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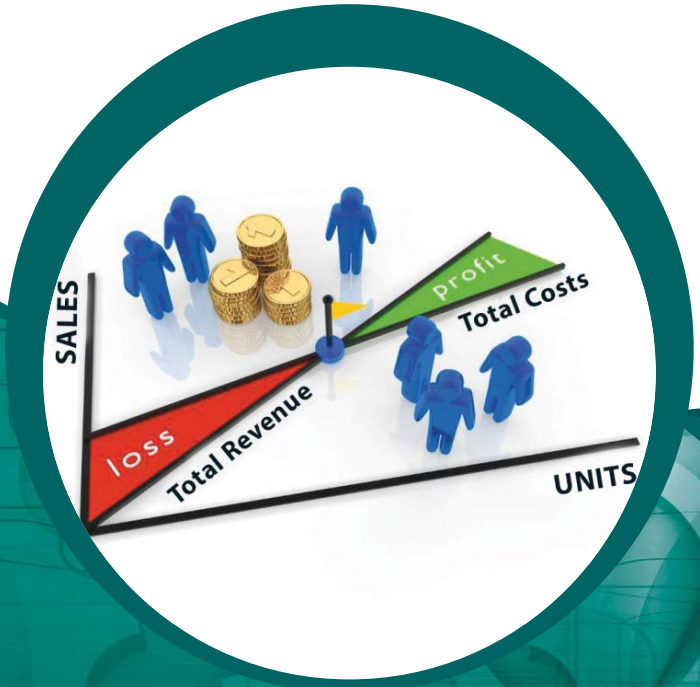
MECHANICAL ENGINEERING

IM & OR

Volume - 1 : Study Material with Classroom Practice Questions



IM & OR

Solutions for Vol – I _ Classroom Practice Questions

Chapter- 01
PERT & CPM

01. Ans: (a)

Sol: CPM deals with deterministic time durations.

02. Ans: (a)

Sol: Critical Path :

- It is a longest path consumes maximum amount of resources
- It is the minimum time required to complete the project

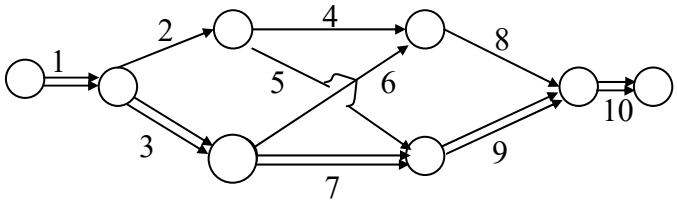
03. Ans: (a)

04. Ans: (a)

Sol: Gantt chart indicates comparison of actual progress with the scheduled progress.

05. Ans: (c)

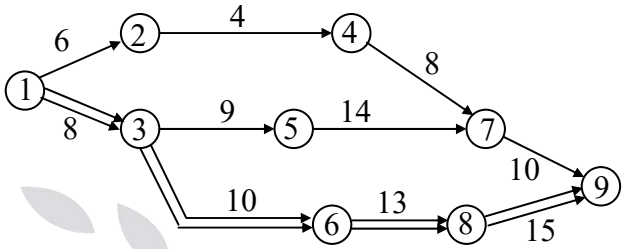
Sol:



Critical path = 1 + 3 + 7 + 9 + 10 = 30 days

06. Ans: (c)

Sol:



Critical path (1-3-6-8-9) = 8 + 10 + 13 + 15 = 46 days

07. Ans: (b)

Sol: Rules for drawing Network diagram:

- Each activity is represented by one and only one arrow in the network.
- No two activities can be identified by the same end events.
- Precedence relationships among all activities must always be maintained.
- No dangling is permitted in a network.
- No Looping (or Cycling) is permitted.

08. Ans: (b)

Sol: Activity: Resource consuming and well-defined work element.

Event: Each event is represented as a node in a network diagram and it does not consume any time or resource.

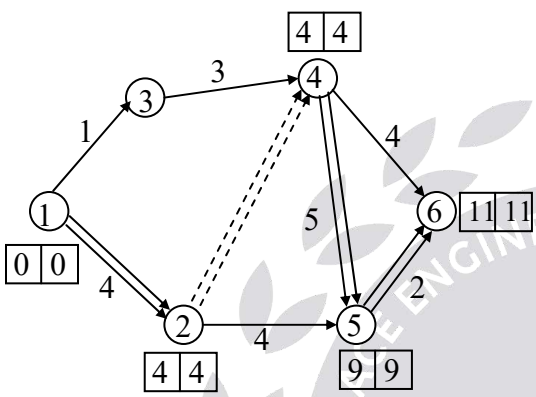
Dummy Activity: An activity does not consume any kind of resource but merely

depicts the technological dependence is called a dummy activity.

Float: Permissible delay period for the activity.

09. Ans: (b)

Sol:



10. Ans: (a)

11. Ans: (b)

Sol:

- Beta Distribution is used to decide the expected duration of an activity.
- The expected duration of the project can be described by Normal distribution.

12. Ans: (b)

Sol: $T_0 = 8$ min, $T_m = 10$ min, $T_p = 14$ min,

$$T_e = \frac{T_o + 4T_m + T_p}{6}$$

$$= \frac{8 + 4 \times 10 + 14}{6} = \frac{62}{6} = 10.33 \text{ min}$$

13. Ans: (a)

Sol: Take 4-3, $T_e = 6$ days

Critical path = 1-2-4-3

= 5 + 14 + 4 = 23 days

$$\sigma_{\text{critical path}} = \sqrt{V_{1-2} + V_{2-4} + V_{4-3}}$$

$$= \sqrt{2^2 + 2.8^2 + 2^2} = 3.979$$

$$z = \frac{\text{Due date} - \text{critical path duration}}{\sigma_{\text{critical path}}}$$

$$z = \frac{27 - 23}{3.979} = 1.005$$

$\therefore$ P(z) = 0.841

14. Ans: (b)

15. Ans: (c)

Sol: D = 36 days, V = 4 days

$$Z = \frac{36 - 36}{\sqrt{4}} = 0$$

$\Rightarrow$ P(z) = 50%

16. Ans: (c)

Sol: $\sigma_{cp} = \sqrt{V_{a-b} + V_{b-c} + V_{c-d} + V_{d-e}}$

$$= \sqrt{4 + 16 + 4 + 1} = 5$$

17. Ans: (a)

Sol: The latest that an activity can start from the beginning of the project without causing a delay in the completion of the entire project. It is the maximum time up to which an activity can be delayed to start without effecting the project completion duration time. (LST = LFT – duration).

18. Ans: (c)

Sol: The earliest expected completion time,

Critical path : A-B-C-D-F-E-H

$\Rightarrow 5 + 4 + 8 + 5 + 8 = 30$ days

19. Ans: (d)

Sol: *Critical path :*

1-3-4-6 = 20 days

$$z = \frac{24-20}{\sqrt{4}} = \frac{4}{2} = 2$$

$\Rightarrow P(z) = 97.7\%$

20. Ans: (d)

Sol: Variance $= \left(\frac{t_p - t_o}{6}\right)^2$

$$= \left(\frac{22-10}{6}\right)^2 = 4$$

21. Ans: (a)

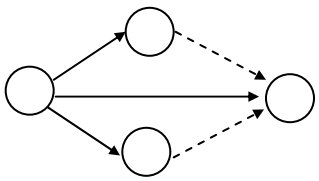
22. Ans: (b)

23. Ans: (a)

24. Ans: (b)

25. Ans: (c)

Sol:

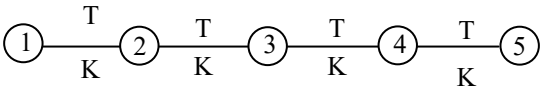


26. Ans: (c)

27. Ans: (b)

28. Ans: (d)

Sol:



Given each activity having time mean duration 'T' and standard deviation 'K'.

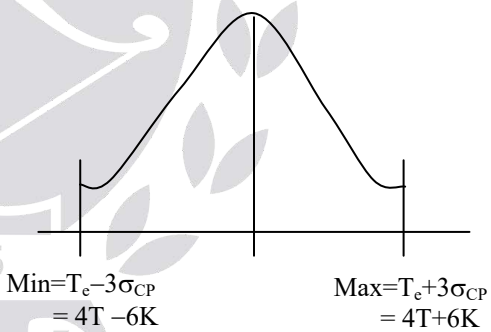
Total time estimate $T_e = 4T$

Variance of the path

$(\Sigma var)_{CP} = R^2 + R^2 + R^2 + R^2$

$= 4R^2$

Standard deviation of CP$= \sqrt{\sum (var)_{CP}}$



$\sigma_{CP} = \sqrt{4K^2}$

$\sigma_{CP} = \pm 2K$

Range of overall project duration likely to be in 4T + 6K and 4T – 6K

i.e., 4T ± 6K

Common solutions for Q.29 & Q.30

29. Ans: (b)

30. Ans: (b)

Sol:

Paths	Duration
1-2-4-5 = (AEF)	8+9+6=23
1-2-3-4-5=(ADF)	8+9+6=23
1-3-4-5 (BDF)	6+9+6 = 21
1-4-5 (CF)	16+6=22

∴ Highest time taken paths are AEF and ADF

∴ Critical path's are AEF and ADF

Critical paths are '2'.

Possible cases to crash

A by 1 day that cost = 80

F by 1 day that cost = 130

E and D by 1 day that cost = 20 + 40 = 60

31. Ans: (c)

32. Ans: (c)

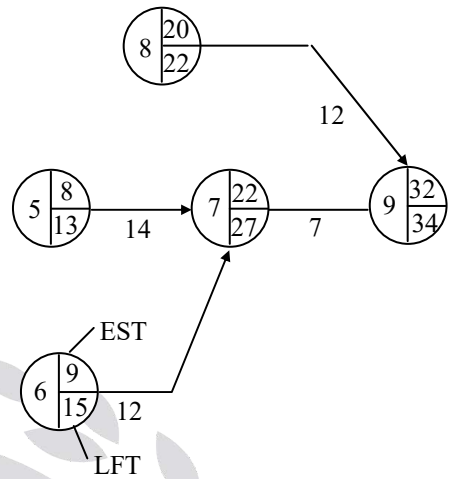
Sol:

Path	Duration
AB	7+5 = 12
CD	6+6 = 12
EF	8+4 = 12

Three critical paths, number of activities to be crashed are 3.

33. Ans: (c)

Sol:



$(\text{Total Float})_{6\text{-}7} = 27 - 9 - 12 = 6$

$(\text{Free float})_{6\text{-}7} = 28 - 9 - 12 = 1$

Chapter- 02
Network Models

01. Ans: (c)

Sol:

d_{ij} → "Distance from any node i to next node j"

s_j → "Denotes shortest path from node P to any node j".

$d_{ij} = d_{QG}$ (Adjacent nodes)

$d_{ij} = d_{RG}$ (Adjacent from node R to G)

$S_j = S_Q$ (Shortest path from node P to node Q)

$S_j = S_R$ (Shortest path from node P to node R)

We can go from P to G via Q or via R.

P to G via Q

$$S_G = S_Q + d_{QG}$$

P to G via R.

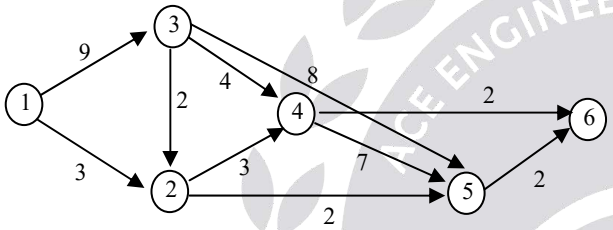
$$S_G = S_R + d_{RG}$$

Optimum answer is minimum above two answers.

$S_G = \text{MIN}\ [S_Q + d_{QG}\ ;\ S_R + d_{RG}]$

02. Ans: (c)

Sol:



Path	Cost
1-3-4-6	9+4+2 = 15
1-3-2-4-6	9+2+3+2 = 16
1-3-4-5-6	9+4+7+2 = 22
1-3-2-5-6	9+2+2+2 =15
1-3-2-4-5-6	9+2+3+7+2 = 23
1-2-4-6	3+3+2 = 8
1-2-5-6	3+2+2 = 7
1-2-4-5-6	3+3+7+2 = 15
1-3-5-6	9+8+2 = 19

From the given statement, we got shortest path (least total cost) is 1-2-5-6 and a path which does not have 1-2, 2-5, 5-6 activities should be considered.

The next path which does not have the above activities is 1-3-4-6 = 15

and 1-3-2-4-6 = 16.

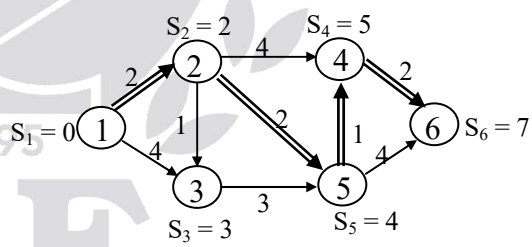
∴ In this second least total cost is 15.

03. Ans: 7

Sol:

Path	Arc length
1-2-4-6	8
1-2-5-4-6	7
1-2-5-6	8
1-2-3-5-4-6	9
1-3-5-4-6	10
1-3-5-6	11

Shortest path length from node 1 to node 6 is 7.



Chapter- 03
Linear Programming

01. Ans: (d)

Sol: A restriction on the resources available to a firm (stated in the form of an inequality or an equation) is called constraint.

02. Ans: (d)

03. Ans: (c)

04. Ans: (d)

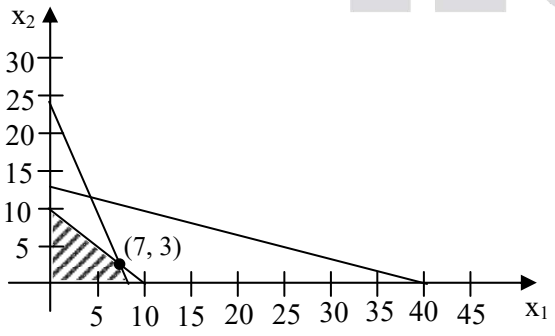
Sol: The theory of LP states that the optimal solution must lie at one of the corner points.

05. Ans: (b)

Sol: The feasible region of a linear programming problem is convex. The value of the decision variables, which maximize or minimize the objective function, is located on the extreme point of the convex set formed by the feasible solutions.

06. Ans: (a)

Sol:



$Z(7, 3) = 2\times7 + 5\times3 = 29$

07. Ans: (a)

Sol: $Z_{max} = x+2y$,

Subjected to

$4y - 4x \geq -1$…… (1)

$5x + y \geq -10$ …….. (2)

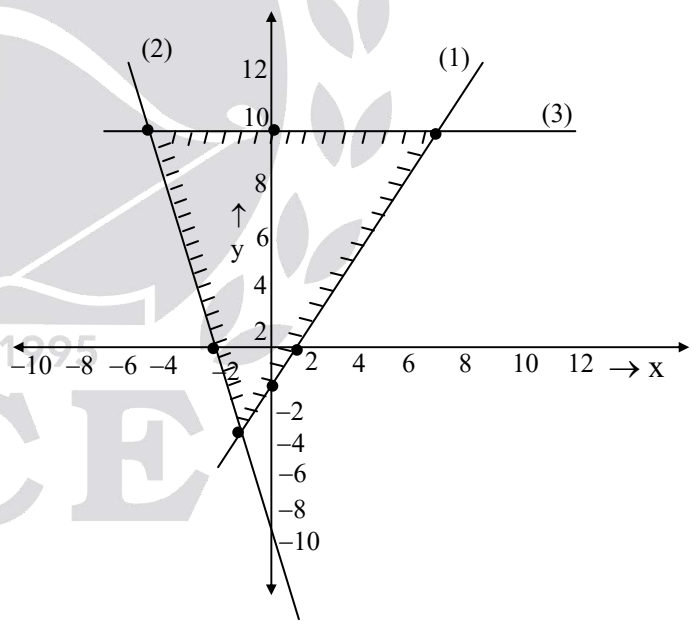
$y \leq 10$ …… (3)

x and y are unrestricted in sign

$$(1) \Rightarrow \frac{x}{\left(\frac{1}{4}\right)} + \frac{y}{\left(\frac{-1}{4}\right)} \leq 1$$

$$(2) \Rightarrow \frac{x}{(-2)} + \frac{y}{(-10)} \leq 1$$

$$(3) \Rightarrow \frac{y}{10} \leq 1$$



Only one value gives max value, then solution is unique.

08. Ans: (b)

Sol: $Z_{max} = 3x_1+2x_2$

Subjected to

$4x_1+x_2 \le 60$ .....(1)

$8x_1+x_2 \le 90$ .....(2)

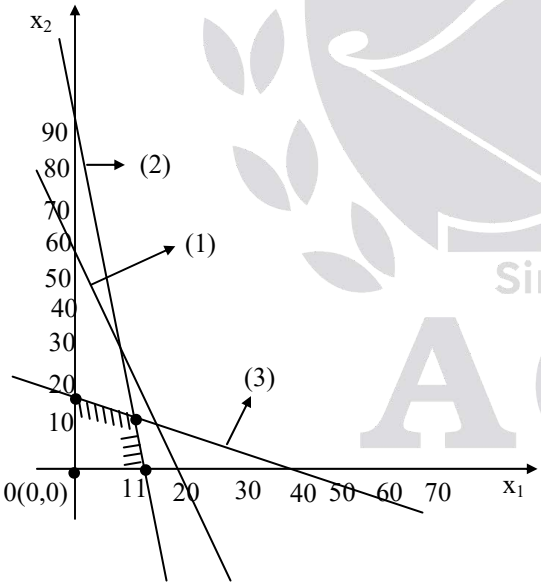
$2x_1+5x_2 \le 80$ ..... (3)

$x_1, x_2 \ge 0$

$(1) \Rightarrow \frac{x_1}{15}+\frac{x_2}{60} \le 1$

$(2) \Rightarrow \frac{x_1}{11.25}+\frac{x_2}{90} \le 1$

$(3) \Rightarrow \frac{x_1}{40}+\frac{x_2}{16} \le 1$



From the above graph the No. of corner points for feasible solutions are 4

09. Ans: (c)

Sol: Let, P type toys produced = x ,

Q type toys produced = y

	P	Q	
Time	1	2	2000
Raw material	1	1	1500
Electric switch	-	1	600
Profit	**3**	**5**	
	x	**y**	

$Z_{max} = 3x + 5y$

$x+2y \le 2000$; $\frac{x}{2000}+\frac{y}{1000} \le 1$

$x+y \le 1500$; $\frac{x}{1500}+\frac{y}{1500} \le 1$

$y \le 600$; $\frac{y}{600} \le 1$

$x, y \ge 0$

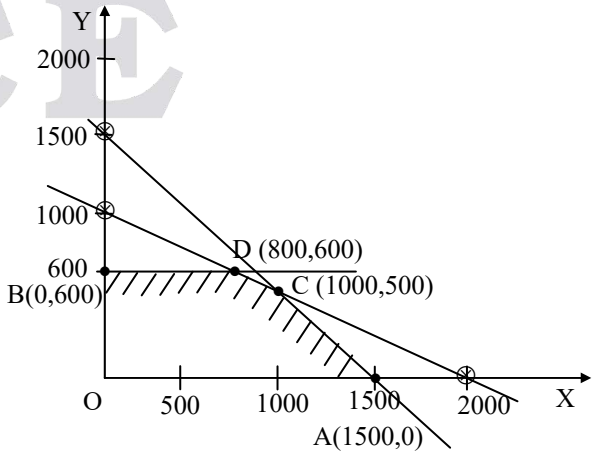
$Z_{max} = 3x + 5y$

$Z_A = 3 \times 1500 + 5 \times 0 = 4500$

$Z_B = 3 \times 0 + 5 \times 600 = 3000$

$Z_C = 3 \times 1000 + 5 \times 500 = 5500$

$Z_D = 3 \times 800 + 5 \times 600 = 5400$



C does not exist in answer.

Hence, Z_{max} is at D, i.e., Z_{max} @ D = 5400

10. Ans: (c)

Sol: $Z_{max} = x_1 + 1.5\, x_2$

Subject to

$2x_1+3x_2 \le 6$ ------- (1)

$x_1 + 2x_2 \le 4$ -------- (2)

$x_1 , x_2 \ge 0$

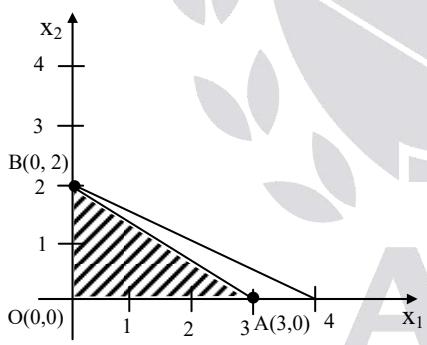
$$\frac{x_1}{3}+\frac{x_2}{2}\le 1$$

$$\frac{x_1}{4}+\frac{x_2}{2}\le 1$$

Let, "c" in the intersection of (1) and (2)

Solve (1) & (2) for 'c'.

It follows, $x_1 = \frac{12}{5}; x_2 = \frac{2}{5}$



$Z_{max} = x_1 + 1.5x_2$

$Z_0 = 0$

$Z_A = 3 + 1.5 \times 0 = 3$

$Z_B = 3\times0+1.5\times2 = 3$

Problem is having multiple solutions and it is Optimal at (A) and (B).

11. Ans: (a)

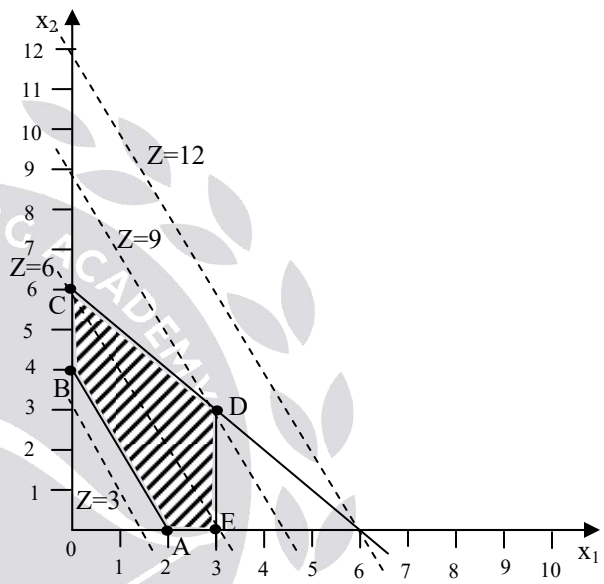
Sol: $Z_{max} = 2x_1 + x_2$

Subjected $x_1 + x_2 \le 6$

$x_1 \le 3$

$2x_1 + x_2 \ge 4$

$x_1 , x_2 \ge 0$



But feasible region is ABCDEA

($\because x_1 , x_2 > 0$)

A(2,0) B(0,4) C(0,6) E(3,0)

D can be obtained by solving

$x_1 \le 3$ & $x_1 + x_2 \le 6$

$\Rightarrow x_1 = 3$ and $x_2 = 3$ and D (3,3)

Z_{max}	A(2,0)	$2\times2+1\times0 = 4$
	B (0,4)	$0\times2+1\times4 = 4$
	C(0,6)	$0\times2+1\times6 = 6$
	E(3,0)	$3\times2+0\times1 = 6$
	D(3,3)	$3\times2+1\times3 = 9$

$Z_{max} = 9$ at D (3,3)

12. Ans: (a)

13. Ans: (b)

14. Ans: (d)

15. Ans: (a)

Sol: $Z_{max} = 4\,x_1 + 6\,x_2 + x_3$

<u>s.t</u>

$2\,x_1 - x_2 + 3x_3 \le 5$

$x_1, x_2, x_3 \ge 0$

$2\,x_1 - x_2 + 3x_3 + s_1 = 5$

$Z_{max} = 4x_1 + 6x_2 + x_3 + 0\,s_1$

$c_j \rightarrow$ s v↓	4 x_1	6 x_2	1 x_3	0 s_1	B_0	min Ratio
0 s_1	2	-1	3	1	5	– 5
z_j $c_j - z_j$	0 4	0 6	0 1	0 0	0	

EV

Entering vector exists but leaving vector doesn't exist as minimum ratio column is having negative values. It is a case of unbounded solution space and unbounded optimal solution to problem.

16. Ans: (d)

Sol: Number of zeros in Z row = 4

Number of basic variable = 3

As the number of zeros in Z row is greater than number of basic variable so it has multiple optimal solutions.

17. Ans: (b)

Sol: Solution is optimal; but Number of zeros are greater than the number of basic Variables in $C_j - Z_j$(net evaluation row) hence multiple optimal solutions.

18. Ans: (b)

Sol: If all the elements in the objective row are non-negative incase of maximization, then the solution is said to be optimal.

Here, the solution is optimal, $Z_{max} = 1350$.

19. Ans: (a)

Sol:

- A tie for leaving variable in simplex procedure implies degeneracy.
- If in a basic feasible solution, one of the basic variables takes on a zero value then it is case of degenerate solution

Common Data

20. Ans: (d) **21. Ans: (a)** **22. Ans: (a)**

Sol: As the No. of zeros greater than No. of basic variables hence it is a case of multiple solutions or alternate optimal solution exists.

Basic	x_1	x_2	S_1	S_2	S_3	RHS
z	0	0	0	2	0	48
s_1	0	5/3	1	–2/3	0	14
s_3	0	–1/3	0	1/3	1	5
x_1	1	2/3	0	1/3	0	8

From the table gives the optimum $x_2 = 0$, $x_1 = 8$, $Z_{max} = 48$

Look at the coefficient of the non basic variable in the z-equation of iterations. The coefficient of non basic x_2 is zero, indicating that x_2 can enter the basic solution without changing the value of Z, but causing a change in the values of the variables.

Alternate optimal solution :

Here x_2 is the entering variable.

Row	Basic	x_1	x_2	S_1	S_2	S_3	RHS	Ratio
R_1	z	0	0	0	2	0	48	
R_2	s_1	0	5/3	1	–2/3	0	14	14/(5/3)=8.4 → Leaving variable
R_3	s_3	0	–1/3	0	1/3	1	5	–
R_4	x_1	1	2/3	0	1/3	0	8	8/(2/3)=12

↑ Entering variable

Row	**Basic**	x_1	x_2	S_1	S_2	S_3	**RHS**
R_1	z	0	0	0	2	0	48
$R_2' = \frac{R_2}{(5/3)}$	x_2	0	1	3/5	–2/5	0	42/5
$R_3' = R_3' + \frac{R_2'}{3}$	s_3	0	0	1/5	1/5	1	39/5
$R_4' = R_4 - \frac{2}{3}R_2'$	x_1	1	0	–3/5	3/5	0	12/5

In the above table $x_1 = \frac{12}{5}$, $x_2 = \frac{42}{5}$, $s_3 = \frac{39}{5}$

23. Ans: (c) **24. Ans: (c)** **25. Ans: (a)**

26. Ans: (c)

Sol: $Z_{min} = 10x_1 + x_2 + 5x_3 + 0S_1$

Dual , $W_{min} = 50y_1$

subjected to

$5y_1 \le 10, \quad y_1 \le 2, \quad W_{max} = 100$

$3y_1 \le 5, \quad y_1 \le 5/3, \quad W_{max} = 250/3$

$y_1, y_2 \ge 0$

$\Rightarrow Z_{max} = 250 / 3$

Common Data for Questions

27. Ans: (c)

Sol: Given, $Z_{max} = 5x_1 + 10x_2 + 8x_3$

Subjected to

$3x_1 + 5x_2 + 2x_3 \le 60 \rightarrow$ Material

$4x_1 + 4x_2 + 4x_3 \le 72 \rightarrow$ Machine hours

$2x_1 + 4x_2 + 5x_3 \le 100 \rightarrow$ Labour hours

$x_1, x_2, x_3 \ge 0$

$3x_1 + 5x_2 + 2x_3 + s_1 = 60$

$4x_1 + 4x_2 + 4x_3 + s_2 = 73$

$2x_1 + 4x_2 + 5x_3 + s_3 = 100$

$Z_{max} = 5x_1 + 10x_2 + 8x_3 + 0s_1 + 0s_2 + 0s_3$

$C_j \rightarrow$		5	10	8	0	0	0	B_0	Min Ratio
C_B	SV	x_1	x_2	x_3	s_1	s_2	s_3		
10	x_2	$\frac{1}{3}$	1	0	$\frac{1}{3}$	$\frac{-1}{6}$	0	8	
8	x_3	$\frac{2}{3}$	0	1	$\frac{-1}{3}$	$\frac{5}{12}$	0	10	
0	S_3	$\frac{-8}{3}$	0	0	$\frac{1}{3}$	$\frac{-17}{12}$	1	18	
Z_j		$\frac{26}{3}$	10	8	$\frac{2}{3}$	$\frac{5}{3}$	0	160	
$C_j - Z_j$		$\frac{-11}{3}$	0	0	$\frac{-2}{3}$	$\frac{-5}{3}$	0		
$\frac{C_j - Z_j}{x_2}$		-11	0	0	-2	10	0	LL=2 UL=10	10–2=8 10+10=20
$\frac{C_j - Z_j}{x_3}$		$\frac{-11}{2}$	0	0	2	-4	0	LL=4 UL=2	8–4=4 8+2=10

In $C_j - Z_j$ row all elements are negatives or zeros, hence the solution is optimal and unique..

Basic variables are:

$x_2 = 8, \quad x_3 = 10, \quad s_3 = 18$

i.e., production of B = 8 units, C = 10 units

18 labours hours remained unutilized

Non Basic variable

$x_1 = 0, \quad s_1 = 0, \quad s_2 = 0$

Resource materials and resource machine hours are fully utilized. In $(C_j - Z_j)$ row at optimality, the values under s_1, s_2 and s_3 columns represents the shadow prices.

So, If 1 kg material increases, contribution increases by $\frac{2}{3}$.

If 1 kg material decreases, contribution decreases by $\frac{2}{3}$.

If 1 kg material increases, then production B increases by $\frac{1}{3}$ and production C decreases by $\frac{1}{3}$

If m/c hr increases by 1 units, contribution increases by 5/3.

If m/c hr decreases by 1 units, contribution decreases by $\frac{5}{3}$

If m/c hr increases by 1 units, production B decreases by $\frac{1}{6}$ and production increases by $\frac{5}{12}$.

If m/c hr decreases by 1 units, production B increases by $\frac{1}{6}$ and production C decreases by $\frac{5}{12}$

If 1 unit of A produces, contribution decreases by $\frac{11}{3}$, production B decreases by $\frac{1}{3}$, production C decreases by $\frac{2}{3}$.

28. Ans: (a)

Sol: If 3 kg material increases, contribution increases by $3\times\frac{2}{3}$ = Rs. 2

29. Ans: (a)

Sol: Present profit = 160 $\Rightarrow 160 - \frac{5}{3}\times 12 = 140/-$

30. Ans: (b)

Sol: New production of B

$$= 8 - \left(12\times\frac{-1}{6}\right) = 8 + \left(12\times\frac{1}{6}\right)$$

$$= 8 + 2 = 10 \text{ units}$$

31. Ans: (c)

Sol: If materials are increased by 3kgs then the new production of C is $= 10 + \left(3\times\frac{-1}{3}\right)$

$$= 10 - \left(3\times\frac{1}{3}\right) = 10 - 1 = 9$$

32. Ans: (a)

Sol: If 1 unit of A produces, contribution decreases by $\frac{11}{3}$

33. Ans: (a)

Sol: If 6 units of A are produced then the new profit is,

$$160 - \left(6\times\frac{11}{3}\right) = 138$$

34. Ans: (a)

Sol: Production of B , $3\times\frac{1}{3} = 1$

Production of C, $3\times\frac{2}{3} = 2$

Common data 35 & 36

35. Ans: (b) , 36. Ans: (b)

Sol: Basic variables

$x_1 = 20$, $x_2 = 10$

Non-basic variables

$s_1 = 0 \Rightarrow$ first constraint is fully consumed.

$s_2 = 0 \Rightarrow$ second constraint is fully consumed.

$x_3 = 0$ (unwanted variable)

	x_1	x_2	x_3	s_1	s_2	RHS
z-row	0	0	2	1	2	110
x_1	1	0	1	1	-1	20
x_2	0	0	0	–1	2	10

	s_1
z-row	1
x_1	1
x_2	–1

If RHS value of 1st constraint increases by 1 unit then

From the table

z increases by 1 unit, x_1 increases by 1 unit, x_2 decreases by 1 unit,

If RHS value of 2nd constraint increases by 1 unit then

	s_2
z-row	2
x_1	-1
x_2	2

From the table

z increases by 2 units, x_1 decreases by 1 unit x_2 decreases by 2 units,

If RHS value of 1st constraint decreases by 10 units then z decreases by 10 units,

The new objective value ,

$$Z_{max} = 110 - 10 = 100$$

37. Ans: (c)

Sol:

	X_1	X_2	S_1	S_2	RHS	Ratio
z-row	–3	–5	0	0	0	0
S_1	2	1	1	0	2	2/1=2
S_2	3	2	0	1	4	4/2=2

Entering variable X_2

Minimum ratio = min(2/1, 4/2) = 2*

*Tie w.r.t leaving variables S_1 and S_2

Thus it has degenerate solution.

38. Ans: (d)

Sol:

	X_1	X_2	S_1	S_2	RHS
z-row	–2	–1	0	0	0
S_1	–2	1	1	0	4
S_2	0	1	0	1	3

Entering variable X_1

Ratio = Min{4/–2, 3/0}

As there is no least positive ratio, there is no leaving variable which results the problem has unbounded solution.

Chapter- 04
Inventory Control

01. Ans: (b)

Sol: $EOQ = \sqrt{\frac{2AS}{CI}}$

$EOQ_1 = \sqrt{2} \times \sqrt{\frac{2AS}{CI}}$

$EOQ_1 = \sqrt{2} \times EOQ$

02. Ans: (c)

Sol: $EOQ = \sqrt{\frac{2DC_o}{C_c}}$

03. Ans: (b)

Sol: A = 900 unit

S = 100 per order

CI = 2 per unit per year

$EOQ = ELS = \sqrt{\frac{2AS}{CI}}$

$= \sqrt{\frac{2 \times 900 \times 100}{2}} = 300$

04. Ans: (c)

Sol: Inventory carrying cost:

It involves the cost of investment in inventories, of storage, of obsolescence, of insurance, of maintaining inventory records, etc.

05. Ans: (b)

Sol: At EOQ, Carrying cost = Ordering cost

06. Ans: (d)

Sol: Inventory carrying cost involves the cost of investment in inventories, of storage, of obsolescence, of insurance, of maintaining inventory records, etc.

07. Ans: (a)

Sol: A = 800 , S = 50/- ,

C_s = 2 per unit = CI

$(TIC)_{EOQ} = \sqrt{2ASCI}$

$= \sqrt{2 \times 800 \times 50 \times 2} = 400$

08. Ans: (c)

Sol: $TC(Q_1) = TC(Q_2)$

$\frac{kd}{Q_1} + \frac{hQ_1}{2} = \frac{kd}{Q_2} + \frac{hQ_2}{2}$

$kd\left(\frac{Q_2 - Q_1}{Q_1 Q_2}\right) = \frac{h}{2}(Q_2 - Q_1)$

$\frac{2kd}{h} = Q_1 Q_2$

$(Q^*)^2 = Q_1 \times Q_2$

$Q^* = \sqrt{Q_1 \times Q_2} = \sqrt{300 \times 600} = 424.264$

09. Ans: (c)

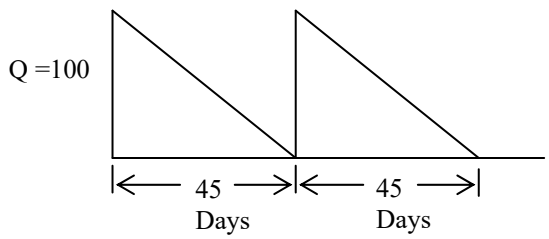
Sol: $\frac{EOQ_1}{EOQ_2} = \sqrt{\left(\frac{2AS}{CI}\right)_A} \times \sqrt{\left(\frac{CI}{2AS}\right)_B}$

$= \sqrt{\left(\frac{2 \times 100 \times 100}{4}\right)} \times \sqrt{\left(\frac{1}{2 \times 400 \times 100}\right)}$

$(EOQ)_A : (EOQ)_B = 1:4$

10. Ans: (d)

Sol: (No of orders $= \frac{A}{Q} = \frac{12\text{ months}}{45\text{ days}} = \frac{12}{1.5} = 8$)



$$TVC = \frac{A}{Q}S + \frac{Q}{2}CI.$$

$$= 8 \times 100 + \frac{100}{2} \times 120 = \text{Rs. } 6800$$

11. Ans: (b)

Sol: Average inventory

$$= \frac{Q}{2} = \frac{6000}{2} = 3000 \text{ per year}$$

$$= 250 \text{ per month}$$

12. Ans: (b)

Sol: P = 1000 , r = 500 , Q = 1000

$$I_{max} = \frac{1000}{1000}(1000 - 500) = 500$$

13. Ans: (c)

Sol: D = 1000 units, C_0 = Rs.100/order,

C_c = 100/unit/year, C_s = 400/unit/year

$$Q_{max} = EOQ_s \times \frac{C_S}{C_C + C_S}$$

$$= \sqrt{\frac{2DC_0}{C_c}}\sqrt{\frac{C_c + C_s}{C_s}} \times \left(\frac{C_s}{C_c + C_s}\right)$$

= 40 units

14. Ans: (d)

Sol: Re-order level = 1.25[Σx p(x)]

= 1.25 [80×0.2+100×0.25+120×0.3+140×0.25]

= 140 units

Demand	80	100	120	**140**
Probability	0.20	0.25	0.30	**0.25**
Cumulative probability (Service level)	0.2	0.45	0.75	**1.0**

Service Level = 100 %

15. Ans: (b)

16. Ans: (b)

17. Ans: (d)

Sol: C – Class means these class items will have very less consumption values. – least consumption values

$B \rightarrow 300 \times 0.15 = 45$

$F \rightarrow 300 \times 0.1 = 30$

$C \rightarrow 2 \times 200 = 400$

$E \rightarrow 5 \times 0.3 = 1.5$

$J \rightarrow 5 \times 0.2 = 1.0$

$G \rightarrow 10 \times 0.05 = 0.5$

$H \rightarrow 7 \times 0.1 = 0.7$

∴ G, H items are classified as C class items because they are having least consumption values.

18. Ans: (b)

Sol: In ABC analysis :

Category "A" = Low safety stock

Category "B" = Medium safety stock

Category "C" = High safety stock

Chapter- 05
Forecasting

01. Ans: (d)

02. Ans: (d)

Sol:

- A simple moving average is a method of computing the average of a specified number of the most recent data values in a series.
- This method assigns equal weight to all observations in the average.
- Greater smoothing effect could be obtained by including more observations in the moving average.

03. Ans: (a)

Sol: 3 period moving avg $= \dfrac{100+99+101}{3}$

$= 100$

4 period moving average

$= \dfrac{102+100+99+101}{4} = 100.5$

5 period moving average

$= \dfrac{99+102+100+99+101}{5} = 100.2$

Arithmetic Mean

$= \dfrac{101+99+102+100+99+101}{6}$

$= 100.33$

04. Ans: (a)

Sol: $D_t = 100$ units , $F_t = 105$ units

$\alpha = 0.2$

$F_{t+1} = 105 + 0.2\,(100 - 105) = 104$

05. Ans: (c)

Sol: $D_t = 105$, $F_t = 97$, $\alpha = 0.4$

$F_{t+1} = 97 + 0.4\,(105 - 97) = 100.2$

06. Ans: (c)

Sol: $F_{t+1} = F_t + a\,(X_t - F_t)$

07. Ans: (c)

Sol: Another form of weighted moving average is the exponential smoothed average. This method keeps a running average of demand and adjusts if for each period in proportion to the difference between the latest actual demand and the latest value of the forecast.

08. Ans: (a)

09. Ans: (b)

Sol:

Period	D_i	F_i	$(D_i - F_i)^2$
14	100	75	625
15	100	87.5	156.25
16.	100	93.75	39.0625
		$\Sigma(D_i - F_i)^2 = 820.31$	

$F_{15} = F_{14} + \alpha(D_{14} - F_{14})$

$= 75 + 0.5(100 - 75) = 87.5$

$F_{16} = F_{15} + \alpha(D_{15} - F_{15})$

$= 87.5 + 0.5(100 - 87.5) = 93.75$

Mean square error (MSE) = $\dfrac{\sum(D_i - F_i)^2}{n}$

$= \dfrac{820.31}{3} = 273.13$

10. Ans: (a)

Sol:

Period	D_i	F_i	$\lvert(D_i - F_i)\rvert$
1	10	9.8	0.2
2	13	12.7	0.3
3	15	15.6	0.6
4	18	18.5	0.5
5	22	21.4	0.6

$\Sigma|D_i - F_i| = 2.2$

11. Ans: (d)

Sol:

m_1 = moving average periods give forecast $F_1(t)$

m_2 = moving average periods give forecast $F_2(t)$

$m_1 > m_2$

$F_1(t)$ is a stable forecast has less variability.

$F_2(t)$ is a sensitive (inflationary) forecast and has high variability.

12. Ans: (d)

Sol: Following are the purposes of long term forecasting :

- To plan for the new unit of production.
- To plan for the long-term financial requirement.
- To make the proper arrangement for training the personal.
- Budgetary allegations are not done in the beginning of a project. So, deciding the purchase program is not the purpose of long term forecasting.

13. Ans: (d)

Sol:

- Time horizon is less for a new product and keeps increasing as the product ages. So, statement (I) is correct.
- Judgemental techniques apply statistical method like random sampling to a small population and extrapolate it on a larger scale. So, statement (II) is correct.
- Low values of smoothing constant result in stable forecast. So statement (3) is correct.

Chapter- 06
Queuing Theory

01. Ans: (a)

Sol: $\lambda = 3$ per day

$\mu = 6$ per day

$$W_q = \frac{\lambda}{\mu(\mu-\lambda)} = \frac{3}{6(6-3)} = \frac{1}{6}\text{day}$$

02. Ans: (c)

Sol: $\lambda = 0.35\ \text{min}^{-1}$,

$\mu = 0.5\ \text{min}^{-1}$

$$P_n = \left[1-\frac{\lambda}{\mu}\right]\left[\frac{\lambda}{\mu}\right]^n$$

$$= \left[1-\frac{0.35}{0.5}\right]\left[\frac{0.35}{0.5}\right]^8 = 0.0173$$

03. Ans: (a)

Sol: $\lambda = 10\ \text{hr}^{-1}$,

$\mu = 15\ \text{hr}^{-1}$

$$L_q = \frac{\lambda^2}{\mu(\mu-\lambda)} = \frac{10^2}{15(15-10)} = 1.33$$

04. Ans: (b)

Sol: $\lambda = 4\ \text{hr}^{-1}$, $\mu = \frac{60}{12} = 5\ \text{hr}^{-1}$

$$L_q = \frac{\lambda^2}{\mu(\mu-\lambda)} = \frac{4^2}{5(5-4)} = \frac{16}{5} = 3.2$$

05. Ans: (b)

Sol: $$L_q = \frac{\lambda^2}{\mu(\mu-\lambda)} = \frac{\lambda^2}{\mu^2\left(1-\frac{\lambda}{\mu}\right)} = \frac{\rho^2}{(1-\rho)}$$

06. Ans: (d)

Sol: $\lambda = \frac{1}{4} = 0.25\text{min}^{-1}$

$\mu = \frac{1}{3} = 0.33\ \text{min}^{1}$

$$\rho = \frac{\lambda}{\mu} = \frac{0.25}{0.33} = 0.75$$

07. Ans: (b)

Sol: $\lambda = \frac{1}{10} = 0.1\text{min}^{-1}$

$\mu = \frac{1}{4} = 0.25\text{min}^{-1}$

System busy $\Rightarrow (\rho) = \frac{\lambda}{\mu} = \frac{0.1}{0.25} = 0.4$

08. Ans: (c)

Sol: $\lambda = 4\text{hr}^{-1}, \mu = 6\ \text{hr}^{-1}$

$$P(Q_S \geq 2) = \left(\frac{\lambda}{\mu}\right)^2$$

$$= \left(\frac{4}{6}\right)^2 = \frac{4}{9}$$

09. Ans: (c)

Chapter- 07
Sequencing & Scheduling

01. Ans: (a)

Sol: SPT rule

Job	Process time (days)	Completion time
1	4	4
3	5	9
5	6	15
6	8	23
2	9	32
4	10	42
	$\Sigma C_i =$	125

Average Flow Time = $\frac{\sum C_i}{n}$

$= \frac{125}{6} = 20.83$

02. Ans: (a)

Sol: According to SPT rule total inventory cost is minimum.

03. Ans: (d)

Sol: EDD rule can minimize maximum lateness.

The job sequence is **R – P – Q – S**

04. Ans: (d)

Sol: Johnson's rule :

Optimum job sequence **III – I – IV – II**

Do the job 1st if the minimum time happens to be on the machine (M) and do it on the end if .it is on second machine (N). Select either in case of a tie.

05. Ans: (b)

Sol:

Job	M			N			Idle
	In	PT	Out	In	PT	Out	
III	0	1	1	1	2	3	-
I	1	3	4	4	6	10	1
IV	4	7	11	11	5	16	1
II	11	5	16	16	2	18	-

Total idle time on machine (N) = 3

06. Ans: (a)

Sol: Optimum sequence of jobs

2	3	1	4

07. Ans: (b)

Sol: Optimum sequence is

R	T	S	Q	U	P

Job	M_1			M_2		
	In	PT	Out	In	PT	Out
R	0	8	8	8	13	21
T	8	11	19	21	14	35
S	19	27	46	46	20	66
Q	46	32	78	78	19	97
U	78	16	94	97	7	104
P	94	15	109	109	6	115

The optimal make-span time = 115 days

08. Ans: (c)

Chapter- 8
Transportation Model

01. Ans: (c)

Sol: A no. of allocations : $m + n - 1$

$\Rightarrow 5 + 3 - 1 = 7$

02. Ans: (a)

Sol: For degeneracy in transportations, number of allocations $< (m + n) - 1$

where m = no. of rows,

n = no. of columns

03. Ans: (b)

Sol: In Transportation problem for solving the initial feasible solution for total cost, Vogel's approximation methods are employed for obtaining solutions which are faster than LPP due to the reduced number of equations for solving.

Optimality is reached using MODI/ U-V method or stepping stone method.

04. Ans: (b)

Sol: It generates the best initial basic feasible solution. This method is the best choice in order to get an optimal solution within minimum number of iterations.

The Vogel's approximation method is also known as the penalty method.

05. Ans: (a)

Sol: No. of allocations = 5

$\therefore$ no. of allocations $= m + n - 1$

$m + n - 1 = 4 + 3 - 1$

$\therefore$ It is a degenerate solution

06. Ans: (a)

Sol:

	1	2	3	4	Supply
A	[10]	[2] 5	[20]	[11] 10	15
B	[12]	[7] 10	[9] 15	[20]	25
C	[5] 5	[14]	[16]	[18] 5	10
Demand	5	15	15	15	50 / 50

Evaluation of empty cells:

Cell (A1) Evaluation $= C_{A1} - C_{A4} + C_{C4} - C_{C1}$

$= 10 - 11 + 18 - 5 = 12$

Cell (A3) Evaluation $= C_{A3} - C_{A2} + C_{B2} - C_{B3}$

$= 20 - 9 + 7 - 2 = 16$

Cell (B1) Evaluation $= 12 - 7 + 2 - 11 + 18 - 4$

$= 10$

Cell (B4) Evaluation $= 20 - 7 + 2 - 11 = 4$

Cell (C2) Evaluation $= 14 - 2 + 11 - 18 = 5$

Cell (C3) Evaluation $= 16 - 9 + 7 - 2 - 18 = 5$

If cell cost evaluation value is '–ve', indicates further unit transportation cost is decreasing and if cost evaluation value is '+ve' indicates further unit transportation cost is increases. If cost evaluation value is zero, unit transportation cost doesn't change.

∴ As for A3 cell cost evaluation is +16, means that, if we transport goods to A3 the unit transportation cost is increased by 16/-.

Common Data for Questions Q07, Q08 & Q09 :

07. Ans: (b) **08. Ans: (a)**

09. Ans: (b)

Sol:

	1	2	3	4
A	[6]	[1]	[9] 25	[3] 45
B	[11] 30	[5]	[2] 25	[8]
C	[10] 55	[12] 35	[4]	[7]

No. of allocations = 6

R + C – 1 = 6

As No. of allocations = R + C – 1

Hence the problem is not degeneracy case.

Opportunity cost of cell (i, j) is

$C_{ij} - (U_i + V_j)$

If $C_{ij} - (U_i + V_j) \geq 0 \Rightarrow$ problem is optimal,

Empty cell evaluation (or) Opportunity cost of cells:

$A_1 = -12$, $A_2 = -19$, $B_2 = -8$

$B_4 = 12$, $C_3 = 3$, $C_4 = 12$

From the above as A2 has opportunity cost '–19' indicates unit transportation cost is decreased by 19/-

By forming loop A2, A3, B2, B3 it is observed that to transport minimum quantity is 25 among 25, 30, 35.

∴ The reduction in the transportation cost is 25 × 19 = 475

10. Ans: (c)

Sol:

	10		14	
7			12	16
5	8			

By stepping stone method,

Cell evaluation of B – 1 cell

= +7 – 5 + 8 – 10 + 14 – 12

= 2/-

	10 – θ	20 + θ	
+θ		5 – θ	35
20 – θ	10 + θ		

θ = minimum of |10 – θ, 5 – θ, 20 – θ| = 0

θ = 5 units

Increase in cost = 5 × 2 = 10/-

11. Ans: (c)

Sol: To find the number units shifted to A_2 cell.

+θ	20 – θ
15 – θ	25 + θ

θ = minimum value of |15–θ, 20–θ| = 0

θ = 15 units

Chapter- 9
Assignment Model

01. Ans: (a)

Sol: Let C_{ij} = unit assignment cost

X_{ij} = Decision variable (allocation)

Minimize $Z = \sum_{i=1}^{n} \sum_{J=1}^{n} C_{ij} X_{ij}$

Subject to : $\sum_{i=1}^{n} X_{ij} = 1$

$\sum_{j=1}^{n} X_{ij} = 1$

$X_{ij} = 1$ (when assigned)

$X_{ij} = 0$ (when not assigned)

- Number of decision variables = n^2 (or) m^2
- Number of basic variables = Number of assignments = n (or) m

02. Ans: (c) **03. Ans: (a)**

04. Ans: (c)

Sol:

	S_1	S_2	S_3
P	110	120	130
Q	115	140	140
R	125	145	165
P	0	10	20
Q	0	25	25
R	0	20	40

Column Transaction

S_1	S_2	S_3
~~0~~	~~0~~	~~0~~
0	15	5
0	10	20
~~5~~	~~0~~	~~0~~
~~0~~	~~10~~	~~0~~
~~0~~	~~5~~	~~15~~

Row Transaction

P-S_2 – 120

Q-S_3 – 140

R-S_1 – 125

Total = 385

05. Ans: (1-B, 2-D, 3-C, 4-A)

Sol: Step-1:

Take the row minimum of subtract it from all elements of corresponding row.

1	0	2	3
0	2	2	1
8	5	0	1
0	6	2	4

Step – 2 :

Take the column minimum & substract it from all elements of corresponding column.

1	0	2	2
0	2	2	0
8	5	0	0
0	6	2	3

Step – 3 :

Select single zero row or column and assign at the all where zero exists. If there is no single zero row or column. Then use straight line method.

	A	B	C	D
1	1	$\boxed{0}$	2	2
2	0	2	2	$\boxed{0}$
3	8	5	$\boxed{0}$	0
4	$\boxed{0}$	6	2	3

1 – B : 7

2 – D : 8

3 – C : 2

4 – A : 5

Total cost = 22

Chapter- 10
PPC & Aggregate Planning

01. Ans: (d) **02. Ans: (b)**

03. Ans: (b)

Sol:

Months		Month 1	Month 2	Month 3	Unused capacity	Capacity Available
1	RT	20 90	22 10	24	10	100
	OT	24	26	28		20
2	RT		20 100	22		100
	OT		24 20	26		20
3	RT			20 80		80
	OT			24 30	10	40
	RT	90	130	110		
	OT					

Level of planned production in overtimes in 3rd period is '30'.

RT = Regular time

OT = Over time

04. Ans: (b)

Sol:

Month	Cumulative Production	Cumulative Demand	Inventory		Cost	
			End	Stock out	End inventory	Stock out cost
1	100	80	20	-	40	-
2	180	180	-	-	-	-
3	250	260	-	10	-	100
4	320	300	20	-	40	-
					80	100
				Total	**180**	

05. Ans: (b) **06. Ans: (d)**

Chapter- 11
Material Requirement & Planning

01. Ans: (b)

02. Ans: (c)

Sol: Based on master production schedule, a material requirements planning system :

- Creates schedules, identifying the specific parts and materials required to produce end items.
- Determines exact unit numbers needed.
- Determines the dates when orders for those materials should be released, based on lead times.

03. Ans: (d)

Sol: *Refer to the solution of Q.No. 02*

04. Ans: (c)

Sol: MRP has three major input components:

1. Master production Schedule of end items required. It dictates gross or projected requirements for end items to the MRP system.
2. Inventory status file of on-hand and on-order items, lot sizes, lead times etc.
3. Bill of materials (BOM) or Product structure file what components and sub assemblies go into each end product.

05. Ans: (c)

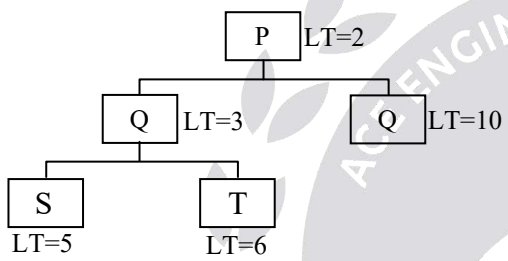
06. Ans: (c)

07. Ans: (b)

08. Ans: (b)

09. Ans: (c)

Sol:



Maximum Lead time = 12 weeks

Chapter- 12
Break Even Analysis

01. Ans: (c)

Sol: Total fixed cost, TFC = Rs 5000/-

Sales price, SP = Rs 30/-

Variable cost, VC = Rs 20/-

Break even production per month,

$$Q^* = \frac{TFC}{SP - VC} = \frac{5000}{30 - 20} = 500 \text{ units}$$

02. Ans: (a)

Sol: Total cost = 20 + 3X ----------(1)

Total cost = 50 + X ----------(2)

By solving equ. (1) and (2)

$2X = 30$

$\therefore \quad X = 15$ units

When X = 10 units

$TC_1 = 20 + (3 \times 10) = \text{Rs } 50/-$

$TC_2 = 50 + (1 \times 10) = \text{Rs } 60/-$

Among both, total cost for process is less

So process-1 is choose.

03. Ans: (c)

Sol: In automated assembly there are less labour, so variable cost is less, but fixed is more because machine usage is more. In job shop production, labour is more but machine is less. So variable cost is more and fixed cost is less.

04. Ans: (c)

Sol: TC = Total cost

TC_A = Total cost for jig-A

TC_B = Total for jig-B

$$TC_A = TC_B$$

$$800 + 0.1X = 1200 + 0.08X$$

$$0.02X = 400$$

$$\therefore X = \frac{400}{0.02} = \frac{400}{2} \times 100 = 20{,}000 \text{ units}$$

05. Ans: (d)

Sol: Sales price – Total cost = Profit

$$(C_P \times 14000) - (47000 + 14000 \times 15) = 23000$$

$$\therefore C_P = 20$$

06. Ans: (b)

07. Ans: (a)

08. Ans: (c)

09. Ans: 1500

Sol:

X	Y
$S_1 = 100$	$S_2 = 120$
$F_1 = 20{,}000$	$F_2 = 8000$
$V_1 = 12$	$V_2 = 40$

$$P = q(S - V) - F$$

$$P_1 = q(100 - 12) - 20{,}000$$

$$P_2 = q(120 - 40) - 80{,}000$$

$$P_1 = P_2$$

$$88q - 20{,}000 = 80q - 80{,}000$$

$$12000 = 8q$$

$$\Rightarrow q = 1500$$

10. Ans: (b)

11. Ans: (c)

Sol: At breakeven point

Total cost = Total revenue

$$FC + VC \times Q = SP \times Q$$

$$Q = \frac{FC}{(SP - VC)}$$

FC = 1000/-

VC = 3/-

SP = 4/-

$$Q = \frac{1000}{(4-3)} = 1000 \text{ units}$$

If sales price is increased to 25%

$$SP = 4 + \frac{1}{4} \times 4 = 5/-$$

$$Q^* = \frac{1000}{(5-3)} = 500 \text{ units}$$

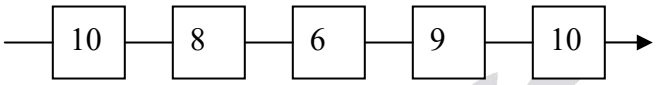
$\therefore$ Breakeven quantity decreases by

$$\frac{100 - 500}{100} \times 100 = 50\%$$

Chapter- 13
Line Balancing

01. Ans: (c)

Sol:



$\sum t_i = 43$; $n = 5$; $C = 10$

$$\text{Balance delay} = 1 - \frac{\sum t_i}{nC}$$

$$= 1 - \frac{43}{5 \times 10}$$

$$= 0.14 \text{ or } 14\ \%$$

02. Ans: (d)

Sol: $$\text{Cycle Time} = \frac{\text{Total time}}{\text{Total production}}$$

$$= \frac{8 \times 60 \times 60}{3000}$$

$$CT = \frac{48}{5} = 9.6 \text{ seconds}$$

Time to assemble one unit

$= 10+20+15+5+30+15+5 = 100$ sec

No. of work station

$$= \frac{\text{Time to assemble one unit}}{\text{Cycle Time} \times \eta}$$

$$= \frac{100}{9.6} = 11 \quad (\text{consider } \eta = 100\%)$$

03. Ans: (c)

Sol: Assembly line balancing :

Line balancing is done to meet the production rate for a given time, minimizing the idle time and maximizing the work output. As the time is minimized, the idle time at the stations decreases, decreasing the in-process inventory.

Statements 1, 3, 4 apply to the benefits of assembly line balancing.

04. Ans: (c)

Sol: $$\text{Cycle Time} = \frac{\text{Total time}}{\text{Total production}}$$

$$= \frac{8 \times 60}{320} = 1.5 \text{ min}$$

Time to assemble one unit

$= 1.3 + 1.5 + 1.4 + 1.5 + 1.3 = 7$ min

No. of work station

$$= \frac{\text{Time to assemble one unit}}{\text{Cycle Time}}$$

$$= \frac{7}{1.5} = \frac{14}{3} \approx 5$$

$$\eta = \frac{\text{Time to assemble one unit}}{\text{No. of work stations} \times \text{Cycle Time}}$$

$$= \frac{7}{5 \times 1.5} = 0.93$$

05. Ans: (d)

Sol: Cycle Time = $\frac{480 \times 60}{1450} = 19.87$ sec

No. of work station = $\frac{310}{19.87} = 15.6 \approx 16$

$$\eta = \frac{310}{16 \times 19.87} \times 100 = 97.5\%$$

06. Ans: (a)

Sol: Cycle time is equal to the time of the bottleneck operation or the maximum station time.