where x is the displacement of Hg level in the left limb due to pressure change in A.

From (1),

$$P_{A} = 100 + 13.6 \times 10 \times 0.1 - 10 \times 1.5$$

= 98.6 kPa

From (2),

$$2 \times 98.6 + 10 \times 1.5 + 10 \times x = 100 + 13.6 \times 10$$
  
  $\times 2x + 13.6 \times 10 \times 0.1$ 

212.2 - 100 - 13.6 = 272x - 10x98.6 = 262 x

 $\Rightarrow$  x = 0.376 m

So, manometric reading when  $P_A$  is doubled is,  $R'_m = 2x + 0.1 = 0.852 \text{ m} = 85.2 \text{ cm}$ 

#### 05. Ans: (d)

Sol: Efficiency of the engine,

$$\eta_{engine} = \frac{Q - 0.5Q}{Q} = 0.5 = 50\%$$

Efficiency of Carnot Engine,

$$\eta_{Carnot} = \frac{T_1 - T_2}{T_1} = \frac{(377 - 27)}{(377 + 273)}$$
$$= 0.5384 = 53.84\%$$

As  $\eta_{engine} < \eta_{Carnot}$ , it is a practical engine.

#### 06. Ans: (b)

Sol: Head loss due friction in the first pipe,

$$h_{f1} = \frac{f_1 L_1 Q_1^2}{12.1 d_1^5} - \dots (1)$$

Head loss due to friction in the second pipe,

$$\mathbf{h}_{f2} = \frac{\mathbf{f}_2 \, \mathbf{L}_2 \, \mathbf{Q}_2^{\ 2}}{12.1 \, \mathbf{d}_2^5} \quad \text{-------(2)}$$

From equations (1) and (2),  $h_f \propto \frac{f}{d^5}$ 

But  $L_2 = L_1$ ;  $Q_2 = Q_1$ ;  $d_2 = 2d_1$ For laminar flow :

$$f \propto \frac{1}{\text{Re}} \propto \frac{v}{\text{Vd}}$$
Or,  $f \propto \frac{1}{\text{Vd}}$ 

$$\frac{f_2}{f_1} = \frac{V_1}{V_2} \frac{d_1}{d_2} = \frac{d_2^2}{d_1^2} \frac{d_1}{d_2} \quad \left[ \text{as } \frac{\pi}{4} d_1^2 V_1 = \frac{\pi}{4} d_2^2 V_2 \right]$$

$$= \frac{d_2}{d_1} = 2$$
Hence,  $\frac{h_{f1}}{h_{f2}} = \frac{f_1}{f_2} \times \left(\frac{d_2}{d_1}\right)^5 = \frac{1}{2} \times (2)^5 = 16$ 
Or,  $\frac{h_{f1}}{h_{f2}} = 16:1$ 

07. Ans: (c)

Sol:





There is reduction in the conduction heat transfer with increasing the length of the fin because some part of heat is transferred due to convection as shown in the figure.

According to Fourier's law of heat conduction

$$q = -k \left( \frac{dT}{dx} \right)$$

As  $q\downarrow \Rightarrow \frac{dT}{dx}\downarrow$ 

#### **08.** Ans: (c)

**Sol:** Internal energy of an ideal gas is a function of temperature only.

Specific enthalpy, h = u + pv

For ideal gas, Pv = RT

$$\mathbf{h} = \mathbf{u}(\mathbf{T}) + \mathbf{R}\mathbf{T}$$

h = h(T) for ideal gas.

#### **09.** Ans: (a)

**Sol:** Since head losses are neglected, Bernoulli's equation can be applied for any two points in the flow.



Thus,

$$\frac{P_1}{\gamma} + \frac{V_1^2}{2g} + Z_1 = \frac{P_2}{\gamma} + \frac{V_2^2}{2g} + Z_2$$

$$P_1 = P_2 = P_{atm} = 0;$$

$$V_1 = 0,$$

$$Z_1 = 5 \& Z_2 = 0$$

$$0 + 0 + 5.0 = 0 + \frac{V_2^2}{2g} + 0$$

$$Or, \quad V_2 = \sqrt{2g \times 5.0} = 10 \text{ m/s}$$
(velocity at exit

Thus, velocity in the pipe,  $V_p = 10/4 = 2.5$  m/s as diameter of pipe is twice the diameter of nozzle. Again, applying Bernoulli's equation for pts (1) and (B)

of nozzle)

$$\frac{P_{B}}{\gamma} + \frac{V_{B}^{2}}{2g} + Z_{B} = \frac{P_{1}}{\gamma} + \frac{V_{1}^{2}}{2g} + Z_{1}$$
  
Here,  $Z_{1} = 1.5$  m,  
 $P_{1} = P_{atm} = 0,$   $Z_{B} = 0$ 

Or, 
$$\frac{P_B}{\gamma} = 1.5 - \frac{2.5^2}{2 \times 10} - 0 = 1.5 - 0.3125$$
  
(as V<sub>B</sub> = V<sub>P</sub>)  
= 1.1875 m

$$\Rightarrow$$
 P<sub>B</sub> = 1.1875×10<sup>4</sup> = 11.875 kPa

#### 10. Ans: (b)

**Sol:** If the Biot number tends to zero, the temperature gradient inside the solid body tends to zero.



#### 11. Ans: (a)

**Sol:** Joule Thomson coefficient,  $\mu_{JT} = \left(\frac{\partial T}{\partial P}\right)_h$ 

In throttling process,  $\Delta P$  is negative. Thus, for  $\mu_{JT}$  to be negative, when dT should be positive.

#### 12. Ans: (c)

**Sol:** Critical Re for flat plate =  $5 \times 10^5$ 

$$\frac{\delta}{x} = \frac{5}{\sqrt{5 \times 10^5}} = \frac{5}{10^2 \sqrt{50}}$$
$$= \frac{5 \times 10^{-2}}{\sqrt{5} \sqrt{10}} = \left(\sqrt{\frac{5}{10}}\right) \times 10^{-2}$$
$$= \frac{1}{\sqrt{2}} \times 10^{-2} = \frac{\sqrt{2}}{2} \times 10^{-2}$$
$$= \frac{1.414}{2} \times 10^{-2} = 0.00707$$
$$\Rightarrow \frac{\delta}{x} = 7.07 \times 10^{-3}$$

#### 13. Ans: (c)

Sol: Fourier's law of heat conduction :

.1**T** 

$$q = -k \frac{d1}{dx}$$
  

$$200 = -k \frac{d}{dx} (110 - 60x)$$
  

$$200 = -k(0 - 60)$$
  

$$60k = 200$$
  

$$k = \frac{200}{60} = 3.33 \text{ W/m} - \text{K}$$

#### 14. Ans: (a)

**Sol:** As there is no change in volume of the system, boundary work (PdV) is zero. As work is needed to push fluid into or out of the boundary of the control volume, flow work is non zero.

#### 15. Ans: (c)

Sol: Since at the edge of the boundary layer  $\frac{du}{dy} = 0$ , the shear stress  $\tau_b = 0$ Hence, the required ratio is 0.

#### 16. Ans: (a)

**Sol:** k = 100 W/m-K, L = 1 m,  $T_0 = 90^{\circ}\text{C}$ ,  $T_{\infty} = 20^{\circ}\text{C}$   $\eta = 0.2$ , d = 4 cm = 0.04 mEfficiency of the long fin :

 $\eta = \frac{1}{mL}$  $0.2 = \frac{1}{mL}$ 

$$m \times 1$$
  
 $m = 5 m^{-1}$ 

Heat loss from the fin = m k  $A_c \theta_0$ 

$$= 5 \times 100 \times \frac{\pi}{4} d^{2} \times (90 - 20)$$
$$= 5 \times 100 \times \frac{1}{4} \times \frac{22}{7} \times 0.04^{2} \times 70$$
$$= 500 \times \frac{22}{7} \times \frac{1}{4} \times 0.04 \times 0.04 \times 70 = 44 W$$





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#### 17. Ans: (b)

**Sol:** dW = PdV

If we multiply by  $\frac{1}{P}$  then it comes to be dV,

which is perfect differential. So  $\frac{1}{P}$  is integrating factor for quasi-static displacement work.

#### **18.** Ans: (a)

Sol: 
$$\frac{u}{U_{\infty}} = \frac{y}{\delta} = \eta$$
  
 $\theta = \int_{0}^{\delta} \frac{u}{U_{\infty}} \left(1 - \frac{u}{U_{\infty}}\right) dy = \delta \int_{0}^{1} \eta (1 - \eta) d\eta$   
 $= \delta \int_{0}^{1} (\eta - \eta^{2}) d\eta = \delta \left[\frac{\eta^{2}}{2} - \frac{\eta^{3}}{3}\right]_{0}^{1}$   
 $\theta = \frac{\delta}{6}$ 

Given that,  $\delta = 15 \text{ mm}$  at x = 1 m

$$\theta = \frac{15 \,\mathrm{mm}}{6}$$

Hence,  $\theta = 2.5 \text{ mm}$ 

#### **19.** Ans: (c)

**Sol:** Given data:

 $Q = 0.016\pi \text{ m}^3/\text{s}, \qquad d_1 = 0.1 \text{ m}$  h = 0.3 m, H = 3 m  $W_{tank} = 1 \text{ kN},$  $A_2 = 0.5 \text{ m}^2$ 



Mass flow rate of jet of water =  $\rho Q$ 

 $= 10^3 \times 0.016\pi = 16\pi$  kg/s

Jet velocity,  $V_1 = \frac{4Q}{\pi d_1^2} = \frac{4 \times 0.016 \pi}{\pi \times (0.1)^2}$ 

$$V_1 = 6.4 \text{ m/s}$$

From projectile motion equation:

$$V_{2x} = V_1 = 6.4 \text{ m/s}$$

Momentum equation in x - direction:

$$-F_{\rm B} = -\dot{m}(V_{2x}) = -16\pi \times 6.4$$
$$\Rightarrow F_{\rm B} = 102.4 \ \pi \ N$$
$$\Rightarrow k = 102.4$$

#### 20. Ans: (b)

Sol: Temperature distribution :

$$\frac{T-T_{\infty}}{T_{i}-T} = e^{\left(\frac{hA}{\rho v c_{p}} \times \tau\right)}$$

For the same temperature difference,

$$e^{\left(\frac{h_1A}{\rho V c_p} \times \tau_1\right)} = e^{\left(\frac{h_2A}{\rho V c_p} \times \tau_2\right)}$$

$$h_1 \tau_1 = h_2 \tau_2$$

$$\begin{split} h_1 \times 30 &= 5h_1 \times \tau_2 \qquad \quad [\because h_2 &= 5 \ h_1] \\ \Rightarrow \quad \tau_2 &= 6 \ min \end{split}$$



#### 21. Ans: (b)

**Sol:** As long as there is temperature difference between the body and the thermal reservoir, work can be obtained through the engine. Once there is no temperature difference, engine will stop working.

#### 22. Ans: (b)

Sol: Air lift pump has vary low efficiency

- Hydraulic ram can lift small quantity of water to the greater heights by using large quantity of water at small heights using principle of water hammer.
- Centrifugal pump gives continuous supply of water than reciprocating pump. The discharge in reciprocating pump is discontinuous or pulsating. Further, the efficiency of reciprocating pump is 10 to 20% more than that of centrifugal pump.

#### 23. Ans: (c)

Sol:

• In free convection :

Characteristic length for a horizontal surface

$$L_{c} = \frac{A_{c}}{P} = \frac{\frac{\pi}{4}D^{2}}{\pi D} = \frac{D}{4}$$

• Velocity and temperature distribution :



#### 24. Ans: (d)

Sol:

- Leakage loss will take place due to pressure difference across pump which is proportional to manometric head (P 2).
- Frictional loss is proportional to  $\frac{V_r^2}{2g}$  (Q-3)
- Entrance loss means entry with shock which is absent when relative velocity is tangential to blade profile at inlet. This happens at design point. (R-1)

#### 25. Ans: (c)

**Sol:** Temperature of the object can be increased by supplying heat to it or by doing work on it.

Sol:



Reynolds number (Re) =  $\frac{\text{VL}}{v} = \frac{5 \times 1}{2 \times 10^{-3}}$ = 2.5 × 10<sup>3</sup> = 2500

Flow is laminar.

Average Nusselt number,

$$\overline{Nu} = 2 \times Nu_x$$

$$\frac{\overline{h} \times L}{k} = 2 \times 0.332 \times (\text{Re})^{1/2} (\text{Pr})^{1/3}$$

$$\frac{\overline{h} \times L}{0.5} = 2 \times 0.332 \times (2500)^{1/2} \times (1)^{1/3}$$

$$\frac{\overline{h} \times 1}{0.5} = 2 \times 0.332 \times 50 \times 1$$

$$\overline{h} = 33.2 \times 0.5$$

$$\overline{h} = 16.6 \text{ W/m}^2 \text{ K}$$
Heat transfer rate (Q) =  $\overline{h}$  A (T<sub>s</sub> - T<sub>∞</sub>)  
= 16.6 × 1 × 0.5 (40 - 20)  
= 166 × 1 × 0.5 × 20  
= 166 W

#### 27. Ans: (b)

Sol: Maximum useful work in a closed system  $(WU)_{MAX} = (E_1 - E_2) - T_0(S_1 - S_2) + P_0 (V_1 - V_2)$ 

On rearrangement

$$(WU)_{MAX} = (E_1 - T_0S_1) - (E_2 - T_0S_2) + P_0(V_1 - V_2)$$

#### 28. Ans: (a)

**Sol:** Make the flow steady by referencing all velocities to the moving vane and let the C.V. move with the vane as shown.



Momentum equation in x - direction:

$$F_{x} = \dot{m}_{2}V_{2x} - \dot{m}_{1}V_{1}$$
  
where  $\dot{m} = \rho AV = 10^{3} \times 8 \times 10^{-3} \times 20$   
 $= 160 \text{ kg/s}$   
$$F_{x} = \left(\frac{\dot{m}}{2}V\cos 60^{\circ} - \dot{m}V\right) = \dot{m}V\left(\frac{1}{4} - 1\right)$$
  
 $= -160 \times 20 \times \frac{3}{4} = -2400 \text{ N}$ 

Momentum equation in y - direction.

$$F_{y} = \dot{m}_{2}V_{2y} - \dot{m}_{3}V_{3y}$$
$$= \frac{\dot{m}}{2}V\sin 60^{\circ} - \frac{\dot{m}}{2}V = \frac{\dot{m}}{2}V(\sin 60^{\circ} - 1)$$



$$=\frac{160\times20}{2}(0.866-1)=-214.36$$
 N

From Newton's third law of motion,  $\Rightarrow F(\text{water on vane}) = (2400\hat{i} + 214.4\hat{j}) \text{ N}$  *Note:* Answer can be determined from  $F_x$ alone. No need to calculate  $F_y$ .

#### 29. Ans: (d)

**Sol:** Boiling is classified as pool boiling or flow boiling, depending on the presence of bulk fluid motion. Boiling is called pool boiling in the absence of bulk fluid flow and flow boiling (or forced convection boiling) in the presence of it.

#### **30.** Ans: (a)

31. Ans: (d)

Sol: Given:  $u = 2U\left(1 - \frac{r^2}{R^2}\right)$  $\frac{du}{dr} = -2U \times \frac{2r}{R^2} = -\frac{4Ur}{R^2}$ 

Shear stress,  $\tau = -\mu \frac{du}{dr} = 4U\mu \frac{r}{R^2}$ 

and

$$\tau_{o}(r=R) = 4U \,\mu \frac{R}{R^{2}} = 4U \mu \times \frac{1}{R}$$

Therefore, the required ratio

$$\frac{\tau}{\tau_o} = 4U\mu \frac{r}{R^2} \times \frac{R}{4U\mu} = \frac{r}{R}$$
  
Thus, for  $\frac{r}{R} = 0.5$ ,  $\frac{\tau}{\tau_o} = 0.5$ 

#### 32. Ans: (b)

#### Sol:

:9:

- Temperature rise of the cold fluid is equal to temperature fall of hot fluid only when heat capacities of both the fluids are same.
- LMTD is dependent on direction of flow (parallel or counter).
- Temperature difference between hot fluid and cold fluid always decreases only in parallel flow heat exchanger. It may increases or decreases in case of counter flow heat exchanger.

#### 33. Ans: (b)



Applying energy equation for points (1) and (2), considering energy loss due to abrupt change in diameter,

$$\frac{P_1}{\gamma} + \frac{V_1^2}{2g} = \frac{P_o}{\gamma} + \frac{(V_1 - V_2)^2}{2g}$$
(as  $P_2 = P_{\text{stagnation}} = P_o$ )
Or,
$$\frac{P_o}{\gamma} - \frac{P_1}{\gamma} = \frac{V_1^2}{2g} - \frac{(V_1 - V_2)^2}{2g}$$



But 
$$\frac{P_o}{\gamma} - \frac{P_1}{\gamma} = \Delta h_\ell$$
 from manometer  
 $\Delta h_\ell = \frac{V_1^2}{2g} \left[ 1 - \left( 1 - \frac{V_2}{V_1} \right)^2 \right] = \frac{V_1^2}{2g} \left[ 1 - \left( 1 - \frac{A_1}{A_2} \right)^2 \right]$   
 $\Delta h_\ell = \frac{V_1^2}{2g} \left[ 1 - \left( 1 - \frac{1}{4} \right)^2 \right]$   
 $0.07 \left( \frac{13.6}{1.2} - 1 \right) = \frac{V_1^2}{2g} \left[ 1 - \frac{9}{16} \right] = \frac{7}{16} \cdot \frac{V_1^2}{2g}$   
Or,  $\frac{0.07 \times 12.4}{1.2} = \frac{7}{32} \frac{V_1^2}{10}$   
Or,  $V_1^2 = \frac{32 \times 10 \times 0.07 \times 12.4}{7 \times 1.2}$   
 $= \frac{32}{12} \times 12.4 = 16 \times 2.07$   
 $V_1 = 4 \times \sqrt{2.07} = 5.75 \text{ m/s}$ 

 $\therefore$  Mass flow rate of the liquid =  $\rho_{\ell}AV_{1}$ 

 $= 1200 \times 2 \times 10^{-3} \times 5.75 = 13.8 \text{ kg/s}$ 

*Note:* Such questions with lengthy calculation are asked in ESE exam to trap the students. Students are, therefore, advised not to spend time on such questions initially.

35. Ans: (a)  
Sol: U = 100 W/m<sup>2</sup>K,  
$$\dot{m} = 60 \text{ kg/min} = 1 \text{ kg/s}$$
  
 $A_s = 42 \text{ m}^2$ ,  
 $c_p = 4.2 \text{ kJ/kgK}$ 

NTU = 
$$\frac{\text{UA}_{\text{s}}}{\text{mc}_{\text{p}}} = \frac{100 \times 42}{1 \times 4.2 \times 10^3} = \frac{4200}{4200} = 1$$

Effectiveness of the condenser

$$(\varepsilon) = 1 - e^{-NTU}$$
  
= 1 - e^{-1}  
= 1 -  $\frac{1}{e}$   
= 1 -  $\frac{1}{2.718}$  = 0.6321 = 63.21 %

#### 36. Ans: (b)

Sol:

- Critical point → Properties of saturated liquid and saturated vapor are same.
- Sublimation → On heating solid changes to vapour state.
- Triple point → (Solid + liquid + vapour) coexist.
- Melting → Phase changes from solid to liquid.

#### **37.** Ans: (a)

Sol: The expression of velocity, V<sub>1</sub> is given as :  

$$2g \times h = 3.88V_1^2 + 5V_2^2$$
  
 $= V_1^2 \left( 3.88 + 5 \times \frac{V_2^2}{V_1^2} \right) = V_1^2 \left[ 3.88 + 5 \times \left( \frac{d_1}{d_2} \right)^4 \right]$   
 $= V_1^2 \left( 3.88 + 5 \times \frac{1}{256} \right)$   
 $= 3.9V_1^2$ 

Or,  $V_1 \propto \sqrt{h}$ 

When 'h' is changed to 2.42 m, then the velocity  $V_1$  will increase to  $V_1'$  when all other data remain constant.

$$\Rightarrow \frac{V_1'}{V_1} = \sqrt{\frac{2.42}{2}} = \sqrt{1.20} = 1.1$$

Thus, the percentage increase in  $V_1$  is 10%

#### **38.** Ans: (b)

Sol: For same heat transfer rate :

 $(U A_s \times LMTD)_{parallel flow} = (U \times A_s \times A_s)$ 

LMTD)<sub>counter flow</sub>

v = constant

 $(A_s \times LMTD)_{parallel \; flow} = (A_s \times LMTD)_{counter \; flow}$ 

As,  $(LMTD)_{counter flow} > (LMTD)_{parallel flow}$ 

$$\therefore \ (A_s)_{counter \ flow} < (A_s)_{parallel \ flow}$$

$$\therefore \ \frac{(A_s)_{counter \ flow}}{(A_s)_{parallel \ flow}} < 1$$

**39.** Ans: (a)

Sol: For an ideal gas :

PV = constant (:: T = constant)

Differentiating we get  $\frac{PdV}{dP} = -V$ 

$$\beta = -\left(\frac{1}{V}\right)\left(\frac{dV}{dP}\right) = \left(\frac{1}{P}\right) \Longrightarrow \beta \times P = 1$$

 $\therefore$  The graph between  $\beta$  and P will be rectangular hyperbola.

40. Ans: (b)

#### Sol:

:11:

- In impulse turbines like Pelton wheel, the pressure remains atmospheric (constant) through out as water passes through runner. The penstocks will have nozzles at the down stream end. As water passes through nozzle pressure energy is completely converted into kinetic energy.
- Water strikes on the wheel tangentially at only one point for single jet Pelton turbine and it strikes at multiple points in case of multi jet Pelton turbine but never at all points along the circumference.

 $\Rightarrow$  Hence, only statements 2 & 3 are correct.

• In case of reaction turbines, at the entry to the runner, only a part of the available pressure energy is converted as kinetic energy. Hence, all along the runner, both pressure and velocity change. The gradual change of pressure is ensured by providing air tight casing.





$$\label{eq:sigma_state} \begin{split} \sigma &= 6{\times}10^{-8}~W/m^2K^4\\ T_1 &= 300~K, \qquad T_2 = 500~K,\\ \epsilon_1 &= \epsilon_2 = 1 \end{split}$$

Net radiative heat exchange

$$(Q_{1-2}) = \frac{\sigma(T_1^4 - T_2^4)}{\frac{1 - \varepsilon_1}{\varepsilon_1 A_1} + \frac{1}{A_1 F_{1-2}} + \frac{1 - \varepsilon_2}{\varepsilon_2 A_2}}$$
$$Q_{1-2} = A_1 F_{1-2} \sigma (T_1^4 - T_2^4)$$
$$\frac{Q_{1-2}}{A_1} = 1 \times 6 \times 10^{-8} (300^4 - 500^4)$$

Net radiative heat flux =  $6(3^4 - 5^4)$ 

$$= -6 \times (5^{2} + 3^{2}) (5 + 3) (5 - 3)$$
$$= -6 \times 34 \times 8 \times 2$$
$$= -6 \times 34 \times 16$$
$$= -3264 \text{ W/m}^{2}$$
$$= -3.264 \text{ kW/m}^{2} = 3.264 \text{ kW/m}^{2}$$

(Negative sign indicates that heat is transferring from surface 2 to surface 1).

#### 42. Ans: (b)

Sol: Available energy

$$= 2000 \times \left[\frac{500 - 300}{500}\right] = 800 \, \text{kJ}$$

Unavailable energy = 2000 - 800 = 1200 kJ

#### 43. Ans: (a)

**Sol:** Given,  $\frac{D_m}{D_n} = \frac{1}{10}$ 

where m and p denote for model and prototype turbine :

and 
$$\frac{N_m}{N_p} = \frac{600}{200} = 3$$
 and  $H_p = 30$  m  
We know that,  
 $U \propto \sqrt{H}$   
 $ND \propto \sqrt{H}$   
Or,  $H \propto N^2 D^2$   
So,  $\frac{H_m}{H_p} = \left(\frac{N_m}{N_p}\right)^2 \times \left(\frac{D_m}{D_p}\right)^2 = 3^2 \times \left(\frac{1}{10}\right)^2$   
 $\Rightarrow H_m = 30 \times 9 \times \frac{1}{100} = 2.7$  m

## **44. Ans:** (b) **Sol:** <sup>G</sup>



$$\alpha = 0.4$$
  
For an opaque body,  $\tau = 0$   
$$\alpha + \rho + \tau = 1$$
  
$$0.4 + \rho + 0 = 1$$
  
$$\rho = 0.6$$
  
$$\frac{\text{Re flected energy}}{\text{Absorbed energy}} = \frac{0.6\text{G}}{0.4\text{G}} = \frac{6}{4} = 1.5$$

#### 45. Ans: (b)

**Sol:** For all variable x, y, z

$$\left(\frac{\partial y}{\partial z}\right)_{x}\left(\frac{\partial z}{\partial x}\right)_{y}\left(\frac{\partial x}{\partial y}\right)_{z} = -1$$

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#### 46. Ans: (a) Sol:

• Isentropic efficiency is,  $\eta_{isen} = R.F \times \eta_{stage}$ where R.F is reheat factor. Reheat factor is always greater than 1.

Therefore  $\eta_{isen} > \eta_{stage}$ .

• Reheat factor increases with increase in number of stage because constant pressure lines diverge in T-s diagram.

#### 47. Ans: (d)

Sol: Total heat transfer (average heat transfer)

 $= \overline{h}.A.\Delta T$   $\overline{h} = 2h_x \quad (For laminar flow)$   $Q = 2 h_x. A \Delta T$   $Q = 2 \times 116.89 \times 1 \times 60$   $Q = 14027.56 \text{ W/m}^2$ 

#### 48. Ans: (d)

Sol: Enthalpy at final state,  $h_2 = h_{f2} + x_2(h_g - h_f)_2$ Initial enthalpy,  $h_1 = h_{f2}$ 

$$ds = \frac{h_2 - h_1}{T_{sat}}$$
$$= \frac{x(h_g - h_f)}{273 + 120.23} = \frac{0.7 \times (2707 - 505)}{(120 + 273)}$$
$$= 3.922$$

#### 49. Ans: (d)

**Sol:** For n-row Curtis stage

$$\rho_{\text{opt}} = \frac{\cos\alpha}{2n} = \frac{\cos 30}{2 \times 2} = \left(\frac{\sqrt{3}}{2 \times 2}\right) = 0.22$$

50. Ans: (a)

**Sol: Biot number** - Ratio of internal thermal resistance to boundary layer thermal resistance

Grashof number - Ratio of buoyancy to viscous force

**Prandtl number** - Ratio of momentum to thermal diffusivities

**Reynolds number** - Ratio of inertia force to viscous force

#### 51. Ans: (a)

#### Sol:

- Maximum temperature that can be allowed in ramjet engine is very high about 2000°C as compared to about 900°C turbojet because in ramjet engines turbine is not used to drive compressor.
- Pulse jet engine has static thrust. Thus, it doesn't need a launching device for initial propulsion.

#### 52. Ans: (d)

**Sol:** TdS = dU + PdV is applicable to reversible or irreversible process performed by closed system.



Sol:



For gas turbine plants with ideal regeneration, efficiency is given by

$$\eta = 1 - \frac{T_1}{T_3} (r_p)^{\frac{\gamma-1}{\gamma}} .$$

As  $r_p$  increases  $\eta$  decreases.

• Work ratio = 
$$\frac{W_T - W_C}{W_T}$$

Work of compression in gas turbine plants is large as compared to pump work in steam power plants due to high specific volume of gas as compared to liquid.

Thus, work ratio of gas turbine plants is quite smaller than that of steam power plants.

• In gas turbines reheating is more beneficial than intercooling because for the same compression ratio reheating gives more net work than intercooling.

#### 54. Ans: (c)

**Sol:** First law of thermodynamics is the law of conservation of energy which is not violated.

55. Ans: (c)

:15:

**Sol:** Thrust power  $(P_T) = F \times c_i$ 

$$= 10 \times 600 = 6000 \text{ kW}$$

Heat input (Q) =  $0.5 \times 40000 = 20000 \text{ kW}$ 

Overall efficiency,

$$\frac{P_{\rm T}}{Q} = \frac{6000}{20000} = 0.3 \text{ or } 30\%$$

56. Ans: (c)

Sol: Change in Available Energy

$$= (h_1 - h_2) - T_0 (s_1 - s_2)$$
$$= (400 - 100) - 300 (1.1 - 0.7)$$
$$= 300 - 120 = 180 \text{ kJ/kg}$$

57. Ans: (b)

Sol: NPSH =  $H_a - H_S - H_L - h_{fs}$ (if sump is below the pump)

$$= 10.1 - (-3) - 0.3 - 0.4$$
$$= 12.4 \text{ m}$$

#### 58. Ans: (a)

**Sol:** All anti clockwise cycles are work consuming cycles. So, the cycle will heat the environment.

59. Ans: (d)

Sol: 
$$K_u = \frac{u}{\sqrt{2gH}} = \frac{\pi DN / 60}{\sqrt{2gH}}$$
  
=  $\frac{\pi \times 0.7 \times 600 / 60}{\sqrt{2 \times 10 \times 45}} = \frac{7\pi}{30} = 0.733$ 



#### 60. Ans: (b)

- **Sol:** For the cycle 1-2-3-1 thermal efficiency can be written as
  - Net work
- $\eta = \frac{1}{\text{Heat sup plied}}$ 
  - $= \frac{\text{Area under T} \text{s diagram for cycle1} 2 3 1}{\text{Area under 3} 1 \text{ process projected on 's'axis}}$

$$\eta = \frac{\frac{1}{2}(s_{b} - s_{a})(T_{3} - T_{1})}{\frac{1}{2}(T_{3} + T_{1})(s_{b} - s_{a})}$$
$$= \frac{T_{3} - T_{1}}{T_{3} + T_{1}}$$

#### 61. Ans: (a)

Sol: Given that:

u = x - 4y and v = -y - 4x  

$$\frac{\partial u}{\partial x} = 1$$
 and  $\frac{\partial v}{\partial y} = -1$   
So,  $\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} = 1 - 1 = 0$ 

 $\Rightarrow$  Continuity equation is satisfied. Thus, the given flow field does describe a possible 2-D incompressible flow.

Also, 
$$\frac{\partial v}{\partial x} = -4$$
 and  $\frac{\partial u}{\partial y} = -4$   
Thus,  $\frac{\partial v}{\partial x} - \frac{\partial u}{\partial y} = -4 - (-4) = 0$   
 $\Rightarrow$  This shows that flow is irrotation

⇒ This shows that flow is irrotational. Hence, statement 2 is wrong.

#### 62. Ans: (b)

**Sol:** We know that for an adiabatic process:

$$\begin{aligned} \frac{T_2}{T_1} &= \left(\frac{P_2}{P_1}\right)^{\frac{\gamma-1}{\gamma}} = \left(\frac{v_1}{v_2}\right)^{\gamma-1} \\ T_2 &= T_1 \times \left(\frac{v_1}{v_2}\right)^{\gamma-1} = T_1 \times 2^{\gamma-1} \dots \dots (i) \\ P_2 &= P_1 \times 2^{\gamma} \dots \dots (ii) \\ \gamma &= 1.67 \text{ for He an Ne} \\ \gamma &= 1.4 \text{ for } O_2 \\ \text{From equation (i), } (T_2)_{\text{He, Ne}} > (T_2)_{O2} \\ \text{From equation (ii), } (P_2)_{\text{He, Ne}} > (P_2)_{O2} \end{aligned}$$

#### 63. Ans: (c)

Sol: Given data:

From continuity equation:

$$A_1 V_1 = A_2 V_2$$
$$V_2 = \left(\frac{d_1}{d_2}\right)^2 V_1$$
$$= \left(\frac{5}{4.5}\right)^2 \times 4.5 = \frac{2.5}{4.5} = 5.55 \text{ m/s}$$

Given that losses vary as the square of the velocity,

$$\frac{(\text{Losses})_{\text{pipe 2}}}{(\text{Losses})_{\text{pipe 1}}} = \frac{V_2^2}{V_1^2} = \frac{5.55^2}{4.5^2} = 1.52$$

 $\Rightarrow$  Thus, losses in 4.5 m diameter pipe are 52% greater than those in 5 m pipe.



#### 64. Ans: (d)

#### Sol:

- 1-D, steady heat conduction equation with internal thermal energy generation :
  - (1) For solid cylinder with internal heat generation :

$$T = -\frac{\dot{q}r^2}{4k} + c_2 \quad (Parabolic)$$

(2) For hollow cylinder without internal heat generation :

$$T = c_1 ln(r) + c_2$$
 (Logarithmic)

(3) For solid sphere :

$$T = -\frac{\dot{q}r^2}{6k} + c_2 \quad (Parabolic)$$

- 65. Ans: (a)
- 66. Ans: (b)

#### Sol:

- The entropy change of an isolated system is the sum of entropy changes of its components and it always increases or, in limiting case of a reversible process, remains constant.
- A system and its surrounding always form an isolated system.

#### 67. Ans: (a)

**Sol:** The momentum equation with respect to accelerated control volume is

$$(-\mathrm{mg}) + (-\mathrm{ma}) = \dot{\mathrm{m}} \vec{\mathrm{V}}_{\mathrm{out}} - \dot{\mathrm{m}} \vec{\mathrm{V}}_{\mathrm{in}} + \frac{\partial}{\partial t} (\mathrm{m} \vec{\mathrm{V}})_{\mathrm{c.v}}$$

external inertia momentum change



Thus, from the above equation it is evident that external forces acting on rocket do not sum to zero and gravitational force is the only external force acting on the rocket during its propulsion.

#### 68. Ans: (d)

Sol:

• Prandtl number is the property of the fluid.

$$\Pr = \frac{\mu c_p}{k}$$

All  $\mu$ ,  $c_p$  and k are the properties of the fluid.

• For laminar flow,

$$\frac{\delta}{\delta_{\star}} = (\Pr)^{1/3}$$

when Pr > 1

$$\delta > \delta_t$$

Here,

 $\delta$  = hydrodynamic boundary layer thickness

 $\delta_t$  = thermal boundary layer thickness





#### 69. Ans: (a)

Sol:

- Integrating total stress (shear stress + normal stress (pressure)) over area gives the net force.
- The net force can be resolved into two components. The component along the direction of flow is called drag force and the normal component is called lift.
- Thus, both statements are correct and statement (II) is the correct explanation of statement (I)



According to the above figure, both the statements are correct but statement - II is not a right explanation of statement - (I).

#### 71. Ans: (a)



Referring to the exit velocity triangle it is evident that for  $\alpha_2$  other than 90°,  $V_{w2}$  is always present and the rejected kinetic energy will be more than that corresponding to  $\alpha_2 = 90^\circ$ . This will result in less efficiency.

#### 72. Ans: (c)

#### Sol:

• Exergy of heat (Q) supplied =  $Q\left(1 - \frac{T_0}{T_H}\right) =$ 

Work output of a Carnot heat engine operating between the reservoir (At temperature  $T_H$ ) and the environment (At temperature  $T_0$ ).

• Exergy of an isolated system will always decrease.

#### 73. Ans: (a)

Sol:



For Kaplan turbine

 $V_{f1} = V_{f2} = \frac{Q}{\frac{\pi}{4} \left( D_0^2 - D_i^2 \right)}$ 

 $u_1 = u_2 = r\omega$ 

$$V_{w2} = 0, V_{w1} > 0$$

$$\tan \beta_1 = \frac{V_{f1}}{u_1 - V_{w1}},$$
$$\tan \beta_2 = \frac{V_{f2}}{u_2} = \frac{V_{f1}}{u_1}$$

$$\frac{\mathbf{V}_{f1}}{\mathbf{u}_1 - \mathbf{V}_{w1}} > \frac{\mathbf{V}_{f1}}{\mathbf{u}_1}$$
$$\therefore \beta_1 > \beta_2$$

74. Ans: (c)

#### Sol:

- Air vessel on suction pipe eliminates the fluctuations in velocity in suction pipe. This reduces frictional head loss. Hence, pumping power is reduced.
- Air vessel attached to suction pipe has no effect on discharge (quantity of flow rate). Thus, statement (II) is wrong.
- It can be shown that for single acting reciprocating pump frictional head loss reduces by 85% and for double acting pump it reduces by 39% with use of air vessels.

#### 75. Ans: (a)

Sol: Temperature distribution inside the slab :



As Q = constant,	
k = constant	and
A = constant	
then $\frac{dT}{dx} = constant$	



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