



CIVIL ENGINEERING



GATE | PSUs

GEOTECHNICAL
ENGINEERING

Volume - I : Study Material with Classroom Practice Questions

Geotechnical Engineering

Solutions for Volume : I Classroom Practice Questions

Chapter- 2 Definitions and Properties of Soil

01. Ans: (d)

Sol:

$$\gamma = \gamma_d (1 + w) \quad \gamma_d \text{ is constant}$$

$$\gamma \propto 1 + w$$

$$\frac{\gamma_2}{\gamma_1} = \frac{1 + w_2}{1 + w_1} \Rightarrow \frac{\gamma_2}{1.8} = \frac{1.1}{1.05}$$

$$\gamma_2 = 1.88 \text{ gm/cc}$$

02. Ans: (a)

Sol:

$$\gamma \propto 1 + w$$

$$\frac{\gamma_2}{\gamma_1} = \frac{1 + w_2}{1 + w_1}$$

$$\frac{2.12}{2.24} = \frac{1 + w_2}{1.12}$$

$$w_2 = 0.06 = 6\%$$

03. Ans: 11.87%

Sol:

To find initial porosity

$$\gamma_d = \frac{\gamma_w \cdot G}{1 + e}$$

$$16 = \frac{9.80 \times 2.67}{1 + e}$$

$$e = 0.637$$

$$n_1 = \frac{e}{1 + e} = \frac{0.637}{1 + 0.637} = 0.388 \approx 38.8\%$$

$$e = \frac{V_v}{V_s} = 0.637$$

$$n = \frac{V_v}{V} \Rightarrow 0.388 = \frac{V_v}{1} \Rightarrow V_v = 0.388$$

Coarse sand

$$V_s = V - V_v = 1 - 0.388 = 0.611 \text{ m}^3$$

Dry silty soil:

$$\gamma_s = G \cdot \gamma_w$$

$$= 2.67 \times 9.80 = 26.16 \text{ kN/m}^3$$

$$V_s = \frac{W_s}{\gamma_s} = \frac{5.5}{26.16} = 0.21 \text{ m}^3$$

Wet Clay:

$$\text{Water content, } w = \frac{W_w}{W_s}$$

$$0.1 = \frac{W - W_s}{W_s}$$

$$W_s = 1.3636 \text{ kN}$$

$$V_s = \frac{1.3636}{2.55 \times 9.8} = 0.0545 \text{ m}^3$$

After compaction:

$$\text{Total volume, } V = 1.2 \text{ m}^3$$

$$V_s = 0.611 + 0.21 + 0.0545 = 0.875 \text{ m}^3$$

$$V_s + V_v = V$$

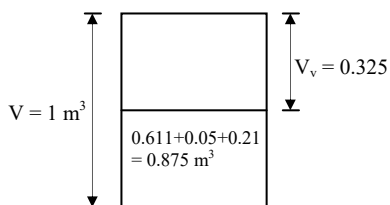
$$V_v = V - V_s$$

$$= 1.2 - 0.875$$

$$= 0.325$$

$$\text{Final porosity, } n_2 = \frac{0.325}{1.2} \times 100 = 27\%$$

Reduction in porosity = $38.8\% - 27\% = 11.8\%$



04. Ans: (b)

Sol: wt of sample = 0.18 kg

Volume = 10^{-4} m^3

$$\gamma_d = 1600 \text{ kg/m}^3$$

water added additionally = 0.02 kg

$$\gamma_d = \frac{W_s}{V} \Rightarrow 1600 = \frac{W_s}{10^{-4}}$$

$$\therefore W_s = 0.16 \text{ kg}$$

wt of water present initially = $0.18 - 0.16$
= 0.02 kg

Total wt of water present = $0.02 + 0.02 \text{ kg}$
= 0.04 kg

$$\begin{aligned} \text{Final water content} &= \frac{W_w}{W_s} \times 100 \\ &= \frac{0.04}{0.16} \times 100 \\ &= 25\% \end{aligned}$$

Common data for Questions 05 & 06

05. Ans: (c)

Sol: Wt of clay = 34.62 gm = W

Given dry wt = 20.36 gm = W_d

Volume = 24.66 cc

$G = 2.68$

Net wt = $34.62 - 20.36$

$W = 14.26 \text{ gms}$

$$\text{Water content of soil} = \frac{W - W_d}{W_d} \times 100$$

$$w = \frac{14.26}{20.36} \times 100 = 70\%$$

$$\gamma = \frac{W}{V} = \frac{34.62}{24.66} = 1.403$$

$$e = \frac{wG}{S_r}$$

$$\therefore e \cdot S_r = 0.70 \times 2.68 = 1.876$$

$$\gamma = \gamma_w \left[\frac{G + e \cdot S_r}{1 + e} \right]$$

$$1.403 = 1 \left[\frac{2.68 + 1.876}{1 + e} \right]$$

$$\therefore e = 2.25$$

06. Ans: (d)

$$\text{Sol: } S_r = \frac{1.876}{2.25} = 0.8345$$

$$S_r = 83.45\%$$

Common data for Questions 07 & 08

07. Ans: (c)

Sol:

Volume of solids in sample A:

Total volume $V = V_s + V_v$

$$\text{Void ratio, } e = \frac{V_v}{V_s}$$

$$V_s = V_v$$

Total volume $V = 1 \text{ m}^3$



$$\therefore V_s = 1 - V_v$$

$$V_s = \frac{1}{2} \text{ m}^3$$

Volume of solids in sample B:

$$\text{Total volume, } V = V_s + V_v$$

$$1 = V_s + V_v$$

$$V_v = 1 - V_s$$

$$\text{Void ratio, } e = \frac{V_v}{V_s}$$

$$1.5 V_s = V_v$$

$$1.5 V_s = 1 - V_s$$

$$2.5 V_s = 1$$

$$V_s = \frac{1}{2.5} = 0.4 \text{ m}^3$$

After compaction solids volume cannot change total volume after compaction $V = 1 \text{ m}^3$

$$V_s = 0.4 + 0.5 = 0.9 \text{ m}^3$$

$$\text{Porosity, } n = \frac{V_v}{V} = \frac{0.1}{1} = 0.1$$

08. Ans: (a)

$$\text{Sol: Water content of mixed sample} = \frac{W_w}{W_{\text{solids}}}$$

Weight of solids cannot change weight of solids in sample of water content 50%

$$\text{Water content, } w = \frac{W_{w_1}}{W_{\text{solid}_1}}$$

$$0.5 = \frac{W_w}{W_{\text{solids}_1}}$$

$$0.5 W_{\text{solids}_1} = W_w$$

Total weight of sample, $W = 1 \text{ kg}$

$$W_s + W_w = 1 \text{ kg}$$

$$0.5 W_s = 1 - W_s$$

$$W_s = \frac{1}{1.5} = 0.667 \text{ kg}$$

Weight of solids in sample of water content 80%

$$w = \frac{W_w}{W_s} \Rightarrow 0.8 W_s = W_w$$

$$0.8 W_s = 1 - W_s$$

$$W_s = \frac{1}{1.8} = 0.556 \text{ kg}$$

$\therefore$ Total weight of mix = 2 kg

$$\begin{aligned} \text{Solids weight of mix} &= 0.667 + 0.556 \\ &= 1.223 \end{aligned}$$

$$\begin{aligned} \therefore \text{water content of mix} &= \frac{W_w}{W_s} = \frac{2 - 1.223}{1.223} \\ &= 63.6\% \end{aligned}$$

Common data for Questions 09 & 10

09. Ans: (b)

Sol: In Borrow pit

$$\gamma = 1.75 \text{ g/cc}$$

$$w_1 = 12\%$$

$$G = 2.7; V_1 = ?$$

After compaction

$$w_2 = 18\%$$

$$\gamma_{d_2} = 1.65 \text{ g/cc}$$

$$V_2 = 1000 \text{ m}^3$$



$$\frac{V_1}{V_2} = \frac{\gamma_{d_2}}{\gamma_{d_1}}$$

$$\gamma_{d_1} = \frac{\gamma}{1+w} = \frac{1.75}{1+0.12} = 1.56$$

$$\frac{V_1}{1000} = \frac{1.65}{1.56}$$

$$\therefore V_1 = 1056 \text{ m}^3$$

10. Ans: (c)

Sol: Amount of water to be added

$$= \gamma_{d_2} V[w_2 - w_1]$$

$$= 1.65 \times 1000 [0.18 - 0.12]$$

$$= 99 \text{ tons} \quad (\because 1 \text{ g/cc} = 1 \text{ t/m}^3)$$

11. Ans: (c)

Sol: $\gamma_1 = 1.66$;

$$w_1 = 8\%$$

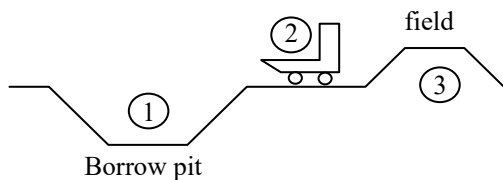
$$\gamma_2 = 1.15$$

$$w_2 = 6\%$$

$$\gamma_3 = 1.82$$

$$w_3 = 14\%$$

$$v_3 = 100 \text{ m}^3$$



$$\frac{v_1}{v_3} = \frac{1+e_1}{1+e_3} = \frac{\gamma_{d_3}}{\gamma_{d_1}}$$

$$\gamma_{d_1} = \frac{\gamma_1}{1+w_1} = \frac{1.66}{1+0.08} = 1.537$$

$$\gamma_{d_2} = \frac{1.15}{1+0.06} = 1.084$$

$$\gamma_{d_3} = \frac{1.82}{1+0.14} = 1.59$$

$$\frac{V_1}{V_3} = \frac{\gamma_{d_3}}{\gamma_{d_1}}$$

$$\frac{V_1}{100} = \frac{1.59}{1.54}$$

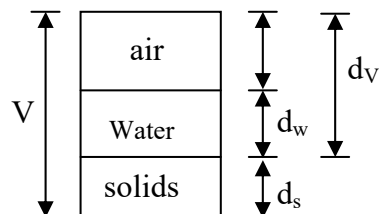
$$V_1 = 104.3 \text{ m}^3$$

$$V_2 = \frac{1.596}{1.084} \times 100 = 147.2 \text{ m}^3$$

$$\text{No. of truck load} = \frac{147.2}{6} = 24.5 = 25 \text{ nos.}$$

12. Ans: (c)

Sol:



$$e = 0.51$$

$$S_r = 80\%$$

$$d_w = 1 \text{ m}$$

$$S_r = \frac{d_w}{d_v} = \frac{1}{d_v} = 0.80$$

$$\therefore d_v = 1.25$$

$$e = \frac{d_v}{d_s} = \frac{1.25}{d_s} = 0.5$$

$$d_s = 2.5$$

$$\therefore \text{Total } d = d_s + d_v = 2.5 + 1.25 = 3.75 \text{ m}$$



Common data for Questions 13 & 14

13. Ans: (d)

Sol: volume of cube = $5^3 = 125 \text{ cm}^3$

$$W_d = 135 \text{ g}; W = 195 \text{ g}$$

$$\text{water content} = \frac{W - W_d}{W_d} \times 100$$

$$e \times S_r = w G$$

$$\therefore e = 0.44 G$$

$$\frac{\gamma_{\text{sat}}}{\gamma_w} = \frac{G + e}{1 + e}$$

$$\gamma_{\text{sat}} = \frac{\text{Saturated wt of cube}}{\text{volume of cube}}$$

$$= \frac{195}{5^3} = \frac{195}{125} \text{ g/cc}$$

$$\therefore \frac{195}{125} = \frac{G + 0.44 G}{1 + 0.44 G}$$

$$\therefore G = 2.07$$

14. Ans: (c)

Sol: $e \times S_r = 0.44 G$

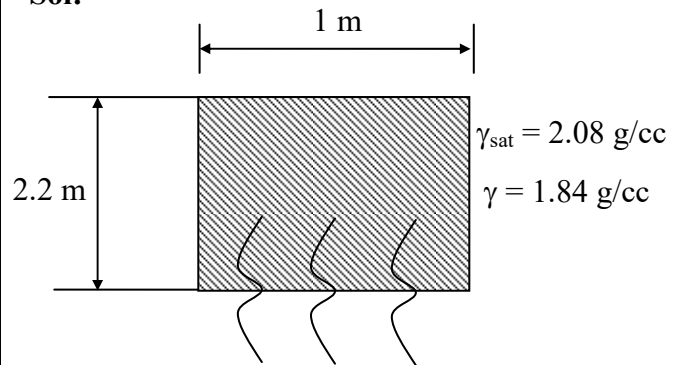
$$e = 0.44 G$$

$$e = 0.44 \times 2.07$$

$$\therefore e = 0.92$$

15. Ans: 528

Sol:



$$\begin{aligned} \text{Volume of soil} &= 1 \times 2.2 \\ &= 2.2 \times 10^6 \text{ cm}^3 \end{aligned}$$

$$\text{Initial cut of soil} = V \gamma_1$$

$$\text{Final cut of soil} = V \gamma_2$$

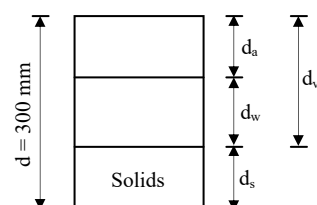
Draining of water (change in weight)

$$\begin{aligned} &= V (\gamma_1 - \gamma_2) \\ &= 2.2 \times 10^6 (2.08 - 1.84) \\ &= 528 \times 10^3 \text{ gm} \end{aligned}$$

$$\begin{aligned} \text{Volume of water} &= 528 \times 10^3 \text{ cm}^3 \\ &= 528 \text{ lit} \end{aligned}$$

16. Ans: 48 mm

Sol:





$$n = \frac{e}{1+e} = 0.4$$

$$d_v = nd = 0.4 \times 300 = 1200 \text{ mm}$$

$$s = \frac{d_w}{d_v}$$

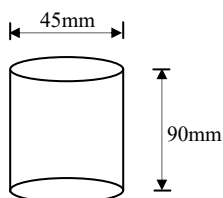
$$d_w = sd_v = 0.6 \times 120 = 72 \text{ mm}$$

$$d_a = d_v - d_w = 120 - 72 = 48 \text{ mm}$$

$\therefore$ rainfall depth required = 48 mm

17. Ans: $W_d = 240.45$ and $W_w = 28.85$

Sol:



Volume of soil

$$= \frac{\pi}{4} \times 45^2 \times 90 = 143138.81 \text{ mm}^3$$

$$= 143.13 \text{ cm}^3$$

$$\rho_w = 1 \text{ gm/cc}$$

$$\rho_d = (1 - n_a) \frac{\rho_w \cdot G}{1 + w \cdot G}$$

$$= (1 - 0.18) \frac{1 \times 2.72}{1 + 0.12 \times 2.72} = 1.68 \text{ gm/cc}$$

$$\therefore \rho = 1.68 (1 + 0.12) = 1.88 \text{ gm/cc}$$

$\therefore$ weight of dry solids

$$W_d = \rho_d \times V$$

$$= 1.68 \times 143.13$$

$$= 240.45 \text{ gm}$$

Weight of soil

$$= \rho \times V$$

$$= 1.68 \times 143.13$$

$$= 269.3 \text{ gm}$$

Weight of water

$$W_w = w \times W_s$$

$$= 0.12 \times 240.45$$

$$= 28.85 \text{ gm}$$

Chapter- 4 Index Properties of Soil

01. Ans: (a)

Sol:

At L.L $w_L = 60\%$,

$$e_1 = \frac{w_L \cdot G}{S} = 0.6G$$

$$w_s = 25\%, \quad e_2 = 0.25G$$

$$\frac{V_1}{V_2} = \frac{1 + e_1}{1 + e_2}$$

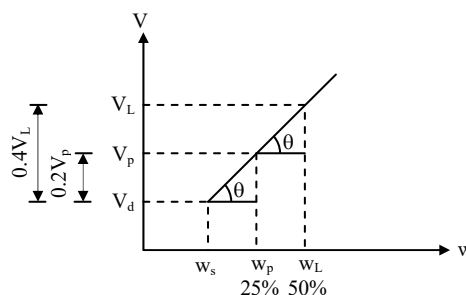
$$\frac{10}{6.5} = \frac{1 + 0.6G}{1 + 0.25G}$$

$$G = 2.5$$

Common data for Questions 02 & 03

02. Ans: (a)

Sol:





$$V_L - V_p = 0.4 V_L - 0.2 V_p$$

$$0.6 V_L = 0.8 V_p$$

$$\therefore V_L = \frac{0.8}{0.6} V_p$$

$$\therefore V_L = 1.33 V_p$$

$$V_p = 0.2 V_p + V_d$$

$$0.8 V_p = V_d$$

$$\frac{w_p - w_s}{V_p - V_d} = \frac{w_L - w_p}{V_L - V_p}$$

$$\frac{25 - w_s}{0.2 V_p} = \frac{50 - 25}{0.4 V_L - 0.2 V_p}$$

$$\frac{25 - w_s}{0.2 V_p} = \frac{25}{0.53 V_p - 0.2 V_p}$$

$$\frac{25 - w_s}{0.2 V_p} = \frac{25}{0.33 V_p}$$

$$w_s = 9.9 \approx 10\%$$

03. Ans: (c)

Sol:

$$S.R = \frac{\frac{V_l - V_d}{V_d} \times 100}{w_l - w_s}$$

$$= \frac{\frac{V_p - V_d}{V_d} \times 100}{w_p - w_s}$$

$$= \frac{\frac{V_p - 0.8 V_p}{0.8 V_p} \times 100}{25 - 10}$$

$$= \frac{\frac{0.2 V_p}{0.8 V_p} \times 100}{25 - 10}$$

$$= \frac{0.2}{15 \times 0.8} \times 100$$

$$= \frac{0.2}{12} \times 100 = \frac{20}{12} = 1.66$$

Common data for Questions 04, 05 & 06

04. Ans: (c)

Sol: G_m = Mass specific gravity = 1.88

Water content, $w = 40\%$

On oven drying, mass specific gravity drops to = 1.74

G of clay = ?

$$e = \frac{w_s \cdot G}{S_r} = 0.40 \times G$$

$$\gamma_{sat} = \frac{\gamma_w (G + e)}{1 + e}$$

$$1.88 = \frac{G + 0.40 G}{1 + .4 G}$$

$$1 + 0.4 G = \frac{G(1 + 0.4)}{1.88}$$

$$G = 2.90$$

05. Ans: (a)

Sol: $w_s = ?$

$$e = 0.4 \times 2.90$$

$$e = 1.16 \Rightarrow e = w_s G$$

$$w_s = \left(\frac{1}{G_m} - \frac{1}{G} \right) \times 100$$

$$= \left(\frac{1}{1.74} - \frac{1}{2.90} \right) \times 100$$

$$= 22.98\%$$

$$w_s = 23\%$$



06. Ans: (c)

Sol: Shrinkage ratio $SR = ?$

$$\text{Shrinkage ratio} = \frac{\gamma_d}{\gamma_w} = G_m = 1.74$$

Common Data for Questions 07, 08 & 09

07. Ans: (b)

Sol:

Initial weight of saturated soil,

$$W_1 = 95.6 \text{ gm}$$

Initial volume of saturated soil,

$$V_1 = 68.5 \text{ cc}$$

Final dry weight = 43.5 gm = W_d

Final dry volume = 24.1 cc = V_d

$w_s = ?$

$$w_s = \left[\frac{W_1 - W_d}{W_d} - \left(\frac{V_1 - V_d}{V_d} \right) \gamma_w \right] \times 100$$

$$= \left[\frac{95.6 - 43.5}{43.5} - \left(\frac{68.5 - 24.1}{43.3} \right) \right] \times 100$$

$$w_s = 17.7\%$$

08. Ans: (c)

Sol: $\gamma_d = \frac{W_d}{V_d} = \frac{43.5}{24.1} = 1.80 \text{ gm/cc}$

$$G_m = \frac{\gamma_d}{\gamma_w} = \frac{1.80}{1} = 1.80$$

$$W_s = \left(\frac{1}{G_m} - \frac{1}{G} \right) \times 100$$

$$17.7 = \left(\frac{1}{1.80} - \frac{1}{G} \right) \times 100$$

$$G = 2.65$$

09. Ans: (c)

Sol: To find initial and final void ratio = ?

To find e_1 :

$$\gamma_{\text{sat}} = \frac{w_1}{v_1} = \frac{95.6}{68.5} = 1.39 \text{ g/cc}$$

$$1.39 = \frac{2.67 + e_1}{1 + e_1}$$

$$e_1 = 3.28 \approx 3.15$$

To find e_2 :

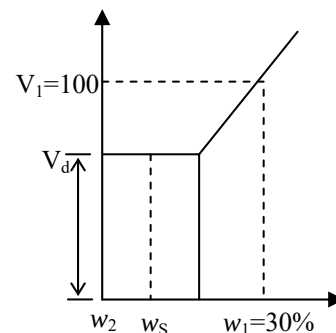
$$e_2 = w_s G$$

$$= 0.17 \times 2.65$$

$$= 0.47$$

10. Ans: (c)

Sol:





Given:

$$V_1 = 100 \text{ cc,}$$

$$w_1 = 30\%$$

$$w_s = 18\%$$

$$G = 2.72$$

$$V_2 = ?$$

$$w = 15\%$$

Let e_1 be void ratio at water content of 30%

$$e_1 = \frac{w_1 G}{S_r} = \frac{0.30 \times 2.72}{1} = 0.816$$

Let e_2 be void ratio, at w_s

$$e_2 = \frac{w_s G}{S_r} = \frac{0.18 \times 2.72}{1} = 0.489$$

$$\frac{V_1}{V_2} = \frac{1 + e_1}{1 + e_2}$$

$$V_2 = \frac{100 \times (1 + 0.489)}{1 + 0.816} = 82 \text{ cc}$$

11. Ans: 21.63%. 347 kN and $w = 25.24\%$

Sol:

$$n = 36\%$$

$$e = \frac{n}{1 - n} = \frac{0.36}{1 - 0.36} = 0.563$$

$$G = 2.6$$

$$w_1 = 11\%$$

Let w_2 be w.c @ full saturation

$$e = \frac{w_2 \cdot G}{s} = w_2 = 0.216 = 21.6\%$$

$$\gamma_d = \gamma_w \left(\frac{G}{1 + e} \right)$$

$$= 9.81 \left(\frac{2.6}{1 + 0.563} \right) = 16.31 \text{ kN/m}^3$$

To rise w.c w_1 to w_2

The weight of water to be added additionally

$$= w_s(w_2 - w_1)$$

$$= \gamma_d \cdot V(w_2 - w_1)$$

$$= 16.31 \times 200 (0.216 - 0.11)$$

$$= 346 \text{ kN}$$

$$\frac{V_2}{V_1} = \frac{1 + e_2}{1 + e_1} \Rightarrow V_2 = 1.06 V_1$$

$$\frac{1.06 V_1}{V_1} = \frac{1 + e_2}{1 + e_1}$$

$$e_2 = 0.657$$

$$e_2 = \frac{w_3 G}{s}$$

$$0.657 = \frac{w_3 \times 2.6}{1}$$

$$w_3 = 0.254 = 25.4\%$$

12. Ans: 15.71 kN/m², 10.1 cm

Sol:

$$(a) I_D = \frac{e_{\max} - e}{e_{\max} - e_{\min}}$$

$$0.36 = \frac{0.91 - e}{0.91 - 0.42}$$

$$e = 0.734$$

$$\gamma_d = \frac{\gamma_w \cdot G}{1 + e} = \frac{9.81 \times 2.68}{1 + 0.734} = 15.71 \text{ kN/m}^3$$



(b)

$$0.66 = \frac{0.91 - e}{0.91 - 0.42}$$

$$e = 0.587$$

$$\frac{V_2}{V_1} = \frac{1 + e_2}{1 + e_1}$$

$$\frac{AH_2}{AH_1} = \frac{1 + e_2}{1 + e_1}$$

$$\frac{H_2}{1.2} = \frac{1 + 0.587}{1 + 0.734}$$

$$H_2 = \left(\frac{1.587}{1.734} \right) \times 1.2 = 1.098 \text{ m}$$

$$\Delta H = H_2 - H_1$$

$$= 10.1 \text{ cm}$$

Chapter- 5 Soil Classification

01. Ans: (c)

Sol: $w_L = 60\%$

$$w_P = 20\%$$

$$I_P \text{ of soil} = w_L - w_P$$

$$= 60 - 20 = 40\%$$

$$I_P \text{ of A line} = 0.73(w_L - 20\%)$$

$$= 0.73(60 - 20)$$

$$= 29.2$$

As the soil lies above A line chart and its liquid limit is 60%

The given soil is CH.

Common data for Q 02 & 03

02. Ans: 9%

Sol:

$$C_u = 18, \quad C_c = 2, \quad I_p = 6$$

From question it is given as gravelly soil.

For GW, $C_v > 4$ and $C_c = 1 - 3$

$$18 > 4 \quad \text{and} \quad C_c = 2$$

$\therefore$ Soil is GW

But lines lies 5% and 12%, border line cases require dual symbol

For GM Atterberg limits fall below A line or $I_p < 4$

For GC Atterberg limits above A-line and $I_p > 7$

Here $I_p = 6$ for GC I_p must be greater

$\therefore$ Soil is GW-GM

03. Ans: (GM)

Sol: Fine fraction = 45%

$$\text{Coarse fraction} = 100 - 45 = 55\%$$

$\therefore$ Soil is coarse grained

% passing 4.75 mm sieve = 58% (out of total soil)

$$\begin{aligned} \text{\% retained or 4.75 mm sieve} &= 100 - 58\% \\ &= 42\% \text{ (out of total)} \end{aligned}$$

$$\text{Gravel + sand} = 55\%$$

$$\text{\% of Gravel} = 42\% \text{ (out of total soil)}$$

$\therefore$ % retaining on 4.75 mm sieve out of coarse fraction

$$= \frac{42}{55} \times 100 = 76\%$$

(out of coarse fraction)



∴ it is gravel

$$w_L = 40\%, \quad w_p = 30\%$$

$$A\text{-line} = 0.73 (w_L - 20)$$

$$= 0.73 (40 - 20) = 14.6\%$$

$$I_p = 40 - 30 = 10\%$$

Point plots below A-line silty gravel (GM)

Chapter- 6 Permeability

01. Ans: (b)

Sol: temperature increases, γ_w decreases to 90%

& μ decreases to 90%

$$\gamma_{w_2} = \frac{90}{100} \gamma_{w_1}; \quad \left[K \propto \frac{\gamma_w}{\mu} \right]$$

$$\mu_2 = \frac{75}{100} \mu_1$$

$$\frac{K_2}{K_1} = \frac{\gamma_{w_2}}{\gamma_{w_1}} \times \frac{\mu_1}{\mu_2}$$

$$\frac{K_2}{K_1} = \frac{90}{100} \times \frac{100}{75}$$

$$K_2 = 1.2 K_1$$

$$K_2 = 20\% \text{ (increases by 20\%)}$$

02. Ans: $1.35 \times 10^{-4} \text{ m}^3/\text{sec}/\text{m}$

Sol:

$$H = 7 \text{ m}, \quad H_1 = 2 \text{ m}, \quad h = 3 \text{ m}, \quad L = 40 \text{ m}$$

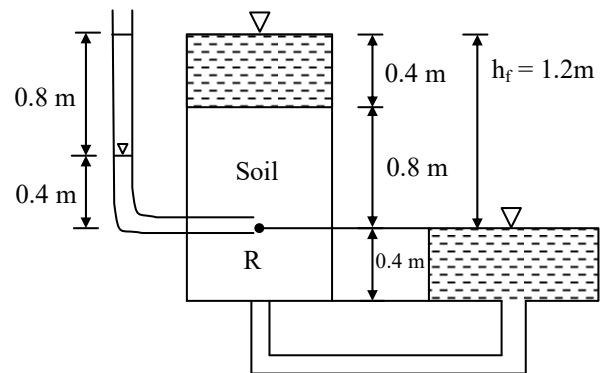
$$i = \frac{h}{L} = \frac{3}{40} = 0.075$$

$$k = 0.09 \text{ cm/sec} = 0.09 \times 10^{-2} \text{ m/sec}$$

$$\begin{aligned} \frac{Q}{1\text{m}} &= k i \frac{A}{1} \\ &= \frac{0.09 \times 10^{-2} \times 0.075 \times 2 \times 1}{1\text{m}} \\ &= 1.35 \times 10^{-4} \text{ m}^3/\text{sec}/\text{m} \end{aligned}$$

Common data for Questions.Q03 & Q04

03. Ans: (a)



$$i = \frac{h_f}{L} = \frac{1.2}{1.2} = 1$$

Loss of head for a seepage length of 0.8 m

$$\text{is } h_f = i \times L = 1 \times 0.8 = 0.8 \text{ m}$$

Pressure head at R is 0.4 m

Assuming datum at d/s water surface,

Elevation head at R is zero

i.e., Datum head = 0

$$\begin{aligned} \text{Total head at R} &= \frac{P}{\gamma_w} + Z \\ &= 0.4 + 0 = 0.4 \end{aligned}$$

If Datum head is chosen at bottom of soil,
then Datum (or) Elevation head = 0.4 m



Pressure head = 0.4

Total head at R = 0.4 + 0.4 = 0.8

04. Ans: (a)

Sol: Discharge velocity, $V = k \cdot i = k \times 1 = k$

Seepage velocity, $V_s = \frac{V}{n} = \frac{k}{0.50} = 2k$

05. Ans: 20

Sol: $k = 8.0$ m/day,

$h = 21.6$ m,

$Q = 162$ lit/day

$L = 96.3$ m,

$A = 180 \text{ cm}^2$, $x = ?$

$Q = kiA$

$$162 \times 10^{-3} = 8 \times \frac{h}{x} \cdot 180 (10^{-4})$$

$$162 \times 10^{-3} = 8 \times \frac{21.6}{x} \times 180 \times 10^{-4}$$

$$x = 19.2 \text{ m}$$

$$\% = \frac{x}{\ell} \times 100 = \frac{19.2}{96.3} \times 100$$

$$\% = 19.33$$

$$\% \simeq 20\%$$

06. Ans: (d)

Sol: Permeability, $k = \frac{CD_{10}^2}{1+e} \left(\frac{\gamma_w}{\mu} \right)$

$$k = k_o \left(\frac{\gamma_w}{\mu} \right)$$

k_o = absolute/intrinsic permeability

$$4 \times 10^{-7} = k_o \times \frac{1}{0.091 \times 10^{-4}}$$

$$k_o = 0.36 \times 10^{-11}$$

07. Ans: 0.183 cm/sec and 0.094 cm/sec

Sol:

Weight of water collected in 1 minute = 6.18 N

Weight = volume $\times$ density

$$6.18 = \text{volume} \times 9810$$

$$\text{Volume} = \frac{6.18}{9810} = 6.3 \times 10^{-4} \text{ m}^3/\text{min}$$

$$Q = 1.05 \times 10^{-5} \text{ m}^3/\text{sec}$$

$Q = kiA$

$$1.05 \times 10^{-5} = k \times \frac{26}{20} \times \frac{\pi}{4} \times 0.075^2$$

$$k_{\text{at } 25^\circ\text{C}} = 1.83 \times 10^{-3} \text{ m/sec} = 0.183 \text{ cm/sec}$$

$$k \propto \left(\frac{e^3}{1+e} \right) \times \frac{1}{\mu}$$



At 25°C

at 20°C

$$K = 0.183 \text{ cm/sec}$$

$$k_2 = ?$$

$$n = 40\%$$

$$n_2 = 35\%$$

$$e = \frac{n}{n-1}$$

$$e_2 = \frac{0.35}{0.65} = 0.5384$$

$$v_1 = 0.9 v_{20^\circ\text{C}}$$

$$v_{20^\circ\text{C}}$$

$$\therefore \frac{k_2}{k_1} = \left(\frac{e^3}{1+e} \right)_2 \left(\frac{1+e}{e^3} \right)_1 \times \frac{\mu_1}{\mu_2}$$

$$= \frac{0.5384^3}{1.5384} \times \frac{1.667}{0.667^3} \times 0.9$$

$$k_2 = 0.094 \text{ cm/sec}$$

Assignment Solutions

01. Ans: (d)

Sol: $k \propto \frac{e^3}{1+e}$

$$\frac{k_2}{k_1} = \frac{0.6^3}{1.6} \times \frac{1.48}{0.48^3}$$

$$k_2 = 1.80 \times 0.02$$

$$= 0.036 \text{ cm/sec}$$

Chapter- 7 Effective Stress

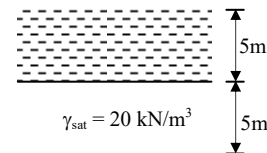
01. Ans: (d)

Sol: For wider area, effective stress remain same with the increase of depth.

$$\therefore \text{Effective stress at 2 m} = 36 \text{ kN/m}^2$$

02. Ans: (a)

Sol:

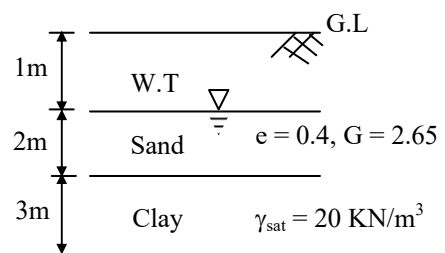


Effective vertical stress at 5 m depth below

$$\begin{aligned} \sigma' &= (\gamma_{\text{sat}} - \gamma_w) h \\ &= (20 - 10)5 \\ &= 50 \text{ kPa} \end{aligned}$$

03. Ans: (d)

Sol:



$$\begin{aligned} \gamma_{\text{sat}} \text{ of sand} &= \frac{\gamma_w (G + e)}{1 + e} \\ &= \frac{10(2.65 + 0.4)}{1 + 0.4} = 21.785 \text{ kN/m}^3 \end{aligned}$$

$$\gamma_d \text{ of soil above water table} = ?$$

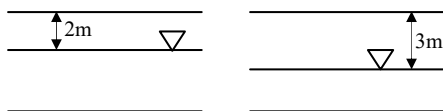


$$\gamma_d = \frac{\gamma_w G}{1+e} = \frac{10 \times 2.65}{1+0.4} = 18.92 \text{ kN/m}^3$$

Effective stress below G.L = ?

$$\begin{aligned}\sigma' &= \sigma - u \\ &= (1 \times 18.92) + (2 \times 21.785) + (20 \times 3) - (5 \times 10) \\ &= 72.49 \text{ kN/m}^2\end{aligned}$$

04. Ans: (d)



$$\begin{aligned}\text{Increase in effective stresses} &= \text{final effective stress} - \text{initial effective stress} \\ &= \text{change in effective stresses} \\ &= (\gamma_d - \gamma_w)(3 - 2) \\ &= (16 - 10) \times 1 \\ &= 6 \text{ kPa}\end{aligned}$$

05. Ans: (c)

Sol:

$$h_c \propto \frac{1}{D_{10}} \text{ where } D_{10} \text{ in cm, } h_c = \text{cm}$$

$$\frac{h_{c_2}}{h_{c_1}} = \frac{(D_{10})_1}{(D_{10})_2} = \frac{0.006}{0.01}$$

$$\begin{aligned}h_{c_2} &= 0.6 \times 60 \\ &= 36 \text{ cm}\end{aligned}$$

06. Ans:

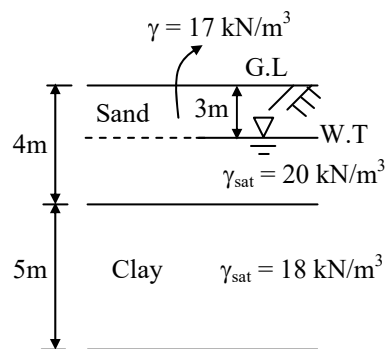
Sol: Take dia of voids 20% of effective grain size.

$$d = \frac{20}{100}(0.002) = 0.0004 \text{ mm} = 0.00004 \text{ cm}$$

$$h_c = \frac{0.3}{d} = \frac{0.3}{0.00004} = 7500 \text{ cm} = 75 \text{ m}$$

$$P = -\gamma_w h = -75 \times 10 = -750 \text{ kN/m}^2$$

Common Data for Questions Q 07 & Q 08



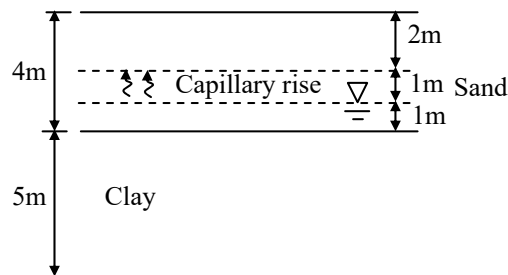
07. Ans: (b)

Sol: σ' at 9m depth below G.L = ?

$$\begin{aligned}\sigma' &= \sigma - u \\ &= (17 \times 3) + (20 \times 1) + (18 \times 5) - (6 \times 9.81) \\ \sigma' &= 102.14 \text{ kN/m}^2\end{aligned}$$

08. Ans: (a)

Sol:





$\Delta\sigma'$ at 9 m depth of soil below G.L = ?

Effective stress after capillary rise at 9m = σ'

$$\sigma' = \sigma - u$$

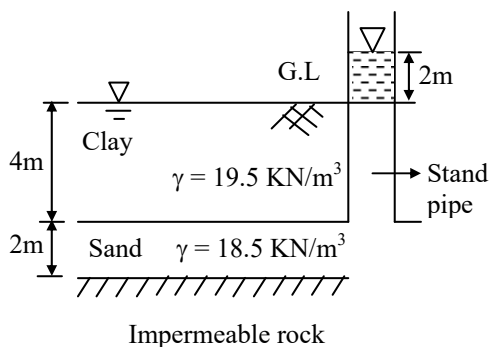
$$= (2 \times 17) + (2 \times 20) + (18 \times 5) - 6 \times 9.81$$

$$\sigma' = 105.14$$

Increase in effective stress = $105.14 - 102.14$

$$\Delta\sigma' = 3 \text{ kN/m}^2$$

Common Data for Questions Q 09 & Q 10



09. Ans: (d)

Sol: Effective stress at a depth of 6m = ?

$$\gamma_w = 10 \text{ kN/m}^3$$

$$\sigma' = \sigma - u$$

$$= (19.5) \times 4 + (18.5 \times 2) - (8 \times 10)$$

$$\sigma' = 35 \text{ kN/m}^2$$

10. Ans: (a)

Sol: $\Delta\sigma' = ?$ when artesian head in the stand is reduced by 1m

Total stress remains same.

Pore water pressure decreases by 10 kN/m^2

$\therefore$ Effective stress increases by 10 kN/m^2

$$\Delta\sigma' = 10 \text{ kN/m}^2$$

Assignment Solutions

05. Ans: (b)

Sol:

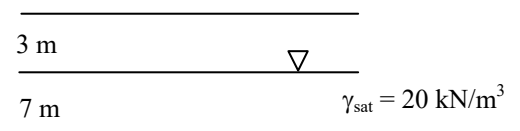
$$\sigma' = \sigma - u$$

$$100 = 20 \times h - 10(h) \quad (\text{Assume } \gamma_w = 10 \text{ kN/m}^3)$$

$$h = 10 \text{ m}$$

06. Ans: (b)

Sol:



$$\sigma' = \sigma - u$$

$$\sigma = 3 \times 18 + 20 \times 7$$

$$= 194 \text{ kN/m}^3$$

$$u = 7 \times 10 = 70 \text{ kN/m}^3$$

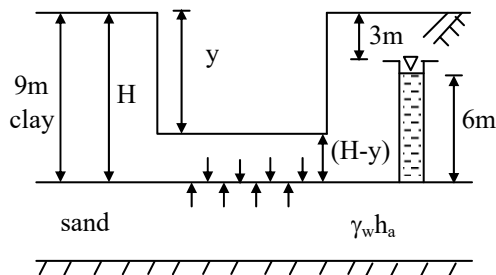
$$\sigma' = 194 - 70 = 124 \text{ kN/m}^3$$



Chapter- 8 Seepage Pressure and Critical Hydraulic Gradient

01. Ans: (c)

Sol:



To find depth of safe excavation:

$$\gamma = 20 \text{ kN-m}^3$$

Downward pressure = uplift pressure

$$\gamma (H - y) = \gamma_w h_a$$

$$20 (9 - y) = 10 \times 6$$

$$y = 6 \text{ m}$$

$\therefore$ Maximum depth of trench will be excavated without failure is 6 m.

02. Ans: (c)

$$\text{Sol: } 20 (9 - 7) = \gamma_w h_a$$

$$h_a = \frac{20 \times 2}{10} = 4 \text{ m}$$

$$\text{Water table to be lowered} = 6 - 4 = 2 \text{ m}$$

03. Ans: 35

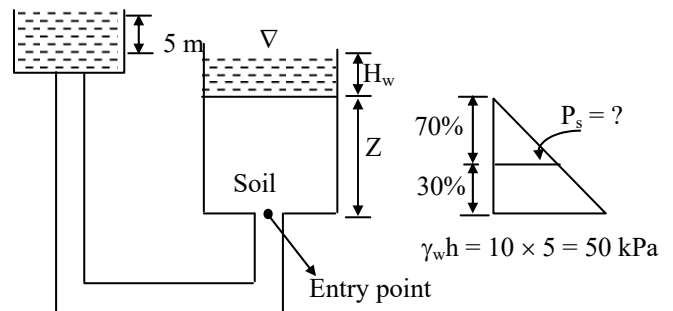
Sol: Given

Net head causing flow $h = 5 \text{ m}$

$$\text{Hydraulic gradient } i = \frac{h}{Z} = \frac{5}{Z} = 1$$

$$\Rightarrow Z = 5 \text{ m}$$

Seepage length $Z = 5 \text{ m}$



For 100% $\rightarrow 50 \text{ kPa}$

$$\text{For 70\%} \rightarrow \frac{50}{100} \times 70 = 35 \text{ kPa}$$

04. Ans: 1.91 m

Sol:

Depth of soil layer = 1200 mm

$$\text{FOS against piping} = \frac{i_c}{i}$$

$$Z = \frac{(G-1)(1-n)}{i}$$



$$i = \frac{1.65 \times 0.7}{2}$$

$$\frac{h}{z} = 0.5775$$

$$z = 3.1168 \text{ m}$$

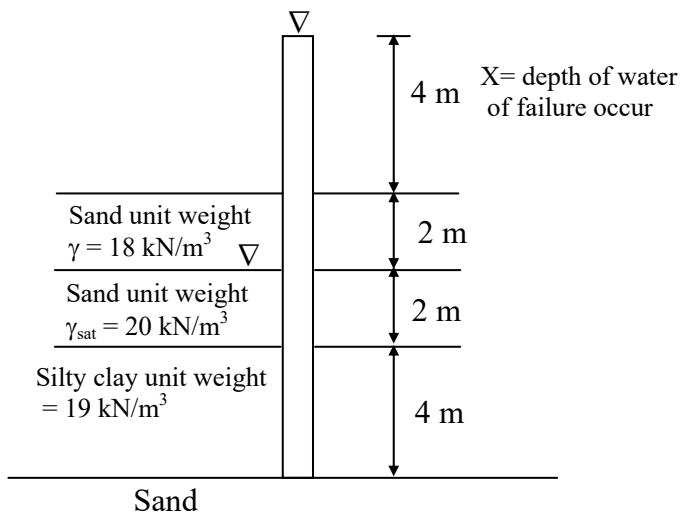
Additional depth of coarse sand

$$= 3.1168 - 1.2$$

$$= 1.9168 \text{ m}$$

05. Ans: 32 kPa & 7.2m

Sol:



I. At bottom of silty clay

Total stress

$$\sigma = 18 \times 2 + 20 \times 2 + 4 \times 19$$

$$= 152 \text{ kPa}$$

Pore water pressure

$$U = (4 + 2 + 2 + 4) \times 10 = 120 \text{ kPa}$$

Effective stress $\sigma' = \sigma - u$

$$= 152 - 120 = 32 \text{ kPa}$$

II. At x m of water failure occur. That is effective stress = 0

Total stress $\sigma = 152 \text{ kPa}$

Pore water pressure $u = 10 (x + 2 + 2 + 4)$

$$\sigma' = 0$$

$$\therefore \sigma - u = 0$$

$$\Rightarrow 152 = 10 [x + 2 + 2 + 4]$$

$$\therefore x = 7.2 \text{ m}$$

06. Ans: 2.2 & 10.38 kN/m³

Sol:

$$V_s = \frac{V}{n}$$

$$V = V_s \cdot n = 2.4 \times 10^{-4} \text{ cm/sec}$$

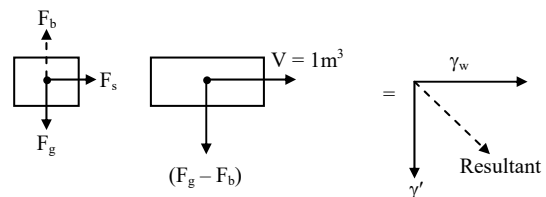
$$V = k \cdot i$$

$$V = k \left(\frac{h_A - h_B}{L} \right)$$

$$2.4 \times 10^{-4} = 1.2 \times 10^{-3} \left(\frac{5 - h_B}{14} \right)$$

$$h_B = 2.2 \text{ m}$$

$$i = 0.2$$



$$\text{Resultant} = \sqrt{\gamma'^2 + (i\gamma_w)^2} = 10.377 \text{ kN}$$



07. Ans: (d)

Sol:

Total stress at point A

$$= 0.7 \times 9.81 + 20.6 \times 1$$

$$= 27.467 \text{ KPa}$$

Neutral stress at point A = $\gamma_w h$

h = total head at point A

$$h = 1 + 0.7 + 0.75 = 2.45$$

$\therefore$ Effective stresses at point A, $\sigma' = \sigma - u$

$$= 27.467 - 9.81 \times 2.45$$

$$= 3.4325 \text{ KPa}$$

08. Ans: (c)

Sol:

Upward seepage force per unit volume

$$= \frac{\gamma_w h \times A}{\text{volume}} = \frac{\gamma_w h \times A}{A \times z} = \gamma_w i$$

$$= 9.81 \times 0.75$$

$$= 7.3575 \text{ kN/m}^3$$

09. Ans: (c)

Sol:

Critical state

Down ward force = upward seepage force

$$\gamma_{\text{sat}} \times 2 + \gamma_w h = \gamma_w \times 4.5$$

$$19 \times 2 + \gamma_w h = \gamma_w \times 4.5$$

$$\gamma_w (4.5 - h) = 38$$

$$h = 0.63 \text{ m}$$

Assignment Solutions

01. Ans: (d)

Sol: $F.O.S = \frac{i_c}{i}$

$$i_c = \frac{G-1}{1+e} = (G-1)(1-n)$$

$$= 1.65 \times 0.65$$

$$= 1.0725$$

$$i = \frac{h}{z} = \frac{0.85}{1.25} = 0.68$$

$$F = \frac{1.0725}{0.68} = 1.577$$

04. Ans: (c)

Sol:

$$i_c = (G-1)(1-n)$$

$$= (1.6)(1-0.375)$$

$$= 1$$



Chapter- 9 Seepage Analysis

01. Ans: 0.0086

Sol:

The quantity of flow into the pond per m² area

$$Q = ki$$

$$i = \frac{h}{z} = \frac{\text{head loss}}{\text{depth of clay}} = \frac{5\text{m}}{5\text{m}} = 1$$

$$\begin{aligned}\therefore Q &= 10^{-5} \times 10^{-2} \times 1 \\ &= 10^{-7} \text{ m}^3/\text{sec} \\ &= 10^{-7} \times 3600 \times 24 \text{ m}^3/\text{day} \\ &= 0.0086 \text{ m}^3/\text{day}\end{aligned}$$

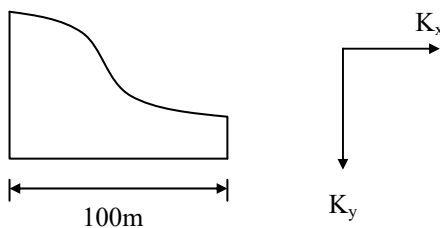
02. Ans: (a)

Sol: Given:

$$K_x = 3.45 \text{ m/day}; \quad K_y = 1.5 \text{ m/day}$$

$$B = 100 \text{ m}$$

Scale factor = 1:25 in vertical direction



$$b = B \sqrt{\frac{K_y}{K_x}}$$

$$b = 100 \sqrt{\frac{1.5}{3.45}} = 65.93 \text{ m}$$

$$\text{For scale } 1:25, \quad b = \frac{65.93}{25} = 2.63 \text{ m}$$

03. Ans: (b)

$$\text{Sol: } H = 18, \quad N_d = 9, \quad n = 3, \quad h = ?$$

$$\Delta H = \frac{H}{N_d}$$

$$h = H - n \cdot \Delta H = 18 - 3 \times \frac{18}{9} = 12 \text{ m}$$

04. Ans: (d)

Sol:

$$\text{Equivalent permeability } k = \sqrt{k_x k_y}$$

$$= \sqrt{6 \times 1.39 \times 1.39}$$

$$= 3.404 \text{ m/day}$$

$$\therefore \text{ Seepage per unit width, } q = kH \frac{N_f}{N_d}$$

$$= 3.404 \times 9 \times \frac{5}{8}$$

$$= 19.152 \text{ m}^3/\text{day/m}$$

$$\begin{aligned}\therefore \text{ Total seepage } &= q \times b = 19.152 \times 50 \\ &= 957.6 \text{ m}^3/\text{day}\end{aligned}$$

05. Ans: 3.933 , 3.367, 1.666, 1.6667,

$$\Delta Q = 2.2667 \times 10^{-5} \text{ m}^3/\text{sec/m}$$

Sol:

$$\text{(A) Total head loss } h = (4.5 - 1.1) = 3.4$$

$$\text{Head loss per one flow net } = \frac{3.4}{6} = 0.566 \text{ m}$$

$\therefore$ Piezeometric head at point

$$a = 4.5 - 0.566$$

$$= 3.933 \text{ m}$$

$\therefore$ Piezeometric head at point

$$b = 4.5 - 2 \times 0.566$$

$$= 3.367 \text{ m}$$

$\therefore$ Piezeometric head at point



$$c = 4.5 - 5 \times 0.566$$

$$= 1.6667 \text{ m}$$

∴ Piezometric head at point

$$d = 4.5 - 5 \times 0.566$$

$$= 1.6667 \text{ m}$$

(B) The rate of seepage through channel II per unit length

$$q = kH \frac{N_f}{N_d}$$

$$N_f = 1, \quad N_d = 6$$

$$q = 4 \times 10^{-3} \times 10^{-2} \times 3.4 \times \frac{1}{6}$$

$$= 2.266 \times 10^{-5} \text{ m}^3/\text{sec}/\text{m}$$

06. Ans: (a)

Sol:

$$\text{FOS against piping} = \frac{i_c}{i_{\text{exit}}}$$

$$i_c = \frac{G-1}{1+e} = 1.083$$

$$i_{\text{exit}} = \frac{\Delta H}{b}$$

$$\Delta H = \frac{H}{N_d} = \frac{4.2}{8} = 0.525$$

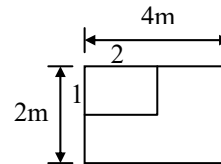
$$i_{\text{exit}} = \frac{0.525}{1.65} = 0.3181$$

$$\text{FOS} = \frac{1.083}{0.3181} = 3.4$$

Chapter- 10 Stress Distribution

01. Ans: (b)

Sol:



At centre:

$$\sigma_z = I q$$

$$Z = 5 \text{ m}$$

To Calculate I:

$$m = \frac{L}{Z} \quad n = \frac{B}{Z}$$

$$m = \frac{2}{5} \quad n = \frac{1}{5}$$

$$m = 0.4n = 0.2$$

From Table, $I = 0.0328$

$$\sigma_z = 0.0328 \times 8 \left. \vphantom{\sigma_z} \right\} \text{At corner of } 1 \times 2 \text{ rectangle}$$

$$= 0.2624$$

$$\sigma_z \text{ at centre} = 0.2624 \times 4 = 1.05 \text{ t/m}^2$$

At corner:

From given table, $I = 0.0931$

$$m = \frac{4}{5} = 0.8$$

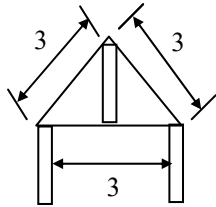
$$n = \frac{2}{5} = 0.4$$

$$\sigma_z = 0.0931 \times 8 = 0.744 \text{ t/m}^2$$



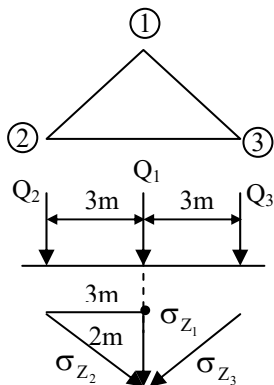
02. Ans: (d)

Sol:



Total load = 200t

Load on each column = $\frac{200}{3} = 66.66 \text{ t}$



$$\sigma_Z = \sigma_{Z_1} + \sigma_{Z_2} + \sigma_{Z_3}$$

$$\sigma_{Z_1} = \frac{Q}{Z^2} \frac{3}{2\pi} = \frac{66.66}{2^2} \frac{3}{2\pi} = 7.95 \text{ t/m}^2$$

$$\sigma_{Z_2} = \frac{Q}{Z^2} \frac{3}{2\pi} \left(\frac{1}{1 + \left(\frac{r}{Z} \right)^2} \right)^{(5/2)}$$

$$= \frac{66.66}{2^2} \frac{3}{2\pi} \left[\frac{1}{1 + \left(\frac{3}{2} \right)^2} \right]^{(5/2)}$$

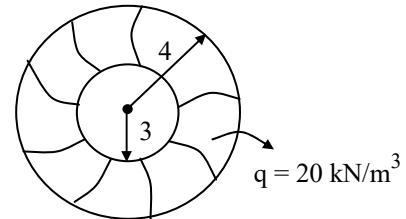
$$\sigma_{Z_2} = 0.417 \text{ t/m}^2 = \sigma_{Z_3}$$

$$\sigma_Z = 7.95 + 0.417 + 0.417$$

$$\sigma_Z = 8.78 \text{ t/m}^2$$

03. Ans: (c)

Sol:



σ_Z at centre = ?

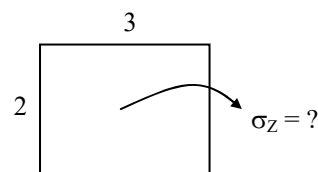
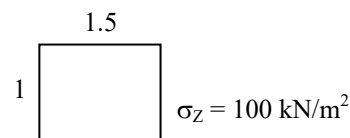
$Z = 10 \text{ m}$

$$\sigma_Z = 20 \left[1 - \left(\frac{1}{1 + \left(\frac{4}{10} \right)^2} \right)^{3/2} \right] - 20 \left[1 - \left(\frac{1}{1 + \left(\frac{3}{10} \right)^2} \right)^{3/2} \right]$$

$$\sigma_Z = 1.56 \text{ kPa} = 1.56 \text{ kN/m}^2$$

04. Ans: (d)

Sol:



$$\sigma_Z = 4 \times \sigma_Z \text{ of small rectangle } (1 \times 1.5)$$

$$= 4 \times 100 = 400 \text{ kN/m}^2$$



05. Ans: 7.41 m

Sol: Vertical stress due to circular loaded area

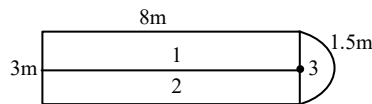
$$\sigma = q \left[1 - \left(\frac{1}{1 + (r/z)^2} \right)^{3/2} \right]$$

$$0.1q = q \left[1 - \left(\frac{1}{1 + (2/z)^2} \right)^{3/2} \right]$$

$$Z = 7.41 \text{ m}$$

06. Ans: 83.05 kPa

Sol:



Total vertical stress

= stresses at 1 + stresses at 2 + stresses at section 3

$$= \sigma_{v_1} + \sigma_{v_2} + \sigma_{v_3}$$

$$\sigma_{v_1} = \sigma_{v_2} = qI$$

$$n = \frac{L}{Z} = \frac{8}{3} = 2.67$$

$$m = \frac{B}{Z} = \frac{1.5}{3} = 0.5$$

$$\therefore m = 0.5, n = 2.67 \Rightarrow I = 0.1365$$

$$\sigma_{v_1} = \sigma_{v_2} = 0.1365 \times 200 = 27.3$$

Vertical stress in circular area

$$\sigma_{v_3} = q \left[1 - \left(\frac{1}{1 + (r/z)^2} \right)^{3/2} \right]$$

$$= 200 \left[1 - \left(\frac{1}{1 + \left(\frac{1.5}{3} \right)^2} \right)^{3/2} \right]$$

$$= 56.89 \text{ KPa}$$

Vertical stress in semi-circular area

$$= \frac{\sigma_{v_3}}{2} = 28.44 \text{ KPa}$$

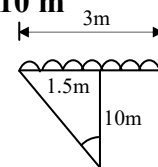
$\therefore$ Total vertical stresses

$$= 27.3 + 27.3 + 28.44$$

$$= 83.05 \text{ KPa}$$

07. Ans: 18.7 kPa

Sol: Take h = 10 m



$$\theta = \tan^{-1} \left(\frac{1.5}{10} \right) = 8.53$$

$$= 0.148 \text{ radians}$$

$$\sigma_z = \frac{q}{\pi} (2\alpha + \sin 2\alpha)$$

$$= \frac{100}{\pi} (2 \times 0.148 + \sin 2(8.53))$$

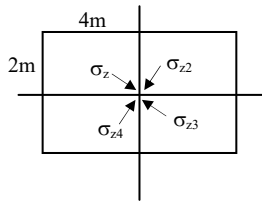
$$= 18.76 \text{ kPa}$$



Assignment Solutions

01. Ans: (a)

Sol:



$$m = \frac{L}{z} = \frac{4}{5} = 0.8$$

$$n = \frac{B}{z} = \frac{2}{5} = 0.4$$

$$\sigma_z = \sigma_{z1} + \sigma_{z2} + \sigma_{z3} + \sigma_{z4}$$

$$\sigma_{z1} = Iq$$

$$m = 0.8, \quad n = 0.4, \quad I = 0.0931$$

$$q = \frac{600}{8 \times 4} = 18.75 \text{ kN/m}^2$$

$$\therefore \sigma_{z1} = 0.0931 \times 18.75$$

$$= 1.7456 \text{ kN/m}^2$$

$$\therefore \text{Total pressure } \sigma_z = 4 \times 1.7456 \\ = 7 \text{ kN/m}^2$$

Chapter- 11 Consolidation

01. Ans: 147.86 mm & 2.86 years

Sol:

$$d = H = 8 \text{ m} = 800 \text{ cm}$$

For a settlement 120 mm in 2 years

$$C_v = 6 \times 10^{-3} \text{ cm}^2/\text{s}$$

$$S_f = ?, \quad t_{90} = ?$$

$$T_v = \frac{C_v t}{d^2}$$

$$= \frac{6 \times 10^{-3} \times 2 \times 365 \times 24 \times 60 \times 60}{800^2} = 0.5913$$

Since $T_v > 0.282$

$$T_v = 1.781 - 0.933 \log_{10} (100 - U\%)$$

$$0.5913 = 1.781 - 0.933 \log_{10} (100 - U\%)$$

$$U = 81.16\%$$

$$\Rightarrow U = \frac{s}{s_f}$$

$$\Rightarrow 81.16 = \frac{120}{s_f} \times 100$$

$$s_f = 147.86 \text{ mm}$$

(b)

$$T_v = 1.781 - 0.953 \log_{10} (100 - 90\%)$$

$$= 0.848$$

$$T_v = \frac{C_v t}{d^2} \Rightarrow 0.848 = \frac{6 \times 10^{-3} \times t}{120^2}$$

$$\Rightarrow t = 2.86 \text{ years}$$



02. Ans: (a)

Sol: $\Delta H_1 = 1 \text{ cm},$

$$\sigma'_{f_1} = 2 \text{ kg/cm}^2, \sigma'_{0_1} = 1 \text{ kg/cm}^2,$$

$$\Delta H_2 = ?$$

$$\sigma'_{f_2} = 4 \text{ kg/cm}^2, \sigma'_{0_2} = 2 \text{ kg/cm}^2$$

$$\Delta H \propto \log_{10} \left(\frac{\sigma'_f}{\sigma'_0} \right)$$

$$\frac{\Delta H_1}{\Delta H_2} = \frac{\log_{10} \left(\frac{\sigma'_{f_1}}{\sigma'_{0_1}} \right)}{\log_{10} \left(\frac{\sigma'_{f_2}}{\sigma'_{0_2}} \right)}$$

$$\frac{1}{\Delta H} = \frac{\log_{10} \left(\frac{2}{1} \right)}{\log_{10} \left(\frac{4}{2} \right)} \Rightarrow \Delta H = 1 \text{ cm}$$

03. Ans: (c)

Sol: $t_1 = 4 \text{ yrs}, S_1 = 80 \text{ mm}$

$$t_2 = 9 \text{ yrs}, S_2 = ?$$

For both conditions, soil is same
(Degree of consolidation).

$$U = \frac{S}{S_f} \times 100$$

$S_f \rightarrow$ same for both

$$\Delta H = 80 \text{ mm}; t_1 = 4 \text{ yrs} \\ = 60\% \text{ (less than)}$$

$$t_2 = 9 \text{ yrs}$$

$$U = \frac{S}{S_f} \times 100 \Rightarrow T_v = \frac{\pi}{4} \left(\frac{U}{100} \right)^2$$

$$\Rightarrow C_v \frac{t}{d^2} = \frac{\pi}{4} U^2$$

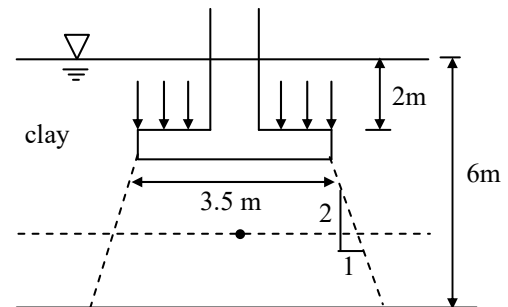
$$\Rightarrow t \propto U^2 \Rightarrow t \propto s^2$$

$$\Rightarrow \frac{t_1}{t_2} = \left[\frac{S_1}{S_2} \right]^2$$

$$\Rightarrow \frac{4}{9} = \left[\frac{80^2}{S_2^2} \right]^2 \Rightarrow S_2 = 120 \text{ mm}$$

04. Ans: 120 mm

Sol:



$$\gamma_w = 10 \text{ kN/m}^3, \gamma_{\text{sat}} = 19.3 \text{ kN/m}^3, q = 500 \text{ kN}$$

$$C_c = 0.36, e_0 = 0.92, S_f = 120$$

$$S_f = H_0 \frac{C_c}{1+e_0} \log_{10} \left(\frac{\sigma'_f}{\sigma'_0} \right)$$

$$S_f = 4 \times \frac{0.36}{1+0.92} \log_{10} \left(\frac{\sigma'_f}{\sigma'_0} \right)$$

$$\Delta \sigma' = \frac{q}{(B+Z)^2} = \frac{500}{(3.5+2)^2}$$

$$\Delta \sigma' = 16.528 \text{ kN/m}^2$$

$$\sigma'_f = \sigma'_0 + \Delta \sigma'$$

$$= 37.2 + 16.528$$

$$= 53.728 \text{ kN/m}^2$$

$$S_f' = 4 \times \frac{0.36}{1.92} \times \log_{10} \left[\frac{53.728}{16.528} \right] = 120 \text{ mm}$$



05. Ans: (c)

Sol: $t \propto \frac{d^2 m_v}{K}$

$$\frac{t_2}{t_1} = \left(\frac{d_2}{d_1} \right)^2 \left(\frac{m_{v2}}{m_{v1}} \right) \left(\frac{K_1}{K_2} \right)$$

$$t_1 = 15 \text{ yrs, } d_2 = 2 d_1, K_2 = 3K_1,$$

$$m_{v2} = 4 m_{v1}$$

$$t_2 = 15 \times \left(\frac{2}{1} \right)^2 \left(\frac{4}{1} \right) \left(\frac{1}{3} \right)$$

$$t_2 = 80 \text{ yrs}$$

Common data for Questions 06 & 07

06. Ans: (a)

Sol: $d_1 = \frac{20}{2} = 10 \text{ mm, } U_1 = 50\%, t_1 = 45 \text{ min [lab]}$

$$d_2 = 5000 \text{ mm, } U_2 = 50\%, t_2 = ? \text{ [field]}$$

$$\text{Same } U, T_v$$

$$t \propto d^2$$

$$\frac{t_2}{t_1} = \frac{d_2^2}{d_1^2}$$

$$t_2 = 45 \left(\frac{5000}{10} \right)^2 = 11250000 \text{ min}$$

$$= 21.4 \text{ years}$$

07. Ans: (b)

Sol: $t_2 = 4 \times 21.4 = 85.6 \text{ yrs}$

Common data for Questions 08 & 09

$$U = \frac{80}{300} = 26.6\%$$

$$T_v = \frac{C_v t}{d^2}$$

$$\frac{\pi}{4} (26.6)^2 = \frac{C_v t}{d^2}$$

$$\frac{C_v}{d^2} = \frac{\pi}{225}$$

08. Ans: (b)

Sol: $T_v = \frac{C_v}{d^2} \times t = \frac{\pi}{225} \times 25 = 0.35$

$$U = 65\%$$

$$\frac{S}{300} \times 100 = 0.65$$

$$S = 195 \text{ mm}$$

09. Ans: (d)

Sol: At $U\% = 70\%, T_v = 0.403$

$$T_v = \frac{C_v}{d^2} \times t$$

$$0.403 = \frac{\pi}{225} \times t \Rightarrow t = 28.8 \text{ yrs}$$

10. Ans: (c)

Sol: NOTE: The time is measured from middle of construction period

$$t = 5 \text{ yrs,}$$

$$S = 90 \text{ mm,}$$

$$S_f = 360$$

$$T_v = \frac{C_v t}{d^2}$$



$$\frac{t_1}{t_2} = \frac{T_{v1}}{T_{v2}} = \frac{(S/360)^2}{(90/360)^2}$$

$$S^2 = 90^2 \times \frac{9}{4}$$

$$S = 135 \text{ mm}$$

Common data for Questions 11 & 12

11. Ans: (b)

Sol: $\gamma_{\text{sat}} = 18 \text{ kN/m}^3$

$$\gamma_{\text{sat}} = 20 \text{ kN/m}^3$$

$$\gamma_w = 10 \text{ kN/m}^3$$

$$\text{Depth} = 4 \text{ m} ; \gamma = 19 \text{ kN/m}^3$$

a) Immediately after load

$$\begin{aligned} \sigma &= q + (18 \times 5) + (20 \times 3) \\ &= 226 \text{ kPa} \end{aligned}$$

$$U = U_{\text{static}} + U_{\text{dynamic}}$$

$$= 8\gamma_w + q = 156$$

$$\sigma' = 70 \text{ kPa} = 70 \text{ kN/m}^2$$

12. Ans: (c)

Sol: Many years after (At the end of consolidation)

$$\sigma = 226 \text{ kPa}$$

$$U = 80 \quad (\because \bar{U} = 0)$$

$$\sigma' = 146 \text{ kPa}$$

13. Ans: (c)

Sol: Site-x

Site -y

$$d_x = 10 \text{ m}$$

$$d_y = 5 \text{ m (layer (2))}$$

$$t_1 = 36 \text{ minutes}$$

$$t_2 = ?$$

$$\frac{t_2}{t_1} = \frac{d_y^2}{d_x^2}$$

$$\frac{t_2}{36} = \frac{5^2}{10^2} \Rightarrow t_2 = 9 \text{ months}$$

14. Ans: 422.7 mm

Sol:

Preliminary analysis	Detailed investigation
H_1	$H_2 = 1.2H_1$
$\Delta\sigma' = 24 \text{ KPa}$	$\Delta\sigma'^2 = \Delta\sigma' + 1 \times \gamma_w$ $= 24 + 9.81$ $= 33.81 \text{ KPa}$
$Sf_1 = 250 \text{ mm}$	$Sf_2 = ?$

$$S_f = m_v H \Delta\sigma'$$

$$S_f \propto H. \Delta\sigma' \text{ assuming 'm}_v\text{' remains same}$$

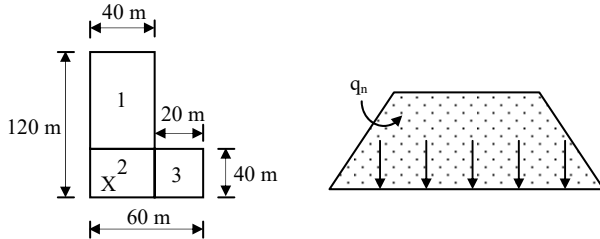
$$\frac{s_{f1}}{s_{f2}} = \frac{H_1 \Delta\sigma'}{H_2 \Delta\sigma'}$$

$$\frac{250}{s_{f2}} = \frac{H_1 24}{1.2H 33.81} = S_{f2} = 422 \text{ mm}$$



15. Ans: 514.5 mm

Sol:



$$q_n = 150 \text{ KPa}$$

$$\mu = 0.5 \text{ (for soft clay)}$$

$$E_s = 15 \text{ MN/m}^2 = 15 \times 10^6 \text{ N/m}^2$$

$$= 15 \times 10^3 \text{ kN/m}^2$$

Rec (1)

$$= \frac{L}{B} = \frac{80}{40} = 2$$

$$I = 0.77$$

$$S_i = \frac{q_n}{E_s} B(1 - \mu^2) I$$

$$= \frac{150}{15 \times 10^3} 40(1 - 0.5^2) 0.77 = 0.231$$

Rec (2)

$$= \frac{L}{B} = 1$$

$$S_i = \frac{150}{15 \times 10^3} \times 40(1 - 0.5^2) = 0.56$$

Rec (3)

$$\frac{L}{B} = \frac{40}{20} = 2$$

$$S_i = 0.115$$

∴ Total settlement

$$S_i = S_{i_1} + S_{i_2} + S_{i_3} = 0.514 \text{ m}$$

Assignment Solutions

01. Ans: (b)

$$\text{Sol: } s_f = H \frac{C_c}{1 + e_o} \log \left(\frac{\sigma'_f}{\sigma'_o} \right)$$

$$s_f \propto \log \left(\frac{\sigma'_f}{\sigma'_o} \right)$$

$$\frac{s_{f_2}}{s_{f_1}} = \frac{\log \left(\frac{200}{50} \right)}{\log \left(\frac{50}{25} \right)} = \frac{\log 4}{\log 2} = 2$$

$$s_{f_2} = 2 \times 16 = 32 \text{ mm}$$

02. Ans: (c)

$$\text{Sol: } a_v = \frac{\Delta e}{\Delta \sigma'} = \frac{0.7 - 0.6}{17.5 - 17} = 0.2 \text{ m}^2 / \text{t}$$

03. Ans: (d)

$$\text{Sol: } T_v = \frac{C_v t}{d^2}$$

Degree of consolidation is same $T_{v_1} = T_{v_2}$

$$\frac{C_v t}{d^2} = \frac{C_v t}{d^2}$$

$$\frac{t}{d^2} = \frac{t}{d^2}$$

$$\frac{300}{(2.5)^2} = \frac{t}{5^2}$$

$$t = 4 \times 300 = 1200 \text{ days}$$



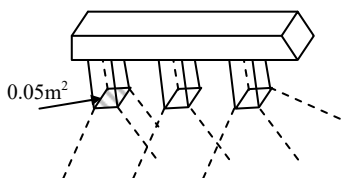
05. Ans: (a)

$$\text{Sol: } C_c = \frac{\Delta e}{\log\left(\frac{\sigma'}{\sigma'_o}\right)} = \frac{0.3}{\log\left(\frac{100}{10}\right)} = 0.3$$

Chapter- 12 Compaction

01. Ans: (c)

Sol:



Energy given by rammer per m³ of soil in the field

$$= \frac{40 \times 1.5}{0.05 \times 0.3} = 4000 \text{ kgm/m}^3$$

Energy given in IS light compaction test in kg-m/m³ of volume of soil

$$\begin{aligned} \text{Standard value } 595 \text{ kJ/m}^3 \\ = 60673.11 \text{ kg-m/m}^3 \end{aligned}$$

∴ No. of passes required

$$= \frac{60673.11}{4000} = 15.16 \approx 16 \text{ No's}$$

02. Ans: (b)

$$\text{Sol: } e_{\max} = 0.75, \quad e = 0.50, \quad e_{\min} = 0.35$$

$$G = 2.67$$

$$\begin{aligned} \gamma_d \text{ field} &= \frac{\gamma_w \cdot G}{1 + e} \\ &= \frac{10 \times 2.67}{1 + 0.5} = 17.8 \text{ kN.m} \end{aligned}$$

$$\gamma_d \text{ lab} = \frac{\gamma_w G}{1 + e_{\min}} = \frac{10 \times 2.67}{1 + 0.35} = 19.77 \text{ kN.m}$$

$$\begin{aligned} \text{Relation compaction} &= \frac{17.8}{19.77} \times 100 \\ &= 90\% \end{aligned}$$

Assignment Solutions

01. Ans: (d)

Sol:

Maximum dry density that can be achieved without air voids.

$$\begin{aligned} \gamma_d &= \frac{\gamma_w G}{1 + wG} \\ &= \frac{10 \times 2.6}{1 + 0.14 \times 2.6} \\ &= 19.06 \text{ kN/m}^3 \end{aligned}$$

02. Ans: 1.1

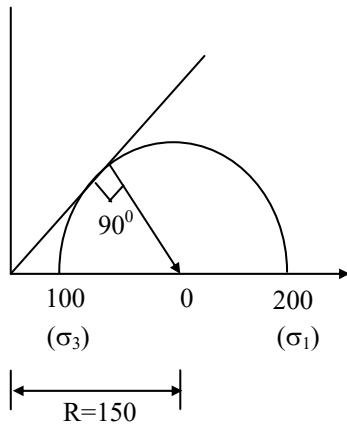
$$\begin{aligned} \text{Sol: } d &= \frac{(1 - n_a) \rho_w G}{1 + wG} \\ 1.85 &= \frac{(1 - n_a) \times 1 \times 2.67}{1 + 0.16 \times 2.67} \\ n_a &= 1.1\% \end{aligned}$$



Chapter- 13 Shear Strength

01. Ans: (a)

Sol:



Angle of internal friction (ϕ) = ?

Direction of failure envelop in CD test of NCC

$$\sin \phi = \frac{50}{150}$$

$$\phi = \sin^{-1} \left(\frac{1}{3} \right)$$

02. Ans: (a)

Sol: Direct stress, $\sigma_1 = 5 \text{ Kg/cm}^2$

All round stress, $\sigma_3 = 3.2 \text{ Kg/cm}^2$

Shear on failure plane, $\tau_f = 0.9$

$\phi = ?$

$$\tau_{\max} = \frac{\sigma_1 - \sigma_3}{2} = 0.9$$

$$\therefore \tau_f = \tau_{\max} \Rightarrow \phi = 0$$

Another method:

$$\tau_f = \frac{\sigma_1 - \sigma_3}{2} \sin 2\alpha_f$$

$$0.9 = \frac{5 - 3.2}{2} \sin 2 \left(45 + \frac{\phi}{2} \right)$$

$$1 = \sin 2 \left[45 + \frac{\phi}{2} \right]$$

$$1 = \cos \phi$$

$$\phi = 0$$

03. Ans: 34.37 kN/m²

Sol:

UCC test

An undrained test ($\Delta V = 0$)

$$A_2 = \frac{V_1}{L_1 - \Delta L}$$

Divided by L_1

$$A_2 = \frac{A_1}{1 - \frac{\Delta L}{L_1}} = \frac{A_1}{1 - \epsilon} = \frac{A_1}{1 - 0.1}$$

$$A_2 = \frac{\pi/4 \times d^2}{1 - 0.1} = 21.81 \text{ cm}^2$$

$$q_u = \frac{Q}{A_2} = \frac{150}{21.81} = 6.87 \text{ N/cm}^2$$

$$= 68.7 \text{ kN/m}^2$$

$$C_u = \frac{q_u}{2} = 34.37 \text{ kN/m}^2$$



Common data for Questions 04 & 05

04 & 05 Ans: (c) & (b)

Sol: Given:

Unconfined compressive test ($\phi = 0$)

$$q_u = 1.2 \text{ kg/cm}^2$$

$$\alpha_f = 50$$

Cohesion of soil = ?

$$\alpha_f = \left(45 + \frac{\phi}{2} \right)$$

$$\sigma_1 = \sigma_3 \tan^2 \left(45 + \frac{\phi}{2} \right) + 2C \tan \left(45 + \frac{\phi}{2} \right)$$

$$\therefore \alpha_f = 50$$

$$50 = 45 + \frac{\phi}{2}$$

$$5 \times 2 = \phi$$

$$\phi = 10^\circ$$

$$q_u = 2 C_u \tan \left(45 + \frac{\phi}{2} \right) \text{ if } \phi > 0$$

$$q_u = 2 C_u \tan \left(45 + \frac{\phi}{2} \right) \text{ if } \phi = 0$$

$$1.20 = 2 C_u \tan \left(45 + \frac{10}{2} \right)$$

$$C_u = 0.5 \text{ kg/cm}^2$$

06. Ans: $\alpha = 55.4^\circ$, $\sigma_n = 338.72 \text{ kN/m}^2$

$$\tau = 128.56 \text{ kN/m}^2$$

Sol: $\sigma_3 = 250 \text{ kN/m}^2$

$$\sigma_d = 275 \text{ kN/m}^2$$

$$\sigma_1 = \sigma_3 + \sigma_d$$

$$= 250 + 275 = 525 \text{ kN/m}^2$$

$$C' = 0 \text{ (for N.C clay in C.D test)}$$

$$\sigma'_1 = \sigma'_3 + \sigma'_d = 525 \text{ kN/m}^2$$

$$\sigma'_1 = \sigma'_3 \tan^2 (45 + \phi/2) + 2C' \tan (45 + \phi/2)$$

$$\sigma'_1 = \sigma'_3 \tan^2 (45 + \phi/2)$$

$$525 = 250 \times \tan^2 (45 + \phi/2)$$

$$45^\circ + \phi/2 = 55.4^\circ$$

On the failure plane

$$\sigma = \frac{\sigma_1 + \sigma_3}{2} + \frac{\sigma_1 - \sigma_3}{2} \cos 2\alpha_f$$

$$= 338.72 \text{ kN/m}^2$$

$$\tau_f = \frac{\sigma_1 - \sigma_3}{2} \sin 2\alpha_f$$

$$= 128.56 \text{ kN/m}^2$$

07. Ans: $C_u = 0$, $\phi_u = 15.8^\circ$, $C' = 0$, $\phi' = 22^\circ$

Sol: $\sigma_3 = 200 \text{ kN/m}^2$

$$\sigma_d = 150 \text{ kN/m}^2$$

$$u_f = 75 \text{ kN/m}^2$$

NCC in Cu test $C_u = 0$ & $C' = 0$

To find, ϕ_u^1 & $\phi_u^{11} = ?$

$$\sigma_1 = \sigma_3 + \sigma_d = 200 + 150$$

$$= 350 \text{ kN/m}^2$$

$$350 = 200 \tan^2 \left(45 + \frac{\phi_u}{2} \right) + 2(0)$$

$$\frac{350}{200} = \tan^2 \left(45 + \frac{\phi_u}{2} \right)$$

$$\phi_u = 15.8^\circ$$

To find ϕ'

$$\sigma_1^1 = \sigma_3^1 \left(45 + \frac{\phi}{2} \right)$$



$$(\sigma_1 - u) = (\sigma_3 - u) \tan^2 \left(45 + \frac{\phi}{2} \right)$$

$$275 = (125) \tan^2 \left(45 + \frac{\phi}{2} \right)$$

$$\phi = 22^\circ$$

08. Ans: B = 0.70 & A = -0.228

Sol:

Change = final value – Initial value

In consolidation stage:

$$\Delta u_3 = 10 - (-60) = 70 \text{ kN/m}^2$$

$$\Delta \sigma_3 = 100 - 0 = 100 \text{ kN/m}^2$$

$$\Delta u_3 = B \times \Delta \sigma_3 \Rightarrow B = 0.7$$

In shearing stage (or) failure stage

$$\Delta u_d = -70 - 10 = -80 \text{ kN/m}^2$$

$\therefore u$ = Pore water pressure

$$\Delta \sigma_d = 500 \text{ kN/m}^2$$

$$\Delta u_d = AB \Delta \sigma_d$$

$$-80 = A \times 0.7 \times 500$$

$$\Rightarrow A = -0.228$$

09. Ans: B = 0.95 & A = 0.357

Sol:

$$\Delta \sigma_3 = 800 - 700 = 100$$

$$\Delta u_3 = 445 - 350 = 95$$

$$\Delta u_3 = B \Delta \sigma_3$$

$$B = 0.95$$

$$\Delta \sigma_d = 575 \text{ kN/m}^2$$

$$\Delta u_d = 640 - 445 = 195 \text{ kN/m}^2$$

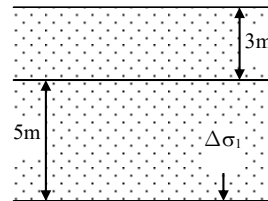
$$\Delta u_d = AB \times \Delta \sigma_d$$

$$195 = A \times 0.95 \times 575$$

$$A = 0.357$$

10. Ans: 78.20 kN/m²

Sol:



$$\Delta \sigma_3 = \frac{1}{2} \Delta \sigma_1$$

$$\Delta \sigma_1 = 3\gamma = 48.6 \text{ KPa}$$

$$\Delta \sigma_3 = \frac{1}{2} \Delta \sigma_1 = 24.3$$

$$\Delta \sigma_d = (\Delta \sigma_1 - \Delta \sigma_3)$$

$$= 48.6 - 24.3 = 24.3$$

$$\Delta u = B (\Delta \sigma_3 + A \Delta \sigma_d)$$

$$= 31.29 \text{ KPa}$$

To find $\sigma' = \sigma - u$

$$= 8 \times 16.2 - 31.29$$

$$= 98.31 \text{ KPa}$$

$$S = C' + \sigma' \tan$$

$$= 50 + 98.31 \times \tan (16^\circ)$$

$$= 78.18 \text{ KPa}$$

Assignment Solutions

02. Ans: (a)

Sol: $\Delta u_d = 130 \text{ kN/m}^2$

$$\Delta \sigma_3 = 250 - 100 = 150 \text{ kN/m}^2$$

$$\Delta u_3 = B \Delta \sigma_3$$

$$\frac{130}{150} = B$$

$$B = 0.87$$

03. Ans: (b)

Sol: $q_u = 100, C_u = \frac{q_u}{2} = 50$

$\sigma_3 = 100$; For UU test, $\phi_u = 0$ or $\tan \alpha_f = 1$

$$\sigma_1 = \sigma_3 + 2C_u$$

$$= 100 + 2 \times 50 = 200$$

Chapter- 14 Earth Pressure

01. Ans: 316.7 kN

Sol: Given:

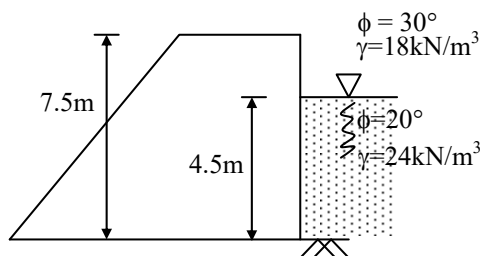


Fig. (1)

$$k_a = \frac{1}{3}, \quad k_{a1} = \frac{1 - \sin 20}{1 + \sin 20} = 0.49$$

$\therefore$ at top $\sigma_v = 0, P_a = 0$

$\therefore$ at 3 m below, $\sigma_v = 18 \times 3 = 54 \text{ kN/m}^2$

$$P_a = 54 \times \frac{1}{3} = 18 \text{ kN/m}^2$$

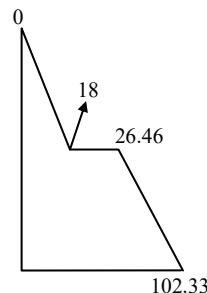
$\therefore$ at 3m just below $P_{a1} = 54 \times 0.49 = 26.46$

At 7.5 m, $\sigma_v = 18 \times 3 + 4.5 \times 14 = 117 \text{ kN/m}^2$

$$P_{a2} = 0.49(117) + 10 \times 4.5 = 102.33 \text{ kN/m}^2$$

Total active thrust

$$= \frac{1}{2} \times 18 \times 3 + \left(\frac{26.46 + 102.33}{2} \right) 4.5 = 316.77 \text{ kN/m}$$



02. Ans: (d)

Sol: $Z_c = \frac{2c}{\gamma} \tan \alpha_f$

$$= \frac{2 \times 10}{18} \times \tan(45 + 0/2)$$

At top $= \sigma_v = q = 20 \text{ kN/m}^2$

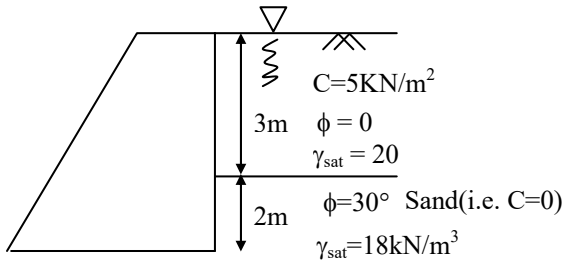
$$P_a = k_a \cdot \sigma_v - 2c \sqrt{k_a}$$

$$= 1 \times 20 - 2 \times 10 \times \sqrt{1} = 0$$



03. Ans: (167 kN/m)

Sol: Given:



To find: Total active thrust on the back

a) At top:

As there is water $K_{a1} = 1, K_{a2} = 0.33$

So $\sigma'_v = 0$

$\sigma_h = K_a (0)$

$\sigma_h = 0$

$$P_a = K_{a1} \sigma'_v - 2C_1 \sqrt{K_{a1}} + \gamma_w h = -10 \text{ kPa}$$

b) At 3 m depth:

a) Just above:

$$\sigma'_v = 3\gamma' = 3(20 - 10) = 30 \text{ kPa}$$

$$\begin{aligned} P_a &= K_{a1} \sigma'_v - 2C_1 \sqrt{K_{a1}} + \gamma_w h \\ &= 1(30) - 2(5)(1) + 10 \times 3 \\ &= 50 \text{ kPa} \end{aligned}$$

b) Just below:

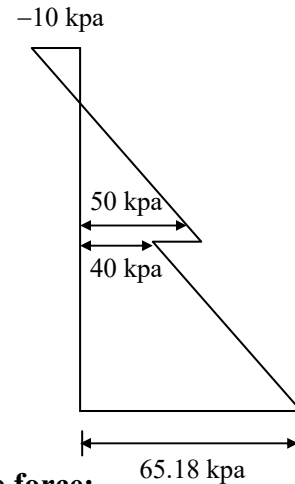
$$\begin{aligned} P_a &= K_{a2} \sigma'_v - 2C_2 \sqrt{K_{a2}} + \gamma_w h \\ &= 0.33(30) - 2(0)\sqrt{0.33} + 10 \times 3 \\ &= 39.9 \approx 40 \text{ kPa} \end{aligned}$$

c) At bottom:

$$\sigma'_v = 3\gamma' + 2\gamma'$$

$$\sigma'_v = 3(20 - 10) + 2(18 - 10) = 46 \text{ kPa}$$

$$\begin{aligned} P_a &= K_{a2} \sigma'_v - 2C_2 \sqrt{K_{a2}} + \gamma_w h \\ &= 0.33(46) - 2(0)\sqrt{K_{a2}} + 10 \times 5 \\ &= 65.18 \text{ kPa} \end{aligned}$$



To compute force:

$$F = P_a \times A$$

$$Z_C = \frac{2C}{\gamma} \sqrt{K_a} \left\} \text{where there is no water}\right.$$

$F = P_a = \text{area of +ve portion of diagram}$

$$= \left(\frac{1}{2} \times 50 \times 2.5 \right) + \frac{1}{2} (40 + 65.4) \times 2$$

$$F = 167 \text{ kN/m}$$

04. Ans: 161.66 kN/m

Sol: $\phi_1 = 30^\circ$; $k_{a1} = \frac{1 - \sin \phi_1}{1 + \sin \phi_1} = 0.333$

$\phi_2 = 10^\circ$; $k_{a2} = \frac{1 - \sin \phi_2}{1 + \sin \phi_2} = 0.704$

At top: $\sigma_v = q = 10 \text{ kN/m}^2$

$$\begin{aligned} P_a &= k_{a1} \sigma_v - 2c_1 \sqrt{k_{a1}} \\ &= 0.333 \times 10 - 0 = 3.33 \text{ kN/m}^2 \end{aligned}$$



At 3 m depth: $\sigma_v = q + \gamma_1 z_1$
 $= 10 + 15 \times 3 = 55 \text{ kN/m}^2$

(a) Just above the 3 m depth,

$$P_a = k_{a1} \sigma_v - 2C_1 \sqrt{k_{a1}}$$

$$= 0.333 \times 55 - 0 = 18.32 \text{ kN/m}^2$$

(b) Just below the 3 m depth,

$$P_a = k_{a2} \sigma_v - 2C_2 \sqrt{k_{a2}}$$

$$= 0.704 \times 55 - 2 \times 10 \sqrt{0.704}$$

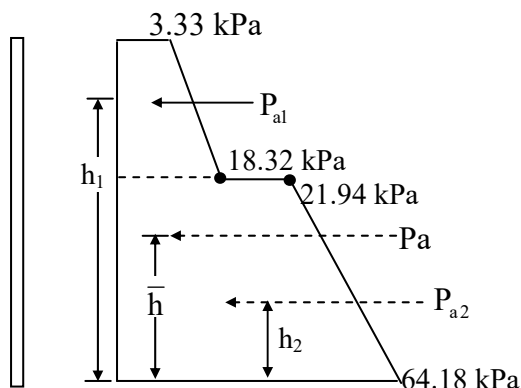
$$= 21.94 \text{ kN/m}^2$$

At 6 m depth: $\sigma_v = q + \gamma_1 z_1 + \gamma_2 z_2$
 $= 10 + 15 \times 3 + 20 \times 3 = 115 \text{ kN/m}^2$

$$P_a = k_{a2} \sigma_v - 2C_2 \sqrt{k_{a2}}$$

$$= 0.704 \times 115 - 2 \times 10 \sqrt{0.704}$$

$$= 64.18 \text{ kN/m}^2$$



The active pressure diagram is shown in the figure. Total active force,

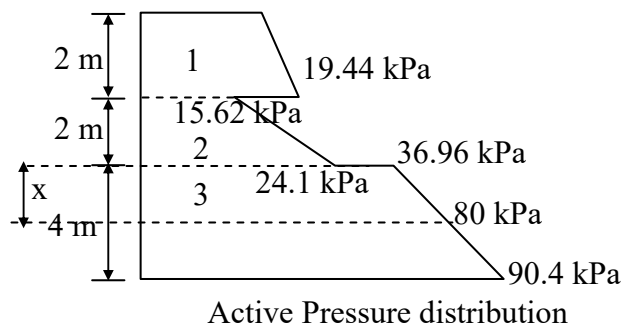
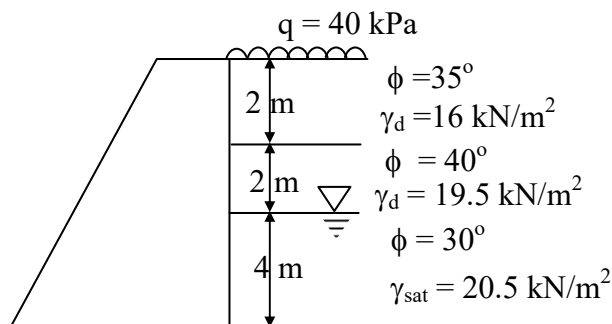
$$P_a = P_{a1} + P_{a2}$$

$$= \frac{1}{2} [3.33 + 18.32] \times 3 + \frac{1}{2} [21.94 + 64.18] \times 3$$

$$= 32.48 + 129.18 = 161.66 \text{ kN/m}$$

05. Ans. 7.23 m

Sol:



Active Pressure distribution

$$K_{a1} = \frac{1 - \sin 35^\circ}{1 + \sin 35^\circ} = 0.27$$

$$K_{a2} = \frac{1 - \sin 40^\circ}{1 + \sin 40^\circ} = 0.217$$

$$K_{a3} = \frac{1 - \sin 30^\circ}{1 + \sin 30^\circ} = \frac{1}{3}$$

Pressure at top:

$$\sigma_v = q$$

$$P_a = \sigma_v \times K_{a1} = 10.8 \text{ kPa}$$

Pressure at a depth 2 m

Case (a): Just above the 2 m depth

$$\sigma_v = q + \gamma_a \times 2$$



$$= 40 + 16 \times 2 = 72 \text{ kPa}$$

$$P_a = \sigma_v K_{a_2} = 72 \times 0.27$$

$$= 19.44 \text{ kPa}$$

Case (b): Just below 2 m depth

$$\sigma_v = 72 \text{ kPa}$$

$$P_a = \sigma_v K_{a_2} = 72 \times 0.217$$

$$= 15.62 \text{ kPa}$$

Pressure at a depth 4 m depth

Case (a) : Just above the 4 m depth

$$\sigma_v = q + \gamma_{d_1} \times 2 + \gamma_{d_2} \times 2$$

$$= 40 + 16 \times 2 + 19.5 \times 2 = 111 \text{ kPa}$$

$$P_a = \sigma_v K_{a_2} = 111 \times 0.217 = 24.1 \text{ kPa}$$

Case(b) : Just below the 4 m depth

$$\sigma_v = 111 \text{ kPa}$$

$$P_a = \sigma_v K_{a_3} = 111 \times \frac{1}{3} = 36.96 \text{ kPa}$$

Pressure at base:

$$\sigma_v = q + \gamma_{d_1} \times 2 + \gamma_{d_2} \times 2 + \gamma' \times 4$$

$$= 40 + 16 \times 2 + 19.5 \times 2 + (20.5 - 9.81) \times 4$$

$$= 153.76 \text{ kPa}$$

$$P_a = \sigma_v K_{a_3} + \gamma_w \times 4 = 90.4 \text{ kPa}$$

In the third layer : At $P_a = 80 \text{ kPa}$

$$\sigma'_v = 40 + 2[16 + 19.5] + [20.5 - 9.81]x$$

$$= 111 + 10.69x \quad (x = \text{depth in the third layer at which } p_a = 80 \text{ kPa})$$

$$80 = \sigma'_v \times K_{a_3} + \gamma_w \times x$$

$$80 = \frac{1}{3}[111 + 10.69x] + 9.81x$$

$$\Rightarrow x = 3.23 \text{ m}$$

$$\text{From top} = 2 + 2 + x = 7.23 \text{ m}$$

Chapter- 15 Stability of Slopes

01. Ans: (d)

Sol: Take $Z = 4 \text{ m}$

$$F = \frac{C' + [\gamma \cdot y + \gamma'(z - y)] \cos^2 i \cdot \tan \phi'}{[\gamma \cdot y + \gamma_{\text{sat}}(z - y)] \cos i \cdot \sin i}$$

$$= \frac{[19 \times 1.5 + 9^2(4 - 1.5)] \cos^2(28^\circ) \cdot \tan(35^\circ)}{[19 \times 1.5 + 19(4 - 1.5)] \cos(28^\circ) \cdot \sin(28^\circ) \gamma}$$

$$\therefore \text{since } \gamma \text{ is not given take } \gamma = \gamma_{\text{sat}}$$

$$F = \frac{15.50}{76 \times 0.88 \times 0.46} = 0.426$$

02. Ans: 4.77 & 0.596

Sol:

Infinite slope, seepage parallel to slope

$$F = \frac{C' + \gamma z \cos^2 i \tan \phi'}{\gamma_{\text{sat}} z \cos i \sin i} \quad Z = H_c$$

$$1 = \frac{25 + 8 \times H_c \cos^2(35^\circ) \tan(28^\circ)}{18 \times H_c \cos(35^\circ) \sin(35^\circ)}$$

$$H_c = 4.77$$

$$F = \frac{H_c}{H} = \frac{4.76}{8} = 0.596$$

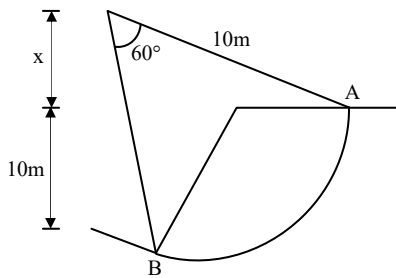


03. Ans: 1.184, 2.66

Sol:

$$C = 50 \text{ kN/m}^2$$

$$\phi = 10^\circ \quad \sigma' = 255 \text{ kN/m}^2, t = 840 \text{ kN}$$



$$N = \sigma' \cdot l$$

$$= 255 \times 1.04 \times 1 = 265.2$$

$$\hat{L} = \frac{(2\pi r) \times 60}{360} = 10.47$$

$$F = \frac{C \cdot \hat{L} + \sum N \tan \phi}{\sum T} = \frac{C \cdot \hat{L} + N \tan \phi}{T}$$

$$F = \frac{50 \times 10.47 + 255(10.47) \tan 10}{840}$$

$$= 1.1836$$

w.r. to height

$$H_c = \frac{4C}{\gamma \sqrt{k_a}}$$

$$= \frac{4C}{\gamma} \tan \left[45 + \frac{\phi}{2} \right] = \frac{4 \times 50}{18} \tan 50 = 13.24 \text{ m}$$

$$H = R - x$$

$$= 10 - R \cos 60^\circ = 5$$

$$F = \frac{H_c}{H} = \frac{13.24}{5} = 2.67$$

04. Ans: $F_c = 1.16$ & $F_\phi = 1.2$

Sol: Given:

Cutting is to be made in soil

Slope of soil = 25°

Depth of soil = 25 m

Cohesion soil $C = 0.35 \text{ kg/cm}^2$

Angle $\phi = 15^\circ$

Bulk density $\gamma = 2 \text{ gm/cc}$

a) FOS w.r.t cohesion, if FOS desired with respect to friction = 1.5

As we know

$$F_s = \frac{\tan \phi}{\tan \phi_m} \Rightarrow 1.5 = \frac{\tan 15^\circ}{\tan \phi_m}$$

$$\tan \phi_m = \frac{\tan 15^\circ}{1.5}$$

$$\phi_m = 10^\circ, \quad S_n = 0.06$$

$$S_n = \frac{C}{F_c \gamma H}$$

$$0.06 = \frac{3500}{F_c \times 2000 \times 25} \quad F_c = 1.16$$

b) If FOS with respect to cohesion is 1.5, then what is FOS with respect to friction = ? ($F_\phi = ?$)

$$S_n = \frac{C}{F_c \gamma H}$$

$$S_n = \frac{3500}{1.5 \times 2000 \times 25}$$

$$S_n = 0.049 \approx 0.05$$

$$\therefore \phi_m = 12.5^\circ$$

$$F_\phi = \frac{\tan \phi}{\tan \phi_m} = \frac{\tan 15^\circ}{\tan 12.5^\circ} = 1.2$$



05. Ans: 3.56 & 1.18

Sol: Given:

A new canal is excavated with

Depth of canal $h = 5$ m

$$C = 1.4 \text{ t/m}^2 ; \phi = 15^\circ$$

$$\gamma_{\text{sat}} = 1.945 \text{ t/m}^3$$

Slope of bank = 1 : 1

To find:

a) FOS w.r.t cohesion when canal runs full = ?

b) If it is suddenly emptied, FOS = ?

$$\text{a) } S_n = \frac{C}{F_c \gamma^1 H}$$

$$0.083 = \frac{1.4}{F_c (1.945 - 1) 5} \Rightarrow F_c = 3.56$$

$$\text{For } \phi = 15^\circ ; S_n = 0.083$$

$$\text{For } \phi = 7.5^\circ ; S_n = 0.122$$

$$\text{b) } \phi_m = \frac{\gamma}{\gamma_{\text{sat}}} \times 15 = 7.5$$

$$S_n = \frac{C}{F_c \gamma_{\text{sat}} H}$$

$$F_c = \frac{1.4}{0.122 \times 1.945 \times 5} = 1.179$$

06. Ans: $F_c = 2.4$ & $F_\phi = 2.89$

Sol: Given:

Embankment is to be made of a soil

Shear parameters of soil:

$$C' = 30 \text{ kN/m}^2 ; \phi' = 15^\circ$$

To find F_ϕ if $F_c = 1$

$$S_m = \frac{C'}{F_c} + \frac{\sigma' \tan \phi}{F_\phi} ; (\phi' = 15^\circ)$$

$$39.25 = \frac{30}{1} + \frac{100 \times \tan 15}{F_\phi}$$

$$F_\phi = 2.89$$

To find F_c if $F_\phi = 1$

$$S_m = \frac{C'}{F_c} + \frac{\sigma' \tan \phi'}{F_\phi}$$

$$39.25 = \frac{30}{F_c} + \frac{26.79}{1} \Rightarrow F_c = 2.40$$

Assignment Solutions

01. Ans: (a)

Sol:

Taylor's stability number

$$S_n = \frac{c}{F \gamma H}$$

When running full condition $\gamma' = \gamma_{\text{submerged}}$

$$0.046 = \frac{15}{1.5 \times 9 \times H}$$

$$\gamma_{\text{submerged}} = \gamma_{\text{sat}} - \gamma_w = 19 - 10 = 9 \text{ kN/m}^3$$

$$H = 24 \text{ m}$$

02. Ans: (d)

Sol:

$$\text{FOS} = \frac{S}{T} = \frac{C + \sigma \tan \phi}{T}$$



$$= \frac{C' + \gamma' z \cos^2 i \tan \phi'}{\gamma_{\text{sat}} z \cos i \sin i}$$

$$= - \frac{10 + 10 \times 5 \times \cos^2 10 \times \tan 25}{20 \times 5 \cos 10 \times \sin 10} = 1.90$$

03. Ans: 1.06

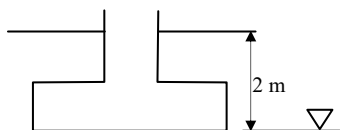
Sol: F.O.S = $\frac{\text{Resisting moment}}{\text{Driving moment}}$

$$= \frac{C_u LR}{W.x}$$

$$= \frac{50 \times 18 \times \frac{\pi}{180} \times 68^\circ \times 18}{2060 \times 8.8} = 1.06$$

Chapter- 16 Bearing Capacity of Soil

01. Ans: 211 kPa; 201 kPa; 4.74%



$$C = \frac{q}{2} = \frac{60}{2} = 30 \text{ KPa}$$

Ultimate bearing capacity

$$q_u = CN_c + \gamma DN_q + 0.5 \gamma BN_\gamma$$

$$\phi_u = 0, N_c = 5.7, N_q = 1, N_\gamma = 0$$

$\therefore q_u$ at W.T 2 m below the G.L

$$= 30 \times 5.7 + 20 \times 2 \times 1$$

$$= 211 \text{ KPa}$$

q_u at W.T 1 m below the G.L

$$= CN_c + \gamma_a DN_q$$

$$\gamma_a = \frac{20 \times 1 + (20 - 9.81)}{2}$$

$$= 15.095$$

$$q_u = 30 \times 5.7 + 15.095 \times 2$$

$$= 201.19 \text{ KPa}$$

% reduction in ultimate bearing capacity

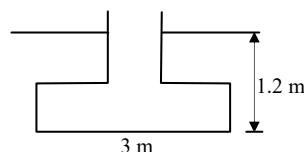
$$= \frac{211 - 201.19}{211} \times 100$$

$$= 4.64\%$$

02. Ans: 2.54, 2.03

Sol:

(a)



Net ultimate bearing capacity

$$q_{nu} = CN_c + (N_q - 1) \gamma_D + 0.4 \gamma BN_\gamma$$

$$C = 0, N_q = 22, N_\gamma = 20$$

$$q_{nu} = 21 \times 17 \times 1.2 + 0.4 \times 17 \times 3 \times 20$$

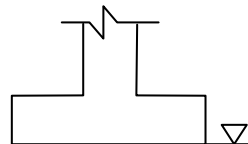
$$= 836.4 \text{ KPa}$$

$$\text{Safe bearing capacity } q_s = \frac{q_{nu}}{F} + \gamma_D$$

$$350 = \frac{836.4}{F} + 17 \times 1.2$$

$$F = 2.54$$

(b)



$$q_{nu} = (N_q - 1) \gamma_D + 0.4 \gamma' BN_\gamma$$

$$= 21 \times 17 \times 1.2 + 0.4 (20 - 9.81) 3 \times 20$$

$$= 672.96$$



Safe bearing capacity

$$q_s = \frac{q_{nu}}{F} + \gamma D$$

$$350 = \frac{672.96}{F} + 17 \times 1.2$$

$$F = 2.04$$

03. Ans: (b)

Sol: Given:

Depth = 1m

Square plate = 30 cm²

Load = 7.2 tones

S_p settlement = 25 mm

To find:

If settlement is limited for 10 mm

Allowable bearing pressure=?

$$q_1 = \frac{7.2}{(0.3)^2} = 80 \text{ t/m}^2$$

$$S_2 = 10 \text{ mm}$$

$$q = ?$$

(S ∝ q in case of granular soils)

$$\frac{S_2}{S_1} = \frac{q_2}{q_1}$$

$$\frac{10}{25} = \frac{q_2}{80}$$

$$q_2 = 32 \text{ t/m}^2$$

04. Ans: 446.7

Sol: B = 2 m

$$L = 2 \text{ m}$$

$$e = 1 - 0.85 = 0.15 \text{ m}$$

$$B' = B - 2e$$

$$= 2 - 2 \times 0.15 = 1.70 \text{ m}$$

There is no effect of water table as it is located well below the base of footing.

$$q_{ns} = \frac{1}{F} [\gamma D (N_q - 1) S_q d_q i_q + 0.5 \gamma B' N_\gamma S_\gamma d_\gamma i_\gamma]$$

Given:

$$F = 3 \quad \gamma = 18$$

$$D = 1 \text{ m} \quad N_q = 33.3$$

$$N_\gamma = 37.16 \quad B' = 1.70 \text{ m}$$

$$\text{Shape factors, } S_q \text{ or } F_{qs} = 1.314$$

$$S_\gamma \text{ or } F_{\gamma s} = 1.314$$

$$\text{Depth factors } d_q \text{ or } F_{qd} = 1.113$$

$$d_\gamma \text{ or } F_{\gamma d} = 1.113$$

Inclination factors

$$i_q \text{ or } F_{qi} = 0.444$$

$$i_\gamma \text{ or } F_{\gamma i} = 0.02$$

Substituting in the equation,

$$q_{ns} = \frac{1}{3} \left[18 \times 1 (33.3 - 1) 1.314 \times 1.113 \times 0.444 + 0.5 \times \right. \\ \left. 18 \times 1.7 \times 37.16 \times 1.314 \times 1.113 \times 0.02 \right]$$

$$= 131.39 \text{ kN/m}^2$$

$$\text{Net safe load} = A' \times q_{ns}$$

$$= B'L \times q_{ns}$$

$$= 1.7 \times 2 \times 131.39$$

$$= 446.7 \text{ kN}$$

05. Ans: 5.06 m

Sol: 1.5m × 1.5m

Gross load = column load + footing load



$$= 1962 + \frac{5}{100} \times 1962$$

$$= 2060.1$$

$$q = \frac{\text{gross load}}{\text{Area}} = \frac{2060.1}{(1.5)^2} = 915.6 \text{ kN/m}^2$$

$$q_u = \gamma D N_q + 0.4 \gamma B N_\gamma$$

$\Rightarrow$ safe Bearing capacity,

$$q_s = \frac{1}{F} [\gamma D (N_q - 1) + 0.4 N_\gamma] + \gamma D$$

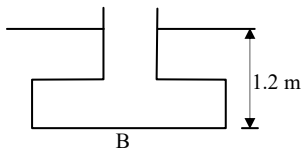
For safety pressure : $q \leq q_s$

$$915.6 = \frac{1}{3} [20.6 D (22 - 1) + 0.4 \times 20.6 \times 1.5 \times 20] + 20.6 \times D$$

$$D = 5.06 \text{ m}$$

06. Ans: 0.92 $\approx$ 1 m

Sol:



$$q_{nu} = C N_c$$

$$= 75 \times 5.7$$

$$= 427.5 \text{ KPa}$$

$$q_{ns} = \frac{q_{nu}}{F} = 142.5 \text{ KPa}$$

Safe bearing capacity $q_s = q_{ns} + \gamma D$

$$= 142.5 + 18.8 \times 1.2$$

$$= 165.06$$

$$\therefore \frac{152}{B \times 1} = 165.06$$

$$B = 0.92 \text{ m} \approx 1 \text{ m}$$

07. Ans: 6.55 m

Sol: Given:

Size of foundation = 14m $\times$ 21m

Unconfined compressive strength = 15 kN/m²

$$C_u = \frac{15}{2} = 7.5 \text{ kN/m}^2$$

Gross pressure intensity $q_u = 140 \text{ kN/m}^2$

$$\text{FOS} = 3; \gamma_{\text{clay}} = 19 \text{ kN/m}^3$$

For safety $q_n \leq q_{na}$

Where, $q_{na} \rightarrow$ net allowable bearing capacity of soil which is smaller of q_{ns} & q_{np}

According to skemtons;

$$q_{nu} = C N_c$$

For Rectangular footing;

$$N_c = 5 \left[1 + 0.2 \frac{D}{B} \right] \left[1 + 0.2 \frac{B}{L} \right]$$

$$q_{ns} = \frac{q_{nu}}{\text{F.O.S}}$$

$$N_c = 5 \left[1 + 0.2 \frac{D}{14} \right] \left[1 + 0.2 \times \frac{14}{21} \right]$$

$$N_c = \frac{17}{3} \left(1 + 0.2 \frac{D}{14} \right)$$

$$q_{nu} = 7.5 \times \frac{17}{3} \left(1 + 0.2 \frac{D}{14} \right)$$

$$= 42.5 \left(1 + 0.2 \frac{D}{14} \right)$$

$$q_{ns} = \frac{q_{nu}}{\text{FOS}} = \frac{42.5}{3} \left(1 + 0.2 \frac{D}{14} \right)$$

$$= 14.17 \left(1 + 0.2 \frac{D}{14} \right)$$

Since there is a provision for basement floor, the footing is not back filled. Hence,

$$q_n = q_u - \gamma D$$

$$= 140 - 19 \times D$$



$$140 - 19 \times D = 14.17 \left(1 + 0.2 \frac{D}{14} \right)$$

$$140 - 19 \times D = 14.17 + 0.202D$$

$$125.83 = 19.202D$$

$$D = 6.55 \text{ m}$$

Assignment Solutions

01. Ans: (c)

Sol:

Unconfined compressive strength $q = 2C_u$

$$100 = 2C_u$$

$$C_u = 50 \text{ kN/m}^2$$

$\therefore$ According to skempton's theory

Net ultimate bearing capacity

$$q_{nu} = CN_c$$

for rectangular footing

$$N_c = 5 \left(1 + 0.2 \frac{0}{B} \right) \left(1 + 0.2 \frac{B}{L} \right)$$

$$N_c = 5 \left(1 + 0.2 \left(\frac{2}{1} \right) \right) \left(1 + 0.2 \frac{1}{2} \right)$$

$$= 7.7$$

$$\therefore q_{nu} = 50 \times 5.7$$

$$= 385 \text{ kN/m}^2$$

Chapter- 17 Pile Foundation

01. Ans: $Q_u = 134.3 \text{ kN}$

Sol: Given:

Diameter of bored concrete pile = 30cm

Length passes through stiff fissures = 6.50m

Depth of shrinkage & swelling = 1.50m

Average undrained stress of clay = 50 kPa

below pile = 100 kPa

$$\alpha = 0.3$$

To find:

Ultimate load capacity = ?

$$Q_u = A_b C N_c + A_s \alpha C$$

$$= 0.070 \times 100 \times 9 + 4.71 \times 0.3 \times 50$$

$$= 134.3 \text{ kN}$$

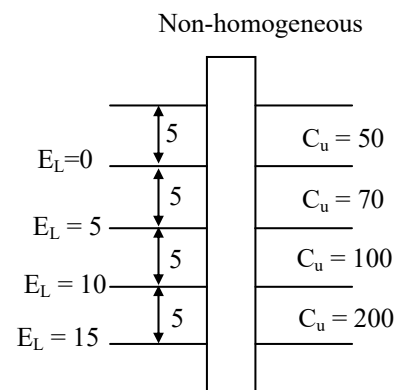
$$\therefore A_s = \pi d l$$

$$= 3.14 \times 5 \times 0.3$$

$$= 4.71 \text{ m}^2$$

02. Ans: 669 kN

Sol:



Given:

$$L = 20 \text{ m}$$

$$\phi = 500 \text{ mm} = 0.5 \text{ m}$$

$$\alpha = 0.4$$

$$F = 2.5$$

$$N_c = 9 ; \phi_u = 0$$



To find:

$$Q_{\text{safe}} = ?$$

$$Q_{\text{safe}} = \frac{1}{F} [A_b C N_C + A_s \alpha C]$$

At base:

$$Q_{\text{safe}} = \frac{1}{2.5} \left[\begin{aligned} &\frac{\pi}{4} \times 0.5^2 \times 200 \times 9 + (\pi \times 0.5) \times 5 \times 0.4 \times 50 \\ &+ \pi \times 0.5 \times 5 \times 0.4 \times 70 \\ &+ \pi \times 0.5 \times 5 \times 0.4 \times 100 \\ &+ \pi \times 0.5 \times 5 \times 0.4 \times 200 \end{aligned} \right]$$

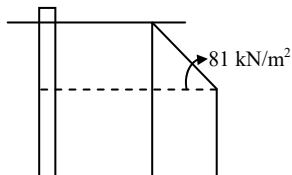
$$= (353.25 + 1318)$$

$$q_u = 1672.26$$

$$q_s = \frac{q_u}{F} = \frac{1672.05}{2.5} = 669 \text{ kN}$$

03. Ans: 813.41 kN

Sol:



Critical depth = 15 × diameter

$$= 15 \times 0.3 = 4.5 \text{ m}$$

Effective vertical pressure $\sigma'_v = 4.5 \times 18$

$$= 81 \text{ kN/m}^2$$

$$\therefore Q_u = A_b f_b + A_s f_s$$

$$= \frac{\pi}{4} \times d^2 \times \sigma'_v \times N_q + k \tan \delta$$

(area of σ'_v diagram) × perimeter of pile

$$= \frac{\pi}{4} \times 0.3^2 \times 81 \times 137 + 2 \times \tan 40^\circ \left(\frac{1}{2} \times 81 \times 4.5 + 81 \times 7.5 \right) \pi \times 0.3$$

$$= 784.40 + 1249.12$$

$$Q_u = 2033.52$$

$$\therefore \text{safe load capacity} = \frac{Q_u}{F} = \frac{2033.52}{2.5} = 813.40 \text{ kN}$$

04. Ans: ($Q_g = 27390.6 \text{ kN}$)

Sol: Given:

$$n = 25$$

$$L = 12 - 2 = 10 \text{ m}$$

$$\text{Dia} = 0.5 \text{ m}$$

$$S = 1 \text{ m c/c}$$

$$C = 180 \text{ kPa}$$

$$C_{\text{avg}} = 110 \text{ kPa}$$

$$\alpha = 0.45$$

$$B_0 = L_0 = 4S + d = 4.5 \text{ m}$$

$$Q_{gi} = n \left[\frac{\pi}{4} (0.5)^2 \times 180 \times 9 + \pi \times 0.5 \times 10 \times 0.45 \times 100 \right] = 27390.76 \text{ kN}$$

$$Q_{gb} = (4.5)^2 \times 9 \times 180 + 4 \times 4.5 \times 10 \times 110 = 52605 \text{ kN}$$

$$Q_g = 27390.6 \text{ kN}$$

$$\left(\begin{array}{l} \text{take minimum of two} \\ \text{i.e., } Q_{gi} \text{ \& } Q_{gb} \end{array} \right)$$



05. Ans: $S = 2.18d$

Sol:

Given:

$$n = 16 \text{ pile group}$$

$$\alpha = 0.6$$

$$Q_{gi} = n \left[\frac{\pi}{4} d^2 \times C \times 9 + \pi d \times L \times 0.6C \right]$$

(neglect end bearing)

$$= n [\pi d L \times 0.6 C]$$

$$Q_{gb} = 4(3S + d) \times L \times C$$

For optimum spacing

$$Q_{gi} = Q_{gb} \quad (\eta_g = 100\%)$$

$$16[\pi d L \times 0.6 C] = 4(3S + d) \times L \times C$$

$$4\pi d \times 0.6 = 3S + d$$

$$6.54 d = 3S$$

$$S = 2.18 d$$

06. Ans: 635 kN

Sol: λ Method:

$$Q_u = A_b \times C \times N_c + A_s \lambda \times [\sigma'_{va} + 2c]$$

$$\lambda = \text{constant} = 0.15,$$

$$\text{Dia} = 0.4 \text{ m}, \gamma = 18 \text{ kN/m}^3, \text{F.O.S} = 3$$

$$\text{Depth (H)} = 25 \text{ m}, N_c = 9 \text{ for pile in clay}$$

$$\sigma'_{va} = \text{Average effective vertical pressure}$$

along the pile length

$$\sigma'_{va} = \frac{0 + \gamma H}{2} = \frac{0 + 18 \times 25}{2}$$

$$= 225 \text{ kPa}$$

$$\begin{aligned} Q_u &= \frac{\pi}{4} (0.4^2) \times 80 \times 9 + \pi \times 0.4 \times 25 \times 0.15 \\ &\quad \times (225 + 2 \times 80) \\ &= 1904.74 \text{ kN} \end{aligned}$$

Safe load (or) Allowable load

$$\begin{aligned} Q_{\text{safe}} &= \frac{Q_u}{\text{F.O.S}} = \frac{1904.74}{3} \\ &= 635 \text{ kN} \end{aligned}$$

07. Ans: 68.25%; 6825 kN

Sol: Engineering News formula for Drop Hammer:

It is based on the assumption that kinetic energy delivered by the hammer during driving operation is equal to work done on the pile.

According to Engineering News's formula,

$$Q_s = \frac{W \cdot h \cdot \eta_h}{F(S + C)}$$

Where,

Q_s = Safe Pile capacity

W = Weight of hammer

h = height of drop

η_h = Efficiency of pile hammer

S = penetration of pile per hammer blow

C = constant

For drop hammer, $C = 2.54 \text{ cm}$, for steam hammer $C = 0.254 \text{ cm}$

Factor of safety = 6



Applications:

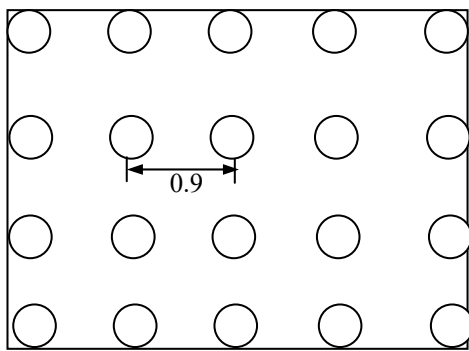
- This formula is more applicable to piles driven into cohesionless soil.
- If the pile is driven into saturated loose sand and silt, liquefaction might result, reducing the pile capacity. So it is not applicable to saturated loose sand.

4 × 5 pile group

Diameter of each pile = 0.3 m

C/C spacing = 0.9 m

capacity of a single pile = 500 kN



According to converse Labarre formula:

$$\eta_g = 1 - \frac{\theta}{90} \left[\frac{(n-1)m + (m-1)n}{mn} \right]$$

$m \rightarrow$ no. of rows of piles = 4

$n \rightarrow$ no. of piles in each row = 5

$$\theta = \tan^{-1} \left(\frac{d}{s} \right) = 18.43$$

$$\begin{aligned} \eta_g &= 1 - \frac{18.43}{90} \left[\frac{(5-1)4 + 5(4-1)}{4 \times 5} \right] \\ &= 1 - \frac{18.43}{90} \left[\frac{16 + 15}{20} \right] \end{aligned}$$

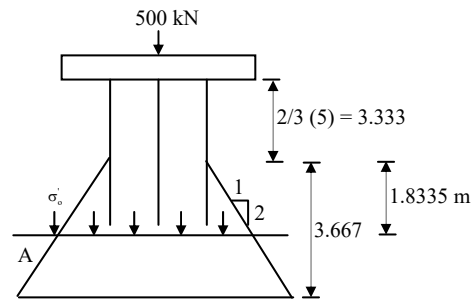
$$\eta_g = 68.25 \%$$

Capacity of free standing pile group

$$= \eta_g \times Q_{gi} \times n = 0.6825 \times 500 \times 20 = 6825 \text{ kN}$$

08. Ans: 15 mm

Sol:



σ_o' at point A

$$\begin{aligned} &= (3.333 + 1.8335) (20 - 9.81) \\ &= 52.6466 \text{ kN/m}^2 \end{aligned}$$

$$\begin{aligned} \text{Cross-section area at A} &= (1.2 + 1.8335)^2 \\ &= 9.202 \text{ m}^2 \end{aligned}$$

$$\Delta \sigma = \frac{500}{9.202} = 54.33 \text{ kN/m}^2$$

$\therefore$ Settlement of clay layer

$$\begin{aligned} S_f &= C_c \left(\frac{H}{1 + e_o} \right) \log \left(\frac{\sigma_f'}{\sigma_o'} \right) \\ &= 0.027 \left(\frac{3.667}{1 + 1.05} \right) \log \left(\frac{54.33 + 52.64}{52.64} \right) \\ &= 14.8 \text{ mm} \approx 15 \text{ mm} \end{aligned}$$



Assignment Solutions

01. Ans: (c)

Sol: Load carrying capacity $q = f_s A_s$

$$q = \alpha C \pi DL$$

$$= 0.7 \times 4 \times \pi \times 0.3 \times 10$$

$$= 26.389 \text{ t}$$

$$\text{Safe load} = \frac{q}{F} = \frac{26.389}{2.5} = 10.55 \text{ t}$$

05. Ans: (c)

Sol: $Q_g = (n \cdot Q_i) \cdot \eta_g$

$$= 9 \times 200 \times 0.8 = 1440 \text{ kN}$$

07. Ans: 251.8 kN

$$\text{Sol: } Q = \frac{W \eta_h \eta_b}{F \left(S + \frac{C}{2} \right)}$$

$$= \frac{3500 \times 0.8 \times 0.476}{4 \left(\frac{2.54}{6} + 9 \right)}$$

$$= 251.8 \text{ kN}$$

Chapter- 18 Soil Exploration

02. Ans: (c)

$$\text{Sol: } N = 6 + 6 + 8 + 7 = 27$$

$$N' = C_N N = 1 \times 27 = 27$$

$$N'' = 15 + \left(\frac{N' - 15}{2} \right) = 21$$

03. Ans: 14

Sol: Corrected value $N' = C_N N$

C_N = correction factor for over burden
pressure

$$C_N = 0.77 \log_{10} \left(\frac{1905}{\sigma'_o} \right)$$

$$\sigma'_o = 2 \times 18 + (18 - 9.81) \times 3$$

$$= 60.57 \text{ kN/m}^2$$

$$C_N = 0.77 \log_{10} \left(\frac{1905}{60.57} \right) = 1.153$$

$$N' = 1.153 \times 12 = 13.8 \approx 14$$



Chapter- 19 Sheet Piles

01. Ans: 98.7 kN

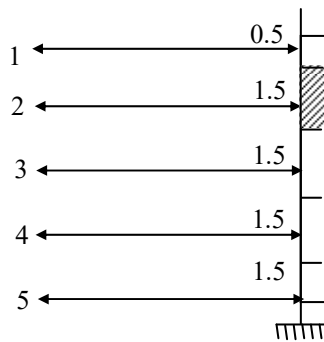
Sol: $k_a = \frac{1 - \sin \phi}{1 + \sin \phi} = 0.259$

$\gamma = 20 \text{ kN/m}^3$

$H = 6.5 \text{ m}$

$\phi = 36^\circ$

$C = 0$



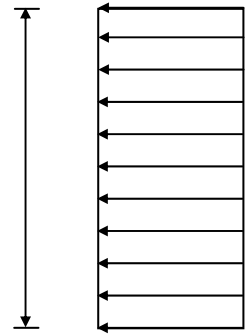
$P' = 0.65 K_a H \gamma$

$P' = 21.93 \text{ kN/m}^2$

Total pressure acting $P = 21.93 \text{ kN/m}^2 \times \text{Height} \times \text{Width}$

$P = 21.93 \times 6.5 \times 3$

$P = 427.7 \text{ kN}$



$P' = 0.65 K_a H \gamma$

The average load taken by the strut

$= \frac{427.7}{5} = 85.55 \text{ kN}$

But in the problem they asked maximum load taken by the strut

struts (1) (2) (3) (4) are taken maximum loads, (5) struts are taken minimum load.

Strut (2) taken load $= 1.5 \times 3 \times P'$

$= 1.5 \times 3 \times 21.93 \text{ kN}$

$= 98.68 \text{ kN}$