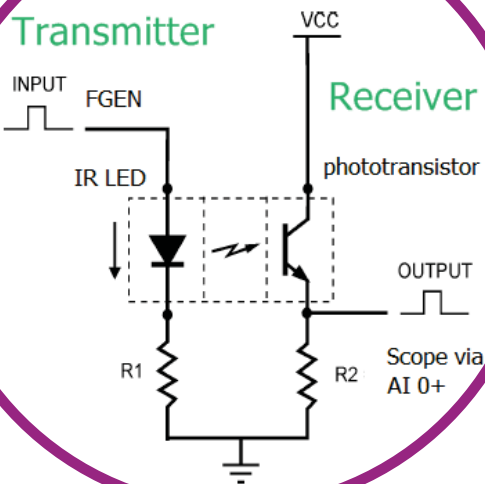




INSTRUMENTATION ENGINEERING



GATE | PSUs

COMMUNICATION &
OPTICAL INSTRUMENTATION

Classroom Practice Solutions
To
Communication & Optical Instrumentation

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Class Room Practice Solutions

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Class Room Practice Solutions

01. Ans: (a)

Sol: $V(t) = A_c \cos \omega_c t + 2 \cos \omega_m t \cdot \cos \omega_c t$.

Comparing this with the AM-DSB-SC signal

 $A \cos \omega_c t + m(t) \cdot \cos \omega_c t$, it implies that

$$m(t) = 2 \cos \omega_m t \Rightarrow E_m = 2$$

To implement Envelope detection,

$$A_c \geq E_m$$

$$\therefore (A_c)_{\min} = 2$$

02. Ans (d)

Sol: $m(t) = (A_c + A_m \cos \omega_m t) \cos \omega_c t$.

$$= A_c \left(1 + \frac{A_m}{A_c} \cos \omega_m t \right) \cos \omega_c t$$

Given

$$A_c = 2A_m$$

$$= A_c \left(1 + \frac{1}{2} \cos \omega_m t \right) \cos \omega_c t$$

$$P_T = \frac{A_c^2}{2} \left[1 + \frac{\mu^2}{2} \right], \quad P_s = \frac{A_c^2}{2} \left[\frac{\mu^2}{4} \right]$$

$$\frac{P_T}{P_s} = \frac{1 + \frac{\mu^2}{2}}{\frac{\mu^2}{4}} = \frac{1 + \frac{1}{8}}{\frac{1}{16}} = \frac{9}{8} \times 16$$

$$P_T = 18 P_s$$

03. Ans: (a)

Sol: $m(t) = 2 \cos 2\pi f_1 t + \cos 2\pi f_2 t$

$$C(t) = A_c \cos 2\pi f_c t$$

$$S(t) = [A_c + m(t)] \cos 2\pi f_c t$$

$$S(t) = A_c \left[1 + \frac{1}{A_c} m(t) \right] \cos 2\pi f_c t$$

$$K_a = \frac{1}{A_c}$$

$$A_{m1} = 2, \quad A_{m2} = 1$$

$$\mu_1 = K_a A_{m1} = \frac{2}{A_c}, \quad \mu_2 = K_a A_{m2} = \frac{1}{A_c}$$

$$\mu = \sqrt{\mu_1^2 + \mu_2^2}$$

$$\Rightarrow 0.5 = \sqrt{\frac{4}{A_c^2} + \frac{1}{A_c^2}}$$

$$\Rightarrow A_c = \sqrt{20}$$

04. Ans: (c)

Sol: $m(t) = -0.2 + 0.6 \sin \omega_1 t$, $k_a = 1$, $A_c = 100$

$$S(t) = A_c [1 - 0.2 + 0.6 \sin \omega_1 t] \cos \omega_c t$$

$$= 100 [0.8 + 0.6 \sin \omega_1 t] \cos \omega_c t$$

$$V_{\max} = A_c [1 + \mu] = 100 [0.8 + 0.6] = 140 \text{ V}$$

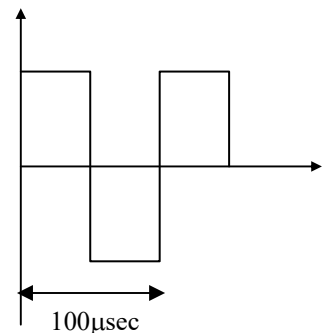
$$V_{\min} = A_c [1 - \mu] = 100 [0.8 - 0.6] = 20 \text{ V}$$

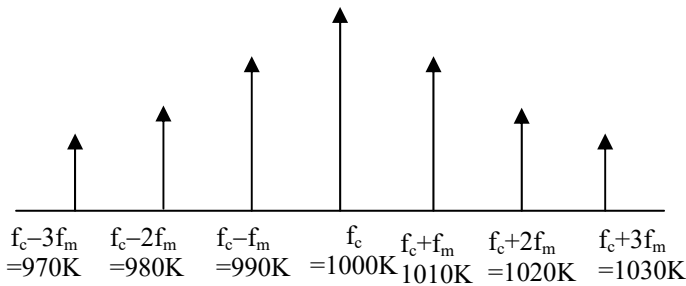
$$= 20 \text{ V to } 140 \text{ V}$$

05. Ans: (c)

Sol: $f_c = 1 \text{ MHz} = 1000 \text{ kHz}$ The given $m(t)$ is symmetrical square wave of period $T = 100 \mu\text{sec}$

$$f_m = \frac{1}{T_0} = 10 \text{ kHz}$$



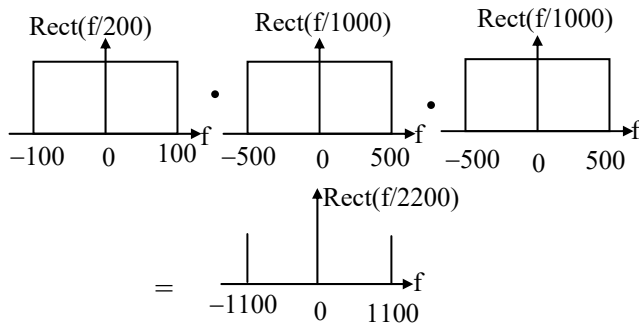


These frequencies 980k, 1020k are not present because the symmetrical square wave it consists of half wave symmetries only odd harmonics are present, even harmonics are dismissed

06. Ans: (d)

Sol: $m(t) = \text{sinc}(200t)\text{sinc}^2(1000t)$

$$= \text{sinc}(200t)\text{sinc}(1000t)\text{sinc}(1000t)$$

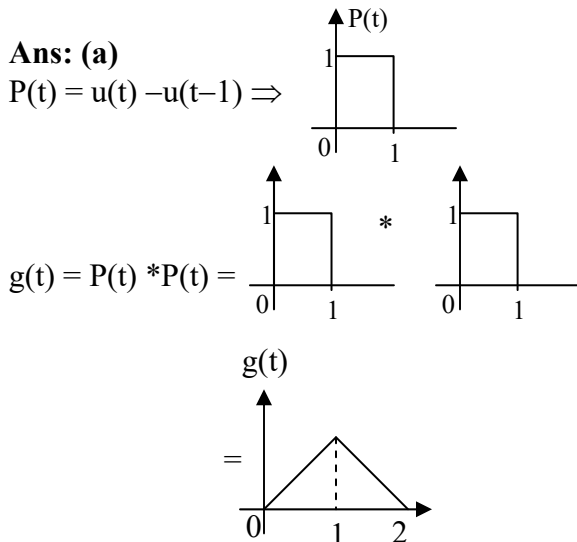


$$\text{BW} = 2 \times 1100$$

$$\text{BW} = 2200 \text{ Hz}$$

07. Ans: (a)

Sol: $P(t) = u(t) - u(t-1) \Rightarrow$



$$X(t) = 100(P(t) + 0.5g(t))\cos\omega_c t$$

$$= 100(1 + 0.5t)\cos\omega_c t$$

$$= A_c(1 + K_a m(t))\cos\omega_c t$$

$$k_a = 0.5, m(t) = t$$

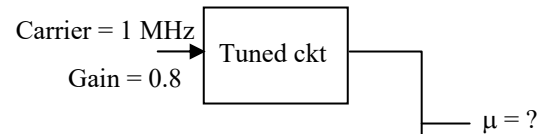
$$\mu = k_a[m(t)]_{\text{max}}$$

$$\mu = 0.5 \times 1 = 0.5$$

08. Ans: (d)

09. Ans (b)

Sol: $S(t) = 10\cos 2\pi 10^6 t + 8\cos 2\pi 5 \times 10^3 t \cos 2\pi 10^6 t$

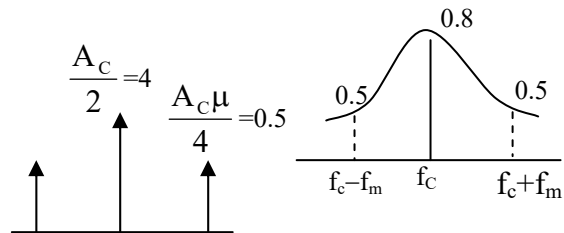


$$S(t) = 0.8 \times 10 \cos 2\pi 10^6 t$$

$$+ 0.5 \times 8 \cos 2\pi 5000 t \cos 2\pi 10^6 t$$

$$= 8 \left(1 + \frac{4}{8} \cos 2\pi 5000 t \right) \cos 2\pi 10^6 t$$

$$\mu = \frac{4}{8} = \frac{1}{2} = 0.5$$



10. Ans: (d)

Sol: $A_{\text{max}} = 10V$

$$A_{\text{min}} = 5V$$

$$\mu = 0.1$$

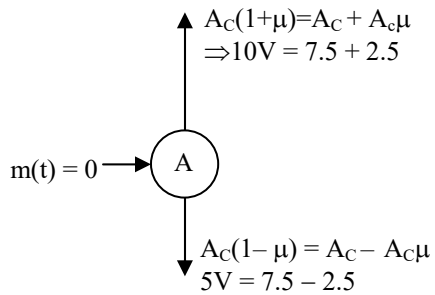


$$\mu = \frac{A_{\max} - A_{\min}}{A_{\max} + A_{\min}}$$

$$= \frac{1}{3} = 0.33$$

$$A_C = \frac{A_{\max} + A_{\min}}{2}$$

$$= \frac{10 + 5}{2} = 7.5 \text{ V}$$



$$\text{Amplitude deviation } A_c\mu = 7.5 \times \frac{1}{3} = 2.5 \text{ V}$$

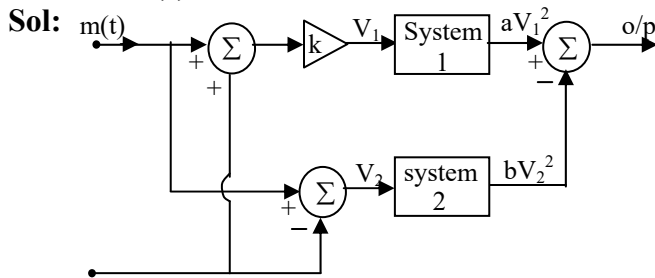
$$\mu_2 = 0.1 \Rightarrow A_{c2}\mu_2 = 2.5$$

$$A_{c2} = 25 \text{ V}$$

Which must be added to attain = 17.5

Class Room Practice Solutions

01. Ans: (c)

 $A \cos \omega_c t$

$$V_1 = k [m(t) + c(t)]$$

$$V_2 = [m(t) - c(t)]$$

$$V_0 = aV_1^2 - bV_2^2$$

$$\begin{aligned} &= ak^2 [m(t) + c(t)]^2 - b[m(t) - c(t)]^2 \\ &= ak^2 [m^2(t) + c^2(t) + 2m(t)c(t)] \\ &\quad - b[m^2(t) + c^2(t) - 2m(t)c(t)] \\ &= [ak^2 - b]m^2(t) + [ak^2 - b]c^2(t) \\ &\quad + 2[ak^2 + b][m(t)c(t)] \end{aligned}$$

on verification if $k = \sqrt{\frac{b}{a}}$

$$S(t) = 4bm(t)c(t) \rightarrow \text{DSBSC Signal}$$

02. Ans: (d)

Sol: Given $A = 10$

$$m(t) = \cos 1000\pi t$$

$$b = 1$$

B.W = ? and power = ?

$$s(t) = 4b.A \cos 2\pi f_c t \cdot \cos 2\pi (500)t$$

$$= 40 \cdot \cos 2\pi f_c t \cdot \cos 2\pi (500)t$$

$$B.W = 2 f_m$$

$$= 2 (500) = 1 \text{ kHz}$$

$$\begin{aligned} \text{Power} &= \frac{A_c^2 A_m^2}{4} \\ &= \frac{1600 \times 1}{4} \\ &= 400 \text{ W} \end{aligned}$$

03. Ans: (c)

Sol: Carrier = $\cos 2\pi (100 \times 10^6)t$ Modulating signal = $\cos(2\pi \times 10^6)t$

Output of Balanced modulator

$$= 0.5[\cos 2\pi (101 \times 10^6)t + \cos 2\pi (99 \times 10^6)t]$$

The Output of HPF is $0.5 \cos 2\pi (101 \times 10^6)t$

Output of the adder is

$$\begin{aligned} &= 0.5 \cos 2\pi (101 \times 10^6)t + \sin 2\pi (100 \times 10^6)t \\ &= 0.5 \cos 2\pi [(100+1)10^6 t] + \sin 2\pi (100 \times 10^6)t \\ &= 0.5[\cos 2\pi (100 \times 10^6)t \cdot \cos 2\pi (10^6)t \\ &\quad - \sin 2\pi (100 \times 10^6)t \cdot \sin 2\pi (10^6)t] \\ &\quad + \sin 2\pi (100 \times 10^6)t \\ &= 0.5 \cos 2\pi (100 \times 10^6)t \cdot \cos 2\pi (10^6)t \\ &\quad + \sin 2\pi (100 \times 10^6)t [1 - 0.5 \sin 2\pi (10^6)t] \end{aligned}$$

Let $0.5 \cos 2\pi (10^6)t = r(t) \cos \theta(t)$ $1 - 0.5 \sin 2\pi (10^6)t = r(t) \cdot \sin \theta(t)$

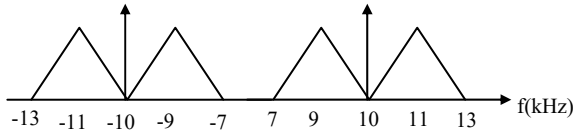
The envelope is

$$\begin{aligned} r(t) &= [0.25 \cos^2 2\pi (10^6)t \\ &\quad + \{1 - 0.5 \sin 2\pi (10^6)t\}^2]^{1/2} \\ &= [1.25 - \sin 2\pi (10^6)t]^{1/2} \\ &= \left[\frac{5}{4} - \sin 2\pi (10^6)t \right]^{1/2} \end{aligned}$$

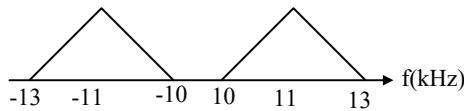


04. Ans: (b)

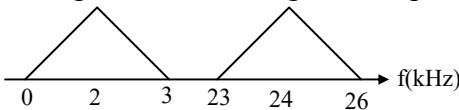
Sol: Output of 1st balanced modulator is



Output of HPF is



The Output of 2nd balanced modulator is consisting of the following +ve frequencies.



Thus, the spectral peaks occur at 2 kHz and 24 kHz

05. Ans: (c)

Sol: Given

$$f_{m_1} = 100\text{Hz}, f_{m_2} = 200\text{Hz}, f_{m_3} = 400\text{Hz},$$

$$f_c = 100\text{KHz}, f_{cLo} = 100.02\text{KHz}$$

$$S(t)/T_X = \frac{A_c A_m}{2} [\cos(f_c + f_{m_1})t + \cos(f_c + f_{m_2})t + \cos(f_c + f_{m_3})t]$$

$$S(t)/R_x = [S(t)/T_X] A_c \cos 2\pi f_{cLo} t$$

$$\Rightarrow \frac{A_c^2 A_m}{4} [\cos(f_c + f_{cLo} + f_{m_1}) + \cos(f_{m_1} - 20) + \cos(f_c + f_{cLo} + f_{m_2}) + \cos(f_{m_2} - 20) + \cos(f_c + f_{cLo} + f_{m_3}) + \cos(f_{m_3} - 20)]$$

Detector output frequencies:

$$80\text{Hz}, 180\text{Hz}, 380\text{Hz}$$

06. Ans: (b)

Sol: Given

SSB AM is used, LSB is transmitted

$$f_{LO} = (f_c + 10)$$

$$S(t)/T_X = \frac{A_c A_m}{2} \cos 2\pi [f_c - f_m]t$$

$$S(t)/R_X = \left[\frac{A_c A_m}{2} \cos 2\pi (f_c - f_m)t \right] \cos 2\pi (f_c + 10)t$$

$$\Rightarrow \frac{A_c A_m}{4} [\cos(2f_c + 10 - f_m)t + \cos(10 + f_m)t]$$

i.e., from 310 Hz to 1010 Hz

07. Ans: (b)

Sol: BW of Basic group = $12 \times 4 = 48$ kHz

BW of super group = $5 \times 48 = 240$ kHz

08. Ans: (d)

Sol: Given 11 voice signals

B.W. of each signals = 3 kHz

Guard Band Width = 1 kHz

Lowest $f_c = 300$ kHz

Highest $f_c =$

$$\Rightarrow f_{cH} + f_{m_{lost}} = 300\text{kHz} + 11(3\text{kHz}) + 10(1\text{kHz}) = 343 \text{ kHz}$$

$$f_{cH} = 343 \text{ kHz} - 3 \text{ kHz}$$

$$= 340 \text{ kHz}$$

09. Ans: (b)

Sol: $f_{m1} = 5$ kHz \rightarrow AM

$f_{m2} = 10$ kHz \rightarrow DSB

$f_{m3} = 10$ kHz \rightarrow SSB

$f_{m4} = 2$ kHz \rightarrow SSB

$f_{m5} = 5$ kHz \rightarrow AM

$f_g = 1$ kHz

$$BW = (2f_{m1} + 2f_{m2} + f_{m3} + f_{m4} + 2f_{m5} + 4f_g)$$

$$= 2 \times 5 + 2 \times 10 + 10 + 2 + 2 \times 5 + 4 \times 1$$

$$= 10 + 20 + 10 + 10 + 6$$

$$= 56 \text{ kHz}$$

$$\therefore BW = 56 \text{ kHz}$$

4

Angle Modulation

Chapter

Class Room Practice Solutions

01. Ans: (a)

Sol: $s(t) = 10 \cos(20\pi t + \pi t^2)$

$$f_i = \frac{1}{2\pi} \frac{d\theta_i(t)}{dt}$$

$$f_i = \frac{1}{2\pi} [20\pi + 2\pi t]$$

$$\frac{df_i}{dt} = \frac{1}{2\pi} \times 2\pi \times 1 = 1 \text{ Hz/sec}$$

02. Ans: (d)

03. Ans: (a)

Sol: In an FM signal, adjacent spectral components will get separated by

$$f_m = 5 \text{ kHz}$$

$$\text{Since BW} = 2(\Delta f + f_m) = 1 \text{ MHz}$$

$$= 1000 \times 10^3$$

$$\Delta f + f_m = 500 \text{ kHz}, \quad \Delta f = 495 \text{ kHz}$$

The n^{th} order non-linearity makes the carrier frequency and frequency deviation increased by n -fold, with the base-band signal frequency (f_m) left unchanged since

$$n = 3,$$

$$\therefore (\Delta f)_{\text{New}} = 1485 \text{ kHz} \quad \&$$

$$(f_c)_{\text{New}} = 300 \text{ MHz}$$

$$\text{New BW} = 2(1485 + 5) \times 10^3$$

$$= 2.98 \text{ MHz}$$

$$= 3 \text{ MHz}$$

04. Ans: (d)

$$\text{Sol: } S(t) = A_c \sum_{n=-\infty}^{\infty} J_n(\beta) \cos(2\pi f_c t + \beta \sin 2\pi f_m t)$$

$$\Delta f = 3(2f_m) = 12 \text{ kHz}$$

$$\beta = \frac{\Delta f}{f_m} = 6$$

$$\therefore S(t) = \sum_{n=-\infty}^{\infty} 5.J_n(6) \cos(2\pi f_c + \beta \sin t)$$

$$f_c = 1000 \text{ kHz}, f_m = 2 \text{ kHz}$$

$$= \cos 2\pi(1008 \times 10^3)t$$

$$= \cos 2\pi(1000 + 4 \times 2) \times 10^3 t$$

$$\text{i.e., } n = 4$$

The required coefficient is $5.J_4(6)$

05. Ans: (c)

$$\text{Sol: } 2\pi f_m = 4\pi \times 10^3$$

$$\Rightarrow f_m = 2 \text{ k}$$

$$J_0(\beta) = 0 \text{ at } \beta = 2.4$$

$$\beta = \frac{k_f A_m}{f_m} \Rightarrow 2.4 = \frac{k_f \times 2}{2 \text{ k}}$$

$$k_f = 2.4 \text{ KHz/V}$$

$$\text{at } \beta = 5.5$$

$$5.5 = \frac{2.4 \text{ k} \times 2}{f_m}$$

$$\Rightarrow f_m = 872.72$$

06. Ans (c)

$$\text{Sol: } \beta = 6$$

$$J_0(6) = 0.1506 ; J_3(6) = 0.1148$$

$$J_1(6) = 0.2767 ; J_4(6) = 0.3576$$

$$J_2(6) = 0.2429 ;$$

$$\frac{P_{f_c \pm 4f_m}}{P_T} = ? \quad P_T = \frac{A_c^2}{2R}$$



$$P_{f_c \pm 4f_m} = \frac{A_C^2}{R} \left[\frac{J_0^2(\beta)}{2} + J_1^2(\beta) + J_2^2(\beta) + J_3^2(\beta) + J_4^2(\beta) \right]$$

$$P_{f_c \pm 4f_m} = \frac{A_C^2}{R} \left[\frac{J_0^2(\beta)}{2} + J_1^2(\beta) + J_2^2(\beta) + J_4^2(\beta) \right]$$

$$\frac{P_{f_c \pm 4f_m}}{P_T} = \frac{0.2879}{1/2} = 0.5759 = 57.6 \%$$

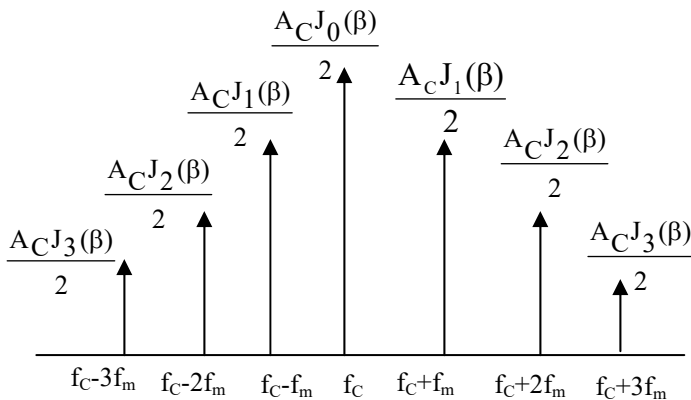
07. Ans: (c)

Sol: $m(t) = 10\cos 20\pi t$

$$f_m = 10 \text{ Hz}$$

inserting correct signal and frequency

$$\beta = \frac{k_f A_m}{f_m} = \frac{5 \times 10}{10} = 5$$



From f_c to $f_c + 4f_m$ pass through ideal BPF

Powers in these frequency components

$$P = \frac{A_C^2}{2R} J_0^2(\beta) + 2 \frac{A_C^2}{2R} J_1^2(\beta) + 2 \frac{A_C^2}{2R} J_2^2(\beta)$$

$$+ 2 \frac{A_C^2}{2R} J_3^2(\beta) + 2 \frac{A_C^2}{1R} J_4^2(\beta)$$

$$= \frac{A_C^2}{2R} \left[(-0.178)^2 + 2(-0.328)^2 + 2(0.049)^2 \right. \\ \left. + 2(0.365)^2 + 2(0.391)^2 \right]$$

$$= 41.17 \text{ Watts}$$

08. Ans: (d)

$$\text{Sol: } P_t = \frac{A_C^2}{2R} \quad (R=1\Omega)$$

$$= \frac{100}{2} = 50 \text{ W}$$

$$\% \text{ Power} = \frac{\text{Power in components}}{\text{total power}} \times 100$$

$$= \frac{41.17}{50} \times 100$$

$$= 82.35\%$$

09. Ans: (d)

10. Ans: (c)

Sol: Given $f_c = 1\text{MHz}$

$$f_{\max} = f_c + k_f A_m$$

$$k_p = 2\pi k_f$$

$$k_f = \frac{k_p}{2\pi} = \frac{\pi}{2\pi}$$

$$= \frac{1}{2}$$

$$= \left(10^6 + \frac{1}{2} \times 10^5 \right) = \left(10^6 + 0.5 \times 10^5 \right)$$

$$= \left(10^6 + 5 \times 10^4 \right)$$

$$= \left(10^3 + 50 \right) 10^3$$

$$= \left(10^3 + 50 \right) \text{ k}$$

$$= 1050 \text{ kHz.}$$

$$f_{\min} = f_c - k_f A_m$$

$$= \left(10^6 - \frac{1}{2} \times 10^5 \right)$$

$$= \left(10^6 - 0.5 \times 10^5 \right)$$

$$= \left(10^6 - 5 \times 10^4 \right)$$



$$= (10^3 - 50)10^3$$

$$= (10^3 - 50) \text{ k}$$

$$= 950 \text{ kHz}$$

11. Ans: (d)

Sol: $\beta = \frac{\Delta f}{f_m}$

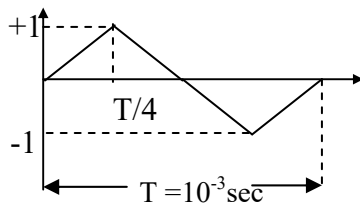
$$\Delta\phi = \frac{\Delta f}{f_m}$$

$$\Delta f = \Delta\phi f_m$$

$$= k_p A_m f_m$$

12. Ans: (c)

Sol: Given



$$f_c = 100 \times 10^3 \text{ Hz}$$

$$k_f = 10 \times 10^3 \text{ Hz}$$

$$m(t)|_{\max} = +1, m(t)|_{\min} = -1$$

$$f_i = f_c \pm \Delta f$$

$$= f_c \pm k_f A_m$$

$$= 100 \times 10^3 \pm 10 \times 10^3 (m(t))$$

$$= 110 \text{ kHz} \text{ \& } 90 \text{ kHz}$$

13. Ans: (c)

Sol: $S(t) = A_c \cos(2\pi f_c t + k_p m(t))$

$$f_i = \frac{1}{2\pi} \frac{d}{dt} \theta_i(t)$$

$$= \frac{1}{2\pi} \frac{d}{dt} (2\pi f_c t + k_p m(t))$$

$$= f_c + \frac{1}{2\pi} k_p \frac{d}{dt} m(t)$$

$$f_{\max} = f_c + \frac{k_p}{2\pi} \frac{1}{\left(\frac{10^{-3}}{4}\right)} = f_c + \frac{k_p}{2\pi} \times 4 \times 10^3$$

$$= 100 \text{ kHz} + \frac{\pi}{2\pi} \times 4 \times 10^3$$

$$= 102 \text{ kHz}$$

$$f_{\min} = f_c - k_p \frac{1}{\left(\frac{10^{-3}}{4}\right)}$$

$$= f_c - 2 \text{ kHz}$$

$$f_{\min} = 98 \text{ kHz}$$

14. Ans: (c)

Sol: Given,

$$S(t) = A_c \cos(\theta_i(t))$$

$$= A_c \cos(\omega_c t + \phi(t))$$

$$m(t) = \cos(\omega_m t)$$

$$f_i(t) = f_c + 2\pi k (f_m)^2 \cos \omega_m t$$

$$f_i = \frac{1}{2\pi} \frac{d\theta_i(t)}{dt}$$

$$\theta_i(t) = \int 2\pi f_i(t) dt$$

$$\theta_i(t) = \int 2\pi [f_c + 2\pi k (f_m)^2 \cos \omega_m t] dt$$

$$\theta_i(t) = 2\pi f_c t + (2\pi f_m)^2 k \frac{\cos \omega_m t}{\omega_m t}$$

$$\theta_i(t) = \omega_c t + \omega_m k \sin \omega_m t$$

15. Ans: (b)

Sol: $\Delta f_{\max} = K_f |m(t)|_{\max}$

$$= \frac{100}{2\pi} \times [10]$$

$$\Delta f_{\max} = \left(\frac{500}{\pi}\right) \text{ Hz}$$



16. Ans: (b)

Sol: Given that

$$s(t) = \cos[\omega_c t + 2\pi m(t)] \text{ volts}$$

$$f_i = \frac{1}{2\pi} \frac{d}{dt} [\omega_c t + 2\pi m(t)]$$

$$= \frac{1}{2\pi} \frac{d}{dt} [2\pi f_c t + 2\pi m(t)]$$

$$f_i = f_c + \frac{d}{dt} [m(t)]$$

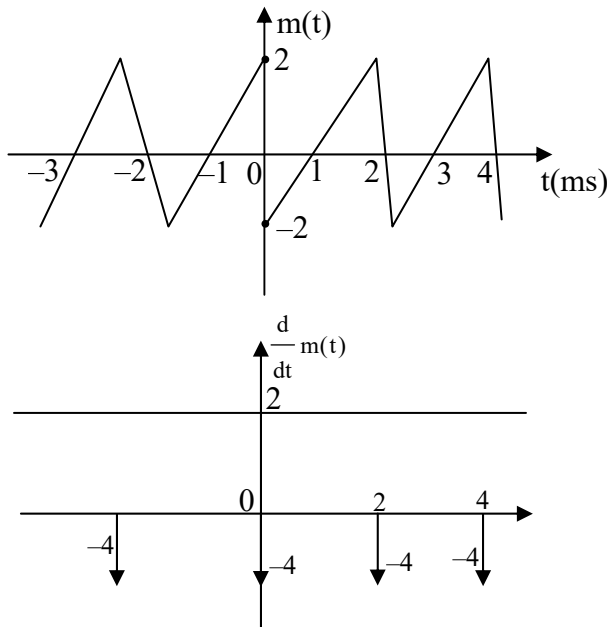
we know that $f_i = f_c + k_f m(t)$

$$\text{Here } k_f m(t) = \frac{d}{dt} [m(t)]$$

$$\Delta f = \max\{k_f m(t)\}$$

$$\Delta f = \max\left[\frac{d}{dt} m(t)\right]$$

$$\Delta f = 2 \text{ kHz}$$



17. Ans: (a)

Sol: $\beta_p = k_p \max [|m(t)|] = 1.5 \times 2 = 3$

$$\beta_f = \frac{k_f \max [|m(t)|]}{f_m}$$

$$= \frac{3000 \times 2}{1000}$$

$$= 6$$

18. Ans: (a)

Sol: Using Carson's rule we obtain

$$BW_{PM} = 2 (\beta_p + 1) f_m = 8 \times 1000 = 8000 \text{ Hz}$$

$$BW_{FM} = 2 (\beta_f + 1) f_m = 14 \times 1000 = 14000 \text{ Hz}$$

19. Ans: 70 kHz

Sol: $s(t) = A_c \cos[2\pi f_c t + k_p m(t)]$

$$f_i = f_c + \frac{k_p}{2\pi} \frac{d}{dt} x(t)$$

$$= 20 \text{ k} + \frac{5}{2\pi} \times 5 \frac{d}{dt} (\sin 4\pi 10^3 t - 10\pi \cos 2\pi 10^3 t)$$

$$= 20 \text{ k} + \frac{25}{2\pi} \times \left[\cos(4\pi 10^3 t - 10\pi \cos 2\pi 10^3 t) \right]$$

$$\left[(4\pi 10^3 + 10\pi \sin 2\pi 10^3 t \times 2\pi 10^3) \right]$$

$$f_{i(t=0.5 \text{ ms})} = 20 \text{ k} + \frac{25}{2\pi} \times \cos(4\pi + 10\pi) \times 4\pi \times 10^3$$

$$= 20 \text{ k} + \frac{25}{2\pi} \times 4\pi \times 10^3$$

$$= 20 \text{ k} + 50 \text{ k}$$

$$f_{i(t=0.5 \text{ ms})} = 70 \text{ kHz}$$

Class Room Practice Solutions

01. Ans: (d)

02. Ans: (b)

03. Ans: (d)

Sol: Given $f_s = 4$ to 10 MHz

$$IF = 1.8 \text{ MHz}$$

$$f_{si} = ?$$

$$f_{si} = f_s + 2 \times IF$$

$$= 7.6 \text{ MHz to } 13.6 \text{ MHz}$$

04. Ans: (a)

Sol: Image frequency $f_{si} = f_s + 2 \times IF$

$$= 700 \times 10^3 + 2(450 \times 10^3)$$

$$= 1600 \text{ kHz}$$

Local oscillator frequency, $f_l = f_s + IF$

$$(f_l)_{\max} = (f_s)_{\max} + IF = 1650 + 450$$

$$= 2100 \text{ kHz}$$

$$(f_l)_{\min} = (f_s)_{\min} + IF = 550 + 450$$

$$= 1000 \text{ kHz}$$

$$R = \frac{C_{\max}}{C_{\min}} = \left(\frac{f_{l\max}}{f_{l\min}} \right)^2 = \left(\frac{2100}{1000} \right)^2 = 4.41$$

05. Ans: (a)

Sol: $f_s(\text{range}) = 88 - 108 \text{ MHz}$ Given condition $f_{IF} < f_{LO}$, $f_{si} > 108 \text{ MHz}$

$$f_{si} = f_s + 2 \times IF$$

$$f_{si} > 108 \text{ MHz}$$

$$f_s + 2IF > 108 \text{ MHz}$$

$$88 \text{ MHz} + 2 \times IF > 108 \text{ MHz}$$

$$IF > 10 \text{ MHz}$$

Among the given options $IF = 10.7 \text{ MHz}$

06. Ans: (a)

Sol: Range of variation in local oscillator frequency is

$$f_{L\min} = f_{s\min} + IF$$

$$= 88 + 10.7$$

$$f_{L\min} = 98.7 \text{ MHz}$$

$$f_{L\max} = f_{s\max} + IF$$

$$= 108 + 10.7$$

$$f_{L\max} = 118.7 \text{ MHz}$$

07. Ans: 5

Sol: $f_s = 58 \text{ MHz} - 68 \text{ MHz}$ When $f_s = 58 \text{ MHz}$

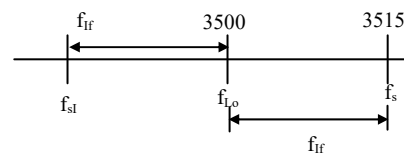
$$f_{si} = f_s + 2IF > 68 \text{ MHz}$$

$$2IF > 10 \text{ MHz}$$

$$1F \geq 5 \text{ MHz}$$

08. Ans: 3485 MHz

Sol:



$$f_{If} = 15 \text{ MHz}$$

$$f_{L_o} = 3500 \text{ MHz}$$

$$f_s - f_{L_o} = f_{if}$$

$$f_s = f_{L_o} + f_{if} = 3515 \text{ MHz}$$

$$f_{si} = \text{image frequency} = f_s - 2 f_{if}$$

$$= 3515 - 2 \times 15$$

$$= 3485 \text{ MHz}$$

Class Room Practice Solutions

01. Ans : (d)

$$\text{Sol: } \Delta = \frac{V_{\max} - V_{\min}}{2^n}$$

$$\Delta \propto \frac{1}{2^n} ; \frac{\Delta_1}{\Delta_2} = \frac{2^{n_2}}{2^{n_1}}$$

$$\frac{0.1}{\Delta_2} = \frac{2^{n+3}}{2^n}$$

$$\Delta_2 = 0.1 \times \frac{1}{8} \\ = 0.0125$$

02. Ans: (3)

$$\text{Sol: } (BW)_{\text{PCM}} = \frac{n f_s}{2}$$

Where 'n' is the number of bits to encode the signal and $L = 2^n$, where 'L' is the number of quantization levels.

$$L_1 = 4 \Rightarrow n_1 = 2$$

$$L_2 = 64 \Rightarrow n_2 = 6$$

$$\frac{(BW)_2}{(BW)_1} = \frac{n_2}{n_1} = \frac{6}{2} = 3$$

$$(BW)_2 = 3 (BW)_1$$

03. Ans: (c)

Sol: Given,

Two signals are sampled with $f_s = 44100$ s/sec and each sample contains '16' bits

Due to additional bits there is a 100% overhead.

Out put bit rate = ?

$$R_b = n |f_s|$$

$$f_s = 2f_{s1} = 2 [44100]$$

(∵ two signals sampled simultaneously)

$$n = 2n$$

(∵ due to overhead by additional bits)

$$R_b = 4 (nf_s) = 2.822 \text{ Mbps}$$

04. Ans (c)

$$\text{Sol: } \text{Number of bits recorded over an hour} \\ = R_b \times 3600 = 10.16 \text{ G.bits}$$

05. Ans: (c)

$$\text{Sol: } p(t) = \frac{\sin(4\pi W t)}{4\pi W t (1 - 16W^2 t^2)}$$

$$\text{At } t = \frac{1}{4W} ; P\left(\frac{1}{4W}\right) = \frac{0}{0}$$

Use L-Hospital Rule

$$\begin{aligned} \lim_{t \rightarrow \frac{1}{4W}} p(t) &= \lim_{t \rightarrow \frac{1}{4W}} \frac{4\pi W \cos(4\pi W t)}{4\pi W - 64\pi W^3 (3t^2)} \\ &= \frac{4\pi W (-1)}{4\pi W - 64\pi W^3 \left(\frac{1}{16W^2}\right)} \\ &= \frac{-4\pi W}{-8\pi W} = 0.5 \end{aligned}$$

06. Ans: 35

Sol: Given bit rate $R_b = 56$ kbps, Roll of factor $\alpha = 0.25$
BW required for base band binary PAM system

$$BW = \frac{R_b}{2} [1 + \alpha] = \frac{56}{2} [1 + 0.25] \text{ kHz} = 35 \text{ kHz}$$

07. Ans: 16

$$\text{Sol: } R_b = n f_s = 8 \text{ bit/sample} \times 8 \text{ kHz} = 64 \text{ kbps}$$

$$\begin{aligned} (B_T)_{\min} &= \frac{R_b}{2 \log_2 M} \\ &= \frac{R_b}{2 \log_2 4} = \frac{R_b}{2 \times 2} \\ &= \frac{R_b}{4} = \frac{64}{4} = 16 \text{ kHz} \end{aligned}$$



08. Ans: (b)

Sol: Given $f_s = 1/T_s = 2k$ symbols/sec

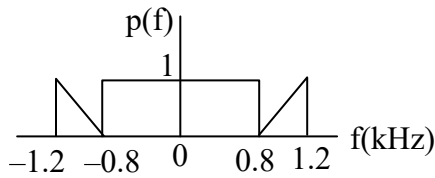
If $P(f) \leftrightarrow p(t)$

Condition for zero ISI is given by

$$\frac{1}{T_s} \sum_{n=-\infty}^{\infty} P(f - n/T_s) = p(0)$$

$$\Rightarrow \sum_{n=-\infty}^{\infty} P(f - n/T_s) = p(0)T_s$$

$p(0) = \text{area under } P(f)$

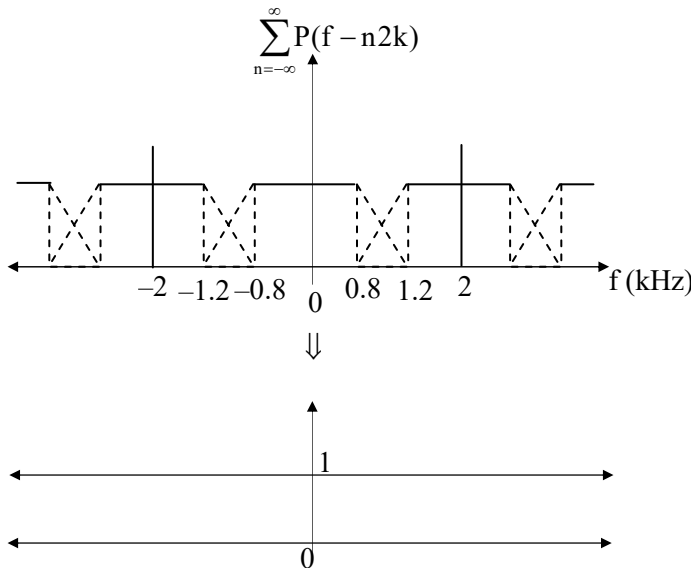


$$\text{Area} = 2 \times \frac{1}{2} (1)(0.4)k + 2 \times 0.8k = 2k$$

$$p(0) T_s = 2k \times \frac{1}{2k} = 1$$

$$\Rightarrow \sum_{n=-\infty}^{\infty} P(f - n/T_s) = 1$$

The above condition is satisfied by only option (b)



$$\therefore \sum_{n=-\infty}^{\infty} P(f - n2k) = 1$$

Option (a) is correct if pulse duration is from -1 to $+1$

Option (c) is correct if the transition is from 0.8 to 1.2 , -0.8 to -1.2

Option (d) is correct if the triangular duration is from -2 to $+2$

09. Ans: 200

Sol: $m(t) = \sin 100\pi t + \cos 100\pi t$

$$= \sqrt{2} \cos [100\pi t + \phi]$$

$$\Delta = 0.75 = \frac{V_{\max} - V_{\min}}{L} = \frac{\sqrt{2} - (-\sqrt{2})}{L} = \frac{2\sqrt{2}}{L}$$

$$L = \frac{2\sqrt{2}}{0.75} \approx 4 = 2^n$$

So $n = 2$

$f = 50$ Hz so Nyquist rate = 100

so the bit rate = $100 \times 2 = 200$ bps

10. Ans: (b)

Sol: Given

$$f_{m_1} = 3.6\text{kHz} \Rightarrow f_{s_1} = 7.2\text{kHz}$$

$$f_{m_2} = f_{m_3} = 1.2\text{kHz} \Rightarrow f_{s_2} = f_{s_3} = 2.4\text{kHz}$$

$$f_s = f_{s_1} + f_{s_2} + f_{s_3}$$

$$= 12\text{kHz}$$

No. of Levels used = 1024

$\Rightarrow n = 10$ bits

\therefore Bit rate = nf_s

$$= 10 \times 12 \text{ kHz}$$

$$= 120 \text{ kbps}$$

11. Ans: (a)

Sol: $(f_s)_{\min} = (f_{s_1})_{\min} + (f_{s_2})_{\min}$

$$+ (f_{s_3})_{\min} + (f_{s_4})_{\min}$$

$$= 200 + 200 + 400 + 800$$

$$= 1600 \text{ Hz}$$

12. Ans: (a)

Sol: Peak amplitude $\rightarrow A_m$

Peak to peak amplitude A_m



$$\frac{-\Delta}{2} \leq Q_e \leq \frac{\Delta}{2}$$

PCM maximum tolerable $\frac{\Delta}{2} = 0.2\% A_m$

$$\Delta = \frac{\text{Peak to peak}}{L} \Rightarrow \frac{2A/m}{2L} = \frac{0.2}{100} A_m$$

$$(\because \Delta = \frac{2A_m}{L})$$

$$\Rightarrow L = 500$$

$$2^n = 500$$

$$n = 9$$

$$R_b = n(f_s)_{TDM} + 9$$

$$f_s = R_N + 20\%R_N = R_N + 0.2R_N$$

$$f_s = 1.2R_N = 1.2 \times 2 \times \omega$$

$$f_s = 2.4 \text{ K samples/sec}$$

$$(f_s)_{TDM} = 5(f_s)$$

$$= 5 \times 2.4 \text{ K}$$

$$= 12 \text{ K sample/sec}$$

$$R_b = (nf_s) + 0.5\%(nf_s)$$

$$= (9 \times 12k) + \frac{0.5}{100} (9 \times 12k)$$

$$= 108540 \text{ bps}$$

13. Ans: (b)

Sol: Number of patients = 10

ECG signal B.W = 100Hz

$$(Q_e)_{\max} \leq (0.25) \% V_{\max}$$

$$\frac{2V_{\max}}{2 \times 2^n} \leq \frac{0.25}{100} V_{\max}$$

$$2^n \geq 400$$

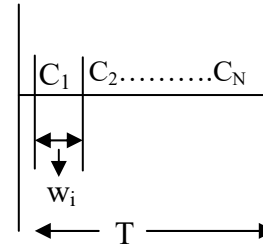
$$n \geq 8.64$$

$$n = 9$$

$$\begin{aligned} \text{Bit rate of transmitted data} &= 10 \times 9 \times 200 \\ &= 18 \text{ kbps} \end{aligned}$$

14. Ans: (c)

Sol:



Minimum B.W of TDM is $\sum_{i=1}^N w_i$

15. Ans: (b)

Sol: To avoid slope over loading, rate of rise of the o/p of the Integrator and rate of rise of the Base band signal should be the same.

$\therefore \Delta f_s = \text{slope of base band signal}$

$$\Delta \times 32 \times 10^3 = 125$$

$$\Delta = 2^{-8} \text{ Volts.}$$

16. Ans: (b)

Sol: $x(t) = E_m \sin 2\pi f_m(t)$

$$\frac{\Delta}{T_s} < \left| \frac{dm(t)}{dt} \right| \rightarrow \text{slope overload distortion}$$

takes place

$$\Delta f_s < E_m 2\pi f_m$$

$$\Rightarrow \frac{\Delta f_s}{2\pi} < E_m f_m \quad (\because \Delta = 0.628)$$

$$\Rightarrow \frac{0.628 \times 40K}{2\pi} < E_m f_m$$

$$f_s = 40 \text{ kHz} \Rightarrow 4 \text{ kHz} < E_m f_m$$

Check for options

$$(a) E_m \times f_m = 0.3 \times 8 \text{ K} = 2.4 \text{ kHz} \quad (4K \not< 2.4 \text{ K})$$

$$(b) E_m \times f_m = 1.5 \times 4K = 6 \text{ kHz} \quad (4K < 6 \text{ K}) \text{ correct}$$



(c) $E_m \times f_m = 1.5 \times 2 \text{ K} = 3 \text{ kHz}$
(4K ✗ 3K)

(d) $E_m \times f_m = 30 \times 1 \text{ K} = 3 \text{ kHz}$
(4K ✗ 3K)

17. Ans: (a)

Sol: Given

$$m(t) = 6 \sin(2\pi \times 10^3 t) + 4 \sin(4\pi \times 10^3 t)$$

$$\Delta = 0.314 \text{ V}$$

$$\text{Maximum slope of } m(t) = \frac{d}{dt}(m(t)) / t = \frac{\pi}{2}$$

$$= 2\pi \times 10^3(6) + 4\pi \times 10^3[4] = 28\pi \times 10^3$$

18. Ans: (c)

Sol: Pulse rate which avoid distortion

$$\Delta f_s = \frac{d}{dt} m(t)$$

$$f_s = \frac{28\pi \times 10^5}{0.314}$$

$$f_s = 280 \times 10^3 \text{ pulses/sec}$$

Class Room Practice Solutions

01. Ans: (c)

Sol: $(BW)_{BPSK} = 2f_b = 20 \text{ kHz}$
 $(BW)_{QPSK} = f_b = 10 \text{ kHz}$

02. Ans: (b)

Sol: $f_H = 25 \text{ kHz}$; $f_L = 10 \text{ kHz}$
 \therefore Center frequency
 $= \left(\frac{25+10}{2} \right) \text{ kHz} = 17.5 \text{ kHz}$

\therefore Frequency offset,
 $\Omega = 2\pi (25 - 17.5) \times 10^3$
 $= 2\pi (7.5) \times 10^3$
 $= 15 \times 10^3 \pi \text{ rad/sec.}$

The two possible FSK signals are orthogonal, if $2\Omega T = n\pi$
 $\Rightarrow 2(15\pi) \times 10^3 \times T = n\pi$
 $\Rightarrow 30 \times 10^3 \times T = n \text{ (integer)}$
 This is satisfied for, $T = 200\mu\text{sec.}$

03. Ans: (a)

Sol: $r_b = 8 \text{ kbps}$
 Coherent detection

$$\Delta f = \frac{nr_b}{2}$$

Best possible $n = 1$

$$\Delta f = \frac{8K}{2} = 4K$$

To verify the options $\Delta f = 4k$

i.e. $f_{c2} - f_{c1} = 4K$

- (a) $20 \text{ K} - 16 \text{ K} = 4 \text{ K}$
- (b) $32 \text{ K} - 20 \text{ K} = 12 \text{ K}$
- (c) $40 \text{ K} - 20 \text{ K} = 20 \text{ K}$
- (d) $40 \text{ K} - 32 \text{ K} = 8 \text{ K}$

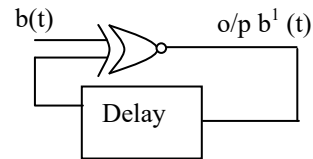
04. Ans: (a) & (c)

05. Ans: (c)

Sol: In QPSK baud rate = $\frac{\text{bit rate}}{2} = \frac{34}{2}$
 $= 17 \text{ Mbps}$

06. Ans: (d)

Sol:



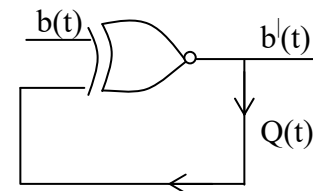
b(t)	0	1	0	0	1
b ¹ (t) _(Ref.bit)	0	0	1	0	0
Phase	π	π	0	π	π

07. Ans: (b)

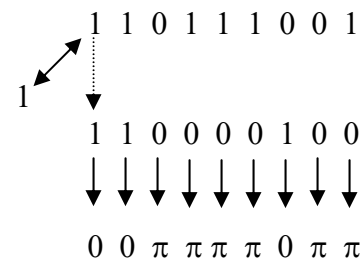
Sol: Given

Bit stream 110 111001

Reference bit = 1



$$b^1(t) = b(t) \odot Q(t)$$



08. Ans: (d)

Sol: $r_b = 1.544 \times 10^6$
 $\alpha = 0.2$



$$\begin{aligned}
 BW &= \frac{r_b}{\log_2^M} (1 + \alpha) \\
 &= \frac{1.544 \times 10^6}{2} (1 + 0.2) \quad (\because M = 4)
 \end{aligned}$$

$$BW = 926.4 \times 10^3 \text{ Hz}$$

09. Ans: 0.25

Sol: $BW = 1500 \text{ Hz}$

BW required for M-ary PSK is

$$\frac{R_b [1 + \alpha]}{\log_2 16} = 1500 \text{ Hz}$$

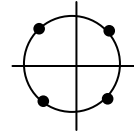
$$\Rightarrow R_b [1 + \alpha] = 1500 \times 4 = 6000$$

$$\Rightarrow (1 + \alpha) = \frac{6000}{4800}$$

$$\text{Roll off factor} \Rightarrow \alpha = \frac{6000}{4800} - 1 = 0.25$$

10. Ans: (b)

Sol:



Minimum shift keying

11. Ans: (b)

12. Ans: (d)

Sol: $BW = \frac{r_b}{\log_2 M} (1 + \alpha)$

$$36 \times 10^6 = \frac{r_b}{2} (1 + 0.2) (\because M = 4, \text{QPSK})$$

$$r_b = 60 \times 10^6 \text{ bps}$$

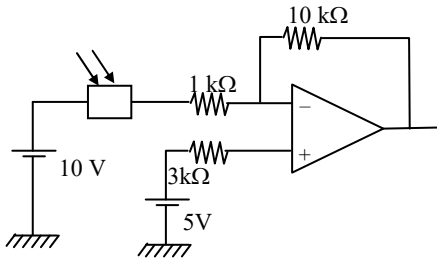
1

Optical Sources and Detectors

Chapter

Class Room Practice Solutions

01.
Sol:



1st case:

$R_p \rightarrow 1 \text{ k}\Omega$, no 10 V source

2nd case:

$R_p \rightarrow 5 \text{ k}\Omega \rightarrow 10 \text{ V}$ source is present

So, $V = V_{01(\text{Only } 10\text{V})} + V_{02(\text{Only } 5\text{V})}$

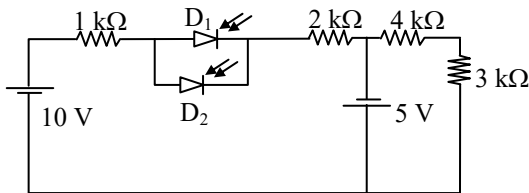
$$V = \frac{-10 \text{ k}\Omega}{1 \text{ k}\Omega + R_p}$$

$$= \left(\frac{-10 \text{ k}\Omega}{1 \text{ k}\Omega + 5 \text{ k}\Omega} \right) \times 10 + \left(1 + \frac{10 \text{ k}\Omega}{1 \text{ k}\Omega + 1 \text{ k}\Omega} \right) \times 5$$

$$V = \left(\frac{-10 \text{ k}\Omega}{6 \text{ k}\Omega} \times 10 \right) + \left(1 + \frac{10 \text{ k}\Omega}{2 \text{ k}\Omega} \right) \times 5$$

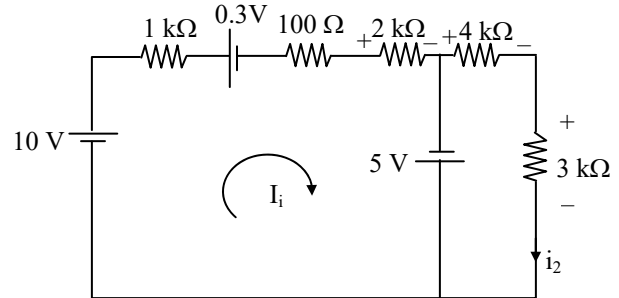
$$V = 13.33 \text{ V}$$

02.
Sol:



D_1, D_2 are in forward bias

D_2 —ON, D_1 —OFF



$$V_{2\text{k}} = ?$$

$$V_{3\text{k}\Omega} = ?$$

$$i_2 = \frac{-5\text{V}}{4\text{k}\Omega + 3\text{k}\Omega} = \frac{-5\text{V}}{7\text{k}\Omega} = -0.714 \text{ mA}$$

$$V_{3\text{k}\Omega} = i_2 \times 3 \text{ k}\Omega$$

$$= (-0.714) \times 3 \times 10^3$$

$$= -2.14 \text{ V}$$

From circuit

$$I_1 = 1.41 \text{ mA}$$

So

$$V_{2\text{k}} = 1.41 \text{ mA} \times 2 \text{ k}\Omega = 2.8 \text{ V}$$

03. Ans: (c)

Sol: Given data.

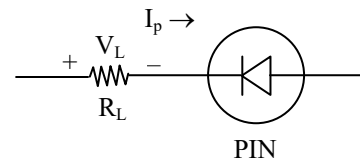
$$C_j = 6 \text{ pF}$$

$$A = 10 \text{ mm}^2$$

$$R = 0.5 \text{ A/W}$$

$$I = 1 \text{ mW/cm}^2$$

$$R_L = 100 \text{ k}\Omega$$



$$V_L = ?$$

We know

$$V_L = I_P \times R_L$$

$$R = \frac{I_P}{P_0}$$

$$P_0 = A \times I$$



$$I_p = \frac{0.5A}{W} \times A \times I$$

$$I_p = \frac{0.5A}{W} \times 10\text{mm}^2 \times \frac{1\text{mW}}{10\text{mm}^2}$$

$$I_p = \left(0.5 \times \frac{10}{100} \times 1\text{m}\right) \text{Amp}$$

$$I_p = 5 \times 10^{-5} \text{ amp}$$

$$V_L = I_p \times R_L = 5 \times 10^{-5} \times 100 \text{ k}\Omega$$

$$\therefore V_L = 5 \text{ volts}$$

04. Ans: (c)

Sol: Given:

$$\eta = 0.65$$

$$\lambda = 900 \text{ nm}$$

$$P_0 = 0.5 \text{ }\mu\text{w}$$

$$I_m = 10 \text{ }\mu\text{A}$$

$$M = ?$$

$$M = \frac{I_m}{I_p} = \frac{10\mu\text{A}}{I_p}$$

We know

$$\eta = \frac{EI_p}{P_0q}$$

$$0.65 = \frac{hcI_p}{\lambda P_0q}$$

$$\Rightarrow 0.65 = \left(\frac{6.6 \times 10^{-34} \times 3 \times 10^8}{900\text{n} \times 0.5 \times 10^{-6} \times 1.6 \times 10^{-19}} \right) \times I_p$$

$$\Rightarrow I_p = 2.36 \times 10^{-7}$$

$$M = \frac{10\mu\text{A}}{2.36 \times 10^{-7} \text{ A}}$$

$$= 42.4 \approx 43$$

05. Ans: -1V

Sol: Output is independent V_r

06. Ans: 2

Sol: Given

$$\text{Area} = 10 \text{ mm}^2$$

$$\text{Sensitivity} = 0.5 \text{ A/W}$$

$$\text{Intensity} = 4 \text{ W/m}^2$$

Photodiode current

$$I_p = \text{Area} \times \text{sensitivity} \times \text{Intensity}$$

$$I_p = 10 \text{ mm}^2 \times 0.5 \text{ A/W} \times 4\text{W/m}^2$$

$$I_p = 20 \text{ }\mu\text{A}$$

I to V converter sensitivity is $100 \text{ mV}/\mu\text{A}$

$$\text{So, } V_o = \frac{100\text{mV}}{\mu\text{A}} \times 20\mu\text{A}$$

$$= 2 \text{ Volt}$$

07. Ans: 75.18

$$\text{Sol: } \frac{I}{P} = \frac{\eta e \lambda}{hc}$$

$$I = \frac{\eta e \lambda}{hc} \times P$$

$$= \frac{0.75 \times 1.6 \times 10^{-19} \times 830 \times 10^{-9} \times 100 \times 10^{-6}}{6.624 \times 10^{-34} \times 2 \times 10^8}$$

$$I = 75.18\mu\text{A}$$

Chapter 2

LED's & LASERS

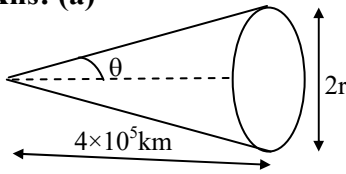
Class Room Practice Solutions

01. Ans: (b)

Sol: $2i = 115^{\circ}.34' = 115.566^{\circ}$,
 $i = 57.783^{\circ}$, $u = \tan i = \tan 57.783^{\circ}$
 $= 1.587$

02. Ans: (a)

Sol:



$$\theta = 1 \text{ mrad}$$

$$\tan \theta = \frac{r}{4 \times 10^5 \times 1000} = 1 \text{ mrad}$$

($\tan \theta \approx \theta$)

$$r = 4 \times 10^5 \text{ meters}$$

$$= 400 \text{ km}$$

$$\text{Diameter} = 2 \times r$$

$$= 2 \times 400 \text{ km}$$

$$= 800 \text{ km}$$

03. Ans: (b)

Sol: Given:

$$L = 500 \text{ mm}$$

$$\text{Bandwidth} = 1500 \text{ MHz}$$

$$\Delta f = ?$$

Number of longitudinal oscillating modes

$$= \frac{\text{BW}}{\Delta f}$$

We know

$$\Delta f = \frac{c}{2L}$$

Number of longitudinal oscillating modes

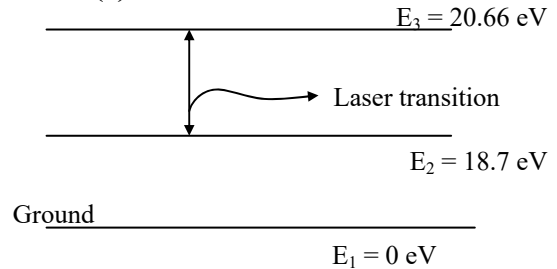
$$= \frac{1500 \text{ MHz}}{\left(\frac{3 \times 10^8}{2 \times 500 \times 10^{-3}} \right)}$$

$$= \frac{1500 \times 10^6}{3 \times 10^8} \times 1000 \times 10^{-3}$$

$$= 5$$

04. Ans: (c)

Sol:



05. Ans: (c)

Sol:

$$E_3 - E_2 = \frac{hc}{\lambda}$$

$$\lambda = \frac{hc}{E_3 - E_2}$$

$$= \frac{6.625 \times 10^{-34} \times 3 \times 10^8}{(20.66 - 18.7) \times 1.6 \times 10^{-19} \text{ J}}$$

$$= 633.8 \text{ nm}$$

06. Ans: (d)

Sol: Given

$$\lambda = 6328 \text{ \AA}$$

$$\text{Bandwidth} = 1 \text{ MHz}$$

$$C_l = ?$$

We know

$$C = \frac{C_\ell}{C_t}$$

$$C_l = 3 \times 10^8 \times \frac{1}{1 \text{ MHz}} \quad (\because C_t = \frac{1}{f})$$

$$C_l = 300 \text{ m}$$

07. Ans: 40

Sol: for photo diode D_1

$$\text{Intensity} = 50 \text{ W/m}^2$$

$$\text{Area} = 10 \times 10^{-3} \times (5 \times 10^{-3} + 100 \times 10^{-6}) \text{ m}^2$$

$$= 2.55 \times 10^{-3} \text{ m}^2$$



Total current of diode D_1

$$I_{D1} = 2.55 \times 10^{-3} \times 0.4A = 1.02 \times 10^{-3} A$$

For photo diode D_2

$$\text{Intensity} = 50W/m^2$$

$$\begin{aligned} \text{Area} &= 10 \times 10^{-3} \times (5 \times 10^{-3} - 100 \times 10^{-6}) m^2 \\ &= 2.45 \times 10^{-3} m^2 \end{aligned}$$

Total current of diode D_2

$$I_{D2} = 2.45 \times 10^{-3} \times 0.4A = 9.8 \times 10^{-4} A$$

Difference between photo currents

$$\begin{aligned} I_{D1} - I_{D2} &= 1.02 \times 10^{-3} A - 9.8 \times 10^{-4} A \\ &= 40 \mu A \end{aligned}$$

08. Ans: 2

Sol: $E_g = \frac{hC}{\lambda}$

$$E_g = \frac{4.13567 \times 10^{-15} \times 3 \times 10^8}{620 \times 10^{-9}} = 2eV$$

Class Room Practice Solutions

01.

Sol: Given data:

$$t = 5 \mu\text{m}$$

$$n = 5$$

$$\lambda = 589 \text{ nm}$$

$$\mu_g = ?$$

We know

$$t(\mu_g - 1) = n\lambda$$

$$\Rightarrow 5 \times 10^{-6}(\mu_g - 1) = 5 \times 589 \times 10^{-9}$$

$$\Rightarrow (\mu_g - 1) = \frac{5 \times 589 \times 10^{-9}}{5 \times 10^{-6}}$$

$$\Rightarrow (\mu_g - 1) = 0.589$$

$$\Rightarrow \mu_g = 1.589$$

02.

Sol: Given data:

$$\lambda = 515 \text{ nm}$$

Refractive index (μ) = 1.6

$$\theta_R = 45^\circ$$

$$t = ?$$

we know

$$t(\mu - 1) = n\lambda$$

$$t = \frac{n\lambda}{(\mu - 1)}$$

$$\Rightarrow t = \frac{515 \times 10^{-9}}{1.6 - 1} = 8.58 \times 10^{-7}$$

$$\Rightarrow t = 0.85 \mu\text{m}$$

03.

Sol: Given data

$$t = 1.5 \mu\text{m}$$

$$\lambda = 0.5 \mu\text{m}$$

$$n = ?$$

We know

$$t = \frac{n\lambda}{2}$$

$$\Rightarrow 1.5 \times 10^{-6} = \frac{n \times 0.5 \times 10^{-6}}{2}$$

$$\Rightarrow \frac{1.5 \times 10^{-6} \times 2}{0.5 \times 10^{-6}} = n$$

$$\Rightarrow n = 6$$

04.

Sol: Given data:

$$n = 100$$

$$\lambda = 6328 \text{ \AA}$$

$$t = 20 \text{ cm}$$

$$\mu = ?$$

We know

$$2t(\mu - 1) = n\lambda$$

$$\Rightarrow 2 \times 20 \times 10^{-2}(\mu - 1) = 100 \times 6328 \times 10^{-10}$$

$$\mu = 1.0001582 \approx 1$$

05.

Sol: Given data

$$\text{R.I} = \mu_g = 1.53$$

$$\mu_{\text{air}} = 1.0$$

$$R = \left(\frac{\mu_g - \mu_{\text{air}}}{\mu_g + \mu_{\text{air}}} \right)^2$$

$$R = 0.044$$

$$R = 4.4 \% \text{ of loss}$$

4

Fiber Optics

Chapter

Class Room Practice Solutions

01. Ans: (d)

$$\begin{aligned} \text{Sol: } NA &= \sqrt{n_1^2 - n_2^2} \\ &= \sqrt{(1.44)^2 - (1.4)^2} \\ &= 0.34 \end{aligned}$$

02. Ans: (c)

Sol: Given data

$$\epsilon_r = 2.5$$

$$n = ?$$

n = refractive index

We know,

$$n = \sqrt{\epsilon_r \mu_r}$$

ϵ_r = relative permittivity

μ_r = relative permeability

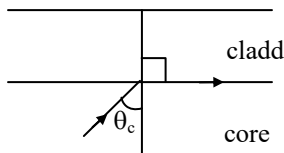
$$\begin{aligned} n &= \sqrt{2.5} \quad (\because \mu_r = 1) \\ &= 1.58 \end{aligned}$$

03. Ans: (d)

Sol: $n_1 = 1.6$

$$n_2 = 1.422$$

$$\theta_c = ?$$



$$\frac{\sin \theta_c}{\sin 90^\circ} = \frac{n_2}{n_1}$$

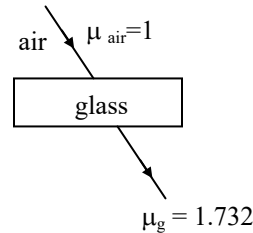
$$\theta_c = \sin^{-1} \left(\frac{1.422}{1.64} \right)$$

$$= 60.12$$

$$\approx 60$$

04. Ans: (c)

Sol: $\mu_g = 1.732$



$$\tan \theta_B = \frac{\mu_g}{\mu_{\text{air}} = 1}$$

$$\theta_B = \tan^{-1}(1.732)$$

$$\theta_B = 60^\circ$$

05. Ans: (a)

Sol: Given $\mu_{\text{glass}} = 1.720$

$$R = \left(\frac{\mu_{\text{air}} - \mu_{\text{glass}}}{\mu_{\text{air}} + \mu_{\text{glass}}} \right)^2 \times 100$$

$$\begin{aligned} R &= \left(\frac{1 - 1.72}{1 + 1.72} \right)^2 \times 100 \\ &= 7\% \end{aligned}$$

06. Ans: (d)

$$\text{Sol: } \theta_c = \sin^{-1} \left(\frac{n_2}{n_1} \right)$$

Given

$$n_1 = 1.641$$

$$n_2 = 1.422$$

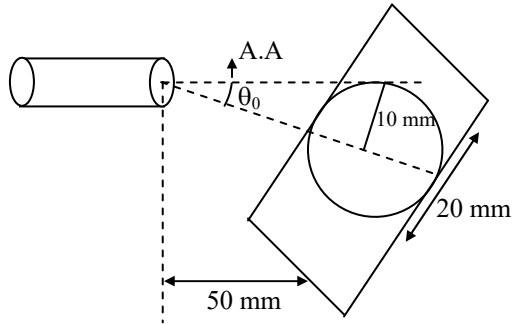
$$\theta_c = \sin^{-1} \left(\frac{1.422}{1.641} \right)$$

$$= 60^\circ$$



08. Ans: (b)

Sol: NA = ?



$$NA = \sqrt{n_1^2 - n_2^2}$$

$$NA = \mu_0 \sin\theta_0$$

$$NA = \sin\theta_0$$

$$NA = \frac{10}{\sqrt{10^2 + 50^2}}$$
$$= 0.196$$
$$\approx 0.2$$

09. Ans: 0.75

Sol: $\frac{n_1}{n_2} = \frac{t_1}{t_2} = 0.75 \quad (n \propto t)$