

Dear ACE students(ECE),

Solutions along with the explanation are given here for typical questions of Communication System booklet which has been issued to you. The student is suggested to try the questions given in the booklet, on his/her own and then refer to the solutions given below.

Good Luck.

ACE Academy.

CHAPTER- 2 Random Signals & Noise

01. From the property of CDF is that $F_x(\infty) = 1$. So, the options 'c' and 'd' can be eliminated since $F_x(\infty)$ is Zero in both of them.

if CDF is a Ramp, the corresponding pdf will be $\frac{d}{dx}(\text{Ramp}) = \text{Step}$. But, since the given pdf is not step, the option 'b' also can be eliminated.

Hence, the correct option is 'a'.

02. $H(f) = \frac{1}{1 + j2\pi fRC}$ & $f_{3db} = f_c = \frac{1}{2\pi RC}$

$$\therefore H(f) = \frac{1}{1 + j(f/f_c)}$$

$$\text{o/p PSD} = |H(f)|^2. \quad \text{i/p PSD} = \frac{k}{1 + (f/f_c)^2}$$

$$\text{o/p Noise Power} = \int_{-\infty}^{\infty} \frac{k}{1 + (f/f_c)^2} df = k\pi f_c.$$

Ans: 'c'

03. Auto correlation is maximum at $\tau=0$

$$\text{i.e. } R(0) \geq |R(\tau)|$$

Ans :- 'b'

04. Power spectral density is always non negative

$$\text{i.e. } S(f) \geq 0$$

Ans:- 'b'

05. This corresponds to Binomial distribution. When an experiment is repeated for n times, the probability of getting the success ‘m’ times, independent of order is

$$P(x=m) = n_{c_m} \cdot p^m \cdot (q)^{n-m}$$

Where p = Prob. of success & q = 1-p

In the present problem, success is getting an error. The corresponding probability is given as ‘p’.

$$\begin{aligned} P(\text{At most one error}) &= P(\text{no errors}) + P(\text{one error}) \\ &= P(X=0) + P(X=1) \\ &= n_{c_0} \cdot (p)^0 \cdot (1-p)^n + n_{c_1} \cdot (p)^1 \cdot (1-p)^{n-1} \\ &= (1-p)^n + np(1-p)^{n-1} \end{aligned}$$

Ans:- ‘c’

06. The random variable y is taking two values 0 & 1.

$$P(y=1) = P(-2.5 < x < 2.5)$$

$$P(y=0) = P(x \geq 2.5) + P(x \leq -2.5)$$

$$\therefore P(-2.5 < x < 2.5) = \int_{-2.5}^{2.5} f(x) dx = 0.5$$

$$P(x \geq 2.5) = \int_{2.5}^5 f(x) dx = 0.25$$

$$P(x \leq -2.5) = \int_{-5}^{-2.5} f(x) dx = 0.25$$

$$\therefore P(y = 1) = 0.5 ; P(y=0) = 0.25 + 0.25 = 0.5$$

$$\therefore f(y) = 0.5 \delta(y) + 0.5 \delta(y-1)$$

Ans :- ‘b’

07. Ans: ‘b’

08. PSD of i/p process $S_{xx}(\omega) = 1$

$$\text{PSD of o/p process } S_{yy}(\omega) = \frac{16}{16 + \omega^2}$$

$$|H(\omega)|^2 = \frac{S_{YY}(\omega)}{S_{XX}(\omega)} = \frac{16}{16 + \omega^2}$$

$$|H(\omega)| = \frac{4}{\sqrt{16 + \omega^2}} \Rightarrow H(\omega) = \frac{4}{4 + j\omega}$$

We have H(ω) for an RL – Low Pass Filter as $H(\omega) = \frac{R}{R + j\omega L}$

∴ Ans :- (a)

09. R = 4Ω ; L = 4H

Ans :- ‘a’

10. o/p Noise Power = (o/p) PSD \times B. ω
 $H(\omega) = 2 \cdot \exp(-j\omega t_d)$
 $|H(\omega)|^2 = 4 \Rightarrow$ o/p Noise PSD = $4N_0$
 \therefore o/p Noise Power = $4N_0 B$

Ans :- 'b'

11. $P(\bar{r}) = \left(\frac{k}{4}\right)\bar{r}$ for $0 \leq k \leq 4$
 = 0 elsewhere

$$\text{Since } \int_0^4 P(\bar{r}) \cdot d\bar{r} = 1 \Rightarrow k = \frac{1}{2}$$

$$\text{Mean Square Value is } \int_0^4 \bar{r}^2 \cdot P(\bar{r}) \cdot d\bar{r} = 8$$

Ans :- 'c'

12. $|H(f)|^2 = 1 + (0.1 \times 10^{-3})f$ for $-10 \text{ KHz} \leq f \leq 0$
 $= 1 - (0.1 \times 10^{-3})f$ for $0 \leq f \leq 10 \text{ KHz}$
 (o/p) PSD = $|H(f)|^2 \times$ i/p PSD

$$\text{Power of o/p Process} = \int_{-10 \times 10^3}^{10 \times 10^3} (\text{o/p}) \text{ PSD} \cdot df = 1 \times 10^{-6} \omega$$

Ans:- 'b'

13. $R(\tau) \xleftrightarrow{\text{FT}} \text{PSD } [S_{xx}(\omega)]$

Since PSD is sinc – squared function, its inverse Fourier Transform is a Triangular pulse.

Ans:- 'b'

14. $\text{Var}[d(n)] = E[d^2(n)] - \{E[d(n)]\}^2$
 $E[d(n)] = E[x(n) - x(n-1)]$
 $= E[x(n)] - E[x(n-1)] = 0$

$$\begin{aligned} \text{Var}[d(n)] &= E[d^2(n)] = E[\{x(n) - x(n-1)\}^2] \\ &= E[x^2(n)] + E[x^2(n-1)] - 2 \cdot E[x(n) \cdot x(n-1)] \\ &= \sigma_x^2 + \sigma_x^2 - 2 \cdot R_{xx}(1) \\ &\Rightarrow 2\sigma_x^2 - 2R_{xx}(1) = \frac{1}{10}\sigma_x^2 \\ &\Rightarrow \frac{R_{xx}(k)}{\sigma_x^2} \text{ at } k=1 = 0.95 \end{aligned}$$

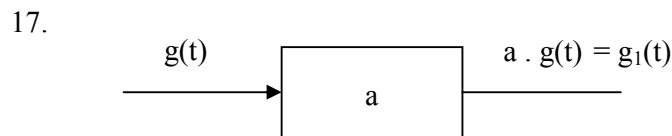
Ans: 'a'

$$\begin{aligned}
 15. P_X(x) &= \frac{1}{3\sqrt{2\pi}} \exp\left[-\frac{(x-4)^2}{18}\right] \\
 &= \frac{1}{\sqrt{2\pi \times 9}} \exp\left[-\frac{(x-4)^2}{2 \times 9}\right] \\
 P\{X=4\} &= P_X(x)|_{x=4} = \frac{1}{3\sqrt{2\pi}}
 \end{aligned}$$

Ans: b

$$\begin{aligned}
 16. P(\text{at most one bit error}) \\
 &= P(\text{No error}) + P(\text{one error}) \\
 &= n_{C_0} \cdot (P)^0 (1-P)^{n-0} + n_{C_1} (P)^1 (1-P)^{n-1} \\
 &= (1-P)^n + n P(1-P)^{n-1}
 \end{aligned}$$

Ans: d



$$\therefore H(\omega) = a \Rightarrow \text{PSD of } g_1(t) = a^2 \cdot S_g(\omega)$$

$$\begin{aligned}
 R_{g_1}(\tau) &= F^{-1} [a^2 \cdot S_g(\omega)] = a^2 \cdot R_g(\tau) \\
 \Rightarrow \text{power of } R_{g_1}(\tau) &= a^2 \cdot R_g(0) = a^2 \cdot P_g
 \end{aligned}$$

Ans: a

18. The Fourier Transform of a Gaussian Pulse is also Gaussian.

Ans: 'c'

19. The Auto correlation Function (ACF) of a rectangular Pulse of duration T is a Triangular Pulse of duration 2T

Ans: 'd'

20. The Prob. density function of the envelope of Narrow band Gaussian noise is Rayleigh

Ans: 'c'

$$21. P(x) = K \cdot \exp(-x^2/2), -\infty < x < \infty$$

$$\int_{-\infty}^{\infty} P(x) \cdot dx = 1 \Rightarrow \int_{-\infty}^{\infty} k \cdot \exp(-x^2/2) dx = 1$$

We have $\frac{1}{\sqrt{2\pi}} \int_{-\infty}^{\infty} e^{-x^2/2} .dx = 1$, since

$\frac{1}{\sqrt{2\pi}} e^{-x^2/2}$ is the Normal density

$N(m, \sigma^2) = N(0,1)$

$$\therefore k = \frac{1}{\sqrt{2\pi}}$$

Ans: 'a'

22. $F^{-1}[\text{PSD}] = \text{Auto correlation Function } R(\tau)$

$\therefore R(\tau) = F^{-1} \left[\left(\frac{\sin f}{f} \right)^2 \right]$, which is a triangular pulse.

Ans: 'd'

23. $R(\tau) = R(-\tau) \Rightarrow$ Even symmetry

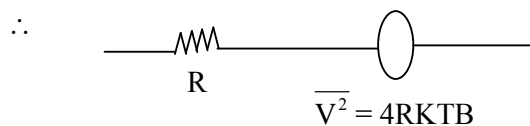
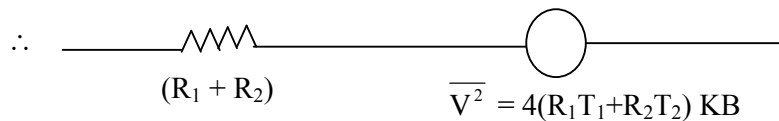
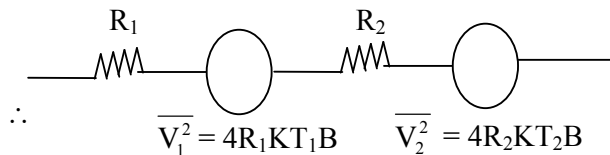
Ans : 'd'

24. Rayleigh

Ans : 'd'

25. 

The Noise equivalent circuit is



$$\therefore RT = R_1T_1 + R_2T_2$$

$$\Rightarrow T = \frac{R_1T_1 + R_2T_2}{R_1 + R_2}$$

$$26. E(X) = \int_{-1}^3 x \cdot P(x) dx = 1$$

$$E(X^2) = \int_{-1}^3 x \cdot P(x) dx = 7/3$$

$$\text{Var}(X) = E(X^2) - [E(X)]^2 = \frac{7}{3} - 1 = \frac{4}{3}$$

Ans: 'b'

27. Half wave rectification is $Y = X$ for $x \geq 0$

= 0 elsewhere

$$f(y) = \frac{1}{2} \delta(y) + \frac{1}{\sqrt{2\pi N}} e^{-y^2/2N}$$

$$E(Y) = 0 \text{ \& } E(Y^2) = N$$

Ans: 'd'

28. $P(X = \text{at most one error}) = P(X = 0) + P(X = 1)$

$$= {}_8C_0 \cdot (P)^0 (1-P)^8 + {}_8C_1 \cdot (P)^1 (1-P)^{8-1}$$

$$= (1-P)^8 + 8P (1-P)^7$$

Ans: 'b'

29. $\text{Var} [(-kx)] = E[(-kx)^2] - \{E(-kx)\}^2$

$$= k^2 E(x^2) - [-k \cdot E(x)]^2$$

$$= k^2 E(x^2) - k^2 \cdot [E(x)]^2$$

$$= k^2 [E(x^2) - \{E(x)\}^2]$$

$$= k^2 \cdot \sigma_x^2$$

Ans: 'd'

CHAPTER – 3**Objective Questions Set – A**

01. $(B.W)_{AM} = 2$ (Highest of the Baseband frequency available)

$$= 2(20 \text{ KHZ}) = 40 \text{ KHZ}$$

02. Percentage Power saving = $\frac{P_T - P_{TX}}{P_T} \times 100 \%$

$$= \frac{2}{2+m^2} \times 100 \%$$

For $m = 1$, Power saving = $\frac{2}{3} \times 100 \% = 66.66 \%$

03. $P_T = P_C \left(1 + \frac{m^2}{2} \right)$

For $m = 0$; $P_T = P_C$

For $m = 1$; $P_T = 1.5 P_C$

\Rightarrow TX. Power increased by 50%

04. $m_T = \sqrt{m_1^2 + m_2^2} = \sqrt{(0.3)^2 + (0.4)^2} = 0.5$

06. $m = \frac{V_{\max} - V_{\min}}{V_{\max} + V_{\min}} = 1/2$

07. The given AM signal is of the form $[A + m(t)] \cos \omega_c t$, which is an AM-DSB-FC signal. It can be better detected by the simplest detector i.e. Diode Detector

08. MW/Broadcast band is 550 KHz – 1650 KHz.

09. Hence the received 1 MHz signal lies outside the MW band.

10. $Q = \frac{f_0}{BW} = \frac{1 \times 10^6}{10 \times 10^3} = 100$

12. $P_T = P_C + P_C \frac{m^2}{2} \Rightarrow \frac{P_c \cdot m^2}{2} = \frac{P_c (0.4)^2}{2} = 0.08 P_c$

$$\therefore P_T = 1.08 P_c$$

\Rightarrow Increase in Power is 8%.

14. $e_m(t) = 10(1 + 0.4 \cos 10^3 t + 0.3 \cos 10^4 t) \cos(10^6 t)$

This is a multi Tone AM signal with $m_1=0.4$ and $m_2=0.3$

$$\therefore m = \sqrt{m_1^2 + m_2^2} = 0.5$$

15. Image freq(f_i) = $f_s + 2$ IF

$$\Rightarrow f_s = f_i - 2 \text{ IF} = 2100 - 900 = 1200 \text{ KHz.}$$

16. Same as Prob. 2

18. Same as 3

19. $P_{SB} = 75 + 75 = 150 = P_C \frac{m^2}{2}$ and $P_c = P_T - P_{SB} = 600 - 150 = 450$

$$\therefore P_C \frac{m^2}{2} = \frac{450 \times m^2}{2} = 150 \Rightarrow m = \sqrt{2/3}$$

20. $P_c = 450 \omega$

22. BW of each AM station = 10 KHz.

$$\text{No. of stations} = \frac{100 \times 10^3}{10 \times 10^3} = 10$$

25. $m = \frac{E_m}{E_c} = \frac{15}{60} \Rightarrow m = 25\%$

26. $(B.W)_{AM} = 2 \times 1500 = 3 \text{ KHz.}$

27. Message B.W = Band limiting freq. of the baseband signal = 10 KHz.

28. $B.W = 2(10 \text{ KHz}) = 20 \text{ KHz.}$

29. The various freq. in o/p are 1000 KHz, $(1000 \pm 1) \text{ KHz}$ & $(1000 \pm 10) \text{ KHz.}$

\therefore The freq. which will not be present in the spectrum is 2 MHz.

30. Highest freq. = USB w.r.t highest baseband freq. available =
 $(1000 + 10) \text{ KHz} = 1010 \text{ KHz}$

CHAPTER – 3**Objective Questions – SET C**

5. A freq. tripler makes the freq. deviation, three times the original.

$$\therefore \text{New Modulation Index} = 3 \cdot \frac{\delta f}{f_m} = 3 m_f$$

6. Mixer will not change the deviation. Thus, deviation at the o/p of the mixer is δ .

20. $B.W_1 = 2(\delta f + 10 \text{ KHz})$

$$B.W_2 = 2(\delta f + 20 \text{ KHz}) \Rightarrow B.W \text{ increases by } 20 \text{ KHz.}$$

29. In NBFM, Modulation Index is always less than 1.

CHAPTER – 3**Additional objective questions – SET D**

1. Amplitude of each sideband = $\frac{m E_c}{2}$

$$= \frac{0.3 \times 10^3}{2}$$
$$= 150 \text{ v}$$

Ans: 'b'

2. $E_c = 1 \text{ KV} \Rightarrow \frac{m E_c}{2} = \frac{1000 \times m}{2} = 200$

$$\Rightarrow m = 0.4$$

Ans: 'c'

3. $P_c = 1 \text{ KW}; P_{SB} = \frac{P_c}{2} = 0.5 \text{ KW}$

$$\therefore P_T = P_C + P_{SB} = 1.5 \text{ KW.}$$

Ans: 'b'

4. As per FCC regulations, in AM, $(f_m)_{\max} = 5 \text{ KHz}$

Ans: 'b'

5. $E_c + E_m = 130 \Rightarrow E_m = 130 - 100 = 30 \text{ V}$

$$m = \frac{E_m}{E_c} = \frac{30}{100} = 0.3$$

Ans: 'b'

6. $V(t) = A[1 + m \sin \omega_m t] \sin \omega_c t$

By comparing the given with above $V(t)$, the unmodulated carrier peak $A = 20$

$$\Rightarrow \text{rms value} = 20/\sqrt{2}$$

Ans : 'b'

7. Side band peak = $\frac{mE_c}{2} = \frac{0.5 \times 20}{2} = 5$

$$\text{Rms value} = 5/\sqrt{2}$$

Ans: 'a'

8. $m = 0.5 \Rightarrow 50\%$ Modulation

Ans: 'b'

09. $V = A[1 + m \sin \omega_m t] \sin \omega_c t$

$$\Rightarrow \omega_m = 6280$$

Ans: 'c'

10. $\omega_c = 6.28 \times 10^6$

Ans : 'a'

11. $m > 1$ results in over Modulation, causing distortion .

Ans : 'd'

12. Ans: 'b'

13. $E_c + E_m = 2E_c \Rightarrow E_m = E_c$

$$\Rightarrow m = \frac{E_m}{E_c} = 100\%$$

Ans: 'd'

14. $E_c + E_m = 110$

$$E_c - E_m = 90$$

$$\Rightarrow E_c = 100V; E_m = 10V$$

Ans: 'c'

15. Using the above results, $m = \frac{E_m}{E_c} = \frac{10}{100} = 0.1$

Ans: 'a'

16. using the above results, the sideband amplitude is $\frac{mE_c}{2} = \frac{0.1 \times 100}{2} = 5V$

Ans: 'b'

17. $m = \frac{E_m}{E_c} \Rightarrow E_m = m.E_c$

The carrier peak is $(100)\sqrt{2}$

$$\therefore E_m = (0.2)(100)\sqrt{2} = 20\sqrt{2}$$

$$\therefore E_c + E_m = (120)\sqrt{2}$$

The corresponding rms value = 120 V

Ans: 'd'

20. $I_t = I_c \sqrt{1 + \frac{m^2}{2}}$

$$I_c = 10 \text{ Amp}; I_t = 10.4 \text{ Amp.}$$

$$\therefore m = 0.4 \Rightarrow \text{Ans: b}$$

21. $m = \sqrt{(0.3)^2 + (0.4)^2} = 0.5$

$$\Rightarrow \text{Modulation Index} = 50\%$$

Ans: 'a'

23. $P_c = P_T - P_{SB} = 1160 - 160 = 1000 \text{ Watts}$

Ans: 'a'

24.
$$m = \frac{I_{\max} - I_{\min}}{I_{\max} + I_{\min}} = \frac{6}{20} = 0.3$$

\Rightarrow Percent Modulation = 30%

Ans: 'b'

27. To implement Envelope detection,

$$T_c < RC < T_m$$

$$T_c = 1 \mu\text{sec}; T_m = 0.5 \text{msec}$$

$$= 500 \mu\text{sec}$$

Since $T_c < RC < T_m \Rightarrow RC = 20 \mu\text{sec}$.

Ans: 'b'

28. As per FCC regulations in FM, $(f_m)_{\max} = 15 \text{KHz}$

Ans: 'c'

29. In FM, $(\delta f) \propto E_m$

\Rightarrow if E_m is doubled, δf also gets doubled

Ans: 'a'

30. If FM, (δf) is independent of Base Band signal frequency. Thus, δf remains unaltered.

Ans: 'd'

31. Ans: 'd'

32. frequency doubler doubles the freq. deviation. Thus at the o/p of the doubler, the modulation index is $2.m_f$

Ans: 'a'

33. Mixer will not change the freq. deviation. Thus freq. deviation at the o/p of Mixer is δ

Ans: 'b'

35. $\delta f = (f_c)_{\max} - f_c = 210 - 200 = 10 \text{KHZ}$

Ans: 'b'

$$37. \quad m_f = \frac{\delta f}{f_m} = \frac{5 \text{ KHz}}{500 \text{ Hz}} = 10$$

Ans: 'a'

$$38. \quad \delta f \propto E_m \Rightarrow \frac{\delta f_1}{\delta f_2} = \frac{E_{m1}}{E_{m2}}$$
$$\Rightarrow \delta f_2 = \frac{(\delta f_1)(E_{m2})}{(E_{m1})} = \frac{(5 \text{ KHz})(10 \text{ V})}{(2.5 \text{ V})}$$
$$= 20 \text{ KHz}$$

$$39. \quad m = \frac{\delta f_2}{f_m} = \frac{20 \times 10^3}{500} = 40$$

$$40. \quad \delta f_2 = \frac{(\delta f_1)(E_{m2})}{E_{m1}} = \frac{5 \times 20}{2} = 50 \text{ KHz}$$

Ans: 'b'

41. Assuming the signal to be an FM signal, the Power of the Modulated signal is same as that of un Modulated carrier.

Ans: 'a'

$$43. \quad v_{\text{FM}}(t) = A \cos(\omega_c t + m_f \cdot \sin \omega_m t)$$

$$\Rightarrow \omega_c = 6.28 \times 10^8$$

Ans: 'a'

$$44. \quad \omega_m = 628 \text{ Hz}$$

Ans: 'a'

$$45. \quad m_f = \frac{\delta f}{f_m} \Rightarrow \delta f = 4 f_m = 25/2 \text{ Hz}$$

Ans: 'c'

46. Figure of Merit in FM is $\gamma = \frac{3}{2} m_f^2$, where m_f is the Modulation Index.

\therefore Noise Performance increases with increase in freq. deviation.

Ans: 'a'

47. In FM, Modulation Index $\propto \frac{1}{f_m}$

Ans: 'a'

48. In FM, o/p Power is independent of modulation Index.

Ans: 'd'

52. B.W = $2(\delta f + f_m) = 2(75 + 15) = 180$ KHz

Ans: 'c'

53. B.W = $2nf_m = 2(8)(15 \text{ KHz}) = 240$ KHz

Ans: 'd'

54. B.W = $2nf_m$ & $n = m_f + 1 = 8$

$$\Rightarrow 2(8)(f_m) = 160 \times 10^3 \Rightarrow f_m = 10 \text{ KHz}$$

$$\therefore \delta f(m_f)(f_m) = (7)(10) \text{ KHz} = 70 \text{ KHz}$$

Ans: 'c'

55. B.W = $2nf_m$

$$\text{The modulation Index } m_f = \frac{\delta f}{f_m} = \frac{10^6}{10 \times 10^3} = 100$$

$$\therefore n = 100 + 1 = 101$$

$$\therefore \text{B.W} = 2(101)(10 \times 10^3) = 2.02 \text{ MHz}$$

Ans: 'b'

56. If E_m gets doubled, δf also get doubled.

$$\therefore m_f = \frac{\delta f}{f_m} = \frac{2 \times 10^6}{10 \times 10^3} = 200$$

$$n = 201$$

$$\text{B.W} = 2(201)(10 \times 10^3) = 4.02 \text{ MHz}$$

Ans: 'd'

58. For WBFM, B.W = $2(\delta f + f_m)$.

Ans: 'd'

59. For NBFM, B.W = $2 f_m$

Ans: 'b'

60. In WBFM, $\delta f \gg f_m \Rightarrow B.W \cong 2 \delta f$

Ans: 'd'

63. Since (δf) is independent of carrier freq. \therefore the peak deviations are same.

Ans: 'c'

66. At the o/p of the mixer, ' δ ' remains the same.

Ans: 'd'

67. $\psi_i(t) = 50t + \sin 5t$

$$\omega_i = \frac{d}{dt} \psi_i(t) = 50 + 5 \cos 5t$$

\therefore At $t = 0$, $\omega_i = 55$ rad/sec

Ans: 'c'

75. IF = 455 KHz; $f_s = 1200$ KHz.

$$\begin{aligned} \therefore \text{Image freq.} &= f_s + 2 \text{ IF} \\ &= 2110 \text{ KHz} \end{aligned}$$

76. Ans: Refer Q. No. 26 Set-F

$$\begin{aligned} 77. \quad f_i &= f_s + 2 \text{ IF} = 1000 + 2(455) \\ &= 1910 \text{ KHz} \end{aligned}$$

Ans: 'd'

$$\begin{aligned} 78. \quad f_i &= f_s + 2 \text{ IF} = 1500 + 2(455) \\ &= 2410 \text{ KHz} \end{aligned}$$

Ans: 'd'

82. $f_i = f_s + 2 IF = 500 + 2 (465)$
 $= 1430 \text{ KHz}$

Ans: 'b'

Chapter – 3

Additional objective

Questions – Set E

01. By comparing with the general AM – DSB – FC signal $A_c \cdot \cos \omega_c t + m(t) \cdot \cos \omega_c t$, it is found that $m(t) = 2 \cos \omega_m t$. To demodulate using Envelope detector,

$A_c \geq m_p$, where m_p is the Peak of the baseband signal, which is 2.

$\therefore (A_c)_{\min} = 2$

Ans: 'a'

02. $v_{FM}(t) = 10 \cos [2\pi \times 10^5 t + 5 \sin (2\pi \times 1500t) + 7.5 \sin (2\pi \times 1000t)]$

$\psi_i(t) = [2\pi \times 10^5 t + 5 \sin (2\pi \times 1500)t + 7.5 \sin (2\pi \times 1000)t]$

$\omega_i = \frac{d}{dt} \psi_i(t) = 2\pi \times 10^5 + 5(2\pi \times 1500) \cos (2\pi \times 1500t) + 7.5(2\pi \times 1000) \cos (2\pi \times 1000t)$

$\delta\omega = 5(2\pi \times 1500) + 7.5(2\pi \times 1000)$

$\delta f = 7500 + 7500 = 15000 \text{ Hz}$

$F_m = 1500 \text{ Hz}$

$\therefore \text{Modulation Index} = \frac{\delta f}{f_m} = 10$

Ans: 'b'

03. $v(t) = \cos \omega_c t + 0.5 \cos \omega_m t \cdot \sin \omega_c t$

Let $r(t) \cdot \cos \theta(t) = 1$

$r(t) \cdot \sin \theta(t) = 0.5 \cos \omega_m t$

$v(t) = r(t) \cdot \cos \omega_c t \cdot \cos \theta(t) + r(t) \cdot \sin \theta(t) \cdot \sin \omega_c t$

$= r(t) \cdot \cos [\omega_c t - \theta(t)]$

Where $r(t) = \sqrt{1 + (0.5 \cos \omega_m t)^2}$

$$\begin{aligned}
 &= [1 + 0.25 \cos^2 \omega_m t]^{1/2} \\
 &= [1 + \frac{0.25}{2}(1 + \cos 2\omega_m t)]^{1/2} \\
 &= [1.125 + 0.125 \cos 2\omega_m t]^{1/2} \\
 &\cong 1.125 + \frac{0.125}{2} \cos 2\omega_m t \\
 \therefore v(t) &= [1.125 + 0.0625 \cos 2\omega_m t] \cos[\omega_c t - \theta(t)]
 \end{aligned}$$

Hence it is both FM and AM

Ans: 'c'

04. To avoid diagonal clipping, $R_c < \frac{1}{\omega}$

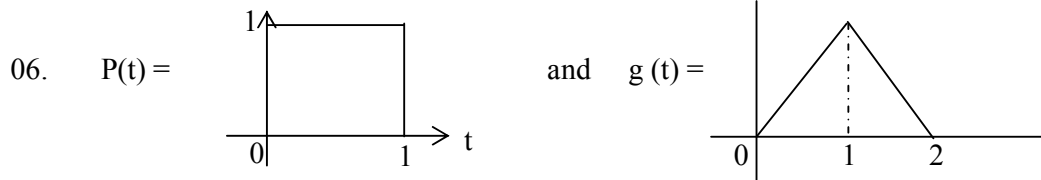
Ans: 'a'

05. The LSB – Modulated signal $f_{c_1} - f_m = 990 \text{ KHZ}$

Considering this as the Baseband signal, the B.ω of resulting FM signal is

$$2(990 \times 10^3) = 1.98 \text{ MHz} \cong 2 \text{ MHz}$$

Ans: 'b'



$$X_{AM}(t) = 100 [P(t) + 0.5 g(t)] \cos \omega_c t \text{ for } 0 \leq t \leq 1$$

By Comparing the above with an AM – DSB – FC signal under arbitrary Modulation

$$\text{i.e. } A [1 + \mu \cdot m(t)] \cos \omega_c t$$

$$\mu = 0.5 \ \& \ m(t) = g(t) \text{ is a ramp over } 0 \leq t \leq 1$$

\therefore one set of Possible values of modulating signal and Modulation Index would be

t, 0.5

Ans: 'a'

07. $X_{AM}(t) = 10 [1 + 0.5 \sin 2\pi f_m t] \cos 2\pi f_c t$

The above signal is a Tone Modulated signal.

$$\begin{aligned} \text{The AM Side band Power} &= \frac{P_c m^2}{2} \\ &= \frac{100}{2} \times \frac{(0.5)^2}{2} \\ &= 6.25 \text{ W} \end{aligned}$$

Ans: 'c'

08. Mean Noise Power is the area enclosed by noise PSD Curve, and is equal to

$$4 \left[\frac{1}{2} \times B \times \frac{N_0}{2} \right] = N_0 B$$

$$\therefore \text{The ratio of Ave. sideband Power to Mean noise Power} = \frac{6.25}{N_0 B} = \frac{25}{4N_0 B}$$

Ans: 'b'

10. $y(t) = x^2(t)$

A squaring circuit acts as a frequency doubler

$$\therefore \text{New } \delta f = 180 \text{ KHZ}$$

$$\therefore \text{B.W of o/p signal} = 2(180 + 5) = 370 \text{ KHZ}$$

Ans: 'a'

11. $(\delta\omega)_{PM} = K_f E_m W_m$, Where $K_f E_m$ is the Phase deviation.

Since, it is given that Phase deviation remains unchanged,

$$(\delta\omega)_{PM} \propto \omega_m$$

$$\Rightarrow \frac{\delta\omega_1}{\delta\omega_2} = \frac{\omega m_1}{\omega m_2}$$

$$\Rightarrow \frac{\delta f_1}{\delta f_2} = \frac{f m_1}{f m_2}$$

$$\Rightarrow \frac{10 \text{ KHZ}}{\delta\omega_2} = \frac{1 \text{ KHZ}}{2 \text{ KHZ}} \Rightarrow \delta f_2 = 20 \text{ KHZ}$$

$$\therefore \text{B.W} = 2 (\delta f_2 + f m_2)$$

$$= 2(20 + 2) \text{ KHZ} = 44 \text{ KHZ}$$

Ans: 'd'

13. Power efficiency $\eta = \frac{P_{SB}}{P_T} \times 100\%$

The sidebands are $m(t) \cdot \cos \omega_c t$

$$= \left[\frac{1}{2} \cos \omega_1 t + \frac{1}{2} \sin \omega_2 t \right] \cos \omega_c t$$

$$= \frac{1}{4} [\cos(\omega_c + \omega_1)t + \cos(\omega_c - \omega_1)t] + \frac{1}{4} [\sin(\omega_c + \omega_2)t - \sin(\omega_c - \omega_2)t]$$

$$\therefore P_{SB} = 4 \left[\frac{1}{2} (1/4)^2 \right] = 1/8$$

$$P_T = P_C + P_{SB} = \frac{1}{2} + \frac{1}{8}$$

$$\therefore \eta = \frac{1/8}{5/8} \times 100\% = 20\%$$

Ans: 'c'

14. $C_1 = B \log \left(1 + \frac{S}{N} \right) \text{ bps}$

Since $\frac{S}{N} \gg 1$

$$C_1 = B \log S/N$$

$$C_2 = B \log (2 \cdot S/N) = B \log 2 + B \log S/N$$

$$= B + C_1$$

$$\therefore C_2 = C_1 + B$$

Ans: 'b'

15. $T_c < RC < T_m \Rightarrow 1 \mu \text{ sec} < RC < 500 \mu \text{ sec}$

$$\therefore RC = 20 \mu \text{ sec}$$

Ans; 'b'

16. $v_{AM}(t) = A \cos \omega_c t + 0.1 \cos \omega_m t \cdot \cos \omega_c t$

$$= A \cos \omega_c t + 0.05 [\cos(\omega_c + \omega_m)t + \cos(\omega_c - \omega_m)t]$$

NBFM is similar to AM signal, except for a Phase reversal of 180° for LSB

$$v_{\text{NBFM}}(t) = A \cos \omega_c t + 0.05 [\cos(\omega_c + \omega_m)t - \cos(\omega_c - \omega_m)t]$$

$$\therefore v_{\text{AM}}(t) + v_{\text{NBFM}}(t) = 2A \cos \omega_c t + \cos(\omega_c + \omega_m)t$$

This is SSB with carrier.

Ans: 'b'

$$17. \text{ Noise Power} = 10^{-20} \times 100 \times 10^6 \\ = 10^{-12} \omega$$

$$\text{Loss} = 40 \text{ dB}$$

$$\Rightarrow \text{loss} = 10^4$$

$$\text{Signal Power at the receiver} = \frac{10^{-3}}{10^4} = 10^{-7} \omega$$

$$\therefore 10 \log \frac{S}{N} = 10 \log \frac{10^{-7}}{10^{-12}} = 10 \log 10^5$$

$$= 50 \text{ dB}$$

Ans: 'a'

$$18. \text{ Carrier} = \cos 2\pi (101 \times 10^6)t$$

$$\text{Modulating signal} = \cos 2\pi (10^6)t$$

$$\text{o/p of BM} = 0.5 [\cos 2\pi(101 \times 10^6)t + \cos 2\pi(99 \times 10^6)t]$$

o/p of HPF

$$= 0.5 \cos 2\pi(101 \times 10^6)t$$

o/p of Adder is

$$= 0.5 \cos 2\pi(101 \times 10^6)t + \sin 2\pi(100 \times 10^6)t$$

$$= 0.5 \cos 2\pi [(100 + 1) \times 10^6]t + \sin 2\pi(100 \times 10^6)t$$

$$= 0.5 [\cos 2\pi(100 \times 10^6)t \cdot \cos 2\pi \times 10^6 t$$

$$- \sin 2\pi (100 \times 10^6)t \cdot \sin 2\pi \times 10^6 t] + \sin 2\pi(100 \times 10^6)t$$

$$= 0.5 \cos 2\pi(100 \times 10^6)t \cdot \cos 2\pi \times 10^6 t$$

$$- \sin 2\pi (100 \times 10^6)t [1 - 0.5 \sin(2\pi \times 10^6)t]$$

$$\text{Let. } 0.5 \cos(2\pi \times 10^6)t = R(t) \cdot \sin \theta(t)$$

$$1 - 0.5 \sin(2\pi \times 10^6)t = R(t) \cdot \cos \theta(t)$$

$$\text{The envelope } R(t) = \left\{ [0.5 \cos(2\pi \times 10^6)t]^2 + [1 - 0.5 \sin(2\pi \times 10^6)t]^2 \right\}^{1/2}$$

$$= [1.25 - \sin(2\pi \times 10^6)t]^{1/2}$$

$$= \left[\frac{5}{4} - \sin(2\pi \times 10^6)t \right]^{1/2}$$

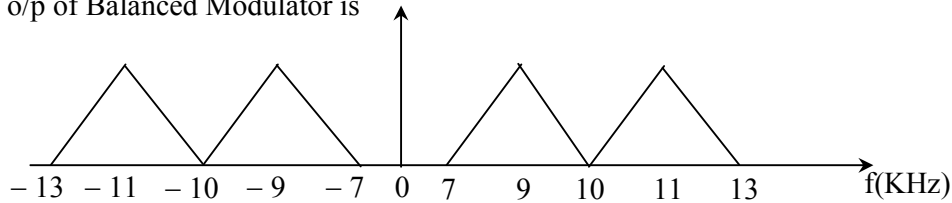
Ans: 'b'

19. A frequency detector produces a d.c voltage (constant) depending on the difference of the two i/p frequencies.

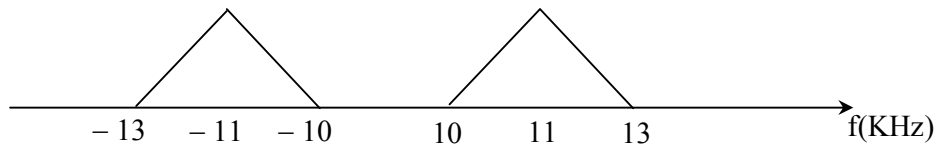
Ans: 'd'

20. Ans: 'c'

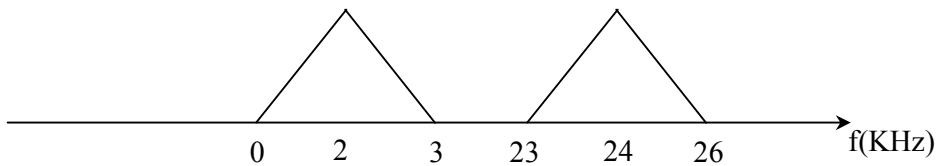
21. o/p of Balanced Modulator is



o/p of HPF is



The freq. at the o/p of 2nd BM are



∴ The +ve frequencies where Y(f) has spectral peaks are 2 KHZ & 24 KHZ

Ans: 'b'

$$\begin{aligned}
 22. \quad V_0 &= a_0 [A_c^1 \cdot \cos(2\pi f_c^1 t) + m(t)] + a_1 [A_c^1 \cos(2\pi f_c^1 t) + m(t)]^3 \\
 &= a_0 [A_c^1 \cos(2\pi f_c^1 t) + m(t)] + a_1 [(A_c^1)^3 \cos^3(2\pi f_c^1 t) + m^3(t) \\
 &\quad + 3 (A_c^1)^2 \cos^2(2\pi f_c^1 t) \cdot m(t) \\
 &\quad + 3 (A_c^1) \cdot \cos(2\pi f_c^1 t) \cdot m^2(t)]
 \end{aligned}$$

The DSB – Sc Components are

$$2 f_c^1 \pm f_m$$

These should be equal to $f_c \pm f_m$

$$\Rightarrow 2f_c^1 = f_c \Rightarrow f_c^1 = f_c/2 = 0.5 \text{ MHz}$$

Ans: 'c'

$$23. \frac{\text{Total side band Power}}{\text{carrier power}} = \frac{P_c m^2 / 2}{P_c} = \frac{m^2}{2} = \frac{1}{8}$$

Ans: 'd'

$$24. f_m = 2\text{KHZ}; f_c = 10^6 \text{ HZ}$$

$$\delta f = 3(2f_m) = 12 \text{ KHZ}$$

$$\text{Modulation index } \beta = \frac{\delta f}{f_m} = 6$$

$$v_{FM}(t) = \sum_{n=-\infty}^{\infty} A_n J_n(\beta) \cos(\omega_c + n\omega_m) t$$

$$= \sum_{n=-\infty}^{\infty} 5 J_n(6) \cos \{2\pi [1000 + n(2)] 10^3 t\}$$

∴ the coefficient of $\cos 2\pi (1008 \times 10^3)t$ is $5 J_4(6)$

Ans: 'd'

$$25. P - 6; Q - 3; R - 2; S - 4$$

Ans: 'a'

$$26. f_0 = f_s + \text{IF}$$

$$(f_0)_{\max} = (f_s)_{\max} + \text{IF} = 1650 + 450 = 2100$$

$$(f_0)_{\min} = (f_s)_{\min} + \text{IF} = 1650 - 450 = 1200$$

$$(f_0)_{\max} = \frac{1}{2\pi\sqrt{Lc_{\min}}} = 2100$$

$$(f_0)_{\min} = \frac{1}{2\pi\sqrt{Lc_{\max}}} = 1200$$

$$\therefore \sqrt{\frac{c_{\max}}{c_{\min}}} = \frac{2100}{1200} = 7/4$$

$$\Rightarrow \frac{c_{\max}}{c_{\min}} = 3$$

Image freq. = $f_s + 2 IF = 700 + 2 (450) = 1600 \text{ KHZ}$

Ans: 'c'

27. Let the i/p signal be

$$\cos\omega_c t \cdot \cos\omega_m t + n(t)$$

$$= \cos\omega_c t \cdot \cos\omega_m t + n_c(t) \cos\omega_c t - n_s(t) \cdot \sin\omega_c t$$

$$= [n_c(t) + \cos\omega_m t] \cos\omega_c t - n_s(t) \cdot \sin\omega_c t$$

When this is multiplied with local carrier, the o/p of the multiplier is

$$[n_c(t) + \cos\omega_m t] \cos^2\omega_c t - \frac{n_s(t)}{2} \cdot \sin 2\omega_c t$$

$$= [n_c(t) + \cos\omega_m t] \left[\frac{1 + \cos 2\omega_c t}{2} \right] - \frac{n_s(t)}{2} \sin 2\omega_c t$$

The o/p of Base band filter is

$$\frac{1}{2} [n_c(t) + \cos\omega_m t]$$

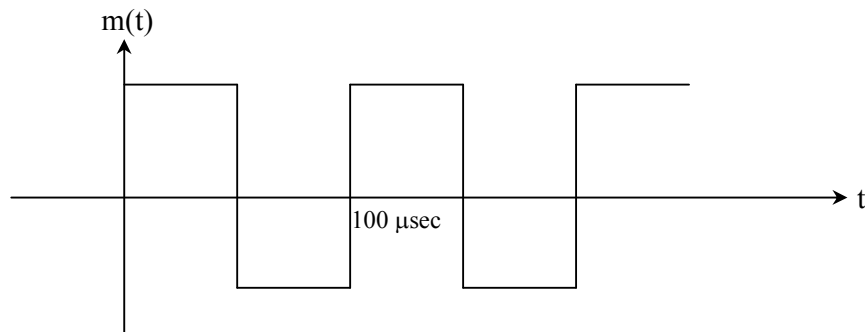
Thus, the noise at the detector o/p is $n_c(t)$ which is the inphase component.

Ans: 'a'

28. The o/p noise in an Fm detector varies parabolically with frequency.

29. Ans: 'a'

30.



$$f_m = \frac{1}{100 \times 10^6} = 10 \text{ KHZ}$$

Its Fourier series representation is

$$\frac{4}{\pi} \left[\cos 2\pi (10 \times 10^3)t - \frac{1}{3} \cos 2\pi (30 \times 10^3)t + \frac{1}{5} \cos 2\pi (50 \times 10^3)t + \dots \right]$$

The frequency components present in the o/p are $f_c \pm 10\text{KHZ} = (1000 \pm 10) \text{ KHZ}$

$$f_c \pm 30 \text{ KHZ} = (1000 \pm 30) \text{ KHZ} \text{ -----}$$

i.e. 970 KHZ, 990KHZ, 1010KHZ, 1030 KHZ -----etc.

Hence, among the frequencies given, the frequency that is not present in the modulated signal is 1020 KHZ

Ans: 'c'

31. $S(t) = \cos 2\pi (2 \times 10^6 t + 30 \sin 150 t + 40 \cos 150 t)$

$$\psi_i(t) = 2\pi (2 \times 10^6 t + 30 \sin 150 t + 40 \cos 150 t)$$

$$\therefore \text{Phase change} = 2\pi [30 \sin 150 t + 40 \cos 150 t]$$

$$\text{Let } r \cos \theta = 30 ; r \sin \theta = 40$$

$$\therefore \text{Phase Change} = 2\pi r \cos (150 t - \theta)$$

$$\text{Where } r = \sqrt{(30)^2 + (40)^2} = 50$$

$$\therefore \text{Phase change} = 100\pi \cos (150 t - \theta).$$

$$\therefore \text{Max Phase deviation} = 100\pi$$

$$\omega_i = \frac{d}{dt} \psi_i(t) = 2\pi [2 \times 10^6 + (30)(150) \cos(150t) - (40)(150) \sin 150t]$$

$$\text{Frequency change} = 2\pi [(30)(150)\cos 150t - (40)(150)\sin 150t]$$

This can be written as

$$(2\pi)(150)r \cos(150 t + \theta), \quad \text{Where } r = 50$$

$$\text{Frequency change} = (2\pi)(150)(50) \cos(150 t + \theta)$$

$$\text{Max frequency deviation } \delta\omega = 2\pi (150)(50)$$

$$\Rightarrow \delta f = (150)(50) = 7.5 \text{ KHz}$$

Ans: 'd'

32. LPF can be used as reconstruction filter.

Ans: 'd'

33. The envelope of an AM is the baseband signal. Thus, the o/p of the envelope detector is the base band signal

Ans: 'a'

34. $2(\delta f + f_m) = 10^6 \text{ HZ}$

$$\Rightarrow \delta f = 495 \text{ KHZ}$$

For $y(t)$, $\delta f = 3(495 \text{ KHZ}) = 1485 \text{ KHZ}$

and $f_c = 300 \text{ MHZ}$

\therefore B. ω of $y(t) = 2(1485 + 5) \text{ KHZ}$

$$= 2980 \text{ KHZ} = 2.9 \text{ MHZ} \cong 3 \text{ MHZ}$$

adjacent frequency components in FM signal will be separated by $f_m = 5 \text{ KHZ}$.

Ans: 'a'

35. o/p of multiplier = $m(t) \cos \omega_0 t \cdot \cos(\omega_0 t + \theta)$

$$= \frac{m(t)}{2} [\cos(2\omega_0 t + \theta) + \cos \theta]$$

$$\text{o/p of LPF} = \frac{m(t)}{2} \cdot \cos \theta$$

$$\text{Power of o/p} = \frac{\overline{m^2(t)}}{4} \cdot \cos^2 \theta$$

Since, $\overline{m^2(t)} = P_m$, the Power of output signal is $\frac{P_m \cdot \cos^2 \theta}{4}$.

Ans: 'd'

36. 'a'

37. 'a'

38. The frequency components available in $S(t)$ are $(f_c - 15) \text{ KHZ}$, $(f_c - 10) \text{ KHZ}$,
 $(f_c + 10) \text{ KHZ}$, $(f_c + 15) \text{ KHZ}$.

\therefore B. $\omega = (f_c + 15) \text{ KHZ} - (f_c - 15) \text{ KHZ}$

= 30 KHZ.

Ans: 'd'

39. Complex envelope or pre envelope is $S(t) + J \cdot S_h(t)$, Where $S(t)$ is the Hilbert Transform of $S(t)$.

Let $S(t) = e^{-at} \cdot \cos(\omega_c + \Delta\omega)t$.

$\Rightarrow S_h(t) = e^{-at} \cdot \sin(\omega_c + \Delta\omega)t$

\therefore pre envelope = $e^{-at} \cdot [\cos(\omega_c + \Delta\omega)t + J \sin(\omega_c + \Delta\omega)t]$

= $e^{-at} \cdot \exp[J(\omega_c + \Delta\omega)t]$

Ans: 'a'

40. To Provide better Image frequency rejection for a superheterodyne receiver, image frequency should be prevented from reaching the mixer, by providing more tuning circuits in between Antenna and the mixer, and increasing their selectivity against image frequency. These circuits are preselector and RF amplifier.

Ans: 'd'

41. Ans: 'a'

42. Ans: 'b'

43. New deviation is 3 times the signal. So, Modulation Index of the output signal is $3(9) = 27$

Ans: 'd'

44. Ans: 'b'

45. Ans: 'c'

46. $a - 2$; $b - 1$; $c - 5$

47. $a - 2$; $b - 1$; $c - 5$

48. $v(t) = 5 [\cos (10^6 \pi t) - \sin (10^3 \pi t) \sin 10^6 \pi t]$

$$= 5 \cos 10^6(\pi t) - \frac{5}{2} [2 \sin 10^3 \pi t \cdot \sin 10^6 \pi t]$$

$$= 5 \cos 10^6 \pi t - \frac{5}{2} [\cos(10^6 - 10^3)\pi t - \cos(10^6 + 10^3)\pi t]$$

$$= 5 \cos 10^6 \pi t + \frac{5}{2} \cos (10^6 + 10^3)\pi t - \frac{5}{2} \cos (10^6 - 10^3)\pi t.$$

It is a narrow band FM signal, where the phase of LSB is 180° out of phase with that of AM.

Ans: d

49. $B.\omega = 2(50 + 0.5) \text{ KHZ} = 101 \text{ KHZ}$

50. $a - 3$; $b - 1$; $c - 2$

51. The given signal is AM – DSB – FC, which will be demodulated by envelope detector.

Ans: 'a'

52. Image frequency = $f_s + 2 \text{ IF}$

$$= 1200 \text{ KHZ} + 2(455) = 2110 \text{ KHZ}$$

53. Power efficiency = $\frac{P_{\text{useful}}}{P_T} \times 100 \%$

$$= \frac{m^2}{2+m^2} \times 100\%$$

For $m = 1$, the Power efficiency is max. and is 33.3 %

54. Picture → AM – VSB

Speech → FM

Ans: 'c'

55. For the generated DSB – Sc signal,

Lower frequency Limit $f_L = (4000 - 2) \text{ MHZ}$

$$= 3998 \text{ MHZ}$$

and Upper frequency Limit $f_H = (4000 + 2) \text{ MHZ}$

$$= 4002 \text{ MHZ.}$$

$$(f_s)_{\text{min}} = 2 f_H = 8.004 \text{ GHZ}$$

Ans: 'd'

56. Ans: 'a'

57. $m_f = \frac{\delta f}{f_m}$ where $\delta f = \frac{K_f E_m}{2\pi}$

$$\therefore \delta f = \frac{10 \times 10^3 \times 2}{2\pi} = \frac{10 \times 10^3}{\pi}$$

$$\omega_m = 10^4 \times \pi \rightarrow f_m = \frac{10^4}{2}$$

$$\therefore m_f = \frac{2}{\pi}$$

Ans: 'd'

58.

$$\boxed{\begin{array}{l} T_e = 21^0 \text{ K} \\ g_1 = 13 \text{ db} \end{array}} \quad \frac{\text{Loss} = 3 \text{ db}}{\quad} \quad T_0 = 300^0 \text{ K}$$

$$\begin{aligned} \text{Noise fig. of amp. } F_1 &= 1 + \frac{T_e}{T_0} \\ &= 1 + \frac{21}{300} \\ &= 1.07 \end{aligned}$$

For a Lossy Network, Noise Figure is same as its loss. $\therefore f_2 = 3 \text{ db} \Rightarrow f_2 = 1.995$

$$\therefore \text{Overall Noise figure } f = f_1 + \frac{f_2 - 1}{g_1}$$

$$g_1 = 13 \text{ db} \Rightarrow g_1 = 19.95$$

$$\therefore f = 1.07 + \frac{1.995 - 1}{19.95} = 1.1198$$

$$\Rightarrow f = 0.49 \text{ db}$$

$$\begin{aligned} T_e \text{ of cable} &= (f - 1) T_0 \\ &= (1.995 - 1) 300 = 298.5^0 \text{ K} \end{aligned}$$

$$\text{Overall } T_e = T_{e_1} + \frac{T_{e_2}}{g_1}$$

$$= 21 + \frac{298.5}{19.95}$$

$$= 35.96^0 \text{ K}$$

Ans: 'c'

60. A preamplifier is of very large gain. This will improve the noise figure (i.e. reduces its numerical value) of the receiver, if placed on the antenna side

Ans: 'a'

61. Ans: 'a'

Chapter – 4

01. A source transmitting 'n' messages will have its maximum entropy, if all the messages are equiprobable and the maximum entropy is $\log n$ bits/message.
Thus, Entropy increases as $\log n$.
Ans: 'a'
02. This corresponds to Binomial distribution. Let the success be that the transmitted bit will be received in error.

$$P(X = \text{error}) = P(\text{getting zero no. of ones}) + P(\text{getting one of ones})$$

$$= P(X = 0) + P(X = 1)$$

$$= {}^3C_0 (1-p)^0 p^3 + {}^3C_1 (1-p)p^2$$

$$= p^3 + 3p^2(1-p)$$
 Ans: 'a'
03. Most efficient source encoding is Huffman encoding.

0.5	0	0.5	0
0.25	10	0.5	1
0.25	11		

$$\bar{L} = 1 \times 0.5 + 2 \times 0.25 + 2 \times 0.25$$

$$= 1.5 \text{ bits/symbol}$$
 Ave. bit rate = $1.5 \times 3000 = 4500$ bits/sec
 Ans: 'b'
04. Considering all the intensity levels are equiprobable, entropy of each pixel = $\log_2 64$

$$= 6 \text{ bits/pixel}$$
 There are $625 \times 400 \times 400 = 100 \times 10^6$ pixels/sec

$$\therefore \text{Data rate} = 6 \times 100 \times 10^6 \text{ bps}$$

$$= 600 \text{ Mbps}$$
 Ans: 'c'
05. Source coding is a way of transmitting information with less number of bits without information loss. This results in conservation of transmitted power.
 Ans: 'c'
06. Entropy of the given source is

$$H(x) = -0.8 \log 0.8 - 0.2 \log 0.2$$

$$= 0.722 \text{ bits/symbol}$$
 4th order extension of the source will have an entropy of $4.H(x) = 2.888$ bits/4 symbol
 As per shanon's Theoram,

$$H(x) \leq L \leq H(x) + 1$$
 i.e., $2.888 \leq L \leq 3.888$ bits/4 messges

07. $12 \times 512 \times \log_2^8 = 18432 \text{ bits}$

08. Code efficiency $= \eta = \frac{L_{\min}}{L} \times 100\% = \frac{H}{L} \times 100\%$

$\bar{L} = 2 \text{ bits/symbol}$ and the entropy of the source is

$$H = -\frac{1}{2} \log \frac{1}{2} - \frac{1}{4} \log \frac{1}{4} - \frac{2}{8} \log \frac{1}{8}$$

$$= \frac{14}{8} \text{ bits/symbol}$$

$$\therefore \eta = \frac{14}{16} \times 100\% = 87.5\%$$

Ans : 'b'

09. $H(X) = -\frac{1}{2} \log \frac{1}{2} - \frac{1}{4} \log \frac{1}{4} - \frac{2}{8} \log \frac{1}{8}$
 $= 1.75 \text{ bits/symbol}$

10. Channel Capacity $C = B \log_2 \left(1 + \frac{S}{\eta B} \right)$

$$\frac{S}{\eta B} = 30 \text{ db} \rightarrow \frac{S}{\eta B} = 1000$$

$$\therefore C = 3 \times 10^3 \log_2 (1 + 1000) = 29904.6 \text{ bits/sec}$$

For errorless transmission, information rate of source $R < C$. Since, 32 symbols are there the number of bits required for encoding each $= \log_2 32$

$$= 5 \text{ bits}$$

$\rightarrow 29904.6 \text{ bits/sec}$ constitute 5980 symbols/sec. So, Maximum amount of

information should be transmitted through the channel, satisfying the constraint $R < C$

$$\rightarrow R = 5000 \text{ symbols/sec}$$

Ans: 'c'

11. Not included in the syllabus

12. $H(x) = \log_2 16 = 4 \text{ bits}$

Ans: 'd'

13. $P(0/1) = 0.5 \rightarrow P(0/0) = 0.5$
 $P(1/0) = 0.5 \rightarrow P(1/1) = 0.5$

$$P(Y/X) = \begin{bmatrix} 1/2 & 1/2 \\ 1/2 & 1/2 \end{bmatrix}$$

A channel with such noise matrix is called the channel with independent input and o/p. Such a channel conveys no information.

\therefore its capacity = 0

Ans: 'd'

14. A ternary source will have a maximum entropy of $\log_2 3 = 1.58$ bits/message. The entropy is maximum if all the messages are equiprobable i.e. $1/3$

Ans: 'a'

15. Ans: 'b'

16. Entropy coding – McMillan's rule
Channel capacity – Shannon's Law
Minimum length code – Shannon Fano
Equivocation – Redundancy

Ans: 'c'

17. Since $\frac{S}{N} \ll 1$
 $C \approx B \log 1 \approx 0$
 \therefore C is nearly 0 bps

Ans: 'd'

18. Ans: 'b'

19. Ave. information = $\log_2 26 = 4.7$ bits/symbol

Ans: 'd'

20. Ans: 'd'

21. Ans: 'b'

22. Ans: 'b'

23. $H_1 = \log_2 4 = 2$ bits/symbol

$$H_2 = \log_2 6 = 2.5 \text{ bits/symbol}$$

$$H_1 < H_2 \quad \text{Ans: 'a'}$$

24. The maximum entropy of binary source is 1 bit/message.
The maximum entropy of a quaternary source is 2 bits/message.
The maximum entropy of an octal source is 3 bits/message.
Since the existing entropy is 2.7 b/symbol the given source can be an octal source
Ans: 'c'

Chapter – 5A

Set A

01. $(f_s)_{\min} = 4 \text{ KHz}$
 $\rightarrow (T_s)_{\max} = \frac{1}{(f_s)_{\min}} = \frac{1}{4 \text{ KHz}} = 250 \mu\text{sec}$
 Ans: 'c'

Set B

05. In PCM, $(B.W)_{\min} = \frac{\gamma f_s}{2} \text{ Hz}$
 If $Q = 4 \Rightarrow \gamma = 2$
 $\therefore (B.W)_{\min} = f_s \text{ Hz.}$
 If $Q = 64 \rightarrow \gamma = 6$
 $\therefore (B.W)_{\min} = 3f_s$
 Ans: 'a'

18. $(f_s)_{\min} = 8 \text{ KHz}; \gamma = \log_2 128 = 7$
 $B.W = \frac{\gamma f_s}{2} = 28 \text{ KHz}$
 Ans: 'd'

Set – C

01. Maximum slope = $S f_s = \frac{75 \times 10^{-3}}{1.5 \times 10^{-3}} = 50 \text{ V/sec}$

Ans: 'a'

02. $\frac{d}{dt} m(t) = \frac{d}{dt} (at) = a$

Rate of rise of the modulator = $\delta \cdot f_s = \delta / T_s$

Slope over loading will occur if $\delta f_s < a \Rightarrow \frac{\delta}{T_s} < a \Rightarrow \delta < a T_s$

Ans: 'c'

03. Ans: 'c'

04. Since with increasing 'n' (increased number of Q levels), N_q reduces, S/N_q increases.
 For every 1 bit increase in 'n'. N_q
 S/N_q improves by a factor of 4.

Ans: 'd'

05. o/p bit rate = γf_s , where $\gamma = \log_2 258 = 8$
 $\therefore \gamma f_s = 64 \text{ kbps}$
 Ans: 'c'

- 06.

07. Ans: 'c'

08. $(Q. E)_{\max} = S/2 = \frac{V_H - V_L}{2Q}$
 $= \frac{1}{264}$ of the total peak to peak range

Ans: 'c'

09. Ans: 'b'

10. For every one bit increase in the data word length, S/N_q improves by a 6 db.
 \therefore The total increase is 21 db

Ans: 'b'

11. Number of samples from the multiplexing system $= 4 \times 2 \times 4 \text{ KHz}$
 $= 32 \text{ KHz}$

Each sample is encoded into $\log_2 256 = 8$ bits

So, the bit transmission rate

$$= 32 \times 8 \text{ kbps} = 256 \text{ kbps}$$

Ans: 'c'

12. $f_s = 10 \text{ KHz}$; $\gamma = \log_2 64 = 6$
 Transmission Rate = 60 kbps

Ans: 'a'

13. $V_{p-p} = 2 \text{ V}$; $\gamma = 8 \Rightarrow Q = 256$
 $S/N_q = (1.76 + 20 \log_{10} \frac{Q}{10}) \text{ db}$
 $= 49.9 \text{ db}$

Ans: 'b'

14. $(f_s)_{\text{Multiplexed system}} = 200 + 400 + 800 + 200$
 $= 1600 \text{ Hz}$

Ans: 'a'

15. Each sample is represented by $7 + 1 = 8$ bits.

$$\text{Total bit rate} = 8 \times 20 \times 8000$$

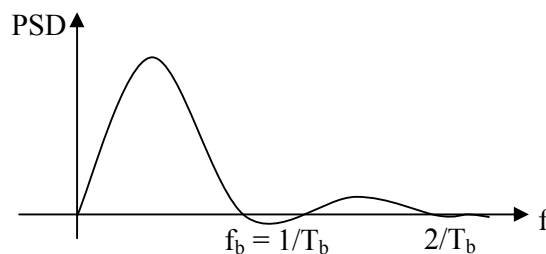
$$= 1280 \text{ kbps}$$

Ans: 'b'

16. 'a' (Question number 5 in set B)

Set – D

01. The power spectrum of Bipolar pulses is



$$(B.W)_{\min} \text{ required} = f_b$$

$$\text{Here } \gamma = 8; \quad f_s = 8 \text{ KHz}$$

$$\therefore \text{Bit rate} = 64 \text{ kbps}$$

$$\therefore (B.W)_{\min} = 64 \text{ KHz}$$

Ans: 'a'

$$02. \quad \text{Signal power} = \int_{-5}^5 x^2 f(x).dx$$

$$f(x) = \frac{1}{10} \quad -5 \leq x \leq 5$$

$$= 0 \quad \text{elsewhere}$$

$$\therefore \text{Signal Power} = 25/3 \text{ watts.}$$

$$\text{Quantization Noise Power } N_q = \frac{s^2}{12}$$

$$\text{Step size} = \frac{V_{P-P}}{Q} = \frac{10}{2^8} = \frac{10}{256} = 0.039 \text{ V}$$

$$\therefore N_q = \frac{(\text{Stepsize})^2}{12} = 0.126 \text{ mW}$$

$$10 \log \frac{S}{N_q} = 48 \text{ db}$$

Ans: 'c'

03. For every one bit increase in the data word length, N_q reduces by a factor of H.

$$\text{Given } \gamma = 8 \Rightarrow \text{Required } \gamma = 9$$

$$\Rightarrow \text{Number of Q - levels} = 2^9 = 512$$

Ans: 'b'

04. Ans: 'd'

05. Since, entropy of the o/p of the quantizer is to be maximized, it implies that all the decision boundaries are equiprobable.

$$\therefore \int_{-5}^{-1} f(x).dx = \frac{1}{3}$$

$$\Rightarrow \int_{-5}^{-1} b . dx = \frac{1}{3} \Rightarrow b = \frac{1}{12}$$

Similarly $\int_{-1}^1 a \cdot dx = \frac{1}{3} \Rightarrow a = \frac{1}{6}$

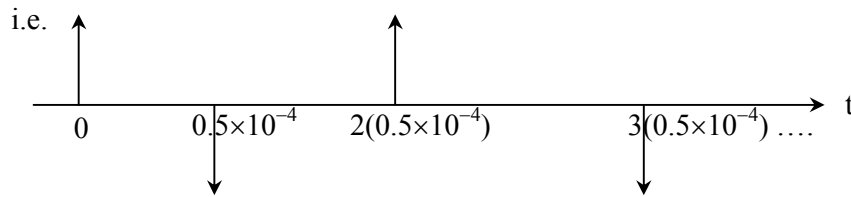
Ans: 'a'

06. Reconstruction levels are $-3V, 0V$ and $3V$.

Step size = $3V \Rightarrow N_q = \frac{9}{12} = \frac{3}{4}$

Signal Power = $2 \cdot \int_{-5}^{-1} x^2 \left(\frac{1}{12}\right) dx + \int_{-1}^1 x^2 \left(\frac{1}{6}\right) dx$
 $= \frac{1}{6} \left[\left[\frac{x^3}{3} \right]_{-5}^{-1} + \left[\frac{x^3}{3} \right]_{-1}^1 \right]$
 $= \frac{1}{6} \left[\frac{124}{3} + \frac{2}{3} \right] = \frac{126}{18} = \frac{21}{3}$
 $\therefore \frac{S}{N_q} = \frac{21}{3} \times \frac{4}{3} = \frac{28}{9}$

07. $g(t)$ is Periodic with period of 10^{-4} sec



In its Fourier series representation, $a_0 = 0$.

The remaining frequency components will be $f_s = 10$ KHZ; $2f_s = 20$ KHZ;

$3f_s = 30$ KHZetc.

\therefore The frequency components in the sampled signal are 10 KHZ ± 500 Hz; 20 KHZ ± 500 Hzetc.

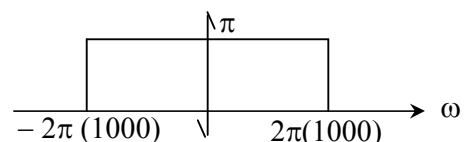
When the sampled signal is passed through an ideal LPF with Band width of 1 KHZ, The o/p of the LPF will be zero.

Ans: 'c'

08. $x(t) = x_1(t) + x_2(t)$

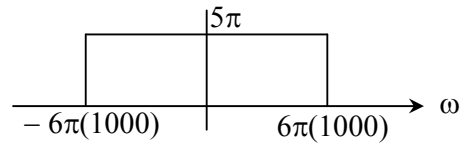
Since $\frac{\sin at}{\pi t} \xrightarrow{F.T} \pi \cdot G_{2a}(\omega)$

$\frac{\sin 2\pi 1000t}{\pi t} \xrightarrow{F.T}$



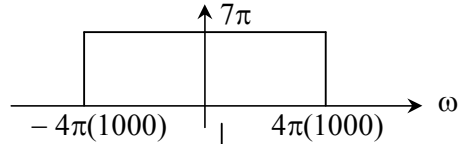
$$\Rightarrow x_1(t) = 5 \left(\frac{\sin 2\pi 1000t}{\pi t} \right)^3$$

← F.T



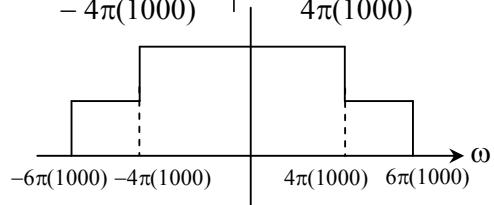
$$x_2(t) = 7 \left(\frac{\sin 2\pi 1000t}{\pi t} \right)^2$$

← F.T



Thus, $x_1(t) + x_2(t)$

← F.T



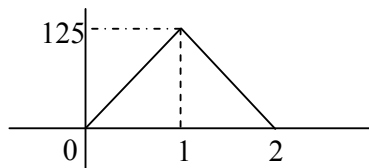
$$\therefore \omega_m = 6\pi(1000) \Rightarrow f_m = 3 \text{ KHz}$$

$$\therefore (f_s)_{\min} = 6 \text{ KHz}$$

Ans: 'c'

09.

$x(t) =$



To Track the signal, rate of rise of Delta Modulator and of the signal should be same,

i.e. $Sf_s = 125$

$$\Rightarrow S = \frac{125}{32 \times 10^3} = 0.0039 \text{ V}$$

$$= 2^{-8} \text{ V}$$

Ans: 'b'

10. In the process of Quantization, the quantizer is able to avoid the effect of all channel noise Magnitudes less than or equal to $S/2$.

If the channel noise Magnitude exceeds $S/2$, there may be an error in the output of the quantizer.

On the given Problem for $y_1(t) + c$ to be different from $y_2(t)$, the minimum value of c

to be added is half of the step size, i.e. $\frac{\Delta}{2}$

Ans: 'b'

11. $\int_{-a}^{+a} P(x) dx = \frac{1}{3} \Rightarrow \int_{-a}^{+a} \frac{1}{4} dx = \frac{1}{3}$

$\Rightarrow a = \frac{2}{3}$ Ans: 'b'

$$\begin{aligned} 12. \quad \int_{-a}^a x^2 f(x) \cdot dx &= \frac{1}{4} \left[\frac{x^3}{3} \right]^{2/3} \\ &= \frac{1}{12} \left[\frac{2 \times 8}{27} \right]^{-2/3} = \frac{4}{81} \end{aligned}$$

Ans: 'a'

$$13. \quad \text{signal Power} = \int_{-5}^5 x^2 \cdot f(x) dx$$

$$\begin{aligned} f(x) &= \frac{1}{10} \text{ for } -5 \leq x \leq +5 \\ &= 0 \text{ elsewhere} \end{aligned}$$

$$\therefore \text{ signal power} = \frac{25}{3} \text{ volts}^2$$

$$\frac{S}{N_q} = 43.5 \text{ db} \Rightarrow \frac{S}{N_q} = 22387.2$$

$$\Rightarrow N_q = 3.722 \times 10^{-4} = \frac{(\text{stepsize})^2}{12}$$

$$\Rightarrow \text{step size} = 0.0668 \text{ V}$$

Ans: 'c'

$$14. \quad \text{Total } N_q = \frac{(0.05)^2}{12} + \frac{(0.1)^2}{12} = 1.041 \times 10^{-3}$$

$$\therefore \frac{S}{N_q} = 40 \text{ db}$$

Ans: 'd'

15. for every one bit increase in data word length, S/N_q improves by a factor of 4. Hence, for two bits increase, the improvement factor is 16.

Ans: 'c'

16. Between two adjacent sampling instances, if the base band signal changes by an amount less than the step size, i.e. if the variations are very less magnitude, the o/p of the Delta Modulator consists of a sequence of alternate +ve and -ve Pulses.

Ans: 'a'

$$17. \quad f(x) = 1 \text{ for } 0 \leq x \leq 1$$

$$= 0 \text{ elsewhere}$$

M.S. value of Quantization Noise

$$\begin{aligned}
 &= \int_0^{0.3} x^2 \cdot f(x) \cdot dx + \int_{0.3}^1 (x-0.7)^2 f(x) dx \\
 &= 0.039 \text{ volts}^2
 \end{aligned}$$

$$\therefore \text{rms value} = 0.198 \text{ Volts}$$

18. FM – Capture effect
 DM – Slope overload
 PSK – Matched filter
 PCM – μ -Law
 Ans: 'c'

19. Step size = $\frac{V_{P-P}}{\text{no. of } Q \text{ levels}} = \frac{1.536}{128} = 0.012 \text{ V}$

$$N_q = \frac{S^2}{12} = 12 \times 10^{-6} \text{ Volts}^2$$

Ans: 'c'

20. slope overload occurs if $S f_s < 2\pi f_m \cdot E_m$
 $S f_s = 25120 < 2\pi (4 \times 10^3) (1.5) = 37699.11$

Ans: 'b'

21. $R = \gamma f_s = 8 \times 8 \text{ KHz} = 64 \text{ Kbps}$
- $$\frac{S}{N_q} = 1.76 + 20 \log Q \text{ (db)} = 49.8 \text{ db}$$

Ans: 'b'

22. Let $S(t) = 5 \times 10^{-6} \sum_n \delta(t - nT_s)$ & $T_s = 100 \mu\text{sec} = 10^{-4} \text{ sec}$

The Fourier series representation of $S(t)$ is

$$\begin{aligned}
 \therefore S(t) &= 5 \times 10^{-6} \left[\frac{1}{T_s} + \frac{2}{T_s} \sum_{n=-\infty}^{\infty} \cos 2\pi n f_s t \right] \\
 &= 5 \times 10^{-2} + 10^{-1} \sum_{n=-\infty}^{\infty} [\cos 2\pi (n \times 10 \times 10^3) t]
 \end{aligned}$$

$$\therefore y(t) = S(t) \cdot x(t)$$

$$= S(t) \cdot 10 \cos 2\pi (4 \times 10^3) t$$

$$= 5 \times 10^{-1} \cos 2\pi (4 \times 10^3) t + \sum_{n=-\infty}^{\infty} \cos 2\pi (n \times 10^4) t \cdot \cos 2\pi (4 \times 10^3) t$$

$$\therefore \text{The o/p of ideal LPF} = 5 \times 10^{-1} \cos (8\pi \times 10^3) t$$

Ans: 'c'

23. $x(t) = 100 \cos 2\pi (12 \times 10^3) t$

$$T_s = 50 \mu\text{sec} \Rightarrow f_s = 20 \text{ KHz}$$

The frequency components available in the sampled signal are
12 KHZ, (20 ± 12) KHZ, (40 ± 12) KHZetc.

The o/p of the ideal LPF are 8 KHZ and 12 KHZ.

Ans: 'd'

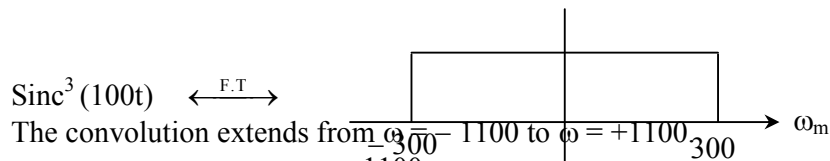
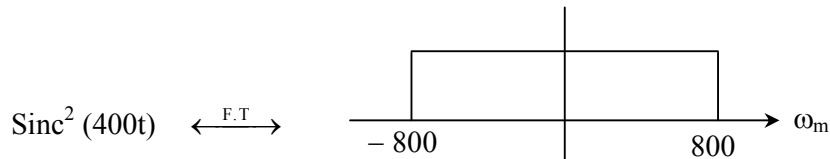
$$\begin{aligned} 24. \quad x(t) &= \text{sinc}(700t) + \text{sinc}(500t) \\ &= \frac{\sin(700t)}{700t} + \frac{\sin(500t)}{500t} \\ &= \frac{\pi}{700} \left[\frac{\sin(700t)}{\pi t} \right] + \frac{\pi}{500} \left[\frac{\sin(500t)}{\pi t} \right] \end{aligned}$$

The band limiting frequency of above x(t) is $\omega_m = 700 \Rightarrow f_m = 350/\pi$

$$\Rightarrow (f_s)_{\min} = \frac{700}{\pi} \text{ Hz}$$

$$\therefore (T_s)_{\max} = \pi/700 \text{ sec}$$

$$25. \quad x(t) = 6 \times 10^{-4} \text{sinc}^2(400t) + 10^6 \text{sinc}^3(100t)$$



The convolution extends from $\omega = -1100$ to $\omega = +1100$

$$\therefore \omega_m = 1100 \Rightarrow f_m = \frac{1100}{2\pi} = 175 \text{ Hz}$$

$$(f_s)_{\min} = 350 \text{ Hz}$$

$$26. \quad \text{step size} = \frac{2}{28} = 0.0078 \text{ Volts}$$

$$N_q = \frac{S^2}{12} = 5.08 \mu \text{ volts}^2$$

$$\text{Signal Power} = \frac{(0.5)^2}{2} = 0.125 \text{ Volts}^2$$

$$10 \log \frac{S}{N_q} = 44 \text{ db}$$

27. For every one bit increase in the data word length, quantization noise power reduces by a factor of 4.

Ans: 'c'

28. Flat Top sampling is observing the baseband signal through a finite time aperture. This results in Aperture effect distortion.
Ans: 'a'
29. In compression the baseband signal is subjected to a non linear Transformation, whose slope reduces at higher amplitude levels of the baseband signal.
Ans: 'a'
30. Most of the signal strength will be available in the Major lobe. Hence,
 $(f_s)_{\min} = 2(1 \text{ KHZ}) = 2 \text{ KHZ}$
Ans: 'b'
31. Irrespective of the value of η , for every one bit increase in Data word length, S/N_q improves by a factor of 4.
Ans: 'd'
32. $10 \log 4 = 6 \text{ db}$
Ans: 'b'
33. The frequency components available in the sampled signal are 1 KHZ, $(1.8 \pm 1) \text{ KHZ}$, $(3.6 \pm 1) \text{ KHZ}$ etc.
The o/p of the filter are 800 Hz and 1000 Hz.
Ans: 'c'
34. Ans: 'c'
35. Ans: a – 2, b – 1, c – 5.
36. Ans: a – 2, b – 1, c – 4.
37. If pulse width increases, the spectrum of the sampled signal becomes zero even before f_m .
Ans: 'a'
38. $(B.\omega)_{\min} = \frac{\gamma f_s}{2}$
 $Q = 4 \Rightarrow \gamma = 2$
 $Q = 64 \Rightarrow \gamma = 6$
 $\Rightarrow B.\omega$ increases by a factor of 3.
39. $(B.\omega)_{\min} = (3\omega + \omega + 2\omega + 3\omega + 2\omega) \text{ Hz}$
 $= 11 \omega \text{ Hz}$

40. The given signal is a band pass signal. $(f_s)_{\min} = \frac{2 f_H}{N}$, where $N = \frac{f_H}{3}$

$$N = \frac{1.8 \times 10^3}{1500} = \frac{1800}{1500} = 1.2$$

$$\Rightarrow N = 1$$

$$\therefore (f_s)_{\min} = 2 f_H = 3600 \text{ Hz}$$

41. LSB = (4000 - 2) MHz = 3998 MHz
 USB = (4000 + 2) MHz = 4002 MHz

$$N = \frac{f_H}{B} = \frac{4002}{4} = 1000.5$$

$$\Rightarrow N = 1000$$

$$(f_s)_{\min} = \frac{2 f_H}{N} = \frac{2 \times 4002}{1000} \text{ MHz} = 8.004 \text{ MHz}$$

42. $P_e = \frac{1}{2} \operatorname{erfc} \left[\frac{E_s}{\eta} \cdot \cos^2 \phi \right]^{1/2}$

\therefore The factor is $\cos^2 20$

Ans: 'b'

43. N_q depends on step size, which in turn depends on No. of Q-levels.

Ans: 'c'

44. $(f_s)_{\min}$ to reconstruct 3 KHz part = 6 KHz

$(f_s)_{\min}$ to reconstruct 6 KHz part = 12 KHz

The frequencies available in sampled signal are 3 KHz, 6 KHz, (8 ± 3) KHz, (8 ± 6) KHz, (16 ± 3) KHz, (16 ± 6) KHz etc.

The o/p of LPF are 3 KHz, 6 KHz, 5 KHz and 2 KHz.

Ans: 'd'

45. Ans: 'c'

Chapter – 5 B & C

01. Required Probability

$$= P(\text{No bit is 1 i.e. zero No. of 1's}) + P(\text{one bit is 1})$$

$$= {}^3C_0 \cdot (P)^3 \cdot (1 - P)^{3-3} + {}^3C_1 \cdot P^2 (1 - P)^{3-2}$$

$$= P^3 + 3P^2(1 - P)$$

Ans: 'a'

02. The given raised cosine pulse will be defined only for $0 \leq |f| \leq 2\omega$. Thus, at $t = 1/4\omega$,
 i.e. $f = 4\omega$, $P(t) = 0$.

Ans: b

03. Required probability = $P(X = 0) + P(X = 1)$
 $= n_{C_0} (P)^0 (1-P)^{n-0} + n_{C_1} P(1-P)^{n-1}$
 $= (1-P)^n + nP(1-P)^{n-1}$

Ans: c

04. Constellation – 1:

$S_1(t) = 0;$ $S_2(t) = -\sqrt{2} a \phi_1 + \sqrt{2} a \phi_2$
 $S_3(t) = -2\sqrt{2} a \phi_1;$ $S_4(t) = -\sqrt{2} a \phi_1 - \sqrt{2} a \phi_2$
 Energy of $S_1(t) = E_1 = 0$
 Energy of $S_2(t) = E_2 = 4a^2$
 Energy of $S_3(t) = E_3 = 8a^2$
 Energy of $S_4(t) = E_4 = 4a^2$

Avg. Energy of Constellation 1

$$E_{C_1} = \frac{E_1 + E_2 + E_3 + E_4}{4} = 4a^2$$

Constellation – 2:

$S_1(t) = a \phi_1 \Rightarrow E_1 = a^2$
 $S_2(t) = a \phi_2 \Rightarrow E_2 = a^2$
 $S_3(t) = -a \phi_1 \Rightarrow E_3 = a^2$
 $S_4(t) = -a \phi_2 \Rightarrow E_4 = a^2$

$$E_{C_2} = a^2$$

$$\frac{E_{C_1}}{E_{C_2}} = 4$$

Ans: b

05. Constellation – 1

Distance $d_{S_1S_2} = 2a$; $d_{S_1S_3} = 2\sqrt{2} a$; $d_{S_1S_4} = 2a$; $d_{S_2S_3} = 2a$; $d_{S_2S_4} = 2\sqrt{2} a$; $d_{S_3S_4} = 2a$
 $\therefore (d_{\min})_{C_1} = 2a$

Constellation – 2

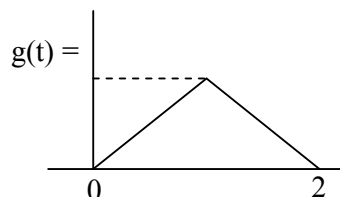
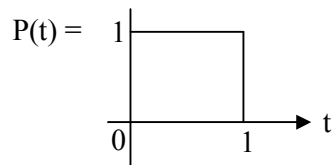
$d_{S_1S_2} = \sqrt{2} a$; $d_{S_1S_3} = 2a$; $d_{S_1S_4} = \sqrt{2} a$; $d_{S_2S_3} = \sqrt{2} a$; $d_{S_2S_4} = 2a$; $d_{S_3S_4} = \sqrt{2} a$;
 $(d_{\min})_{C_2} = \sqrt{2} a$

Since $(d_{\min})_{C_2} = (d_{\min})_{C_1}$,

Probability of symbol error in Constellation – 2 (C_2) is more than that of constellation – 1 (C_1).

Ans: a

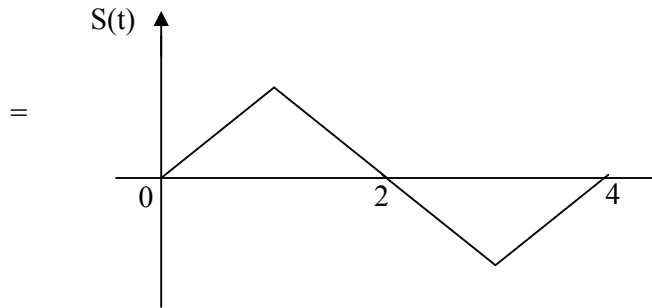
06.



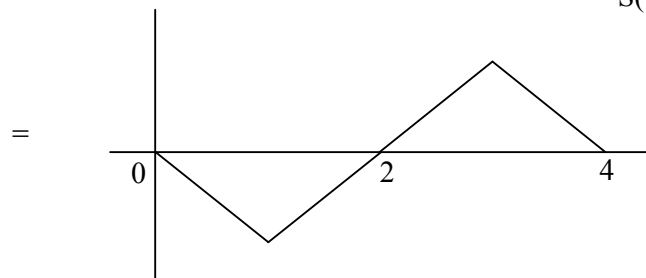
$$S(t) = g(t) - \delta(t - 2) * g(t)$$

We have $\delta(t - 2) * g(t) = g(t - 2)$

$$S(t) = g(t) - g(t - 2)$$



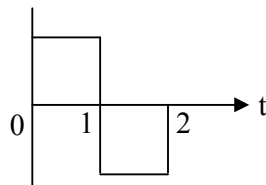
The impulse response of corresponding Matched filter is $h(t) = S(-t + 4)$
 $= -S(t)$



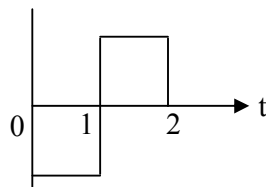
Ans: c

07. Since $P(t) = 1$ for $0 \leq t \leq 1$, and $g(t) = t$ for $0 \leq t \leq 1$, the given $x_{AM}(t) = 100[1 + 0.5t] \cos\omega_c t$
 Ans: a

08. Output of the matched filter is the convolution of its impulse response and its input.
 The given input $S(t) =$



The corresponding impulse response is $h(t) =$

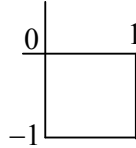


The response should extend from $t = 0$ to $t = 4$.

$$\text{Response} = \int_{-\infty}^{\infty} s(\tau) h(t - \tau) d\tau$$

Let $t = 1$

$$S(\tau) h(-\tau + 1) =$$



\therefore The response at $t = 1$ is -1

Ans: 'c'

09. Let z be the received signal.

$$P(z/0) = \begin{cases} \frac{1}{0.5} & \text{for } -0.25 \leq z \leq 0.25 \\ 0 & \text{elsewhere} \end{cases}$$

$$P(1/0) = \int_{-0.25}^{0.25} \left(\frac{1}{0.5} \right) dz$$

$$= 0.1$$

$$P(z/1) = \begin{cases} 1 & \text{for } 0 \leq z \leq 1 \\ 0 & \text{elsewhere} \end{cases}$$

$$P(0/1) = \int_0^{0.2} dz = 0.2$$

$$\text{Ave. bit error prob.} = \frac{0.1 + 0.2}{2} = 0.15$$

Ans: 'a'

10. Ans: 'c'

$$11. (B.W)_{\text{BPSK}} = 2f_b = 20 \text{ KHz}$$

$$(B.W)_{\text{QPSK}} = f_b = 10 \text{ KHz}$$

Ans: 'c'

$$12. \frac{S_0}{N_0} = \frac{2E_b}{N_0} = \frac{2 \times 10^6}{10^5} = 20$$

$$10 \log 20 = 13 \text{ db}$$

Ans: 'd'

$$13. \text{B.W efficiency} = \frac{\text{data rate}}{(B.W)_{\text{min}}}$$

For BPSK, $(B.W)_{\text{min}}$ required is same as data rate.

\therefore B.W efficiency for BPSK = 1

Since, coherent detection is used for BPSK, Carrier synchronization is required.

Ans: 'b'

$$14. (P_e)_{\text{PSK}} = \frac{1}{2} \operatorname{erfc} \left[\frac{A^2 T}{2\eta} \right]^{1/2}$$

$$(P_e)_{\text{FSK}} = \frac{1}{2} \operatorname{erfc} \left[0.6 \frac{A^2 T}{2\eta} \right]^{1/2}$$

$$10 \log 0.6 = -2.2 \text{ db} = -2 \text{ db}$$

Ans: 'c'

15. $f_H = nf_b$ & $f_L = mf_b$, where n and m are integers such that $n > m$.

Ans: 'd'

16. Ans: 'd'

17. $f_H = 25 \text{ KHz}$ & $f_L = 10 \text{ KHz}$

$$\Rightarrow f_c + \frac{\Omega}{2\pi} = 25 \text{ KHz}$$

$$f_c - \frac{\Omega}{2\pi} = 10 \text{ KHz}$$

$$\Rightarrow \frac{\Omega}{\pi} = 15 \text{ KHz}$$

$$\Rightarrow \Omega = 15 \pi (10^3)$$

For FSK signals to be orthogonal,

$$2\Omega T_b = n\pi \Rightarrow 2(15 \times \pi \times 10^3) T_b = n\pi$$

$\rightarrow 30 \times 10^3 \times T_b$ should be an integer. This is satisfied for $T_b = 280 \mu \text{ sec}$

Ans: 'd'

18. Ans: 'c'

19. In PSK, the signaling format is NRZ and in ASK, it is ON-OFF signaling. Both representations are having same PSD plot.

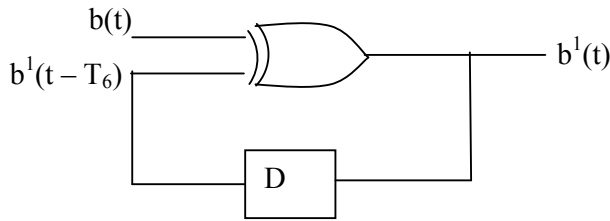
Ans: 'c'

20. Ans: 'd'

21. Ans: 'b'

22. Ans: a - 3; b - 1; c - 2

23.



$b(t)$		0	1	0	0	1
$b^1(t)$	1	1	0	0	0	1
Phase		0	π	π	π	0

Ans: 'c'

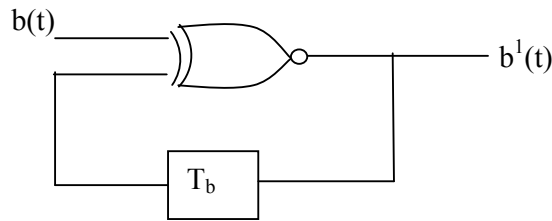
24. a

25. c

26. QPSK

27. a

28.



$b(t)$		1	1	0	0	1	1
$b^1(t)$	1	1	1	0	1	1	1

since the phase of the first two message bits is π, π , the received is

0)	0	1	0	1	1	1
	0	0	1	0	1	1
<hr/>						
	0	0	0	0	1	1
	π	π	π	π	0	0

Ans : d

29. P(at most one error)

$$= P(X=0) + P(X=1)$$

$$= 8C_0 \cdot (1-P)^8 \cdot P^0 + 8C_1 \cdot (1-P)^7 \cdot P = (1-P)^8 + 8P(1-P)^7$$

Ans: b

Chapter – 6 (Objective Questions)

01. $(B.W)_{\min} = w+w+2w+3w = 7w$

Ans: 'd'

02. The total No.of channels in 5 MHz B.W is

$$\frac{5 \times 10^6}{2 \times 10^5} \times 8 = 200$$

With a five cell repeat pattern, the no. of simultaneous channels is $\frac{200}{5} = 40$

Ans : B

03. $R_C = 1.2288 \times 10^6$

$$G_p = \frac{R_c}{R_b} \geq 100$$

$$\Rightarrow \frac{R_c}{100} \geq R_b$$

$$\Rightarrow 1.2288 \times 10^4 \geq R_b$$

$$\Rightarrow R_b \leq 12.288 \times 10^3 \text{ bps}$$

Ans: a

04. Bit rate = $12 (2400 + 1200 + 1200)$
= 57.6 kbps

Ans: c

05. Sample rate = $200 + 200 + 400 + 800$
= 1600 Hz

Ans : a

06. d

07. $12 \times 5 \text{ KHz} + 1 \text{ KHz} = 61 \text{ KHz}$

08. b

09. d

10. Theoretical $(B.W)_{\min} = \frac{1}{2} (\text{data rate})$
= $\frac{1}{2} (4 \times 2 \times 5 \text{ KHz})$
= 20 KHz

11. c

12. a

13. The path loss is due to
- a) Reflection : Due to surface of earth, buildings and walls
 - b) Diffraction : This is due to the surfaces between Tx. and Rx. that has sharp irregularities (edges)
 - c) Scatterings: Due to foliage, street signs, lamp posts, i.e. scattering is due to rough surfaces, small objects or by other irregularities in a mobile communication systems.

14. 1333 Hz.

15. Min. Tx. Bit rate = $(2 \times 4000 + 2 \times 8000 + 2 \times 8000 + 2 \times 4000)8$
= 384 kbps

Ans: 'd'

16. 12×8 KHz

Ans : c

17. a

18. c

19. b

20. c

21. b

All the Best.

ACE Academy